

DATA :

Data are known facts which can be stored or recorded.

Information : Processed data

DATABASE :

It is a collection of related data.

*) A database is a logically coherent collection of data with some inherent meaning.

A random collection of data can't be treated as database.

*) A database represents some aspects of the real world.

*) A database is designed, built and populated with data for a specific purpose. It has some intended group of users and some preconceived applications in which the users are interested.

*) Database is meant for computerized data storage for data management.

DBMS :

It is a general purpose software system which task is \rightarrow defining a database.

\rightarrow Conforming a database

\rightarrow Manipulating a database

\rightarrow Sharing the database among various users and applications.

\rightarrow Protecting of database and

\rightarrow Maintaining the database over a long period of time.

\Rightarrow Defining a database

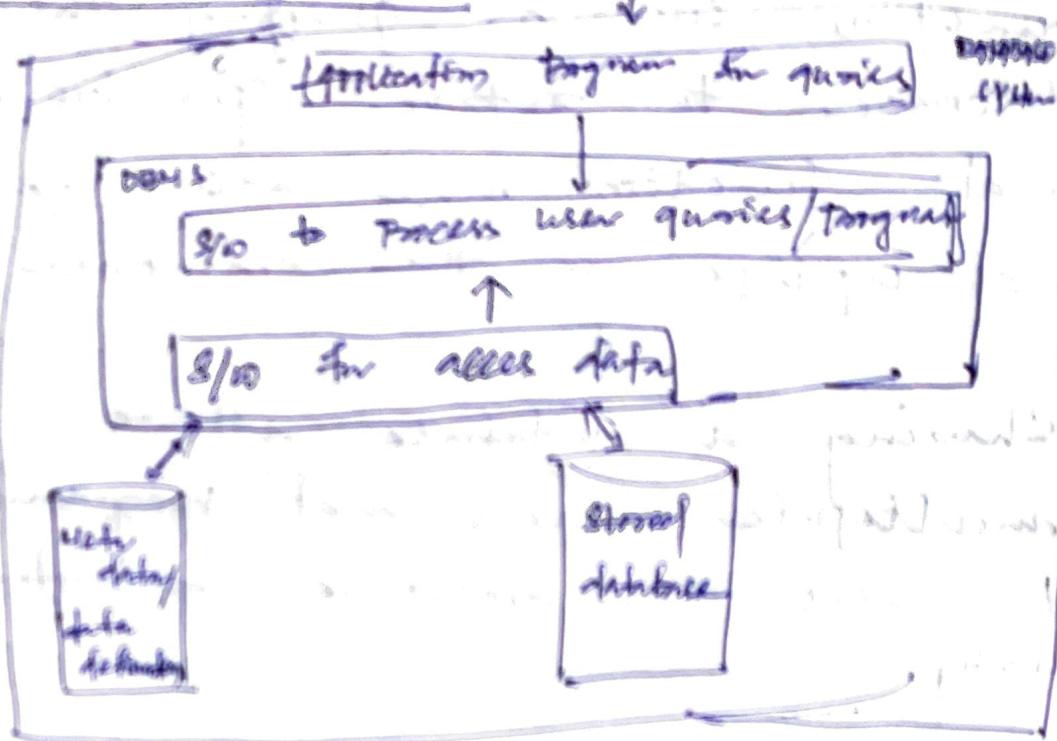
This part deals in details of it means specifying datatypes structures and constraints of the data to be stored in the database and the way of defining them in DBMS.

\Rightarrow Controlling the database means

storing of data on some storage medium which is controlled by the DBMS.

- Manipulating a database includes functions such as querying the database to retrieve specific data and function like insert, delete and update in the database.
- Sharing a database allows multiple users and programs to access the database simultaneously.
- Protection of database means to protect database from hardware malfunction and protection from unauthorized access.
- Maintaining a database means to maintain the requirement of the database belongs to the user world.
DBMS SYSTEM:
Database system = DBMS + Database language or interface.
eg: DB2, ORACLE, MySQL, SQL SERVER, DB2, PostgreSQL, MS Access
Distributed and Standard.

DATABASE ENVIRONMENT



CHARACTERISTICS OF DATABASE APPROACH

OR ADVANTAGES OF DATABASE SYSTEM OVER TRADITIONAL FILE SYSTEM:

→ Self describing nature of the database system:

→ The database system contains not only the database itself but also a complete ^{definition/} description of the database structure and constraints.

→ This definition is stored in DBMS Catalog which contains information such as the structure of each file, the type and storage format of each data item and

Various constraint on the data.
This catalog is also known as data dictionary. The information is stored in the database. Catalog is known as meta data.

→ Information about program and data:

→ Support multiple views of data:

A view may be a subset of the database or it may contain virtual data that is derived from the database but not stored explicitly in the database.

→ Controlling Redundancy:

(Data Redundancy means storing of same data in multiple times in different location). (is known as data Redundancy)

Redundancy leads to the following problems:

- 1) Duplication effort
- 2) Wastage of storage space
- 3) Leads to inconsistent data.

(Meta data: The information stored in the catalog is called Meta data it describes the structure of Polarity database.)

- ~~Redundancy~~ can't be zero, it only
be reduce or minimize.
- Restricting unauthorised access.
- Providing storage structure for
efficient query processing.
- (Searching will be easy or take
less time to search.)
- Providing Backup and Recovery.
- Providing multiple user interface.
- Representing complex relationship
among data.
- Data integrity or enforcing
integrity constraint on the data
(Some Rules enforcing int.
in the database so that there
~~will~~ ~~be~~ will not occur any
error.)

DATABASE LANGUAGES

10.12.24 Dec 24

① DDL (Data Definition Language)

→ It is used to define the conceptual schema.

→ DDL statements are used to specify the database structure or schema.

→ So it specifies relations, attributes, constraints and relationships.

N.B : After compilation of DDL statements database catalog

central data dictionary is created which stores meta data.

② Storage definition Language (SDL)

SDL is defines internal schema.

It is used for defining storage structures

storage structures or access methods to ~~enhance~~ the performance of the database system.

③ VIEW definition Language (VDL)

It is used to define external schema. i.e. it is used to specify user needs and their

mapping to the conceptual schema.

A Data Manipulation Language (DML)

DML provides a set of operations to support the basic data manipulation operations on the data held in the database, independently of its structure, e.g.

Typical manipulation includes

- ① Retrieval ② update ③ delete
- ④ Insert

Actions in operations in a database.

There are two main types of DML

- ① High Level / Non-procedural DML

- ② Low Level / Procedural DML

Introducing privileges at level of DB

③ Data Control Language (DCL)

goes environment with privileges

DCL is used for granting and revoking user access on a database.

DCL statement includes GRANT and REVOKE

Grant (via insert statements) commands.

GRANT : It gives user access
privileges to the database.

REVOKE : It withdraws user's access
privileges given by using
GRANT command.

⑥ Transaction Control Language (TCL)

→ It is used to manage transaction
in a database.

→ These are used to manage the
changes made by DML statements.

The following are the statements
under TCL:

(i) COMMIT

(ii) ROLLBACK

(iii) SAVEPOINT

Schemas is also called table structure.

The description of a database is
known as database schema.

A schema represents the names
of data items, their formats or
data types and some type of constraints.

The schema can be defined in
any of the following ways.

Student (Rollno: Number)

Name: String

Dob: Date

Course: String

GPA: Number

(Rollno, Name, Dob, Course, GPA)

Student (Rollno, name, Dob, course, GPA)

(U.P) Student (Rollno, Name, Dob, Course, GPA)

Rollno	Name	Dob	Course	GPA
--------	------	-----	--------	-----

(constraint) (Can't be duplicate)

N.B: Here the key fields are underlined.

DATABASE STATE: The parallel of STT

The state in a database

at a particular moment in time is known as database state.

It is also known as "snapshot" of a database or "database instant".

N.B: The schema is sometimes called the extension and the database state is called the snapshot or the extension of the schema.

In parallel DBMS we have two

parallel parallel with two

DATABASE ARCHITECTURE

Data model determines the structure of data. How is data organized?

i) data model defines the logical design and structure of a database and in which format the data stored, accessed and updated in a database.

The data model supports concepts of data abstraction in a database system.

The types of data model :-

- (i) High level or Conceptual data model
- (ii) Low level / Physical data model
- (iii) Representational or implementation data model
- (iv) Logical data model (e.g.: Relational Model)

Database Architecture

Three schema architecture / ANSI

Goals of three-schema architecture for DBS

- ① To ~~access~~ achieve
 - Use of a Catalog to store the database descriptions (Schema)
 - So as to make it self describing.

- Insulation of program and data (data independence)
- Support multiple user views

In three Schema architecture
the schema can be defined in
following ways.

→ Internal / Physical Schema

→ Conceptual / logical Schema

- The internal level has an external schema, which describes the physical storage structure of the database.

The internal schema uses a physical data model and describes the complete storage details of data storage and access path for the database.

(The data structures used to recover data efficiently is known as access path)

- The conceptual level has a conceptual schema which describes the structure of whole database.

SS So it describes entities / relations
attributes, data types, constraints,
relationships, and user operations.

and it describes details of the physical storage structure.

Usually, a representational
datamodel is used to describe
the conceptual schema.
It includes a number of external
schemas or user views.

Each external schema describes
the part of the database that
a particular user group is interested
in and hides the rest of the
database from that user group.



Properties of levels of storage :-
- indexed, sorted, etc. forms

Mapping

The process of translating the requests and responses between Schemas is known as mappings.

Data Independence:

Data independence can be defined as the capacity to change Schema at one level of a database system without having to change the Schema at the next higher level.

* **Physical data independence**

* **Logical data independence**

PDI

Physical data inde. has the capacity to change a internal Schema without having to change the conceptual Schema.

Hence the internal Schema need not be changed as well.

→ Changes to the internal Schema may be needed because

Some physical files were unorganized.

Ex: by creating additional access structures to improve the performance of the retrieval or update.

→ If the same data is before remains in the database, the conceptual schema need not even be changed.

(AIS) without changing the external & logical

→ It gives the capacity to change the conceptual schema without having to change external schema or application programs.

→ We may change the conceptual schema to expand the database (by adding record type or data items) or to reduce the database (by removing data records type or data item).

In these cases, the external schema should not be affected.

DATABASE USERS

Database users are the people who are involved in work related to design, use and maintenance of large database. There are following categories of users.

→ Database Administrator (DBA)

→ Database Designers

→ Frontend developers

→ End users

→ System Analyst/Application

Frontend developer is a person who

works with front end of application

→ DBA :-

(Database Administrator) is a person or a group

of people who are organization

whose duties include administer,

oversee and manage the database

tools and related software.

Duties/Responsibilities of DBA :-

• Create and maintain schema

→ Schema definition

→ Storage structure and access

and deletion

- Ensuring data security
(Prevent unauthorized access)
- Schema modifications and performance monitoring
- Assisting application programmers
- Backup and Recovery

~~These jobs are done by DBA~~

→ Database Designers :-
Database design points present in centralized (Integrated) databases

→ End Users :-
Diff. type of end users
→ casual end users
→ ~~novice or~~ novice or practitioners
→ sophisticated
→ standalone users

E-R MODEL

- ① It is a high-level conceptual data model.
- ② It is used for conceptual design of database application or a database.
- ③ This model describes the basic data structuring concepts relationship and constraints.

(iv) Diagrammatic notation for generating ER model
(also known as ER model)

For representation model to
practical

COMPONENTS:

entity, attribute, relationship

① Entity

It is a real life object
or thing which has either
physical existence or conceptual existence.

Entity is represented by a
rectangular box

Entity name is always a
naming in capital letters

e.g.

EMPLOYEE

② Attributes

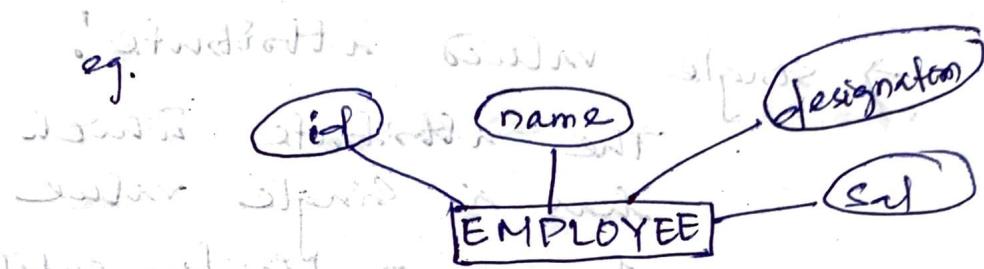
The properties which

describe the entity is known as

attribute

e.g. An EMPLOYEE can be
described by his/her
name, designation,
salary etc.

Attributes are represented by ovals in E-R diagram.



TYPES OF ATTRIBUTE:

(a) Simple attribute and composite attribute

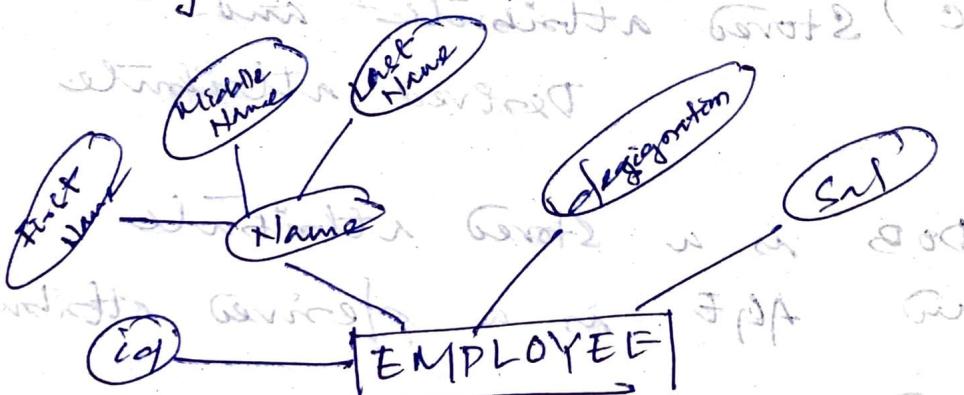
→ Simple attribute: the attributes which can't be divided are not divisible.

eg Roll no., Id etc

→ Composite attribute: the

attributes that are
divisible to subparts
or component attributes
are known as composite
attribute.

eg. Name, Address, Contact



(b) Single valued and Multivalued attributes

Attributes:

→ Single valued attribute:

The attribute which has a single value for a particular entity.

e.g.: Id, Roll no., DOB, etc.

→ Multivalued attribute:

The attribute which has more than one value for a particular entity.

e.g.: Qualification, Department

location, etc.

Like first name, last name.

In E-R diagram the multivalued attributes are represented by double-line ovals.

attribute



(c) Stored attribute and Derived attribute

DOB is a stored attribute

and AGE is a derived attribute

• Derived attributes are represented by dashed-line ovals.

Q6) Key attributes

A set of attributes of an entity of an entity type is known as entity key iff its values are distinct for each individual entity type in this entity set.

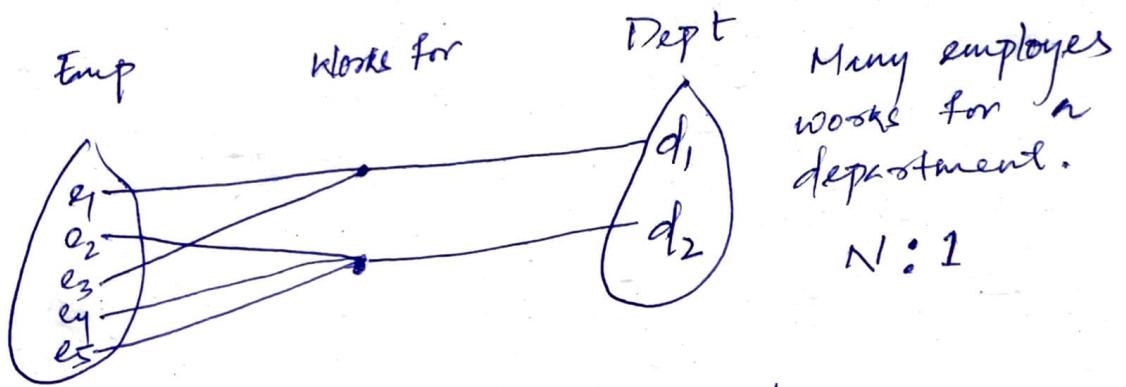
OR A set of attributes (one or more attribute) of an entity type is known as key if the value of this set of attribute uniquely identify each and every entities of that entity type.

The key attributes are underlined inside the oval. — Ed

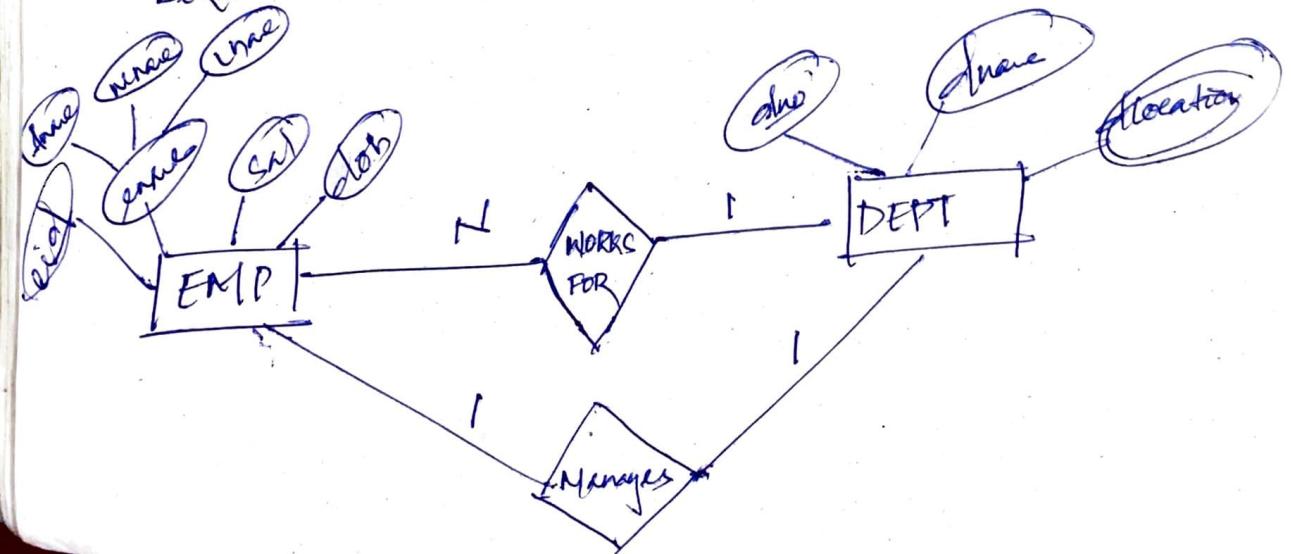
EMP Constraints on Relationship type / Structural constraints

- (i) Cardinality ratio Constraints
- (ii) Participation Constraints / Existence dependence

(iii) Cardinality ratio Constraints :-



Like that $1:N, 1:1, M:N$



ii) Participation Constraint

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Existence of an entity depends upon its relationship with other entities via relationship type or through relationship type.

In this constraint no entity can't be represent in an E-R diagram independently.

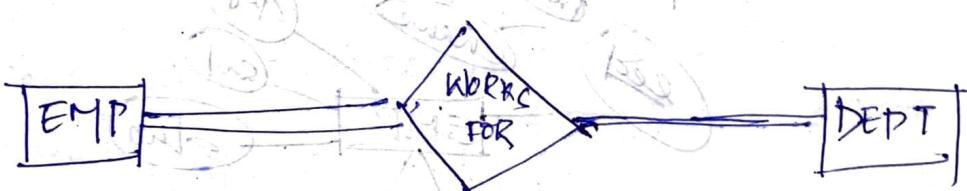
It specifies minimum no. of relationship instances that each entity can participate in and sometimes it is called as minimum cardinality constraint.

- a) Total participation constant
- b) Partial participation constant

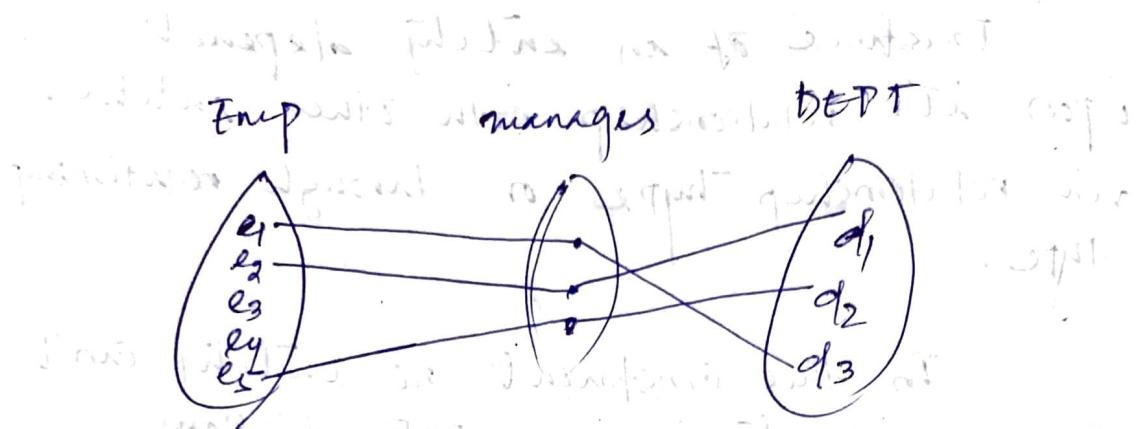
a) Total participation constant

Here total participation constant means that every entity of an entity type participate in a relationship type.

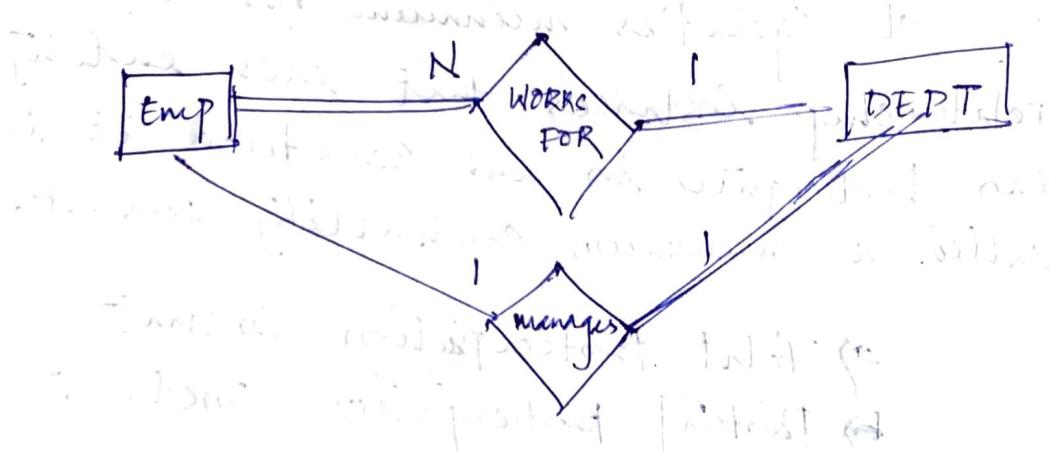
It is represented by double line.



b) Partial participation Constant.

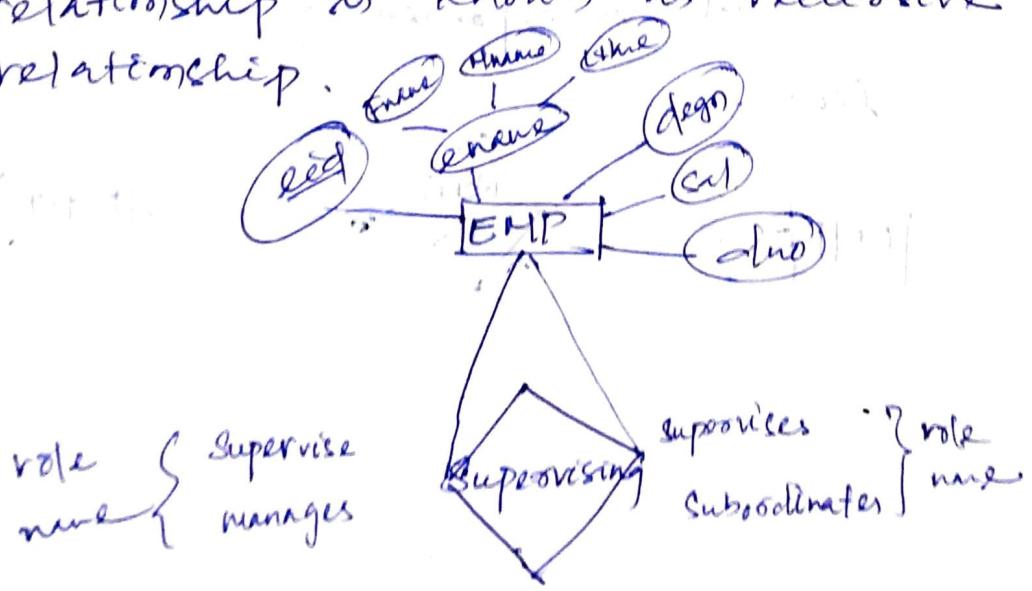


It is represented by single line.



Recursive Relationship :-

When some entities of an entity type participates more than once in a relationship type in different roles the relationship is known as recursive relationship.



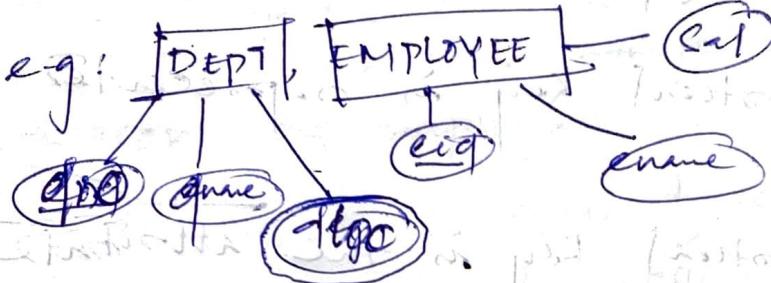
Role name: Role played by an entity type
with respect to relationship type

④ W.r.t recursive relationship "RoleName" are mandatory.

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Strong Entity type:

Entity type which has a key attribute of its own to identify its ~~entities~~ unique entities



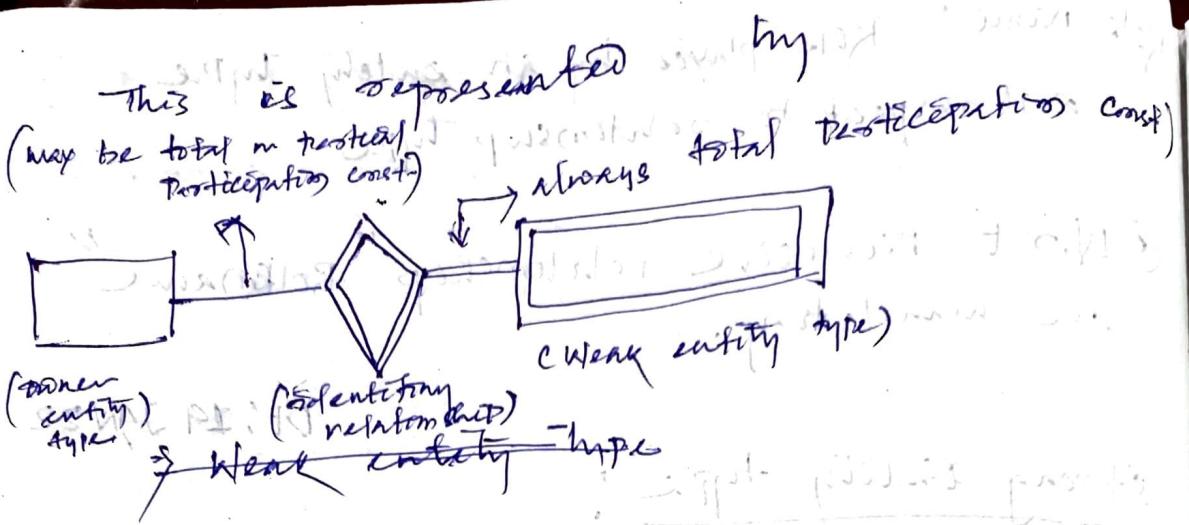
Weak entity type:

Weak entity type is an entity type that does not have key attributes of its own.

→ Entities belonging to weak entity type are identified by being related to specific entities of another entity type.

→ The entity type which identifies weak entity type is known as identifying entity type or owner entity type.

→ The relationship that relates a weak entity type with its owner entity type is called identifying relationship.



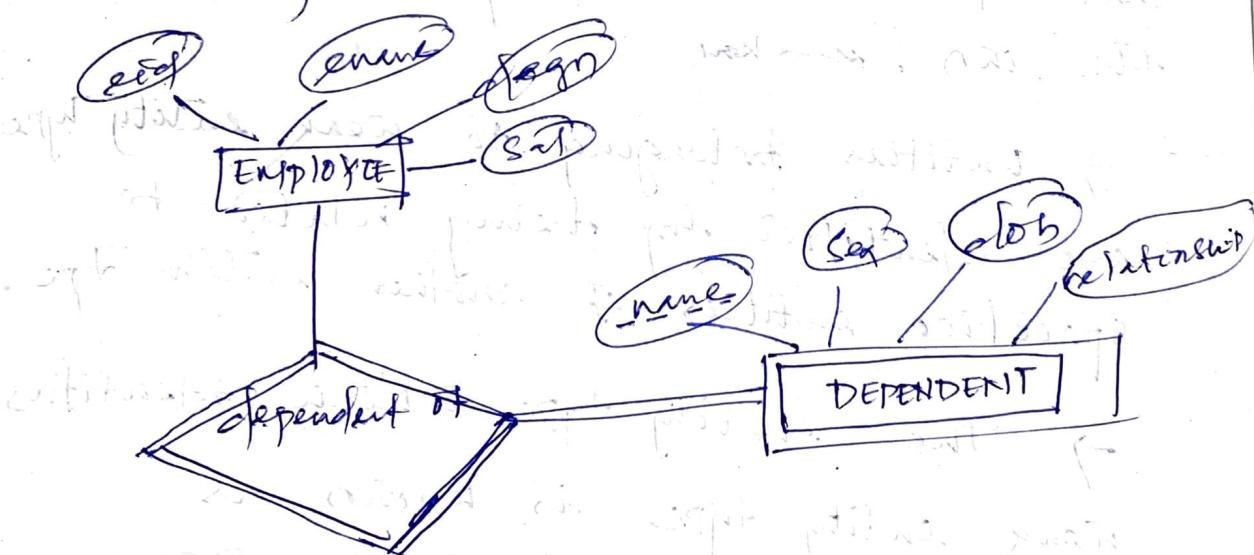
Protocol Key

→ weak entity type normally have
a protocol key.

→ Protocol key is represented by

→ Protocol key is the attribute

that can uniquely identify weak entities
that are related to the owner
entity.



- Q. Consider a company database which keeps track of its employees, department and projects.

The company is organised into departments.

Each department has one or

unique number, name and the location.
Dectorator employee who manages the department.

A. dept. may have several locations.

A dept. controls no. of projects each of which has a unique name, unique number and a single location.

We store each employee name, id, address, salary, sex, and dob. An employee works for a department and works on different projects. We should track of managers of each department and direct supervisor of employees.

We want to keep track of dependent of each employee for insurance purposes, we keep each department name, project, we keep each employee - sex, dob and relationship to the employee.

Based on the above information.

Now the
Company database.

E-R diagram for the

Dept	Loc	Proj	Emp	Dep	Supervisor	Dependent
IT	Delhi	Project A	John	IT	John	John
HR	Mumbai	Project B	Mike	HR	Mike	Mike
Marketing	Bangalore	Project C	Sarah	Marketing	Sarah	Sarah
Finance	Pune	Project D	David	Finance	David	David

ER diagram & bank database 20 JAN 22

ER diagram of Hospital management

ER diagram examples

• Library management system

University management system

Airline reservation system

online food delivery

online shopping

Bank system

Relational Model

→ It represents a database as

collection of relation

→ A relation is a table

→ A table is collection of rows and columns with values.

	led	ename	deg	sl	dbo
t ₁	e ₁	xxx	mg		
t ₂	e ₂	xyy			
t ₃	e ₃	zzz			

Domain of attribute: static, capital 2
A set of values assigned to an attribute
is known as domain of the attribute.

dom(eed) = varchar 2(3) ← any 3 alphanumeric
characters, 0 to 2 digits + character

Relation Schema:

A relation schema $R(A_1, A_2, \dots, A_n)$ is
made up of the Relation R and list
of attributes $A_1, A_2, A_3, \dots, A_n$.

EMPLOYEE(eed, ename, degr, sal, dno)

Relation Schema

EMPLOYEE (eed:

ename:

dob:

ca:

degr:

afno:

{eid, ename, degr, sal, dno} static, contains all

$R(A_1, A_2, A_3, \dots, A_n)$

attribute A_i ($1 \leq i \leq n$) \in ~~domain~~ \rightarrow ~~domain~~ \rightarrow $\text{dom}(A_i)$

Relation State

$R(A_1, A_2 \dots A_n) \rightarrow \text{Rel}^n \text{ schema}$

$t_1 = \langle 'e1', 'sax', 'mgr', 35000, 1 \rangle$

$t = \langle \text{value of } A_1, \text{ value of } A_2 \dots, \text{value of } A_n \rangle$

$r(R) = \{ t_1, t_2, t_3 \}$

$r(R)$ is a set of n -tuple

$t_i = \langle v_1, v_2, v_3 \dots v_n \rangle$

$v_1 = \text{value of } A_1$, $v_2 = \text{value of } A_2$, \dots , $v_n = \text{value of } A_n$

i) If relⁿ schema R is represented by
 $R(A_1, A_2 \dots A_n)$

where R = Relation name

$A_1, A_2 \dots A_n$ = Attributes

The relation state $r(R) = \{ t_1, t_2 \dots t_n \}$

$t_i = \langle v_1, v_2 \dots v_n \rangle$

$v_1 = \text{value of } A_1$

$(v_2) = \text{value of } A_2$

$v_n = \text{value of } A_n$

Let $R(A_1, A_2, \dots, A_n)$ $\{A_1 \text{ of } R = R \cdot A_2$
 $S(A_1, A_2, \dots, A_n)\} \{A_2 \text{ of } S = S \cdot A_2$

$R, S \leftarrow$ denotes Relation name

Value or dom of tuple $t_2 \in R$

$$\boxed{t_2[A_2] = 2}; t_2 \cdot A_2 = 2 \quad \boxed{t_2[\text{dom}] = 5}$$

The attribute A_j of tuple t_2 is represented by $t_2[A_j] = \text{value}$.

Degree of a Relation

No. of attributes in a relation is known as degree of a Relation.

$R(A, B, C) \rightarrow$ Degree = 3

$R(A, B, C, D) \rightarrow$ Degree = 4

Relationship for tuples with degree n can be represented by $R(A_1, A_2, \dots, A_n)$

(a) A relation with degree k can be represented by $R(A_1, A_2, \dots, A_k)$

(b) A relation with degree $k+1$ can be represented by $R(A_1, A_2, \dots, A_k, A_{k+1})$

$R(A_1, A_2, \dots, A_k, A_{k+1})$

Schema Based constraint

① Domain constraint

The value of an attribute must come from its domain.

② Key constraint

Basically in this constraint we discuss following two things:

① Super key and Subkey.

② Key

③ Candidate key

④ Primary key

⑤ Alternate key

⑥ Key

→ uniqueness property

→ distinct values

→ key is a set of attributes of a relation which uniquely identifies tuples in that relation.

Mathematically, a key is a set of attributes of a relation R (Cartesian product) such that any two tuples t_i and t_j in R satisfy

$$\{t_i\} \cup t_i[R] \neq t_j[R].$$

② Super Key

→ set (of attributes) of R attributes
relation $R(A_1, A_2, \dots, A_n)$ is called Super
key of R iff for any tuple
 t_i and t_j ($i \neq j$)

$$t_i[S_k] \neq t_j[S_k] \text{ i.e. } t_i \neq t_j$$

→ if superkey's set specifies uniqueness
constraint that no two distinct
tuple in my state $r(R)$ can
have the same value for S_k .

→ Super key can have redundant
attribute i.e. removal of attribute
from the superkey set still has
the uniqueness property.

e.g. student(Rollno, name, course, class)

{Rollno, name, course} - Super key

{Roll no, name} - Super key

{course} & {SA} = part

Q What is the default Super key of $R(G, G, D, E)$

Ans. {A, B, C, D, E}

★ Key is the minimal super key
i.e. you can't remove any attribute
from the Key set. For ex. in

Q. 2 If set of attributes K of a relation $R(A_1, A_2, \dots, A_n)$ is a key
iff for any two tuple t_i, t_j
 $(i \neq j)$ then $t_i[K] \neq t_j[K]$

Q. $R(A, B, C, D, E)$

What is the key of R ?

Ans: - Can't be determined
as value is not given.

e.g. (A) \rightarrow A has no sign

e.g.: Student (Roll no, name)

The answer is uniqueness
Student \rightarrow Roll no has uniqueness
and name has uniqueness
then { Roll no } is primary key

* Key are underlined.

$R(A_1, A_2, A_3; A_1, A_2, A_K, A_{n-1}, A_n)$

post req: { name, roll no }

key = { A_2 }, { A_1, A_K }

Can candidate key { name, roll no }
candidate key

only if more than one key present
in a relation each key
is known as a candidate key.

Primary Key

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(one or more) thus some candidate key is present in the relation then one of the candidate key is chosen as primary key.

* It is chosen by database designer

Primary key has following properties

→ uniqueness property
i.e. a set of attribute P_K of a relation $R(A_1, A_2, \dots, A_n)$ is a primary key if for any two tuples t_i and t_j ($i \neq j$) $t_i[P_K] \neq t_j[P_K]$

→ Duplicate not allowed

→ Primary key does not allow null values

→ Only one primary key is allowed for relations.

$R(A_1, A_2, \dots, \underline{A_i}, \underline{A_j}, \underline{A_{i+j}}, \dots, A_n)$

is primary key candidate (candidate)

Set of keys of R are $\{A_i, A_j\}$, $\{A_{i+j}\}$, $\{A_i, A_{i+j}\}$, $\{A_j, A_{i+j}\}$

Candidate Keys

R(A₁, A₂, ..., A_n)

Primary keys are {A₃, {A₁, A₂}} (Wrong)

Because for a relation, only one primary key is possible.

Alternate key and needs to be

The keys other than the primary key.

Composite key = {A₁, A₂, ..., A_n}

Relationship schema of primary key

R(A₁, A₂, ..., A_n) + Components

e.g. R(A₁, A₂, ..., A_n) = R = {A₁, A₂, ..., A_n}

Relational Database Schema :

(R₁, R₂, ..., R_n)

Relational database schema is a collection of relational schema.

S = {R₁, R₂, ..., R_n}

Valid state

A database state which satisfies all the constraints specified in the database.

③ INTEGRITY CONSTRAINT

INTEGRITY CONSTRAINT is into two types

Entity Integrity

It talks → Primary key value can't

be null.

(~~and~~ → Reference) Integrity constraint

→ It is used to establish relationship

between relations.

→ It is used to maintain consistency among tuples in a relation.

→ It is described by the concept of foreign key.

Foreign key

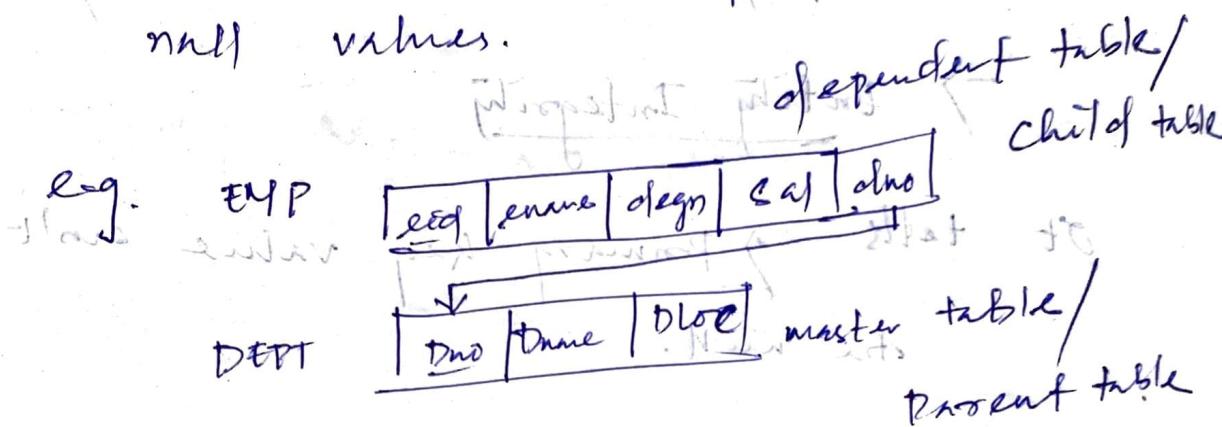
→ Primary key of one table can be used as foreign key in another table provided $\text{dom}[P_k] = \text{dom}[F_k]$

datatype k
size

data type
k size

Primary key constraints force foreign key constraints with the constraint that primary key values must also be unique.

Binary key does not allow null except values. But unique key allows null values.



$$\text{dom}(\text{DEPT}. \text{dno}) = \text{dom}(\text{EMP}. \text{dno})$$

queries involving joins of two or more tables

pointwise relations, $\text{dname}, \text{dname}$ FROM DEPT } SQL

SELECT eno, ename, dname
FROM EMP, DEPT

WHERE sal > 25,000

Relational algebra } $\{ \pi_{\text{eno}, \text{ename}, \text{dname}} \}$ relational algebra

Let SQL transfer to Relational algebra.

$$(\exists \vec{x}) \vec{y} = (\exists \vec{y}) \vec{z} \text{ where } \vec{y} \text{ is disjoint from } \vec{z}$$

disjoint
subset
of symbols

Relational Algebra:

- Basic set of operations for a relational Model.
- Specifies the retired request.
(the way in which you can access the data from database)
- The result obtained after performing relational algebra operation on a relation produce a new relation.

SELECT operation:

- It retrieves or selects a set of tuples/rows, which satisfies a given condition.
- General form is $\text{select operation } (R) \rightarrow \text{Res name} | \{cond\}$
- Then the condition is of the form:
attribute op value / attribute op
 \rightarrow op is one of the operator among
 $>, >=, <, <=, =, \neq$. (Mathematical symbols)
- More than one operation can be combined by AND(\wedge), OR(\vee), NOT(\neg).

Q. Retrieve the informations of employees
of dno = 4.

Ans: $\pi_{dno=4}(\text{EMP})$

Q. Find the managers who are getting
more than 5000 salary.

Ans: $\pi_{\text{degm}=\text{mgr}}(\text{EMP})$
 $\text{degm}=\text{mgr} \wedge \text{sal} > 5000$

Imp: $\text{deg}(\pi_c(R)) = \text{deg}(R)$

$\text{deg}(R) = \text{no. of attributes in } R$.

Project Operation:

→ Resolve certain columns from a
relation.

→ General form is

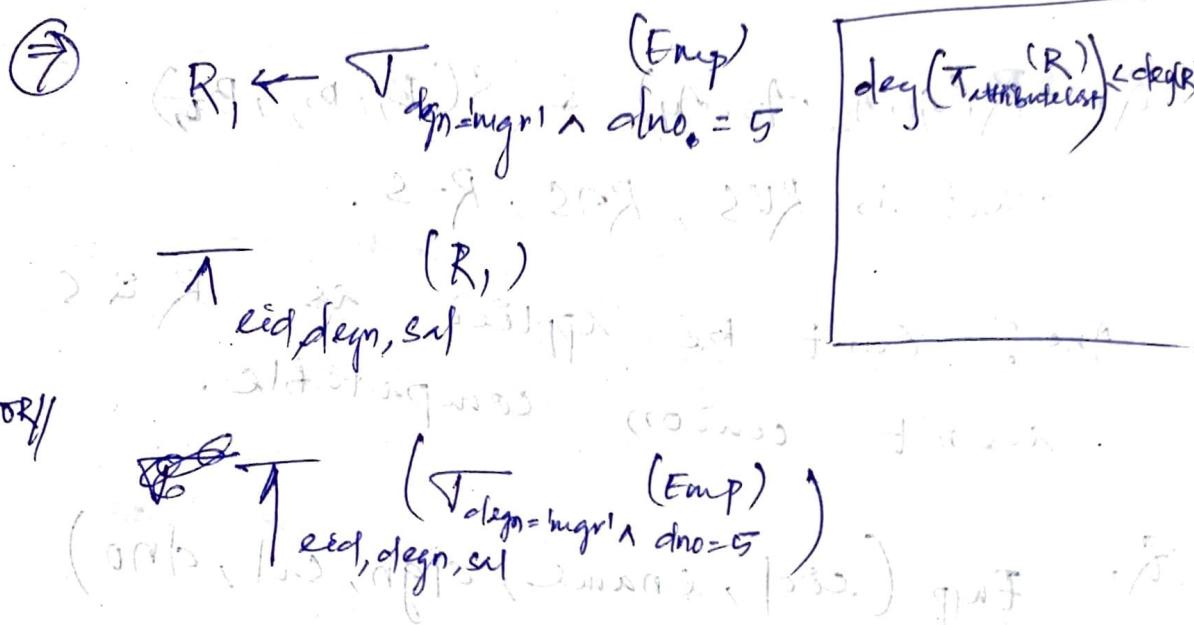
$\pi_{\langle \text{columnlist} \rangle} / \text{Table}(R)$

Q. Find eid, ename, sal of all managers.

Ans: $\pi_{\text{eid}, \text{ename}, \text{sal}}(\text{EMP})$
 $\text{degm}=\text{mgr}$

Or/ $\pi_{\text{eid}, \text{ename}, \text{sal}}(\text{EMP})$

Q. Find cod, deg & Srf of null manager who are working under dno. 5.



$\deg(T_{\text{null manager}}^{(R)}) = \deg(R)$

SET operations :- T, T_1 unary operator

UNION # U, v binary operators

INTERSECTION # \cap , Δ binary operators

SET DIFFERENCE / MINUS

CARTESIAN PRODUCT

The set operations UNION(U), INTERSECTION

& MINUS can be applicable on reps
if the relations are union compatible.

UNION COMPATIBILITY :-

Two operations $R(A_1, A_2, \dots, A_n) \times S(B_1, B_2, \dots, B_m)$

are union compatible if

$\deg(R) = \deg(S)$ i.e. $n = m$

and $\text{dom}(A_i) = \text{dom}(B_i)$ ($i \leq n$)

i.e. domain of corresponding attributes of R & S are same.

e.g. $\text{dom}(R \cdot A_1) = \text{dom}(S \cdot B_2)$

$\text{dom}(R \cdot A_2) = \text{dom}(S \cdot B_3)$ & so on.

Q. $R(A_1, A_2, A_3, A_4)$ & $S(B_1, B_2, B_3)$

what is RUS , RUS , $R-S$.

Ans: Can't be applied as R & S aren't union compatible.

Q. $\text{Emp}(\text{eod}, \text{ename}, \text{dgn}, \text{sal}, \text{dno})$

dependent(eod, dgn, cname), of sex, of rep

EMP-dependent \Rightarrow Find the employees

with dgn who does not have any dependent.

Ans: They can't perform any operation (v,n,.)

(a) Because they are not union compatible

(b) Emp have 'sal, dno' and dependent

have - 'dsex, ofsk' different attributes.

$\text{emp}_1 = \overline{\text{eod, dgn}}^{\text{(EMP)}}$

$\text{dependent}_2 = \overline{\text{eod, dgn}}^{\text{(dependent)}}$

Now (domain) and (degree) are same.

$[\text{Emp}_1 \cup \text{dependent}_1]$

$[\text{Emp}_2 \cap \text{dependent}_2]$

EMP1 - dependent 1

rvs = $\{ t \mid t \in r \text{ or } t \in s \}$

rns = $\{ t \mid t \in r \text{ and } t \in s \}$

n-s = $\{ t \mid t \in r \text{ but } t \notin s \}$

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RENAME Operation

↳ To rename a relation / Renaming the rel.

Symbol: $f_s^{(r)}$

Renaming a relation

(i) $f_s^{(R)}$ → The relation R is renamed to relation S.

(ii) To rename the attributes of a rel.

$R(A_1, A_2, A_3, \dots, A_n)$ to $R(B_1, B_2, \dots, B_n)$

$f^{(R)}$

(B_1, B_2, \dots, B_n)

(iii) Change or renaming

to $S(B_1, B_2, \dots, B_n)$

$f^{(R)}$

$\{ S(B_1, B_2, B_3, \dots, B_n) \}$

EMP (eno, ename, adm)

DEPT (dno, dname)

Q. Find the eno, name of employees who are working under 'research' dept.

Cartesian Product (Cross Product)

Symbol is \times (cross)

Though it is a left operation, but union compatibility may not be satisfied.

(Union compatibility is not required to be satisfied)

Result of \times is a new relation which contains combinations of every tuple from one relation with every tuple from other relation.

$$R \times S = \{ (t_1, t_2, t_3) | t_1 \in R, t_2 \in S \}$$

$$R \times S = \{ (1, 2, 3), (1, 4, 5), (2, 1, 4), (2, 1, 5), (2, 4, 1), (2, 4, 5) \}$$

Fig-1

Emp

eno	ename	gno.
e1	x	1
e2	y	2
e3	z	1

DEPT

dno.	dname
1	Research
2	Finance

$$\text{Emp} = \{ t_1, t_2, t_3 \}$$

$$\text{DEPT} = \{ t_4, t_5 \}$$

$$\text{Emp} \times \text{DEPT} = (t_1, t_4) \cup \{ (e1, R, 1), (e1, F, 2), (e2, R, 1), (e2, F, 2), (e3, R, 1), (e3, F, 2) \}$$

+ gets combined after projection with attr

EMP X DEPT

eno	ename	dno	dno	dname	
e1	x	1	1	Research	(t ₁ , t ₄)
e1	x	1	2	Finance	(t ₁ , t ₅)
e2	y	2	1	Research	(t ₂ , t ₄)
e2	y	2	2	Finance	(t ₂ , t ₅)
e3	z	1	1	Research	(t ₃ , t ₄)
e3	z	1	2	Finance	(t ₃ , t ₅)



$\prod_{\text{eno, ename}} (\sigma_{\text{EMP.dno} = \text{DEPT.dno} \wedge \text{dname} = 'Research'} (\text{EMP} \times \text{DEPT}))$

N.B:

① Let $R(A_1, A_2, \dots, A_n)$ and $S(B_1, B_2, \dots, B_m)$

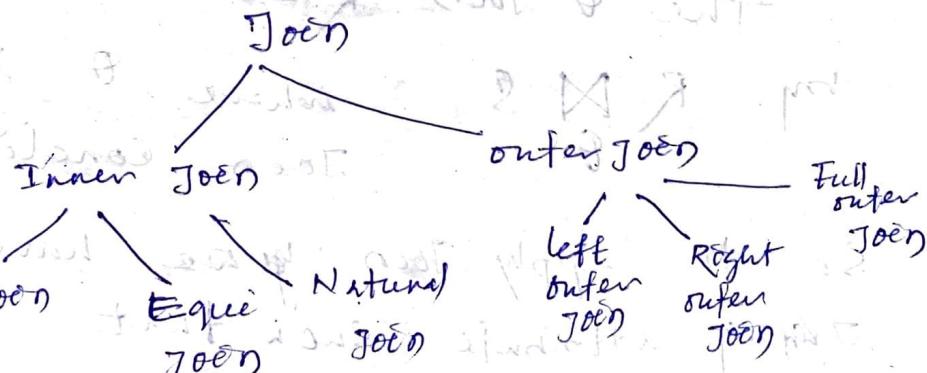
So here $\deg(R \times S) = n+m$

② If R has i no. of tuples and S has j no. of tuples

$$|R| = i \quad \text{and} \quad |S| = j$$

$$|R \times S| = i \times j$$

JOIN operation



Join

Symbol: \bowtie

Let $R(A_1, A_2, \dots, A_n)$ is ~~a relation~~ and $S(B_1, B_2, \dots, B_m)$ are two relations, where then the join operation on R and S is, represented by

$R \bowtie S$
cond?

The result of Join operation contains tuple from both the relations which satisfies the cond?

$$\deg(R) = n \text{ and } \deg(S) = m$$

$$\deg(R \bowtie S) = n+m$$

$$|R \bowtie S| \leq |R| + |S|$$

Theta Join

Let $R(A_1, A_2, \dots, A_n)$ & $S(B_1, B_2, \dots, B_m)$

be two relations.

The θ join $R \bowtie S$ can be represented by $R \bowtie_{\theta} S$ where θ is the join condition.

So to apply join we have to a joining attribute such that

$\text{dom}(R \cdot A_i) = \text{dom}(S \cdot B_j)$ (join domain)

Hence, A_i and B_j are the joining attributes of R and S respectively.

Condition of the form

$(A_i \oplus B_j) \cdot A_i \oplus B_j \neq \text{dom}$

\oplus is one of the operator among

$<, \geq, >, \leq, =, \neq$ (less than, greater than, less than or equal to, greater than or equal to, equal to, not equal to)

Equi join

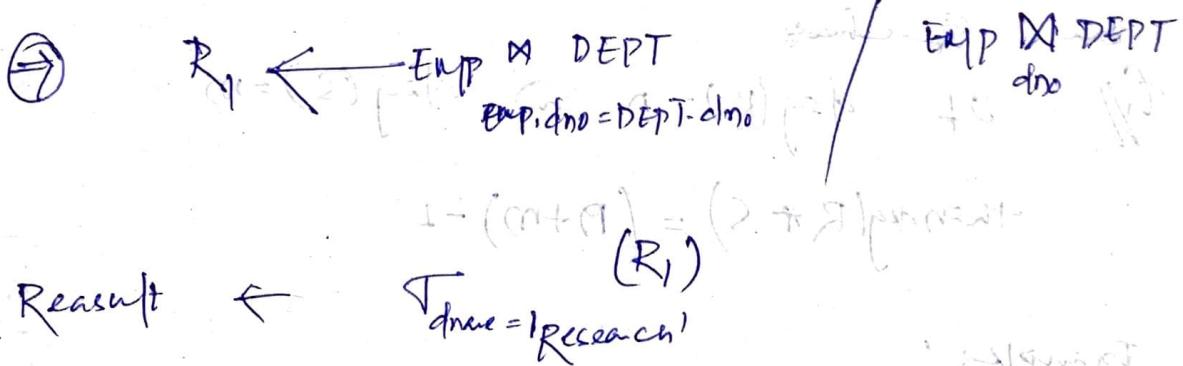
If equality is the operator in \oplus

Join it is known as equi join.

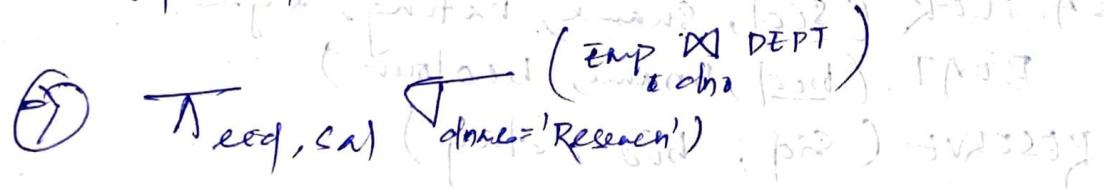
Ex: $\text{Emp}(\underline{\text{eno}}, \text{ename}, \text{dgn}, \underline{\text{sal}}, \underline{\text{dno}})$

$\text{DEPT}(\underline{\text{dno}}, \text{dname}, \underline{\text{loc}})$

Q. Find the employee who are working under research department.



Q. Find eno, sal (not employees who are working under research dept).



Natural Join

→ Represented by the symbol ~~*~~ ~~*~~.

Let $R(A_1, A_2, A_3, \dots, A_n)$ and $S(B_1, B_2, B_3, \dots, B_m)$ be two relations with ~~domains~~ of

$$\text{dom}(R, A_3) = \text{dom}(S, B_3)$$

i.e. A_3 is the joining attribute.

Natural join of R and S is

represented by Δ .

$\Delta R = R * S$
i.e. Δ has attributes $(A_1, A_2, A_3, A_4, B_1, B_2, B_4, \dots, B_m)$

e.g. Natural Join of EMP and DEPT

EMP & DEPT

eno	ename	dno	dname
100	John	10	IT
101	Jill	10	IT
102	Richie	10	IT
103	Mark	20	HR
104	Steve	20	HR
105	Mike	20	HR
106	David	30	SA
107	Tom	30	SA
108	Paul	30	SA
109	Mike	30	SA
110	John	30	SA

Given R & S

if $\deg(R) = n$ and $\deg(S) = m$

$$\text{then } \deg(R * S) = (n+m) - 1$$

Examples:

Given 3 relational schemes as

SA FLOR (sid, sname, rating, age)

BOAT (bid, bname, bcolour)

RESERVE (sid, bid, day)

Q. Find the names of 8 sailors who have reserved boat 103.

④ $R_1 \leftarrow (\text{SAILOR} \bowtie \text{RESERVE})$

$R_2 \leftarrow (\underset{\text{boat} = 103}{\text{SIG}} (R_1))$

Result $\leftarrow \underset{\text{name}}{\text{SIG}} (R_2)$

$\underset{\text{boat} = 103}{\text{SIG}} (\text{name} (\text{SIG} (\text{SAILOR} \bowtie \text{RESERVE})))$

Q. Find the names of sailors who have reserved the boat boat 103 interlace.

⑤ $R_1 \leftarrow (\text{SAILOR} \bowtie \text{RESERVE})$

Result $\leftarrow \underset{\text{name} = \text{interlace}}{\text{SIG}} (\text{SAILOR} \bowtie R_1)$

Q. Find the names of sailors who have reserved a red boat.

⑥ $\underset{\text{color} = \text{red}}{\text{SIG}} (\text{SAILOR} \bowtie (\text{BOAT} \bowtie \text{RESERVE}))$

~~Q. 1~~ Find the names of sailors who have reserved a reef boat and a green boat.

$R_1 \leftarrow \text{color} = \text{Red} \cap (\text{BOAT} \setminus \text{RESERVE})$

$R_2 \leftarrow \text{color} = \text{green} \cap (\text{BOAT} \setminus \text{RESERVE})$

~~Result $\leftarrow R_1 \cap R_2$~~

Result $\leftarrow \text{Tname} (R_3 \setminus \text{SAILOR})$

Q. Find the names of sailor who have reserved a reef or a green boat

Q. Find the names of sailor who have reserved a reef boat but not green boat

Q. Find the colour of boat Reserved by Mr. John.

Ans. The colour of boat reserved by Mr. John is Blue.

Diagram:

⑦

w/
m/

(~~BOAT X (SAILOR X RESERVE)~~)
(~~SAILOR NAME - JOHN~~)

(~~SAILOR X RESERVE~~)
(~~SAILOR NAME - JOHN~~)

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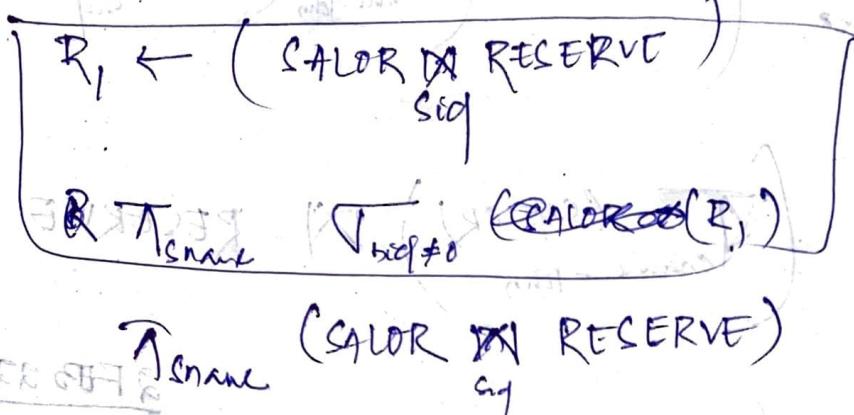
Q. Name of the salon whose age > 20, who
have not received a neg bath.

(X) basic refit Aug 88
(X) R/T ~~201~~ Dages 201 (SAILOR X RESERVE)
SIC

(X) R_2 \leftarrow ~~Boat = RED~~
 (R, ~~Boat = RED~~) b_{eq}
~~Debounce~~ R_3 \leftarrow
~~Debounce~~ R_2 \rightarrow
 R, ~~Boat~~ b_{eq}

$$T_{\text{source}} (R_3 - R_2) \rightarrow \text{Result}$$

Q. Find the names of sailor who have reserved at least one boat.



OUTER JOIN Operation

1. Left outer join (X)

2. Right outer join (X)

3. Full outer join (X)

Left outer join (X)

Col1	Col2
A	1
B	2
C	3
D	4

Col1	Col2
A	A
C	C
D	D

$R \bowtie S$

Col1	Col2	Col1	Col2
A	1	A	A
B	2	Null	Null
C	3	C	C
D	4	D	D

Q. Find the sailors who have received all the boats.

Division Operation

For queries like all, every division operation is used.

Consider two relations R and S where R has two attributes X and Y (i.e. $R(X, Y)$) and S has just attribute Y with same domains that of R i.e. $\text{dom}(R, Y) = \text{dom}(S, Y)$

We define division operation by R/S or $R \div S$ such that R/S contains set of all X values for which there exists ~~such that~~ $\forall Y \in S$ If a tuple $(x, y) \in R$.

Ex.

<u>$R(\text{Name}, \text{Pen})$</u>		<u>$S_1(\text{Pen})$</u>	<u>$S_2(\text{Pen})$</u>
Name	Pen		Pen
Ram	Black		
Sita	Blue		
Hari	Red		
Sita	Green		
Hari	Blue		
Sita	Red		
Ram	Green		

~~Black~~ ~~Blue~~

		Sita	black
		Ram	Red

$R \div S =$

GRICE	
RENAME	
SITAR	

$R \div S_2 =$

GRICE	
Ram	
Sita	

part 3

⑦ $R_1 \leftarrow \pi_{\text{SNAME}} \text{ sig. rated TAN}$ (RESERVE)

$R_2 \leftarrow \pi_{\text{BOAT}}$ (BOAT)

$R_3 \leftarrow R_1 / R_2$ (sailors who have received all the boats)

RESULT $\leftarrow \pi_{\text{SNAME}} \text{ sig} (R_3 \bowtie \text{SAILOR})$

(SVS+239)

* Complete set of Relational Algebra operations.

$S \oplus S \rightarrow S^2$

$(S1 \sqcup S2 \sqcap S3) \text{ ref. } \rightarrow \text{max}$

Q. Find the SAILORS who have reserved
 all the boat boats named DRAGUE
 Root 'BIDE-HAEN'.

$R_1 \leftarrow T_{\text{Sailor}}(\begin{array}{l} \text{BOAT DR RESERVE} \\ \text{true=bluehaven} \end{array})$

$R_2 \leftarrow T_{\text{Sailor}}(\begin{array}{l} \text{R, } \forall \text{ SAILOR} \\ \text{true=bluehaven} \end{array})$

$(SAILOR \sqcap L \sqcap) \rightarrow TUV238$

(RESERVE)

$\cancel{R_1 \leftarrow T_{\text{Sailor}}(\begin{array}{l} \text{BOAT DR RESERVE} \\ \text{true=bluehaven} \end{array})}$

$R_2 \leftarrow T_{\text{Sailor}}(\begin{array}{l} \text{BOAT} \\ \text{true=bluehaven} \end{array})$

$R_3 \leftarrow R_1 \sqcap R_2$

Result $\uparrow_{\text{same}}(R_3 \sqcap \text{SAILOR})$

Functional Dependency

→ If functional dependency set? two sets of attributes in FD of a rel" R is represented by $x \rightarrow y$.

Functional dependency is a constraint which is specified on any rel" state $r(R)$ and it is like - for any two tuples t_1 & t_2

$$\text{if } t_1[x] = t_2[x] \text{ and } \\ \& t_1[y] = t_2[y]$$

then $x \rightarrow y$ is satisfied.

i.e. the value of y-component of a tuple is determined by the value of x-component.

Otherwise we can say that x-component of a tuple uniquely / functionally determine the value of y-component of that tuple.

N.B.

$$(1) x \rightarrow y$$

L.H.S of F.D = x

R.H.S of F.D = y

as, second one is not sufficient.

(2) If $x \rightarrow y$, we can't say that $y \rightarrow x$.

Inference Rules for Functional Dependencies

Inference rules are used to derive new functional dependencies from a given set of functional dependencies.

IR 1: Reflexive Rule: If $y \subseteq x$ ($x \supseteq y$)

then $x \rightarrow y$, where $x, y \subseteq R$

IR 2: Augmentation Rule: If $\{x \rightarrow y\} \subseteq F$ and $z \in R$

where $x, y, z \subseteq R$

IR 3: Transitive Rule: If $\{x \rightarrow y, y \rightarrow z\} \subseteq F$

where $x, y, z \subseteq R$

N.B

Reflexive rule, Augmentation rule & Transitive rule are known as "Armstrong's inference rule" for Fds.

Armstrong's Inference rules are sound and complete.

IR 4: Decomposition Rule: If $\{x \rightarrow y\} \models \{x_1 \rightarrow y_1\}$ and $x = x_1, y = y_1$

$$\{x \rightarrow y\} \models \{x_1 \rightarrow y_1\} \quad x, y, x_1, y_1 \in R$$

then also $\{x_1 \rightarrow y_1\}$

IR 5: Union or additive Rule:

$$\{x \rightarrow y, \{x \rightarrow z\}\} \models \{x \rightarrow yz\} \quad x, y, z \in R$$

IR 6: Pseudo transitive Rule:

$$(x \rightarrow y, y \rightarrow z) \models \{wz \rightarrow z\} \quad x, y, z \in R$$

$$x, y, z \in R$$

e.g.: If $F = \{A \rightarrow B, B \rightarrow C, CD \rightarrow E\}$

$$A \rightarrow C \models IR3 \quad A \rightarrow C, F = \{A \rightarrow B, B \rightarrow C, A \rightarrow D, CD \rightarrow E\}$$

$$\frac{AD \rightarrow A, A \subseteq AD}{AD \rightarrow D} \quad A \rightarrow C \models IR1$$

Reflexive

$$A \rightarrow B, B \rightarrow C$$

$A \rightarrow C \models$ attribute closure

the other fols thus can be derived from the attributes.

Closure & Set of Functional Dependencies

The set of all functional dependencies that includes F & all the functional dependencies that can be inferred from F is known as closure of F .

$$F = \{A \rightarrow B, B \rightarrow C\} \quad \xrightarrow{\text{inferred from } F}$$

$$\{A \rightarrow B, B \rightarrow C, A \rightarrow C\}$$

Given set

F -cls

Closure of F (Closure set of F -cls) is represented by F^+

$F^+ = F \cup \{ \text{the set of f.cls that can be derived from } F \}$

e.g. $F = \{A \rightarrow B, B \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, CD \rightarrow E, AD \rightarrow BC\}$

A^+ = What other attributes can be derived from A .

and its called as

closure of A .

Attribute Context
Object

$$\Gamma = \{ A \rightarrow m, B \rightarrow c \}$$

Find Γ^+ .

Ans: consider $A \rightarrow B$

$$A \subseteq \Gamma$$

$$\Rightarrow \Gamma^+ = \Gamma B$$

Consider $B \rightarrow C$

$$B \subseteq \Gamma^+$$

$$\Rightarrow \underline{\Gamma^+ = \Gamma B C}$$

Γ can derive A	$A \rightarrow A$
Γ can derive B	$A \rightarrow m$
Γ can derive C	$A \rightarrow c$

Consider $B \rightarrow C$

$$B^+ = B$$

$$B \subseteq B$$

$$\underline{B^+ = BC}$$

- Q. Given a set of Fals $F = \{ A \rightarrow B, B \rightarrow C, CD \}$
 Find $\Gamma^+, B^+, A^+, B^+, AD^+, CD^+$

state ins'. Finding f_A^+ using

Consider $A \rightarrow B$

With $\{A\} \subseteq A$ $f_A^+ = f_A$ $f_A^+ \subseteq f_A$

(at most left) $f_A^+ = AB$ $f_A^+ \subseteq f_A$

Consider $B \rightarrow C$

$B \subseteq f_A^+$

$$\Rightarrow [f_A^+ = AB] \quad f_A^+ \text{ is project}$$

Finding f_B^+

Consider $B \rightarrow C$

$B \subseteq B$

$$\Rightarrow [B^+ = BC] \quad f_B^+ \text{ is project}$$

Finding f_D^+

Consider $D^+ = D$

Finding f_{AD}^+

Consider $A \rightarrow B$

$$AB^+ = ABCD \quad A \subseteq AB$$

Consider

$B \rightarrow C$

$$B \subseteq AB^+$$

$$AB^+ = ABCD$$

Finding f_{AD}^+

Consider $A \rightarrow B$

$$A \subseteq AD$$

$$B \subseteq AD^+$$

$$AD^+ = ABCD$$

$$\cancel{AD^+ = ABCDE}$$

$$AD^+ = ABCD$$

Consider $CD \rightarrow E$ ~~function~~ function

$$CD \subseteq AD^+$$

$$\Rightarrow AD^+ = ABCDEQR$$

Here AD is the
Key attribute

Finding CD^+

consider $CD \rightarrow E$

$$CD \subseteq CD\Theta$$

$$\Rightarrow CD^+ = CDE \leftarrow \Theta \text{ reflexive}$$

Q. Given $F = \{A \rightarrow BC, CD \rightarrow E, E \rightarrow C,$
 $D \rightarrow AEH, ABH \rightarrow BD,$
 $BH \rightarrow BC\}$

on $R(CAB, CDEH)$

Find $A^+, AE^+, AD^+, ABH^+, D^+$

Finding A^+

consider $A \rightarrow BC$

$$A \subseteq A^+$$

$$\Rightarrow A^+ = ABC$$

$$A \subseteq A^+ \text{ reflexive}$$

$$A^+ = A^+$$

$$\Rightarrow AD^+ = ADE$$

Consider $A \subseteq A$

Finding my D⁺

consider $D \rightarrow AEFH$

$$D \subseteq D$$

$$D^+ = D-AEFH$$

consider $A \rightarrow BCL$

$$A \subseteq D^+$$

$$D^+ = ABCLDEHF = R$$

Finding ~~AET⁺~~

$$\text{Initially } AET^+ = AE$$

Consider $A \rightarrow BCL$

+

$$A \subseteq AE$$

$$AET^+ = ABCE$$

consider $E \rightarrow C$

$$E \subseteq AET^+$$

Finding $\rightarrow AET^+ = ABCE \rightarrow AET^+ = ABCE$

Consider $D \rightarrow AEFH$

$$D \not\subseteq AET^+$$

$$\therefore AET^+ = ABCE$$

Finding AD^+

consider $A \rightarrow BCL$

$$A \subseteq AD$$

$$\Rightarrow AD^+ = ABCD \quad \Rightarrow AD^+ = ABCDE$$

consider $BH \rightarrow DC$

$$BH \not\subseteq AET^+$$

$$\Rightarrow AET^+ = ABCE$$

consider $DH \rightarrow DC$

$$DH \not\subseteq AET^+$$

$$\Rightarrow AET^+ = ABCE$$

Consider $D \rightarrow AEFH$

$$D \subseteq AD^+ \text{ (closed under union)}$$

$$\Leftrightarrow AD^+ = ABCDEFH = R$$

Defining BD^+

$$BD^+ = ABDEHF$$

$$BD^+ = ABCDEHF$$

Final $f(DH)$

$$ABH^+ = ABCDEHF = R$$

$$A^+ \subseteq ABE$$

$$B^+ \subseteq B$$

$$H^+ = H$$

$$AH^+ = ABCDE$$

$$BH^+ = BH$$

$$AB^+ = ABC$$

COVER :-

If set of f-cls F is said to cover another set of f-cls G if all the f-cls in G is in F^+ i.e. all the f-cls in G can be inferred from F .

Then we can say F covers G .

$$\text{e.g. } F = \{A \rightarrow B, B \rightarrow C, B \rightarrow D\}$$

$$G = \{A \rightarrow C, A \rightarrow D\}$$

check whether F covers G or not.

Ans: Consider $A \rightarrow C$ in G :-

Find A^+ under F

$$A^+ = A \cup CD$$

$\Rightarrow C \subseteq A^+$ follows by first

$\Rightarrow A \rightarrow C$ can be inferred from F . \rightarrow ①

Consider $A \rightarrow D$ in G :-

Find A^+ under F by 2nd method

$$A^+ = A \cup CD$$

$\Rightarrow D \subseteq A^+$ follows by first

$\Rightarrow A \rightarrow D$ can be inferred from F . \rightarrow ②

So from (1) and (2), all the f.d.s $A \rightarrow G$ can be inferred from F .

$\Rightarrow F$ covers G .

Equivalent Set of functional dependencies:-

Two sets of f.d.s F & G are equivalent if $F^+ = G^+$ i.e. all the f.d.s in G can be inferred from F and all the f.d.s in F can be inferred from G .

$$\text{i.e. } F \equiv G.$$

$$F = \{A \rightarrow B, B \rightarrow C, B \rightarrow D\}$$

$$G = \{A \rightarrow C, A \rightarrow D\}$$

Now we have to check whether F & G are equivalent or not.

Ans: Let's check whether F covers G .

Consider $A \rightarrow C$ in G :

Find A^+ under F
 $= ACD$

① $\rightarrow F$ is not symmetric
 $\Rightarrow C \subseteq A^+$

$\rightarrow A \rightarrow C$ can be inferred from F

Consider $A \rightarrow D$ in G :

Find A^+ under F
 $= ACD$

② F is not reflexive
 $\Rightarrow D \subseteq A^+$

$\rightarrow A \rightarrow D$ can be inferred from F . — (ii)

So from eqn ① to ②, all the fields of G can be inferred from F .

So F covers G — (iii)

Let us check whether G covers F :

Consider $A \rightarrow B$ in F :

Find A^+ under G
 $= ACD$

- $B \not\models A^+$ $\therefore F$ contains A^+ and B
- $\Rightarrow A \rightarrow B$ can't be inferred from F .
 - $\Rightarrow G$ can't cover F . \therefore $F \neq G$.

Q. Given $F = \{A \rightarrow B, A \rightarrow C, D \rightarrow AC, D \rightarrow E\}$

$$G = \{A \rightarrow BC, D \rightarrow AE\}$$

Check whether F & G are equivalent or not.

Ans: Let us check whether R covers G :-

Consider $A \rightarrow BC$ in G .

Find A^+ covers F

$$= ABC$$

$\Rightarrow BC \subseteq A^+$

$\Rightarrow A \rightarrow BC$ can be inferred from F . — (I)

Consider $D \rightarrow AE$ in G .

Find D^+ covers F

$$= DACEB$$

$\Rightarrow AE \subseteq D^+$

$\Rightarrow D \rightarrow AE$ can be inferred from F .

As (I) & (II) can be inferred from F L (1)

$\Rightarrow F$ covers G (III)

Now let's check whether G covers F :-

Consider $A \rightarrow B$ in F

Find A^+ under G

$$= ABC$$

$$\Rightarrow B \subseteq A^+$$

$\{ \Rightarrow A \rightarrow B$ can be inferred from G . iv

Consider $AB \rightarrow C$ in F

Find $A^+ B^+$ under G

$$= ABC$$

$$\Rightarrow C \subseteq A^+ B^+$$

$\Rightarrow AB \rightarrow C$ can be inferred from G . v

Consider $D \rightarrow AC$ in F

Find D^+ under G

$$= ACDEB$$

$$\Rightarrow AC \subseteq D^+$$

$\Rightarrow D \rightarrow AC$ can be inferred from G . vi

Consider $D \rightarrow E$ in F

Find D^+ under G

$$= ABCDE$$

$$\Rightarrow E \subseteq D^+$$

$\Rightarrow D \rightarrow E$ can be inferred from G . vii

So ~~first~~ $\text{eg} \quad \textcircled{I}, \textcircled{II}, \textcircled{V}, \textcircled{VI}$, \textcircled{VII} can be inferred from y .

So G covers $F \rightarrow \textcircled{VII}$

from y \textcircled{III} & \textcircled{VII} ,

$F \neq G$

④ Non-redundant covers:

Given a set of fds F .

Let redundant set of fds in F = Redundant

Non-redundant cover $F = F - \text{Redundant}$

Ex:- $F = \{A \rightarrow B, A \rightarrow C, B \rightarrow C\}$

Find non-redundant cover of F .

Ans:- Check whether $A \rightarrow B$ is redundant

Find A^+ under $F - \{A \rightarrow B\}$
 $= AC$

$\Rightarrow B \notin A^+$ under $F - \{A \rightarrow B\}$

$\therefore A \rightarrow B$ is non-redundant.

Check whether $A \rightarrow C$ is redundant

Find A^+ under $F - \{A \rightarrow C\}$

$= ABC$

$\Rightarrow C \in A^+$ under $F - \{A \rightarrow C\}$

$\therefore A \rightarrow C$ is redundant

$\therefore F = F - \{A \rightarrow C\}$

$\therefore F = \{A \rightarrow B, B \rightarrow C\}$

Check whether $B \rightarrow C$ is redundant.

Find B^+ under $F - \{B \rightarrow C\}$

$$= \cancel{B} B$$

$C \notin B^+$ under $F - \{B \rightarrow C\}$

$\Rightarrow B \rightarrow C$ is non-redundant in F .

Hence the non-redundant cover of

F is $F = \{A \rightarrow B, B \rightarrow C\}$

eg. Given $F = \{A \rightarrow B, C \rightarrow D, AC \rightarrow E, BD \rightarrow E\}$

Find the non-redundant cover of

F .

Ans:- check whether $A \rightarrow B$ is redundant

Find A^+ under $F - \{A \rightarrow B\}$

$$\Rightarrow A^+ = A$$

$A \rightarrow B \Rightarrow A^+ \not\Rightarrow B$

$\Rightarrow A \rightarrow B$ is non-redundant.

check whether $C \rightarrow D$ is redundant

Find C^+ under $F - \{C \rightarrow D\}$

$$\Rightarrow C^+ = \cancel{C} C$$

$$\Rightarrow D \not\in C^+$$

$\Rightarrow C \rightarrow D$ is non-redundant

check whether $AC \rightarrow E$ is redundant

Find g^+ under $F - \{AC \rightarrow E\}$

$$g^+ = \{B, C, D, E\}$$

$$\Rightarrow g^+ \subseteq g^t$$

$\Rightarrow g^t \rightarrow E$ can be inferred from $F - \{AC \rightarrow E\}$

$\Rightarrow AC \rightarrow E$ is redundant.

Now $F = \cancel{\{AC \rightarrow E\}} \cup \{A \rightarrow B, C \rightarrow D, BD \rightarrow E\}$

check whether $BD \rightarrow E$ is redundant

Find g^+ under $F - \{BD \rightarrow E\}$

$$g^+ = \{B, D, E\}$$

$$\Rightarrow E \notin g^+$$

$\Rightarrow BD \rightarrow E$ is non-redundant.

Thus the non-redundant cover

of F is given by $F = \{A \rightarrow B, C \rightarrow D, BD \rightarrow E\}$

LEFT-Reduction For Removing redundant attribute from the left hand side of F.O.

The Left-Reduction process is used to remove redundant attribute from L.H.S of each F.O. if the L.H.S contains more than one attribute.

Algorithm:
 not presentation each R.D. $b \rightarrow a$ in F .
 for each attribute $b \in X$
 of $\{f - f[x \rightarrow b] \cup \{x \rightarrow b\} \rightarrow f[x \rightarrow b]\}$
 Then replace
 $\{F \cup \{a \rightarrow b\} \cup \{f[x \rightarrow b]\}$

e.g. Given to do Left-Reduction with the
 following set of Fd's

$$F = \{A \rightarrow D, BC \rightarrow AD, C \rightarrow B, E \rightarrow A, E \rightarrow D\}$$

Check whether $BC \rightarrow D$ is redundant

$$\cancel{BC^+} = BC^+ \cap D^+ = \emptyset$$

Ans: Consider $BC \rightarrow AD$

~~Find B^+~~ Find B^+ under F .

$$\text{from } BC \rightarrow D \Rightarrow B^+ = B$$

now $C^+ \Rightarrow AD \cap B^+ = \emptyset$

Now Find C^+ under F .

$$C^+ = CB^+D$$

After left reduction the set is given by $F = \{A \rightarrow D, C \rightarrow AD, C \rightarrow B, E \rightarrow A, E \rightarrow D\}$

~~THE~~ THE CANONICAL COVER / MINIMAL COVER / MINIMAL SET OF FDs.

Step-1:

R.H.S of each F.D. should contain single attribute.

i.e. for each F.D. $x \rightarrow \{A_1, A_2, \dots, A_n\}$

in F can be represented as $\{x \rightarrow \{A_1\}, \{x \rightarrow \{A_2\}$

$\dots, \{x \rightarrow \{A_n\}\}$

Step-2:

Do left reduction from the set of F.D obtained from step-1.

Step-3:

Do find non-redundant cover from the set of F.D obtained from step-2.

Example

Q. Find the canonical / minimal cover of

$F = \{A \rightarrow D, B \rightarrow AD, C \rightarrow B, E \rightarrow A, E \rightarrow D\}$.

Ans: Step-1 (Right hand side of each F.D. should contain single attribute)

So. Now $F = \{A \rightarrow B, BC \rightarrow A, DC \rightarrow D, C \rightarrow B, E \rightarrow A, E \rightarrow D\}$

Step-2 (left reduction on the set of
all FD obtained from step-1)

Consider $BC \rightarrow A$

Given $B^+ \text{ and } \text{when } F$

Ans. $B^+ = B$ $\Rightarrow B^+ = B$ $\Rightarrow C \subseteq B^+ \text{ and } F \vdash C \rightarrow A$

$C \rightarrow A$ & B^+ was not in
given F

~~Now~~ $C \rightarrow A$ can be inferred from F .

Consider $\Rightarrow C^+ = ABCD$

$\Rightarrow A \subseteq C^+$

$\Rightarrow C \rightarrow A$ can be inferred.

Consider $BC \rightarrow D$

Given $B^+ = B$

Ans. $B^+ = B$ $\Rightarrow B^+ = B$ $\Rightarrow D \subseteq C^+$

$A \Rightarrow C^+ = ABCD$

$D \subseteq C^+$

$C \rightarrow D$ can be inferred.

It is clear that B is extensible
in $BC \rightarrow A$ as $DC \rightarrow D$.

So F can be

Now $F = \{A \rightarrow D, C \rightarrow A, C \rightarrow D, C \rightarrow B, E \rightarrow A, E \rightarrow D\}$

Step-3: Check whether $A \rightarrow D$ is redundant.

Find c^+ under $F - \{A \rightarrow D\}$

$$\Rightarrow c^+ = A$$

$$\Rightarrow D \notin c^+$$

$\Rightarrow A \rightarrow D$ is non-redundant.

Check whether $C \rightarrow A$ is redundant

Find c^+ under $F - \{C \rightarrow A\}$

$$\Rightarrow c^+ = CDB$$

$$\Rightarrow A \notin c^+$$

$\Rightarrow C \rightarrow A$ is non-redundant.

Check whether $C \rightarrow D$ is redundant

Find c^+ under $F - \{C \rightarrow D\}$

$$\Rightarrow c^+ = \cancel{ACBD}$$

$$\Rightarrow D \subseteq c^+$$

can be inferred from $F - \{C \rightarrow D\}$

$\Rightarrow C \rightarrow D$ is redundant in F .

Now $F = \{A \rightarrow D, C \rightarrow A, C \rightarrow B, E \rightarrow A, E \rightarrow D\}$

Check whether $C \rightarrow B$ is redundant

Find ~~the~~ c^+ under $F - \{C \rightarrow B\}$

$$\Rightarrow c^+ = ACB$$

$$\Rightarrow B \notin c^+$$

$\Rightarrow C \rightarrow B$ is non-redundant.

Check whether $E \rightarrow A$ is redundant

Find E^+ under $F = \{E \rightarrow A\}$

$$\Rightarrow E^+ = ED$$

$$\Rightarrow A \notin E^+$$

$\Rightarrow E \rightarrow A$ is non-redundant.

Check whether $E \rightarrow D$ is redundant.

Find E^+ under $F = \{E \rightarrow D\}$

$$\Rightarrow E^+ = EAD \rightarrow D \in E^+$$

$$\Rightarrow D \subseteq E^+$$

$\Rightarrow E \rightarrow D$ can be inferred from $F = \{E \rightarrow D\}$

$\Rightarrow E \rightarrow D$ is redundant

Now $F = \{A \rightarrow D, C \rightarrow A, C \rightarrow B, E \rightarrow A\}$

Thus the non-redundant cover of F is given by $F = \{A \rightarrow D, C \rightarrow A, C \rightarrow B, E \rightarrow A\}$

The canonical cover of F is $\{A \rightarrow D, C \rightarrow A, C \rightarrow B, E \rightarrow A\}$.

($\{A \rightarrow D, C \rightarrow A, C \rightarrow B, E \rightarrow A\}$ is not a canonical cover)

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N.D:- The canonical cover or minimal cover is also known as irreducible set of F.D.

Q. Find the minimal set of F.D

$$F = \{ B \rightarrow A, BD \rightarrow A, AB \rightarrow D \}$$

SOP:

Step-2: (Left-reduction)

consider $AB \rightarrow D$

Find A^+ under F

$$\Rightarrow A^+ = A$$

$$\Rightarrow D \notin A^+$$

Find B^+ under F

$$\Rightarrow B^+ = ABD$$

$$\Rightarrow D \subseteq B^+$$

$\Rightarrow B \rightarrow D$ can be inferred.

It is clear that A is extraneous in $AB \rightarrow D$

Now $F = \{ B \rightarrow A, D \rightarrow A, B \rightarrow D \}$

$$\text{Now } F = \{ B \rightarrow A, D \rightarrow A, B \rightarrow D \}$$

Step-3 (non-redundant)

Check whether $B \rightarrow A$ is redundant.

Find B^+ under $F - \{B \rightarrow A\}$

$$\Rightarrow B^+ = BDA$$

$$\Rightarrow A \subseteq B^+ \text{ (A is a part of } B^+)$$

$\Rightarrow B \rightarrow A$ can be inferred from $F - \{B \rightarrow A\}$

$\Rightarrow B \rightarrow A$ is redundant in F .

Now $F = \{D \rightarrow A, B \rightarrow D\}$

Check whether $D \rightarrow A$ is redundant

Find D^+ under $F - \{D \rightarrow A\}$

$$\Rightarrow D^+ = \cancel{D} D$$

$$\Rightarrow + \neq D^+$$

$\Rightarrow D \rightarrow A$ is non-redundant.

check whether $B \rightarrow D$ is redundant

Find B^+ under $F - \{B \rightarrow D\}$

$$\Rightarrow B^+ = B$$

$$\Rightarrow D \not\subseteq B^+$$

$\Rightarrow B \rightarrow D$ is non-redundant.

So the canonical cover is minimal cover
 $F = \{B \rightarrow D, D \rightarrow A\}$

Key Finding Algorithm

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→ T

→ Take different combinations of attribute present → the said combination is called a candidate key (provided the set shouldn't contain any extraneous attribute).

Q. Given $R(a, b, c, d, e, f)$

$$F = \{ A \rightarrow BC, CD \rightarrow E, E \rightarrow C, D \rightarrow AEH, ABH \rightarrow BD, BH \rightarrow BC \}$$

Find the candidate keys of R / keys of R.

Ans:

Consider $A \rightarrow BC$

$$A^+ = A \cup BC$$

$$CD^+ = ACD \cup H = R$$

$$E^+ = EC$$

$$D^+ = AEDBC = R$$

(If $D^+ \supseteq D$, then D is a key.)

$$ABH^+ = ABHCD$$

$$A^+ = ABC \neq R$$

$$H^+ = H \neq R$$

$$B^+ = B \neq R$$

$A^0 - \{ABC\} + R$ and $\{AHT\} = R$

$$BH^+ = ABCH$$

$\Rightarrow AHT$ is a key.

Hence candidate keys of R are AHT .

- X. Given a Relation $BOOK$ (Book-title, author-name, mention, book-type, list-price, author-affil, publisher)

Find a set of rule is given by

$$F: \{Book_title\} \rightarrow \{Book_type, Publisher\}, \{Book_type\} \rightarrow \{list_price\}$$
$$\{Author_name\} \rightarrow \{Author_affil\}$$

Find the key.

Ans. $\{Book_title\}^+ = \{Book_title, Publisher, Book_type, list_price\} \neq Book$

$$\{Book_type\} = \{list_price, Book_type\} \neq Book$$

$$\{Author_name\} = \{Author_name, Author_affil\} \neq Book$$

METHOD #2

- Finds the attribute present in L.H.S of each F.Ds in F. (if any)
 - Finds the attributes present in R.H.S of each F.Ds in F.
 - Finds the attribute present in both the sides of F.Ds is F.
 - Finds the attributes which are present only in the R.H.S.
(R.H.S - Both the sides)
 - The attributes which are present only in the R.H.S can't be part of any key.
 - Finds the attribute which are present only in the L.H.S.
(L.H.S - Both the sides)
there too cases arises
- Case - I
- Take different combinations of attribute present only in the L.H.S.
- of the closer of these attributes = R, these set of attributes are the Key.

Case-2

(If case-1 is not satisfied)

Take different combinations of attributes L.H.S. and both the sides of F.Ds. in R.F. and

If closer set of the attributes $\subseteq R$,
then these set of attributes are
keys.

Ans : L.H.S : $\{ \text{Book-title}, \text{Book-type}, \text{Author-name} \}$

R.H.S : $\{ \text{Book-type} \}$

only L.H.S = $\{ \text{Book-title}, \text{Author-name} \}$

$\{ \text{Book-title}, \text{Author-name} \} \rightarrow \{ \text{Book-type} \}$

Q₂: R(M, Y, P, MP, C)

$$F = \{ \{M\} \rightarrow \{MP\}, \{m, Y\} \rightarrow \{P\}, \{MP\} \rightarrow \{C\} \}$$

Find keys.

$$\text{Soln: } \{MP^+\} = \{MP\} \neq R$$

$$\{M, Y\}^+ = MPYC \neq R$$

$$\{MP\}^+ = MPC \neq R$$

$$\{Y^+\} = Y + R$$

\Rightarrow MY is a key (Primary key)

Q₃: R(A, B, C, D, E, F)

$$F = \{ C \rightarrow F, E \rightarrow A, EC \rightarrow D, A \rightarrow B \}$$

Find keys?

$$\text{Soln: } \{C^+\} = \{CF\} \neq R \quad EC^+ = EA \neq R$$

$$E^+ = EA \neq R \quad A^+ = AB \neq R$$

$$C^+ = CF \neq R$$

Hence ECT is the key.

Q4.

Book (Book-title, Author-name, Book-type,
List-Price, Author-affil, Publisher)

$$F = \{ \{ \text{Book-title} \} \rightarrow \{ \text{Book-type}, \text{Publisher} \}, \\ \{ \text{Book-type} \} \rightarrow \{ \text{List-Price} \}, \\ \{ \text{Author-name} \} \rightarrow \{ \text{Author-affil} \} \}$$

Solⁿ:

$$\cancel{\{ \text{Book-title} \}}^+ = D_B$$

L.H.S

$$\{ \text{Book-title}, \text{Book-type}, \text{Author-name} \}$$

Both

$$\{ \text{Book-type} \}$$

Only LHS

$$\{ \text{Book-title}, \text{Author-name} \}$$

$$\{ \text{Book-title}, \text{Author-name} \}^+$$

= R

Q5. $R(A, B, C, D, E, H)$. Find the key.

$$F = \{ A \rightarrow B; B \rightarrow D, E \rightarrow C, D \rightarrow AH \}$$

LHS:

$$A^+ = \{ AB \} \neq R$$

$$B^+ = BCDAH \neq R$$

$$E^+ = C \neq R$$

$$D^+ = AHDDB \neq R$$

$$\{ HADBD, AHDDB, HDABD, AHDDB \} \neq R$$

LHS

$$\{ \cancel{A}, \{ B, C, E, D \} \} \neq R$$

RHS

$$\{ \cancel{B}, \cancel{D}, \cancel{C}, \cancel{AH} \} \{ \cancel{D}, \cancel{B}, \cancel{A}, \cancel{C} \}$$

Only LHS

$$\{ A / BC / E \}$$

$$\{ A, BC \}^+ = ABCDH \neq R$$

$$\{ BC, E \}^+ = BCBH \neq R$$

$$\{ A, E \}^+ = ABCDH = R$$

So $\{ A, E \}$ is the key.

Q.6 $R(A, B, C, D, E, H)$

$$F = \{ A \rightarrow B, B \leftarrow C, E \rightarrow C, D \rightarrow H \}$$

$$\text{1}^{\text{st}} \text{EF} = ABCDEH = R$$

~~AEH~~ is the key
~~EDH~~ ~~BTH~~

Q.5. $R(A, B, C, D, E, H)$

$$F = \{ A \rightarrow B, B \leftarrow C, E \rightarrow C, D \rightarrow AH \}$$

Neither
Say n:

$$L+L^+ = \{ A, B, C, E, D \}$$

Both the side: $\{ A, B, C, D \}$

$$A^B^+ = AB \neq R$$

$$A^C^+ = ACBDH \neq R$$

$$\boxed{A^E^+ = ABCDHE = R}$$

$$A^D^+ = ADH \neq R$$

$$B^C^+ = ABCDH \neq R$$

$$B^D^+ = AHBHD \neq R$$

$$C^D^+ = ABDCH \neq R$$

$$\boxed{E^D^+ = ADHEBC = R}$$

$$\boxed{B^E^+ = ABCDEH = R}$$

$$C^E^+ = CE \neq R$$

∴ the keys are $\{ AE \}, \{ ED \}, \{ BE \}$

NORMALISATION

Process of decomposition of complex relations into smaller relations.

Assignment

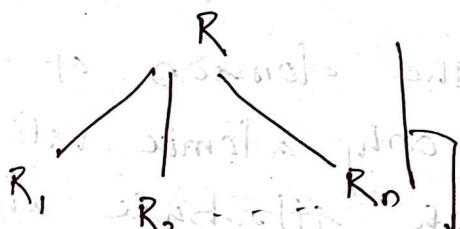
- ① What are the anomalies discuss each anomaly with example.

→ Normalisation is the process to decomposing a "complex ref" into smaller relation based on normal form const's

→ The goal of normalisation is to minimise

- i) minimising redundancy
- ii) avoids anomalies

- Insert anomalies
- update anomalies
- delete anomalies



→ This process of decomposition

is known as normalisation.

The reverse process of normalisation

is denormalisation.

DENORMALISATION!

The reverse process of normalisation

is de-normalisation.

→ getting the original reln by joining the decomposed rel's is known as denormalization.

Different Normal forms are :-

- Based on functional dependencies:
 - First normal form (1NF)
 - Second Normal Form (2NF)
 - Third Normal Form (3NF)
 - Boyce Codd Normal Form (BCNF)
 - Fourth Normal Form (4NF) { Based on multivalued dependencies.
Join on dependencies }
 - Fifth Normal Form (5NF)

FIRST NORMAL FORM (1NF)

(It does not allow)

It states that the domains of an attribute must exclude only atomic values and the value of each attribute in a tuple must be a single value from its domain in a relation R.

1NF does not permit composite and multivalued attributes or their combinations for a tuple in a relation R.

→ Prime attribute :-
An attribute of a reln R is said to be a prime attribute candidate if it is part of any key of R.

e.g. If the R $\{A, B, C, D\}$

and $\{A, B\}$ is the key

then prime attributes are $\{A, B\}$

⇒ Full functional dependency :-

If function dependency $X \rightarrow Y$ is known as full F.D. if removal of any attribute $\{a\}$ from X does not hold the F.D. any more.

i.e. $X - \{a\} \rightarrow Y$ does not hold F.D.
(Here X is a set)

⇒ Trivial Functional Dependency :-

If F.D. $X \rightarrow Y$ is said to be trivial if $Y \subseteq X$.

It is non-trivial if $Y \not\subseteq X$.

SECOND NORMAL FORM (2NF)

It is based on the concept of Prime attribute and Full F.D.

Def": A Relation is said to be in 2NF if

i) It is in 1NF.

ii) Every non-prime attribute of R is fully F.D on any key of R.

e.g. Given a Relation EMP_PROJECT

(Eeef , Pro , hours , ename ,

Prname , Ploc)

and a set of F.Ds F is given by

$\{\text{Eeef}, \text{Pro}\} \rightarrow \{\text{hours}\}$

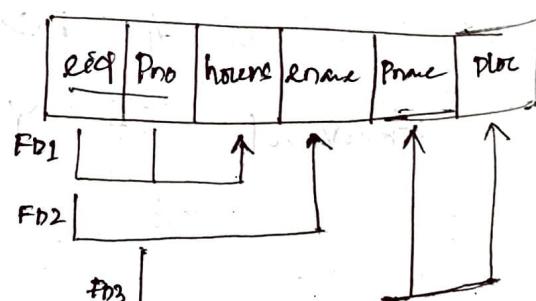
$\{\text{Eeef}\} \rightarrow \{\text{ename}\}$

$\{\text{Pro}\} \rightarrow \{\text{Prname}, \text{Ploc}\}$

decompose the above refⁿ to 2NF refⁿ.

Ans:

Key $\{\text{Eeef}, \text{Pro}\}$



First you have to find out the key by applying finding algorithm, we have the key = $\{\text{Eeef}, \text{Pro}\}$

- Hence FD₁ i.e. {Eod, Pro} → {Hours} establishes 2NF conditions as well as the non-prime attribute Hours} is fully functional dependent on the key {Eod, Pro}
- FD₂ i.e. {Eod} → {Sname} violates 2NF conditions as {Sname} partially dependent on the key.
- FD₃ i.e. {Pro} → {Pname, Ploc} violates 2NF conditions as {Pname, Ploc} partially dependent on the key.

By decomposing we have EMP + PROJ

EMP - PROJ2

Eod	Ename
-----	-------

so EMP PROJ

thus PROJ

EMP PROJ2

EMP - PROJ3

Pro	Pname	Ploc
-----	-------	------

Q. R(A, B, C, D, E, F, G, H, I, J)

$$LUF = \{A \rightarrow C, A \rightarrow DE, B \rightarrow F, F \rightarrow GH, D \rightarrow IJ\}$$

decompose the above reln in 2NF
reln?

$$\text{Soln: } A B^+ = A B F D E G H I J C = R$$

$$A^+ = A D E I J + R$$

$$B^+ = B F G H + R$$

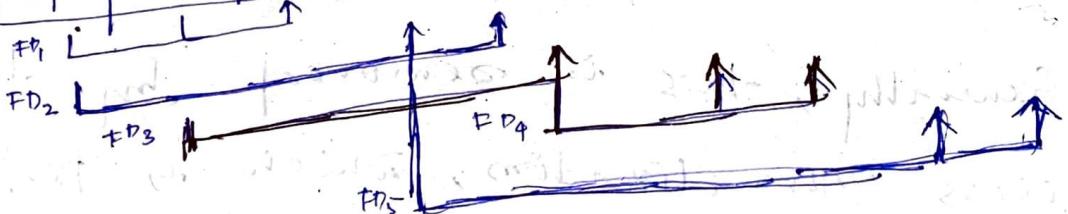
$$F^+ = F G H + R$$

$$D^+ = D I J + R$$

} FD₁ A → C does
not violate
2NF cond's

A B⁺ is the key.

A	B	C	D	E	F	G	H	I	J
---	---	---	---	---	---	---	---	---	---



By decomposing, we have

R_1

A	b	c
L	↑	↑

A	D	E	I	J
L	↑	↑	↑	↑

R_2

A	D	E	I	J
L	↑	↑	↑	↑

R_3

B	F	G	H
L	↑	↑	↑

R_3

B	F	G	H
L	↑	↑	↑

$R_1(A, B, C)$, $R_2(A, D, E, I, J)$, $R_3(B, F, G, H)$ $\downarrow 2NF$

Q. What

Ans: Database anomaly is normally the flaw in databases which occurs because of poor planning & storing everything in a flat database.

→ Generally, this is removed by the process normalization, which is performed by splitting / joining of tables.

There are 3 types of anomalies

- (i) Insertion anomaly
- (ii) Update anomaly
- (iii) Deletion anomaly

(i) Insertion anomaly

→ An insertion anomaly occurs when we are not able to insert certain attribute in the database without

Third Normal Form (3NF)

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It is based on the concept of transitive dependency.

Def': If relation is in 3NF
it satisfies

- it is in 2NF
- No non-prime attribute is transitively dependent on the Primary key.

Q. R(A,B,C,D,E,F,I,J)

$$F = \{ AB \rightarrow C, A \rightarrow DE, B \rightarrow F, F \rightarrow G, F \rightarrow I, J \}$$

decompose R into 3NF.

Ans:

$$\text{Key} = \{ A, B \}$$

Decomposing R into 2NF

FD₁ AB → C does not violate 2NF condition.

FD₂ A → DE does not violate 2NF condition.

FD₃ B → F violates 2NF condition.

Decomposing R_1 into 3NF we have

R_1	A B C
FD_1	↓ ↓ ↑

R_2	A D E I J
FD_2	↓ ↑ ↑ ↑ ↑

R_3	D F G H
FD_3	↓ ↑ ↑ ↑

$R_1(AB \rightarrow C)$ satisfies 3NF.

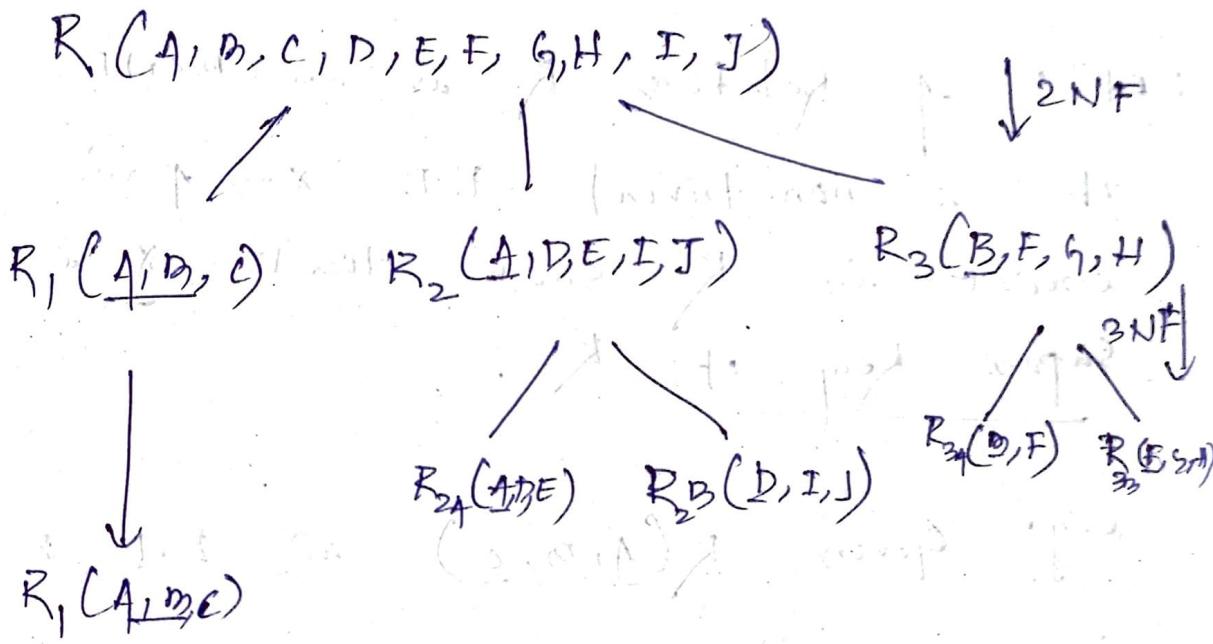
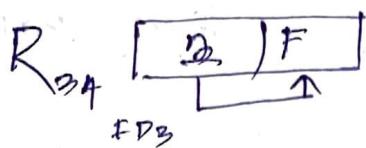
$R_2(A, B, E, I, J)$ does not satisfy 3NF as transitive dependency because of $A \rightarrow DE, B \rightarrow IJ$.
after decomposing R_2 into 3NF we have

R_{2A}	A D E
	↓ ↓ ↑

R_{2B}	D I J
	↑ ↑ ↑

$R_3(D, E, G, H)$ does not satisfy 3NF as transitive dependency because of $D \rightarrow F, F \rightarrow G, H$.

Decomposing R_3 into 3NF we have



General def' of 3NF

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A relation R is in 3NF if
a non-trivial F-D $X \rightarrow Y$ exists in R
such that
either (i) X is a super key
or (ii) Y is a prime attribute

BCNF (Boyce Codd Normal Form)

It is most strict ~~form~~ than
3NF and it is simpler than 3NF
also.

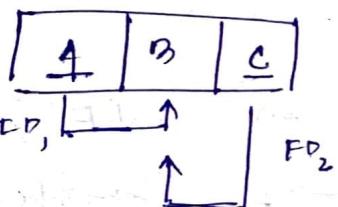
Every BCNF is 3NF but every 3NF
is not in BCNF

Segment 19

Discuss 3NF and BCNF and show that BCNF is stronger than 3NF.

Defn: If Relation R is in BCNF if a non-trivial F.D $x \rightarrow y$ is present in R such that x is a super key of R.

e.g. Given R(A, B, C) and F.D F is given by $F = \{A \rightarrow B, C \rightarrow B\}$



Hence FD₁, i.e. $A \rightarrow B$ does not violate 3NF condition as A is a key.

FD₂, $C \rightarrow B$ does not violate the 3NF condition because C is a key.

So the reln is in 3NF.

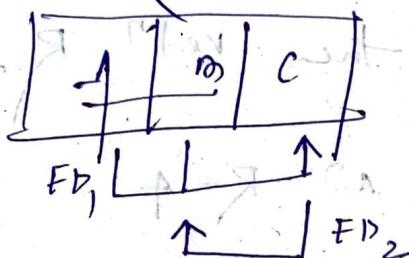
FD₁ and FD₂ does not violate BCNF condition because A is a key and C is a key so that the reln

R is in BCNF.

e.g. Given $R = (A, B, C)$ w.r.t. FD's given

by $F = \{A \rightarrow B, C \rightarrow B\}$ find

whether it is in BCNF or not.



$$FD_1 = \{A \rightarrow B\} \quad FD_2 = \{C \rightarrow B\}$$

\Rightarrow the rel' is not in BCNF because

FD_2 violates BCNF condition as

C is not a key

\Rightarrow But the rel' is in 3NF

Because here FD_1 satisfy the 3NF

cond' as A is the key and

FD_2 satisfies 3NF cond' as

B is a prime attribute

So here this rel' is in 3NF

But not in BCNF.

BCNF DECOMPOSITION PROCESS :-

Given a Relation R as a set

of F.D. We have to decompose

R in BCNF

Step-1 : Identify the dependencies which violates the BCNF conditions with R not consider that Σ as $X \rightarrow A$.

Step-2 : Decompose the reln R into XA (i.e. $\{X\} \cup \{A\}$) and $R - A$

Step 3 : Validate if A is in the decomposed items are in BCNF or not.

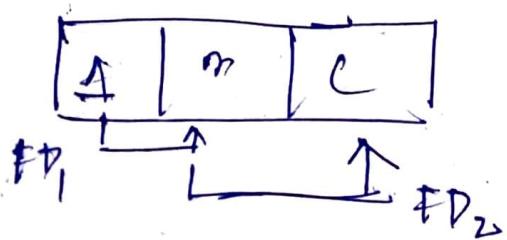
If not then apply the algorithm of step-2 on the decomposition item that is not in BCNF.

It gives $R(A, B, C)$ as F is $R = \{A \rightarrow B, B \rightarrow C\}$ is R in BCNF if not decompose it into BCNF.

Sol :

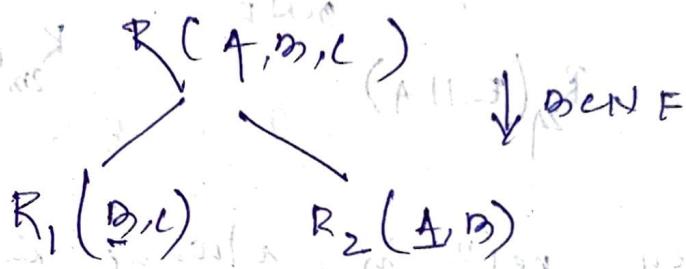
$$A^+ = \{A, B, C\} \subseteq R$$

Key = {A}



F_D_1 does not violate BCNF as
 f is the key.

F_D_2 violates BCNF condition as B is
not a key.



④ Rel² having two attribute is in BCNF.

All Given $R(A, B, C, D, E, F)$, AD, F on R
is given by $F = \{A \rightarrow BC, E \rightarrow HA\}$
so whether the rel² is in BCNF if not
decompose it into BCNF.

$$A^+ = \{A, B, C\}$$

$$E^+ = \{A, EH, BC\}$$

so the key is DE

A	B	C	D	E	H
↑	↑			↑	

F_D_1 is $A \rightarrow BC$ violation BCNF
Condition as A is not a key.

$R(A, B, C, D, E, H)$

Q

$\rightarrow BCNF$
violation

$R_1(A, B, C)$

$\rightarrow BCNF$

$R_2(A, D, E, H)$

$\rightarrow BCNF$
violation

$R_3(E, H, A)$

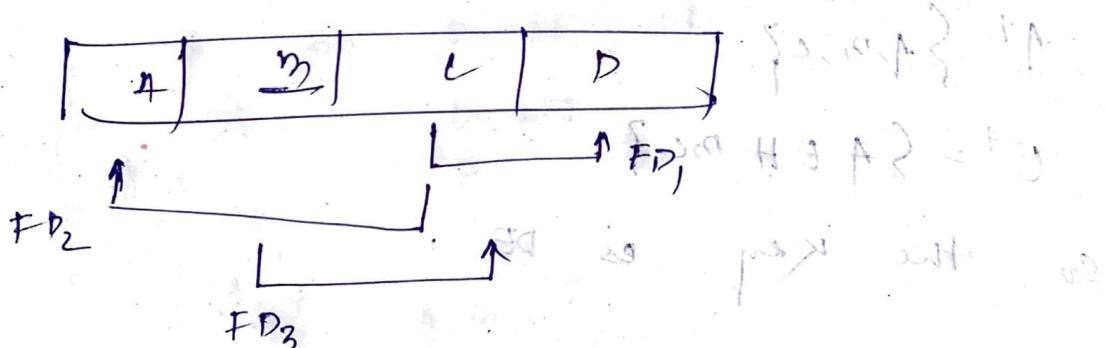
$R_4(D, E)$

* all key relns are always in BCNF
Means all the attributes in key

$R(A, B, C, D)$ & FDs $F = \{C \rightarrow D, C \rightarrow A, B \rightarrow C\}$
as R is in BCNF.

$D^+ = \{C, D, A, B\}$

Key is $\{B\}$

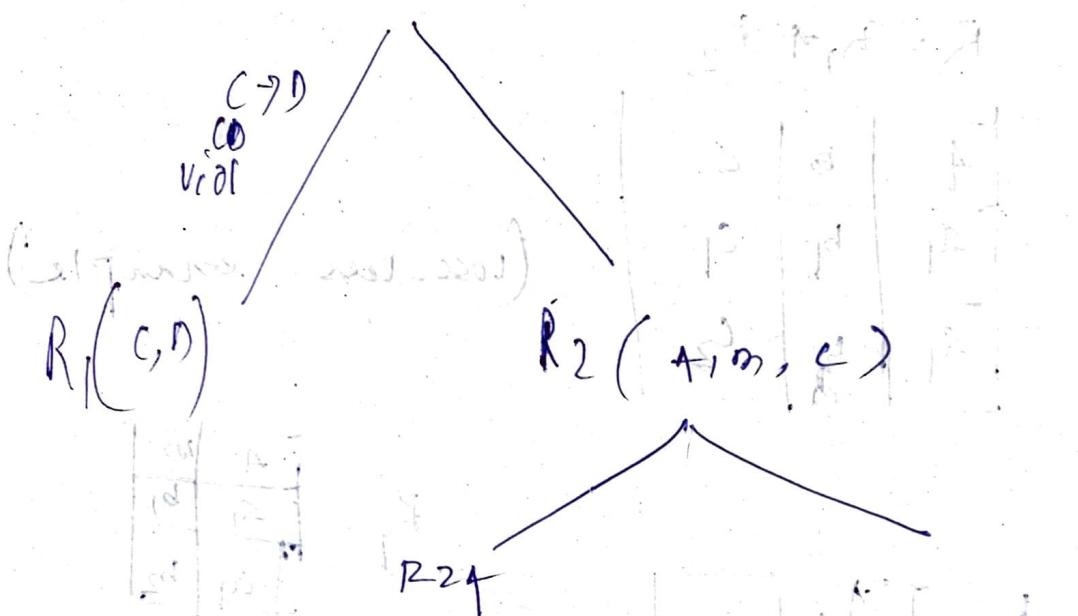
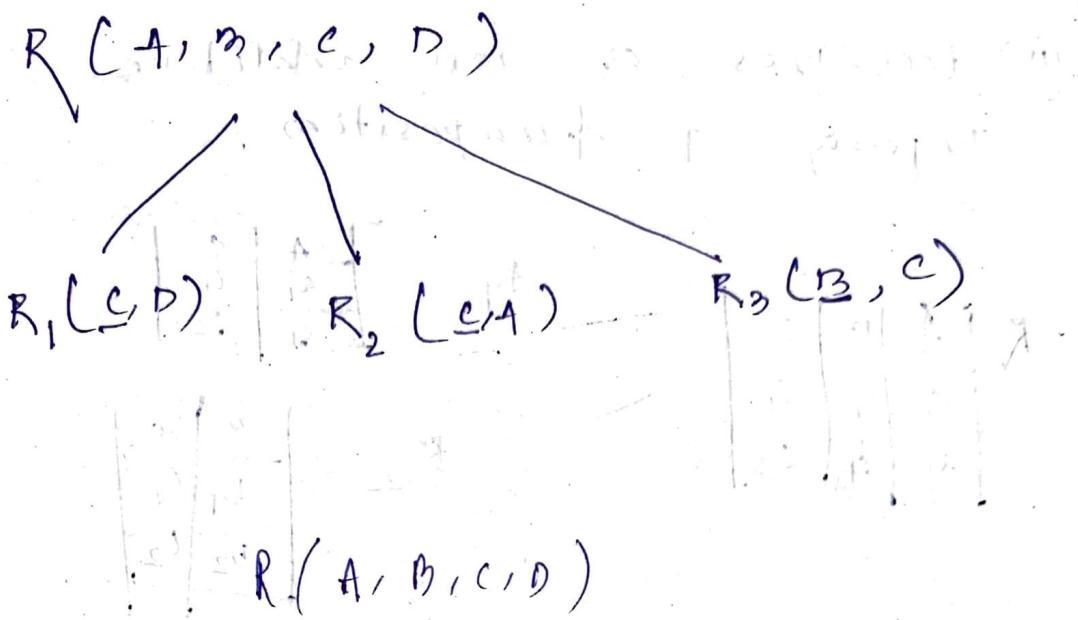


So here FD_1 & FD_2 violates

BCNF cond'n as C is not a key.

The red portion describes part

of part A (so in part A is contained)



Properties of Decomposition

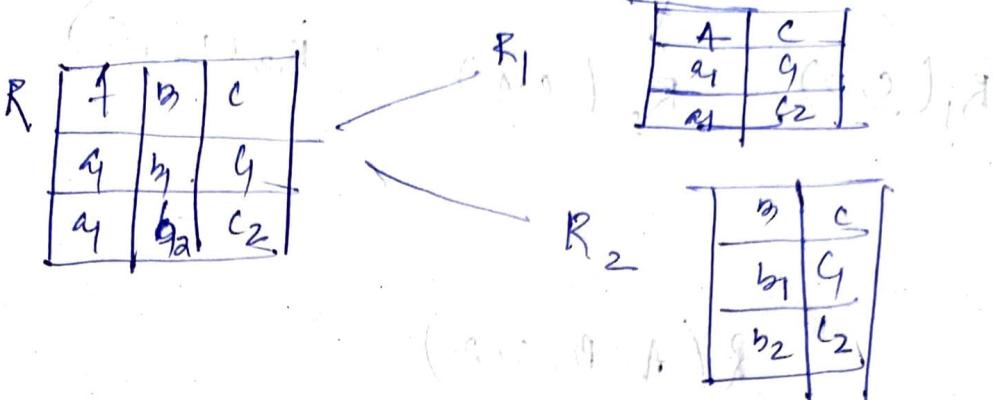
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Let R be a relation and R can be decomposed into a set of relations $D = \{R_1, R_2, \dots, R_n\}$ w.r.t a set of f.o. of some decomposition algorithm.

The decomposition D should satisfy the following properties.

- (1) Dependency preserving scheme of decomposition.

(11) loss-less or non-redundant
property + decomposition:



$$R = R_1 \# R_2$$

A	B	C
a ₁	b ₁	c ₁
a ₂	b ₂	c ₂

(loss-less example)

A	B	C
a ₁	b ₁	c ₁
a ₂	b ₂	c ₂

A	B
a ₁	b ₁
a ₂	b ₂

A	C
a ₁	c ₁
a ₂	c ₂

A	B	C
a ₁	b ₁	c ₁
a ₂	b ₂	c ₁
a ₃	b ₁	c ₂
a ₄	b ₂	c ₂

- V.V. gmp
- ① Whether a decomposition is reversible or not.
 - ② Whether a decomposition is lossless,

~~WV and~~ Loss-less Joins Property or Non-additive
Joins Property.

- ④ Every 3NF is dependency preserving but may not satisfy loss-less.
- ⑤ Every BCNF is loss-less but may not satisfy dependency.

Generally, a decomposition D should cause a non-additive or loss-less join property if no starless tuple (e.g. extra tuple that is not in the original rel') are generated when a natural join operation is applied to a decomposed relation.

Formally, a decomposition D which is $D = \{R_1, R_2, \dots, R_n\}$ of R , has the loss-less join or non-additive join property if for every $\pi(F)$ a set of F , if for every rel' state $w(R)$ that satisfy the following note where $\#$ is the natural join operation

$$T(r) = T_{R_1}(r) + \dots + T_{R_n}(r) = r(R)$$

(VVV group)
Ex:

Given R (ecol, ename, Pno, Ploc, hours)

$F = \{ \text{Stock, Name} \}, Pno$

$\{Pno\} \rightarrow \{Pname, Ploc\}$

$\{\text{ecol, Pno}\} \rightarrow \{\text{Hours}\}$

and the decomposition $D = \{R_1, R_2, R_3\}$ is given by

$R_1(\text{ecol, ename})$

$R_2(Pno, Pname, Ploc)$

and $R_3(\text{ecol, Pno, hours})$

Check whether the decomposition D is lossless.

Ans:

Initial matrix

R_0	ecol	ename	Pno	Pname	Ploc	hours
R_1	a_1	a_2	b_{13}	b_{14}	b_{15}	b_{16}
R_2	b_{21}	b_{22}	a_3	a_4	a_5	b_{26}
R_3	a_1	b_{32}	a_3	b_{34}	b_{35}	a_5

FINAL MATRIX (by considering P.D.F)

	a_{11}	a_{12}	b_{13}	b_{14}	b_{15}	b_{16}
R_1	a_1	a_2				
R_2	b_2	b_{22}	a_3	a_4	a_5	b_{26}
R_3	a_1	b_{32}	a_2	a_3	b_{34}	a_5

N.B.

If any one row contains all the a values, the decomposition is lossless otherwise, the decomposition is lossy.

Here the last row contains all the a values so this implies the decomposition is lossless.

Q/ R(ABCDHG)

$$F = \{ AB \rightarrow C, AC \rightarrow B, AD \rightarrow E, B \rightarrow D, BC \rightarrow A, E \rightarrow G \}$$

$$D = \{ AB, BC, AD \rightarrow E, EG \}$$

Initial matrix

Ans

	A	B	C	D	E	G
R_1	a_1	a_2	b_{13}	b_{14}	b_{15}	b_{16}
R_2	b_2	a_2	a_3	b_{24}	b_{25}	b_{26}
R_3	a_1	a_2	b_{32}	a_4	a_5	b_{36}
R_4	b_{41}	b_{42}	b_{43}	b_{44}	a_5	a_6

Range uniform

$A \rightarrow D$
 $E \rightarrow G$

	A	B	C	D	E	G
R ₁	a ₁	a ₂	b ₁₃	b ₁₄ a ₄	b ₁₅ a ₅	b ₁₆ a ₆
R ₂	b ₂₂	a ₂	a ₃	b ₂₄ a ₄	b ₂₅ a ₅	b ₂₆ a ₆
R ₃	a ₁	a ₂	b ₃₃	a ₄	a ₅	b ₃₆ a ₆
R ₄	b ₄₁	b ₄₂	b ₄₃	b ₄₄	a ₅	a ₆

st. is lossy.

if R(A B C D E G)

$\{AB \rightarrow C, AC \rightarrow D, AD \rightarrow E, B \rightarrow D,$
 $BC \rightarrow A, E \rightarrow G\}$

D = {A B C, A C D E, A D G ?}

	A	B	C	D	E	G
R ₁	a ₁	a ₂	a ₃	b ₁₄	b ₁₅	b ₁₆
R ₂	a ₁	b ₂₂	a ₃	a ₄	a ₅	b ₂₆
R ₃	a ₁	b ₃₂	b ₃₃	a ₄	b ₃₅	a ₆

A	B	C	D	E	G
a ₁	a ₂	a ₃	a ₄	a ₅	b ₁ b ₂ a ₆
a ₁	b ₂ a ₂	a ₃	a ₄	a ₅	b ₂ a ₆
a ₁	b ₂ a ₂	b ₂ a ₃	a ₄	b ₂ a ₅	a ₆

It is loss-less.

A	B	C	D	E	G
a ₁	a ₂	a ₃	a ₄	a ₅	b ₁ b ₂
a ₁	a ₂	a ₃	a ₄	a ₅	a ₂ b ₁ a ₆
a ₁	b ₂ a ₂	b ₂ a ₃	a ₄	b ₂ a ₅	a ₆

It is lossless.

Sheet 9
Multivalued Dependency

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TRANSACTION PROCESSING

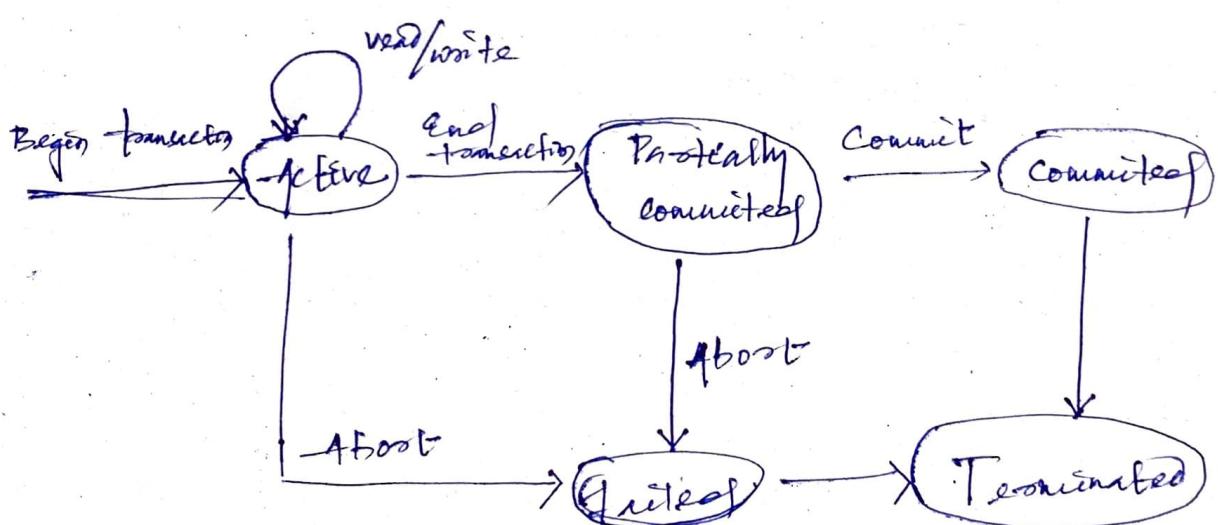
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* Transaction is a logical unit of database processing.

The operations that characterizes the transaction are

- (i) Read()
- (ii) Write()
- (iii) Commit
- (iv) Abort

Transaction states :



Active state :-

When the instructions of the transaction are running then the transaction is in active ~~stage~~ state. If all the 'read and write' operations are performed without any error then

it goes to the "Partially committed state", if any transaction fails it goes to the failed state.

Partially committed state :-

After completion of all the read and write operation the changes we made in user memory. If the changes we made permanent on the database the state will change to "committed state" and in case of failure it will go to the "failed state".

Failed state :-

When any instruction of the transaction fails, it goes to the "failed state" or if failure occurs in making a permanent change of data on database.

Committed state :-

It is the state when the changes we made permanent on the database and the transaction is completed and therefore terminated as the "terminated state".

Terminated state :-

If there is not any roll back in the transaction comes from the "committed state", then the system is consistent and ready for new transaction and the old transaction is terminated.

Properties of transaction

A - Atomicity

C - Consistency Preserving

I - Isolation

D - Durability

Atomicity: It is difficult to separate the effect of a transaction from the rest of the database. If one part of a transaction fails, then the whole transaction fails.

→ Transaction is as atomic unit of processing it should either be performed in its entirety or not. If performed at all, then it must be successful.

Consistency Preserving :-

→ Transaction should be Consistency Preserving meaning that it is completely executed from beginning to end and it should take the database from one Consistency state to another.

Isolation :-

→ Transaction should appear as though it is been executed by itself from other transactions even those many transactions are executed concurrently. That means the execution of a transaction

should not be interleaved, ~~with~~ by my other transactions executed concurrently.

Durability: The changes applied to the database by a committed transaction must persist in the database. These changes must not be lost because of my failure.

Schedule/History of Transaction:-

<u>T₁</u>	In which order operations of the transaction are executed.
read(x);	read() → r
$x = x - N$	
write(x)	write() → w
read(y);	read() → r
$y = y + k$	
read(z);	read() → r
$w = w + y$	
commit	commit → c
abort	abort → a

Sequence: $r_1(x); w_1(x); r_1(y); r_2(z); w_1(y); c; a$

T_1	T_2
read(x)	
	read(y)
	$y = y + k$
	write(y)
$x = x - N$	
write(x)	
read(z)	
	read(x)
	$x = x + M$
	write(x)
	abort
Commit	

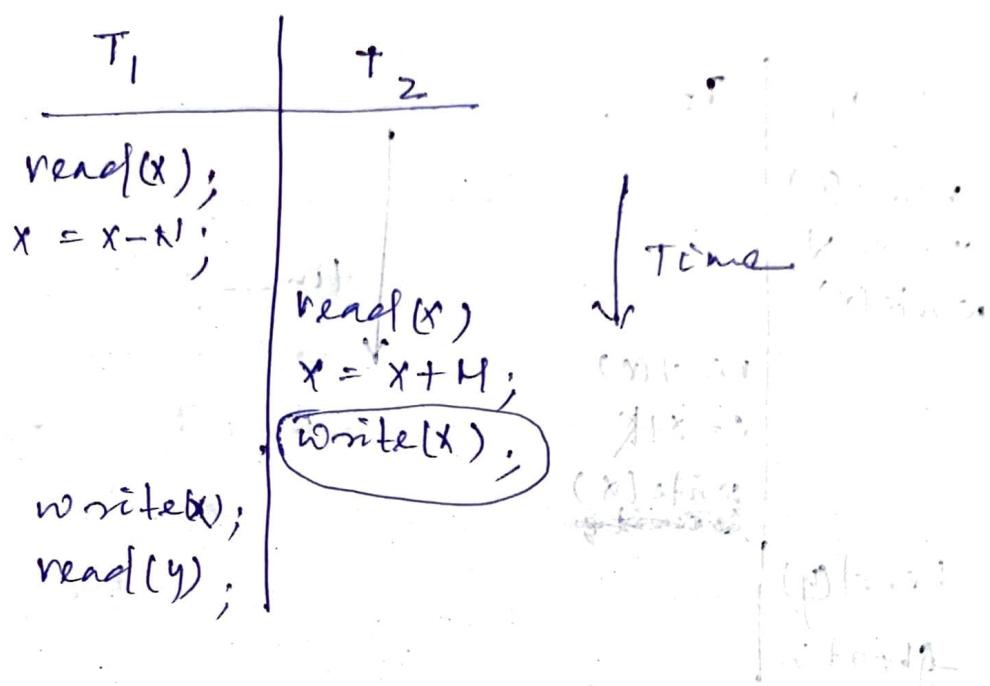
$S : r_1(x), r_2(y) ; w_2(y) ; w_1(x) ; r_1(z) ; r_2(x) ; w_2(x) ; q ; q$

CONCCURRENT TRANSACTION :-

→ When the transactions are executed simultaneously, it is known as concurrent transactions.

- When concurrent transactions are executed in an uncontrolled manner, different problems arises such as
 - Lost update problem (Crump)
 - Dirty read / Temporary update problem
 - Incorrect summary problem

LOST UPDATE PROBLEM :-



Consider $x = 50$

Value of x after T_1 will be $50 - 10 = 40$

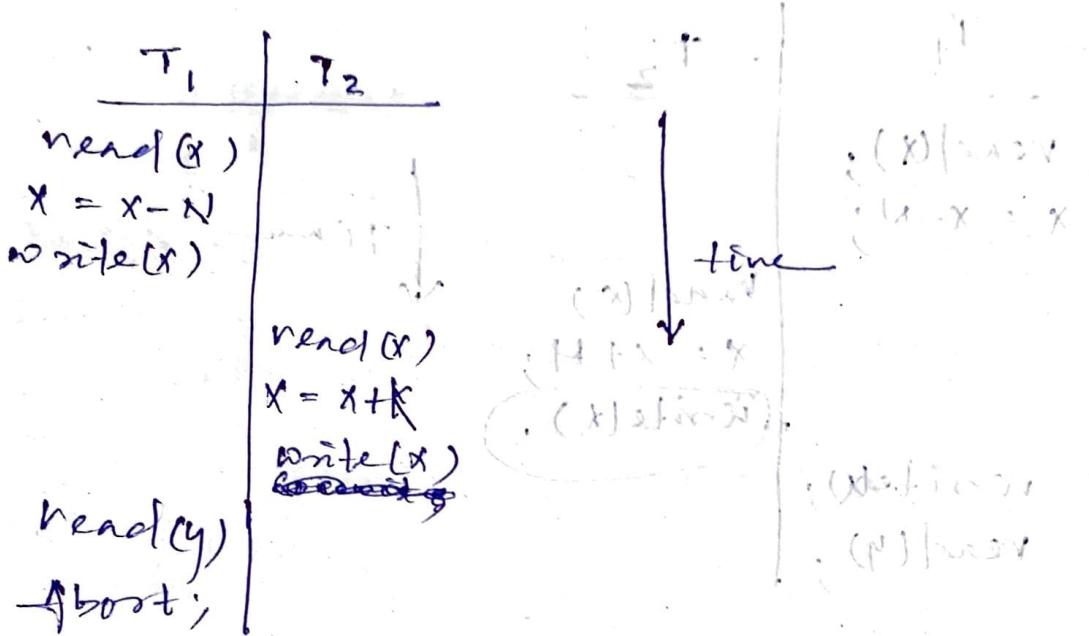
$$N = 10$$

According to transaction semantics, the result will be 45. But in this case, that is when the transaction is executed in this manner, the output is 55 which is wrong.

See In the above case the

item x has incorrect value because the update of T₁ is lost.

Destry READ / TEMPORARY UPDATE PROBLEM



When one the problem occurred

When one transaction updates a database item, then the transaction fails for some reason. If another transaction tries to access the updated item before it changes back to its original value.

Instead of getting a correct data from a Destry database is update

Inconnect Summary Problem 29.3.22

If one transaction is calculating an aggregate summary function of a number of records while other transactions are updating some of these records, the aggregate function may calculate some values before they are updated and then after they are updated.

Initial State	Final State
read(a); sum = 0; sum = sum + a;	read(a); sum = 0; sum = sum + a;
write(a)	write(a)
read(x); followed by no. $x = x - N$; write(x)	initial value time
read(y); sum = sum + y; read(y)	initial value time
read(y); $y = y - K$; write(y)	initial value time

General Schedule:

If schedule S is general for every transaction T participating in the schedule, all the operations of T

The transactions are executed ~~concurrently~~
in the schedule.

Otherwise the schedule violation
Serial.

e.g.: $s; n_1(x); w_1(x); n_1(y); n_2(x); w_2(x)$

Therefore in a serial schedule only
one transaction is performed at a time.

The Commit or Abort of the
active transaction initiate the
execution of the next transaction.

* No interleaving
occurred in a serial
Schedule.

* A serial schedule is always serial
to be connect.

~~Ans~~: For n -transactions How many
serial schedule can be possible.

Ans: $n!$

Generalizable schedule:
A schedule S of an transaction
is said to be generalizable if it
is equivalent to some serial schedule
of same transaction.

N.B. $(a), (b), (c), (d), (e)$

- *) If (a) non-general schedule S is
generalizable, then it is assumed
to be connect.

W.M.P

Conflict Equivalent

Two schedules will said to be
conflict equivalent if the order of
any two conflicting operations ~~are~~ is
same in both the schedule.

Conflict operations in a Schedule

Two operations in a schedule
are said to be conflict if
the following conditions holds

- i) They belong to different
transaction

(ii) they access the same data item.

(iii) at least one of the operation which is the write operations.

e.g.: Given a schedule -

$S: r_3(y); w_3(y(z)); r_1(x); w_1(x); w_3(y);$
 $w_3(x); r_2(z); r_1(y); w_1(y); r_2(y);$
 $w_2(y); r_2(n); w_2(x);$

Find the conflict pair?

Ans: $r_3(y); w_3(y);$

$r_3(y); w_2(y);$

~~$r_1(z); r_1(n); w_2(x);$~~

$w_1(n); r_2(n)$

$w_1(x); w_2(x);$

$w_3(y); r_1(y);$

$w_3(y); w_1(y);$

$w_3(y); r_2(y);$

$w_2(y); w_2(y);$

$w_3(z); r_2(z);$

~~$w_2(z);$~~

$r_1(y); w_2(y);$

$w_1(y); r_1(y);$

$w_1(y); w_2(y);$

Serializability :-

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The concept of serializability is used to identify which non-serial schedules are correct.

Serializability Test :-

① Conflict Serializability test :-

This algorithm takes only the read and write operations in a schedule to construct a precedence graph (serialization graph) which is a directed graph.

Step - 1

For each transaction T_i participating in the schedule S , create a node, labeling T_i in the precedence graph.

Step - 2

choose the conflict pair in S .
For each conflict pair i.e.

$r_i(x); w_j(x)$

$w_i(x); r_j(x)$

$w_i(x); w_j(x)$

Create an edge $t_i \rightarrow t_j$ in the
precedence graph.

Step - 3:

The Schedule S is serializable
if the precedence graph has no
cycle.

* If a Schedule S is serializable
the corresponding equivalence serial
schedule can be obtained by topological
ordering of nodes in the graph.

Correspondingly consider the following schedules

$S_1: r_2(y); r_2(x); r_1(x); w_1(x); w_2(y); w_3(z); r_2(z); r_1(y);$
 $w_1(y); r_2(y); w_2(y); r_2(x); w_2(x);$

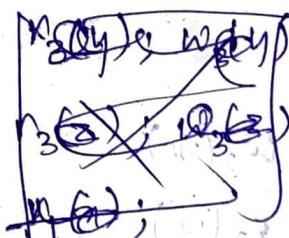
$S_2: r_2(x); r_2(y); w_2(y); r_3(y); r_3(z); r_1(x); w_1(x);$
 $w_3(y); w_3(z); r_2(x); r_1(y); w_1(y); w_2(x);$

check whether the given schedule is serializable.

If serializable, find the corresponding serial schedules.

Ans 1. Checking

The conflicts pairs in S_1 are



$n_3(y); w_3(y)$ $w_3(y); w_2(y)$

~~$n_3(y); w_3(y)$~~ $w_3(y); n_2(y)$

$n_3(y); w_2(y)$ $n_1(y); w_2(y)$

$(\cancel{n_3(y)}; w_1(y)); n_2(y)$

$(\cancel{w_3(y)}; w_1(y)); n_2(y)$

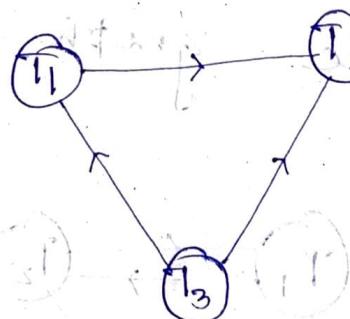
$(\cancel{n_3(y)}; w_2(y))$

$(\cancel{w_3(y)}; n_1(y))$

$(\cancel{w_3(y)}; w_1(y))$

$(\cancel{w_3(y)}; w_2(y))$

The Precedence graph is as follows



The Precedence graph Doesn't contain any cycle.

So the Schedule S_1 is serializable.

Corresponding lexical schedule by topological ordering is

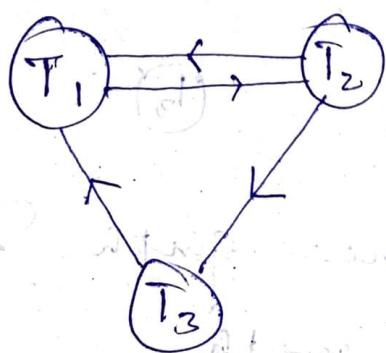
$$T_3 \rightarrow T_1 \rightarrow T_2$$

of Area.

The correct pattern

- (x), $n_2(z)$; $w_3(z)$;
- (y), $n_2(x)$; $w_2(x)$
- (z), $n_2(y)$; $w_3(y)$
- (w), $n_2(y)$; $w_1(y)$
- (x), $w_2(y)$; $n_3(y)$
- ~~(y), $w_2(y)$; $n_3(y)$~~
- ~~(z), $w_3(y)$; $w_1(y)$~~
- ~~(w), $w_3(y)$; $w_1(y)$~~
- ~~(x), $w_2(y)$; $n_1(y)$~~
- ~~(y), $w_1(y)$~~
- ~~(z), $n_3(y)$; $w_1(y)$~~
- ~~(w), $n_3(y)$~~

The precedence graph is as follows



If the graph contains a cycle,
the schedule is not serializable.

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LOCKING TECHNIQUE IN CONCURRENCY CONTROL

LOCK: Lock is a variable associated with a data item that describes status of the data item with respect to possible operations.

WILLINGLY WAITING FOR A SHARED LOCK

→ Thread classification based on locks
→ Thread which is waiting for a lock
→ It starts to wait for locks. ~~when it is not in use~~
~~addressing lock~~ → the process waits until it gets the lock.

Shared Lock / Exclusive Lock
↳ Read lock / Write lock

In this scheme there are 3 operations

(i) Read-lock(α) / S-lock(α)

(ii) Write-lock(α) / X-lock(α)

(iii) Unlock(α)

Shared lock / Read-lock / S-lock :

→ A transaction must release a S-lock(α) operation before any read(α) operation is performed in T.

→ Multiple transaction can hold a S-lock or an database item simultaneously.

Write-Lock / Exclusive-Lock / X-Lock:

→ A transaction T must own the operation write-lock(x) / X-lock(x) before any write(x) operation performed in T.

→ Only one transaction can hold a particular write-lock(x) / X-lock(x) on a data item at any time.

→ No other transactions can hold any lock (not even read lock) if a transaction has a write-lock / X-lock.

- No. of Deadlock conditions:
A transaction which holds a write-lock on a database item can read and write the data item. whereas in case of S-lock operation the transaction can only read the data.

→ If there are two (transaction T1 and T2) and both have S-lock on different database items. Then T1 will wait for T2 to release its lock.

start	T₁	Convert to transaction
new(x)	T₁	in lock based protocol
$x = x - N$	T₁	T₁ creates new
write(y)	S-lock(x)	L-lock(x)
$y = y + k$	read(x)	read(x)
write(y)	$x = x - N$	$x = x - N$
$y = y + k$	x-lock(x)	L-lock(x)
write(y)	write(x)	write(x)
read(y)	(S) lock(y)	Unlock(y)
$y = y + k$	read(y)	read(y)
read(y)	x-lock(y)	$y = y + k$
$y = y + k$	constly(y)	Unlock(y)
constly(y)	Unlock(y)	x-lock(y)
constly(y)	constly(y)	Unlock(y)

2 Phase Locking Protocols

2PL (Basic 2PL)

Each transaction must obtain a shared lock on an object before reading and exclusive lock on an object before writing, and write after reading.

→ transaction releases its lock once it has performed its desired operation (read, write).

→ transaction can't request additional locks once it releases any lock.

If a transaction holds exclusive lock on an object to other transaction then can get a lock(s or x) on that object.

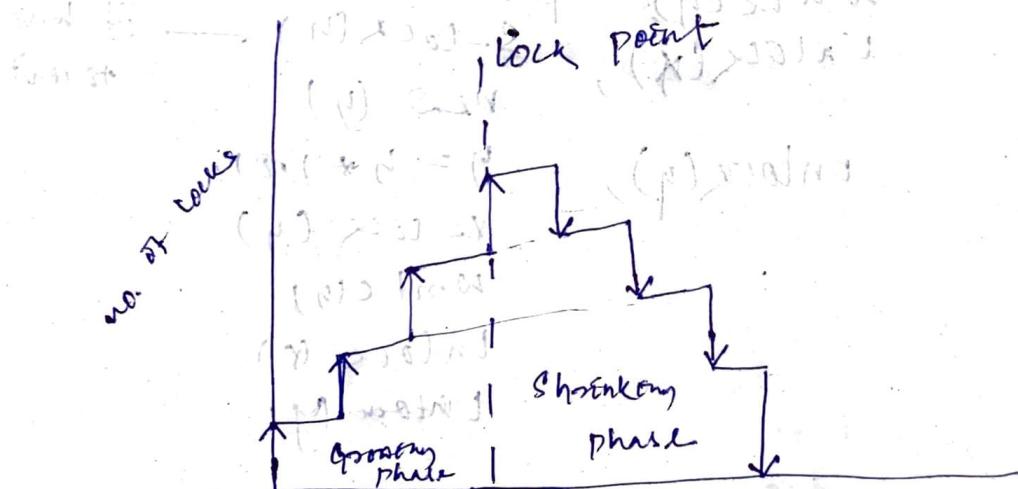
2PL is divided into 2 phases

- Growing Phase :

New locks can be obtained but ~~non~~ ~~the~~ locks can be released.

- Shrinking Phase :

locking locks can be released but no new locks can be obtained.

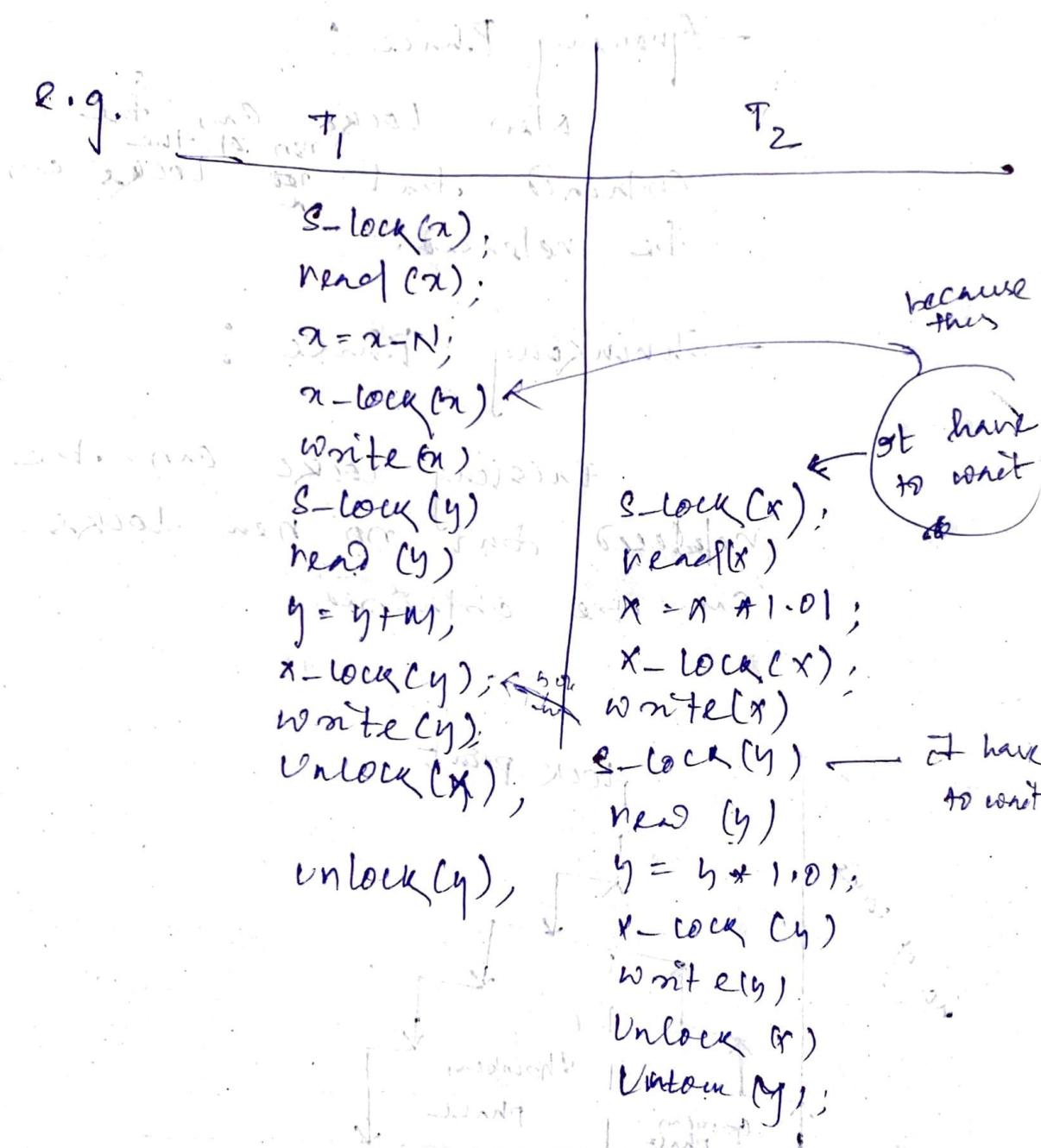


LOCK POINT :-

The point where the transaction obtains its last lock. It is the end of growing phase.

Two Phase Locking Protocol
ensure serializability (Conflict Serializability)

Transactions can be serialized in the order of their lock points.



The above example does not follow two phase locking protocol.

In two phase locking protocol the transaction T_1 & T_2 can be specified as follows

(with 3 steps) \rightarrow (with 2 steps)

s-lock (x);
read (x)

$$x = x + 1.01;$$

r-mod-lock (y)

write (y)

s-lock (y)

read (y)

2. $s \rightarrow r$ if $y = y + 1.01$

lock point

for T_1 \leftarrow r-mod-lock (y)

write (y)

unlock (x)

s-lock (x)

read (x)

$$x = x + 1.01;$$

x -lock (x)

write (x)

unlock (y)

s-lock (y)

read (y)

$$y = y + 1.01;$$

x -lock (y)

to wait for

write (y)

unlock (x)

unlock (y)

at last T_1 can continue

T_2 can't proceed until T_1 is done

if T_2 starts before T_1 is done

Q/ Prove that 2PL is Serializable.
or 2PL ensures Serializability.

(Book by method of Contradiction)

Brief: statement

If S is a schedule containing the interleaved operations from a number of transactions T_1, T_2, \dots, T_n and all the transactions are using a DL Protocol, then schedule S is serializable.

Assume that the schedule S is not serializable.

\Rightarrow The Precedence graph for S will have a cycle made up off a subset of $\{T_1, T_2, T_3, \dots, T_k\}$

Assume that the cycle consists of $T_a \rightarrow T_b \rightarrow T_c \rightarrow \dots \rightarrow T_n \rightarrow T_a$

i.e. a lock operation in T_b is followed by an unlock operation of T_a , a lock operation by T_c is followed by

an unlock operation in T_b and so on.

Finally a lock operation by T_a is followed by an unlock operation in T_a .

However, this is a ~~conflict~~ contradiction of the statement that T_a is using 2PL Protocol, as once T_a is unlocked it can't again access any lock.

Thus, the assumption that there is a cycle in the Precedence graph is incorrect and S is serializable.

Hence 2PL ensures serializability.