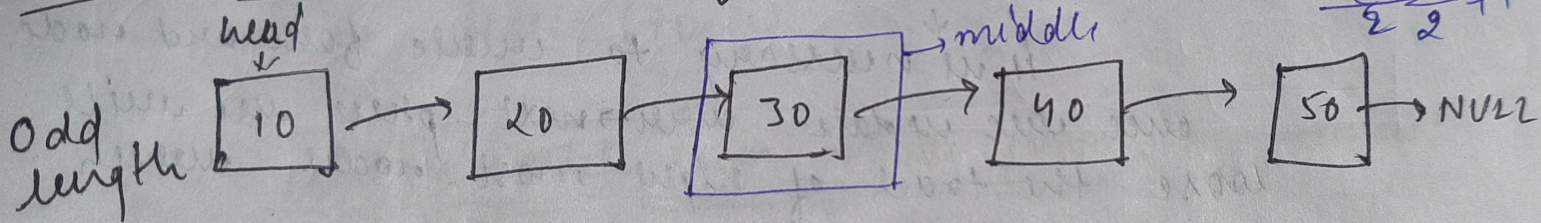
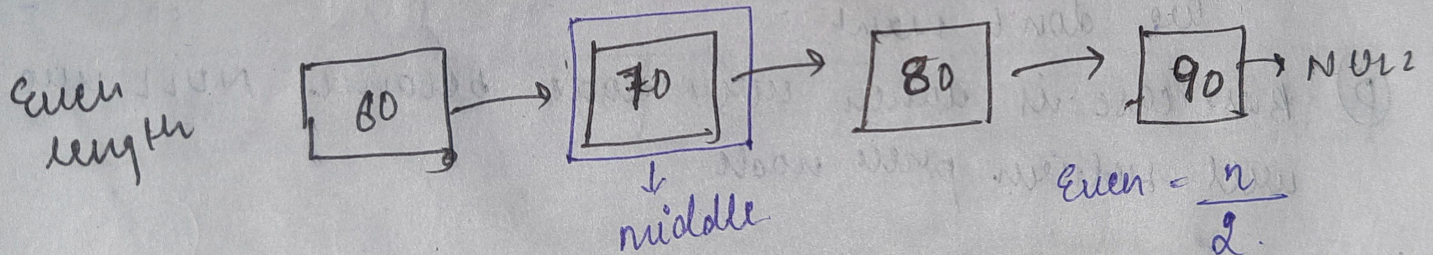


Ques: 2 Find the middle of Linked List:



$$\text{Odd} = \frac{n+1}{2}$$



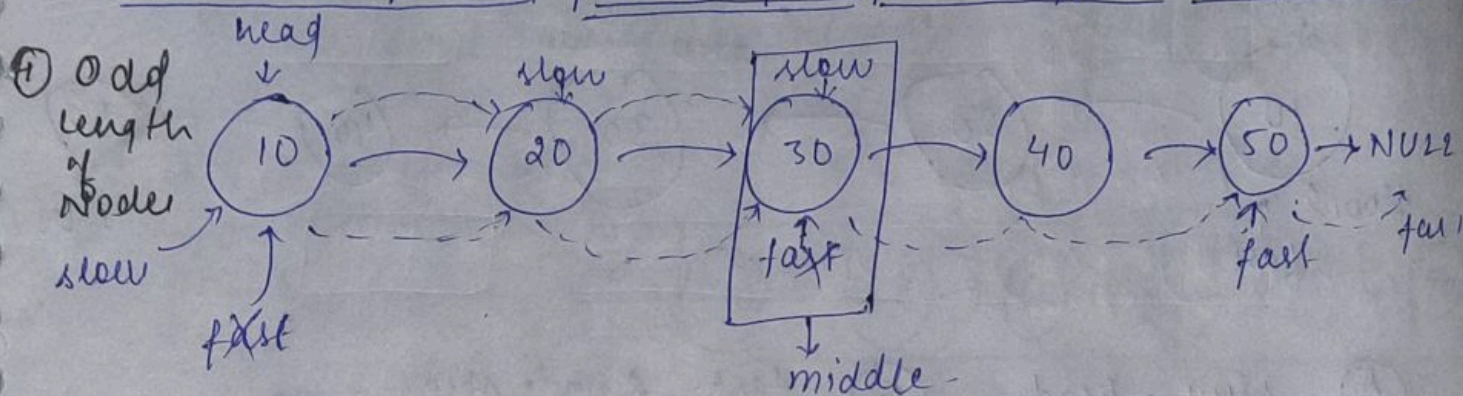
$$\text{Even} = \frac{n}{2}$$

Approach 1

$\left[\begin{array}{l} \text{length} \rightarrow O(n) \rightarrow \Phi \\ \text{length} \rightarrow \text{even} \rightarrow \frac{\text{length}}{2} \\ \quad \rightarrow \text{odd} \rightarrow \frac{\text{length}}{2} + 1 \end{array} \right] \rightarrow O(n)$
Total T.C. = $O(n)$

Approach 2

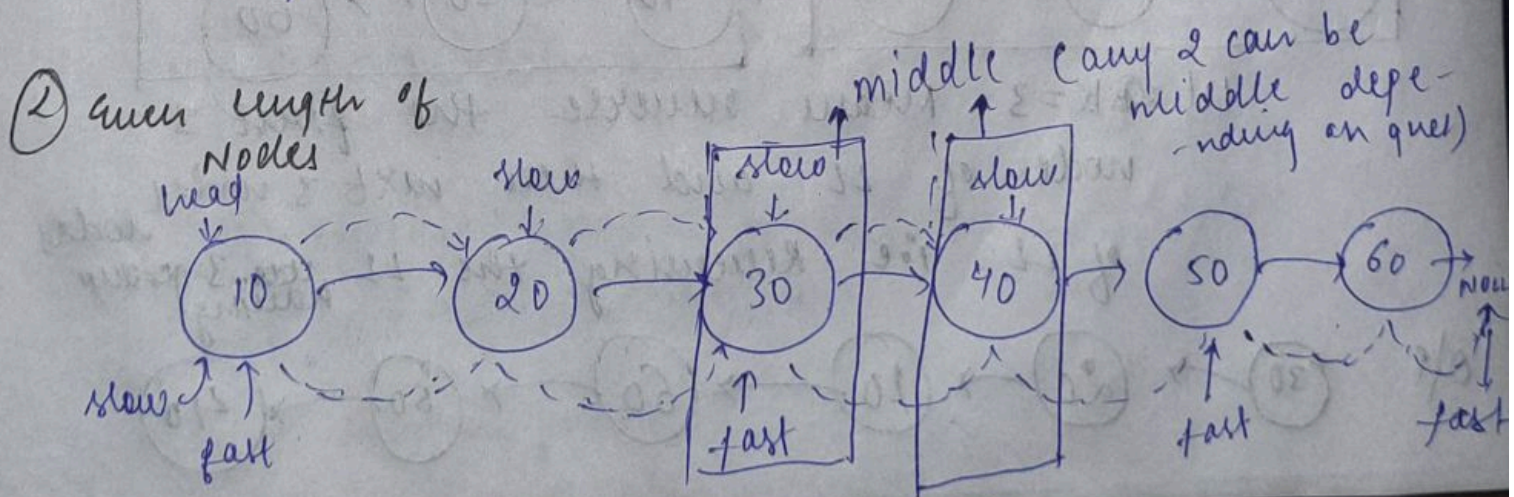
Tortoise Algorithm / slow & fast pointer approach / 2-pointer



Step 1 slow & fast pointers point to the first node i.e. head

Step 2 slow always takes 1 step & fast always takes 2 steps steps means move 1 node forward and 2 node forward.

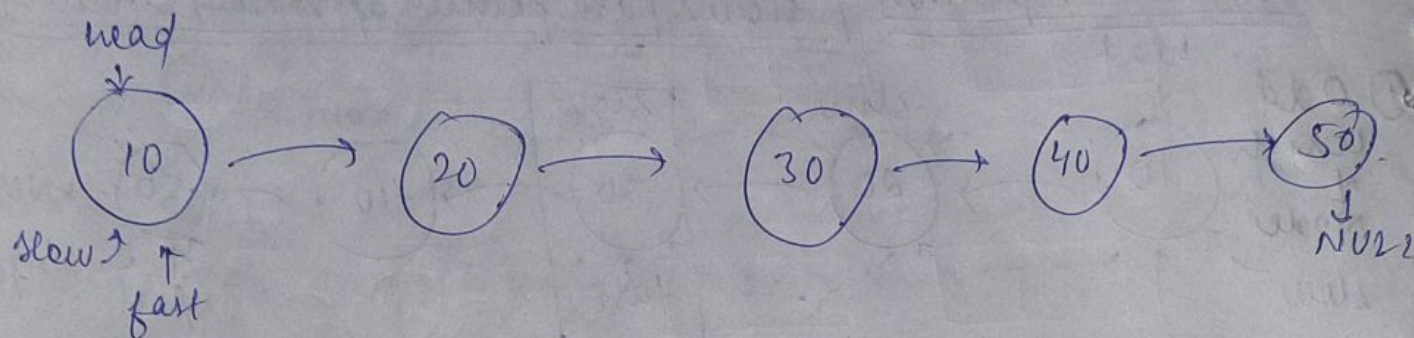
Step 3 If fast node is unable to move 2 nodes ahead then only slow node will move 1 node forward.



Step

① same as odd no. of nodes

when fast node reach to NULL. for even no. of nodes then its our choice whether to move slow pointer one node ahead or to and say that particular node to be middle node or consider the current ~~slow~~ ~~prev~~ node where slow pointer point to be the middle node that totally depends on ques



(A) slow = head
fast = head

(B) fast = 2 node step
if fast is able to
take 2 step
then slow = 1 step

do this
i.e.
traverse the
complete LL
slow & fast
become NULL

① return slow when fast unable to take 2 steps.

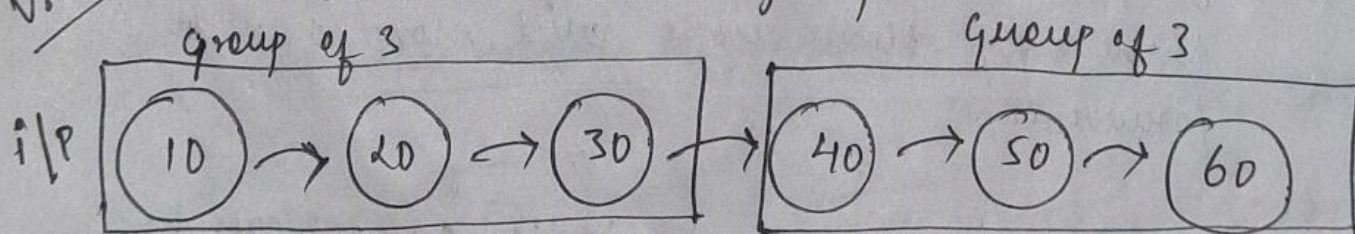
Que: 3

K-group reverse a linked list

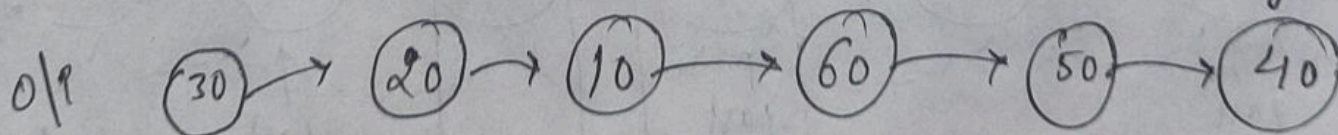
OR

Reverse a LL in K-groups

Imp
V.V.V.V

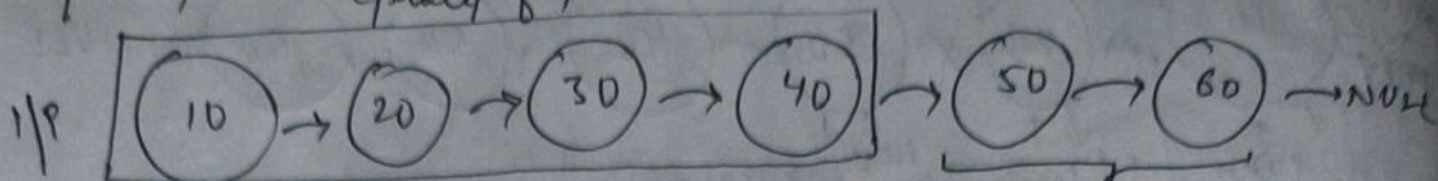


Let ~~K~~ K=3. Means reverse the first 3 nodes of LL and then next 3 nodes of LL i.e. reversing the LL in 3 group having



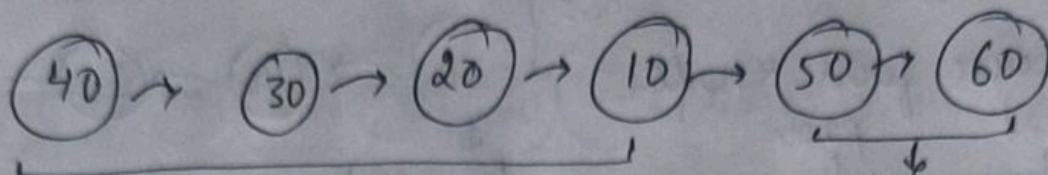
if $K=4$

Group of 4



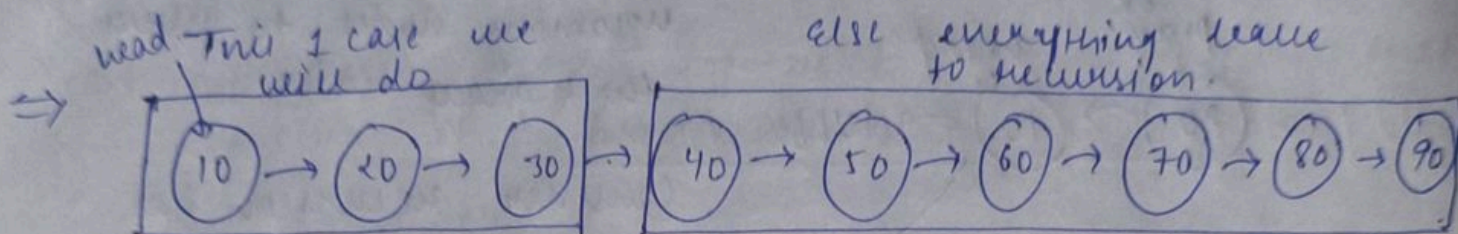
can't form group of 4 so will print as it is

o/p

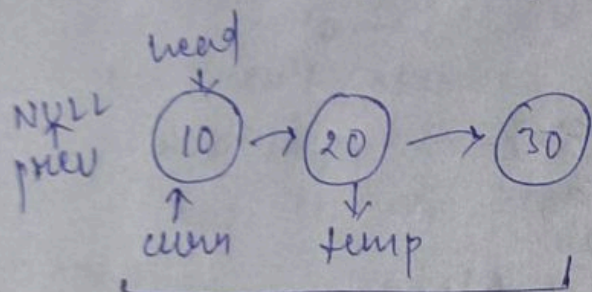


first 4 nodes are reversed

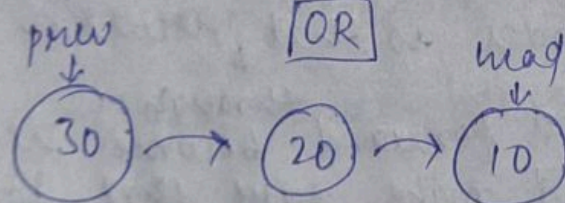
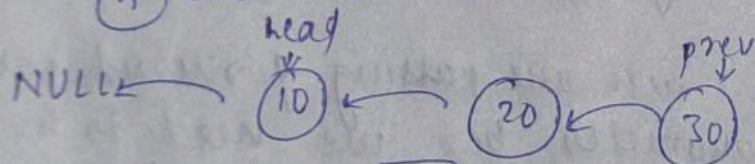
last 2 are same as in input



if $K=3$ mean reverse the nodes in the group of 3



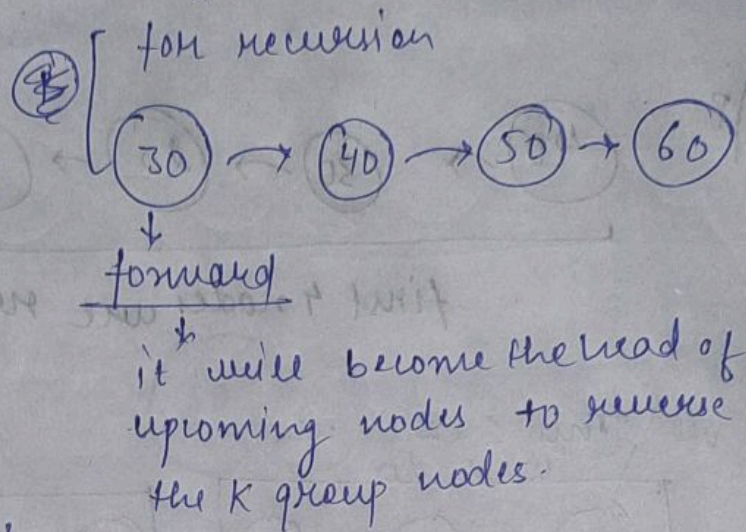
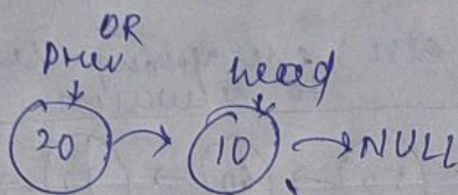
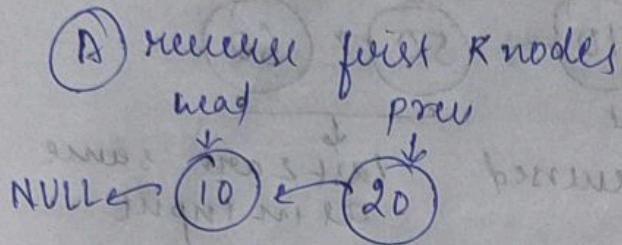
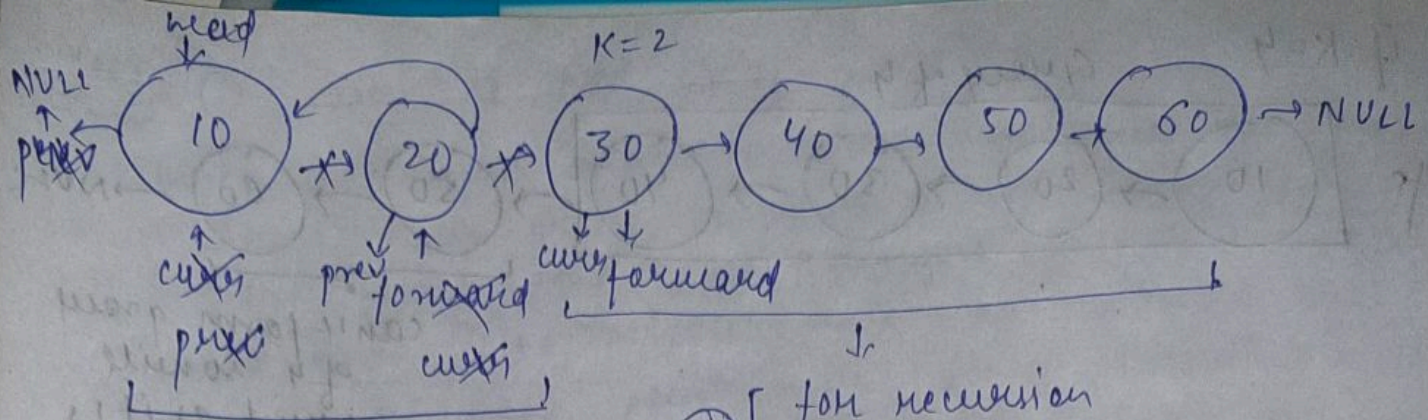
(A) we will reverse K nodes.



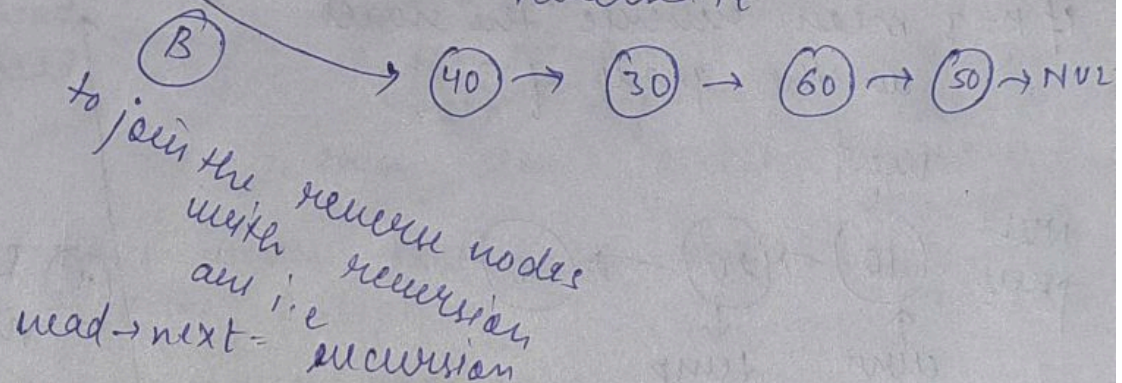
(B) Recursion will return something we will link head → next = Recursion

Steps

- Reverse ^{first} K nodes
- head → next = Recursion
- return prev.



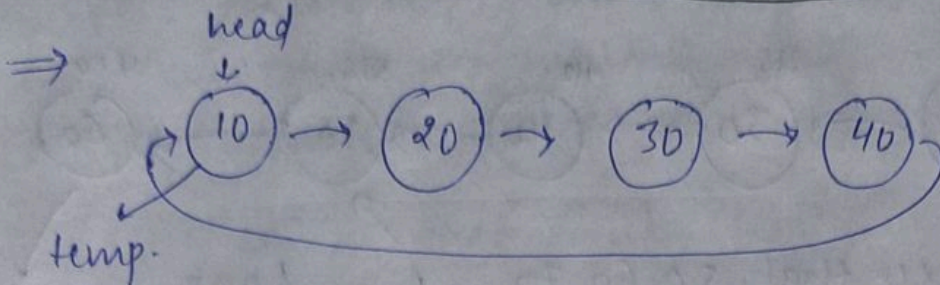
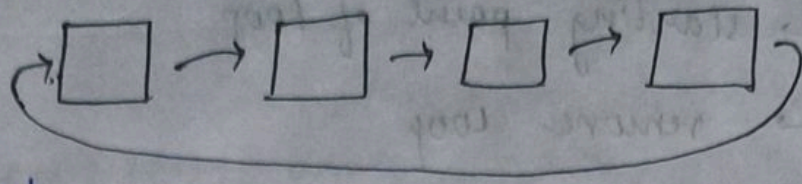
Consider recursion has reversed it



(C) to return the head of updated LL.

(Note) → for recursion we are passing forward pointer as a head in parameters because we need to have access of further nodes so that, recursion we can reverse K nodes and forward through become head of upcoming nodes and make sure that forward should not be NULL.

Ques:4 1/p: Linked List to check it is circular or not
return o/p True / False



(A) temp = head.

(B) Now check from temp → next ~~that~~ i.e. from 20 that whether it is head or not.

i.e. 20 → head ×

30 → head ×

40 → head ×

10 → head ✓ [The LL is circular]

We aren't starting from 10 because initially we have used temp = head so if we check whether 10 is head or not it will become useless.

(C) return true/false if it is LL.

Approaches

- (1) 1 pointer approach [temp pointer]
- (2) slow/fast pointer approach
- (3) Mapping

Do Yourself

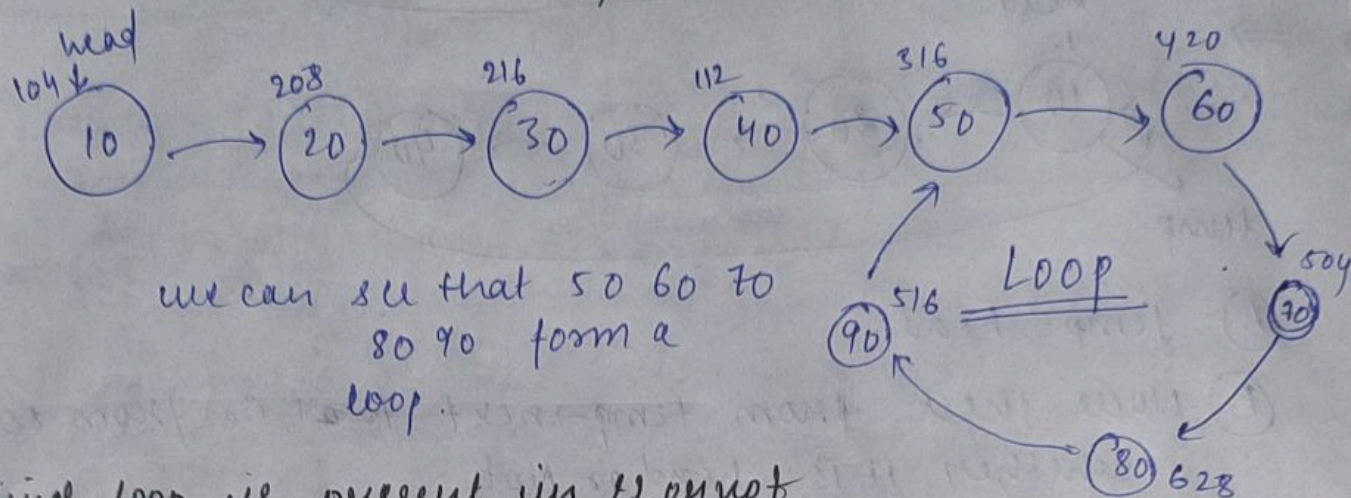
Ques: 5

V.V.V Imp

Different variations of Question

Detect and Delete Loop

- check loop is present in LL or not
- starting point of loop
- remove loop



① find loop is present in LL or not

→ Approach 1 we can solve it with map

map <Node*, bool> map.

address T/F

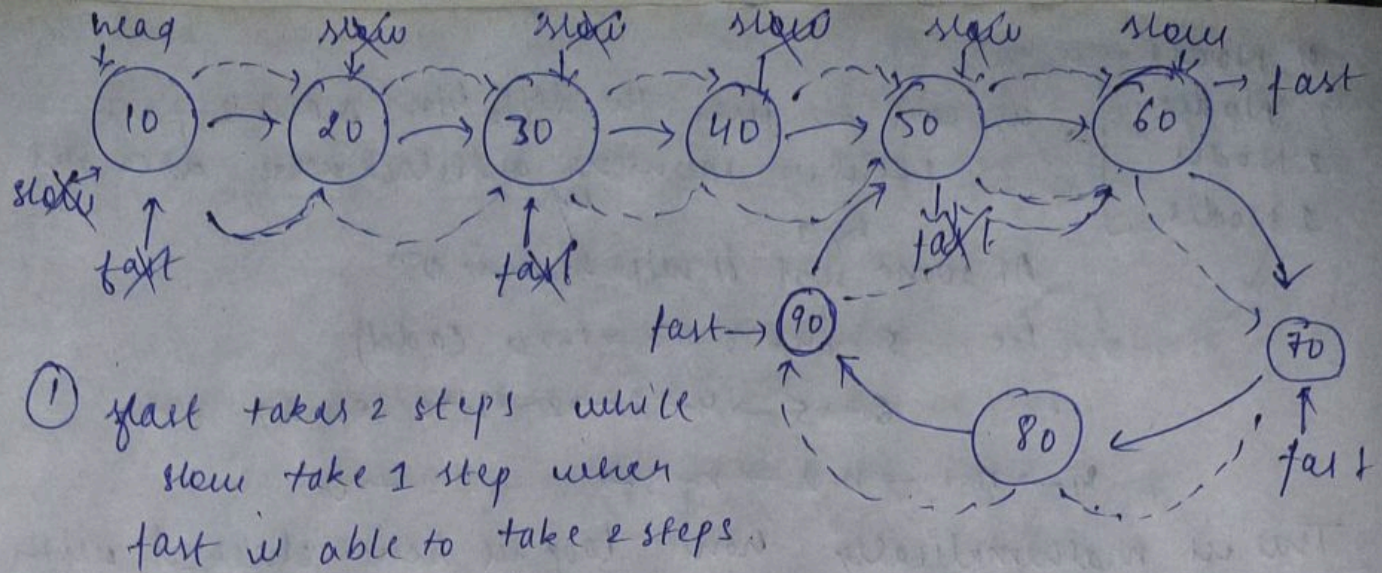
Address	value
104	true
208	true
216	true
112	true
316	true
420	true
504	true
628	true
516	true
316	Again as it is present at above

Here 316 is true

already present [we can say that loop is present]

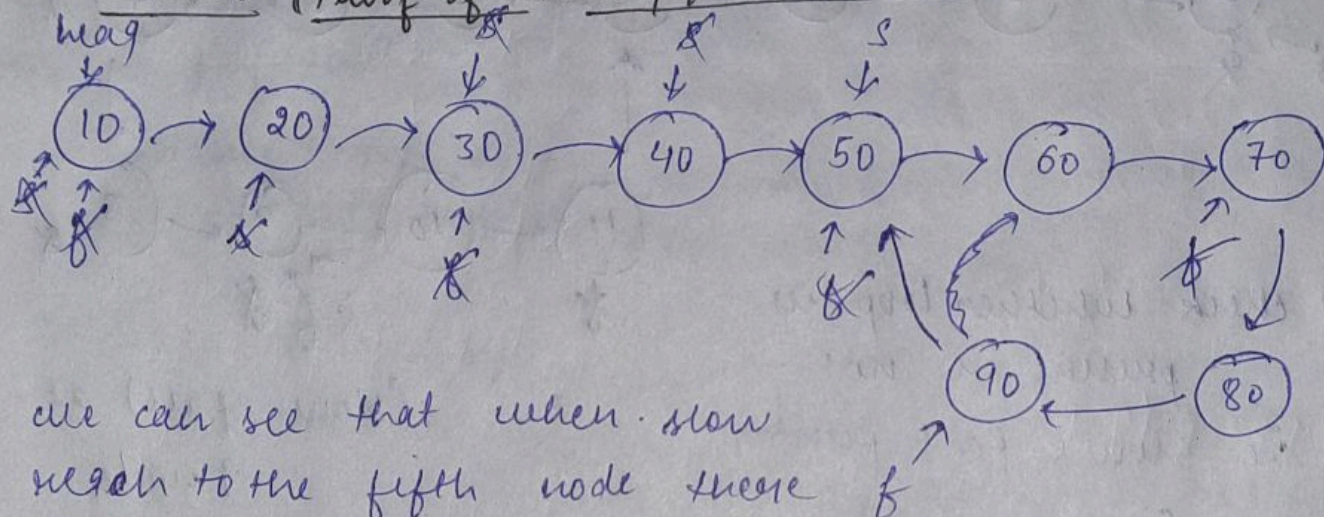
→ Approach 2

Floyd Cycle Detection (FCD) Algorithm can be used to check whether loop is present in LL or not. In this we use slow/fast pointers.



so we can see that when $slow == fast \rightarrow$ loop present
 else $fast == NULL \rightarrow$ loop absent.

Mathematically how it is working to check loop is present or not (Proof of slow / fast pointer)



we can see that when slow reach to the fifth node there is 100% possibility that fast node must be inside loop.

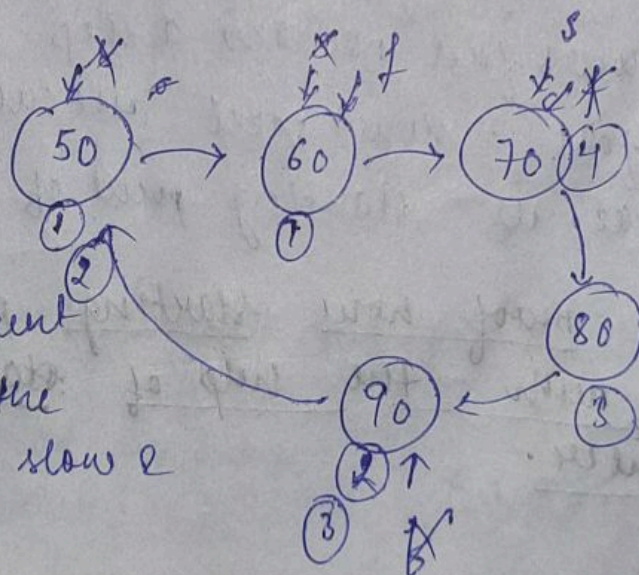
consider

slow is at 50

fast is at

70. Now count

anticlockwise the difference b/w slow & fast pointer



4 Nodes.
 3 Nodes.
 2 Nodes
 1 Node

4 Nodes
3 Nodes
2 Nodes
2 Nodes

→ we can see that the diff b/w slow & fast pointer counting anti-clockwise decreases by 1.
At some sort it will become 0.

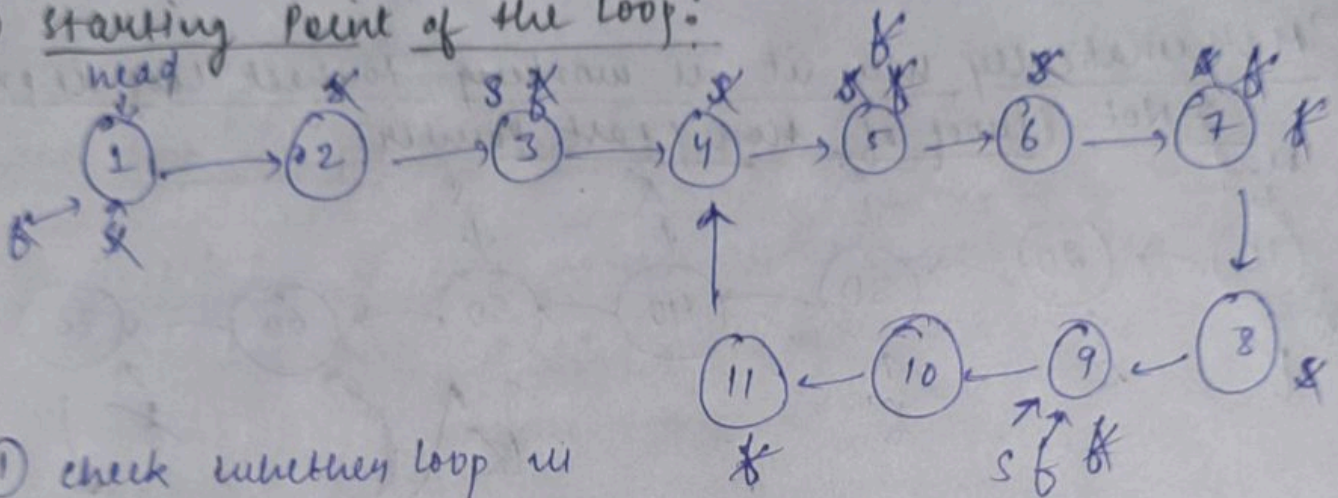
i.e. $5 \rightarrow 4 \rightarrow 3 \rightarrow 2 \rightarrow 1 \rightarrow 0$ (odd)

$6 \rightarrow 5 \rightarrow 4 \rightarrow 3 \rightarrow 2 \rightarrow 1 \rightarrow 0$ (even)

$n \rightarrow n-1 \rightarrow n-2 \rightarrow n-3 \rightarrow \dots \rightarrow 0$

This is mathematically how loop is being checked with the help of slow/fast pointer.

② Starting Point of the Loop:



① check whether loop is present or not.

i.e. slow & fast pointers

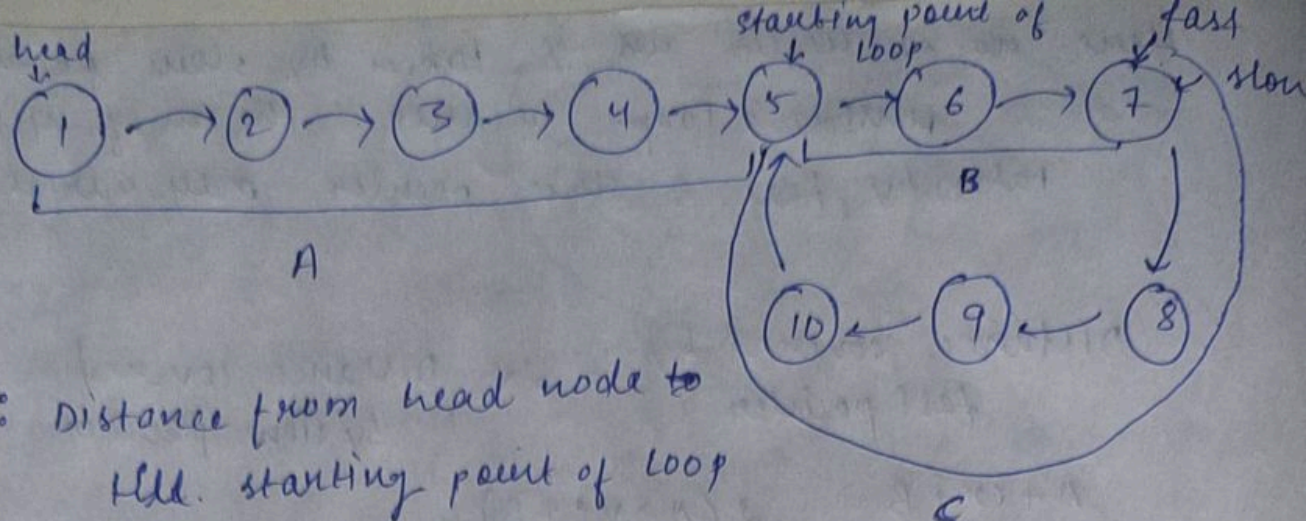
(slow == fast)

(slow == fast) at 9 node

② assign slow = head (when slow == fast become)

③ Now move slow & fast pointers 1 step till slow != fast when (fast == slow) meet we can say that is starting point of loop.

mathematically proof how starting point of a loop is found with the help of slow and fast pointer.



A: Distance from head node to the starting point of loop

B: Distance from starting point of loop till where fast & slow meet

C: Distance of complete loop in a linked list

As fast takes 2 step whereas slow take 1 step. we can say that

$$\text{Distance covered by fast pointer} = 2 \times \text{Distance covered by slow pointer}$$

$$\text{Distance covered by fast pointer} = A + xC + B$$

As fast pointer must have started from head till starting point of loop.

Here x : no. of cycles fast pointer takes inside a loop

As after covering x cycles the distance B will be covered

$$A + xC + B \text{ [distance covered by fast pointer]}$$

$$\text{Distance covered by slow pointer} = A + yC + B$$

Here no. of cycles is y taken by slow pointer inside a loop. because the no. of cycles taken by fast & slow pointer may varies.

Distance covered by fast pointer = $2 \times$ Distance covered by slow pointer

$$A + xC + B = 2(A + yC + B)$$

$$A + xC + B = 2A + 2yC + 2B$$

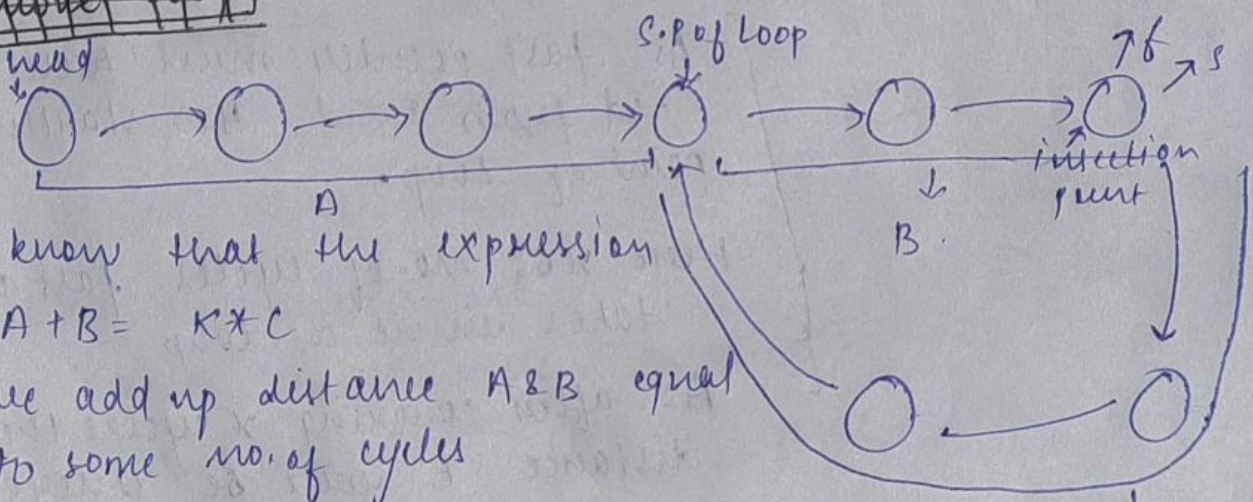
$$(x - 2y)C = A + B$$

$$\text{let } K = x - 2y$$

$$A + B = K \times C$$

So we can see that if we add up distance A and B means to reach where fast & slow pointer meet. there is requirement some no. of cycles taken by both fast & slow pointer inside a loop.

~~Remove loop:~~



We know that the expression $A + B = K \times C$

If we add up distance A & B equal to some no. of cycles

Now B is: Distance from S.P. till intersection
if C : distance of whole loop

We can say that

Then half cycle will become

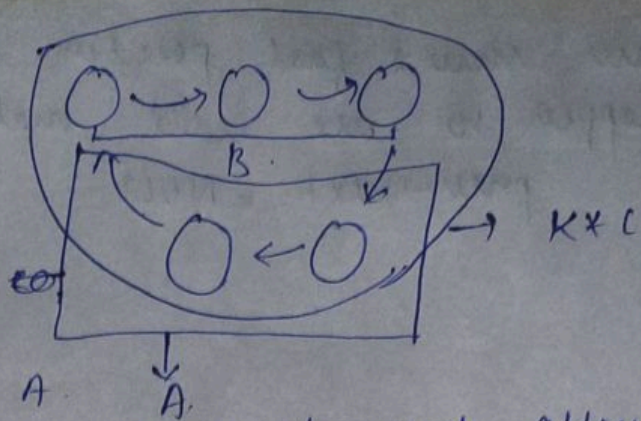
$$A + B = K \times C$$

$$A = K \times C - B$$

so lower part of cycle become distance A

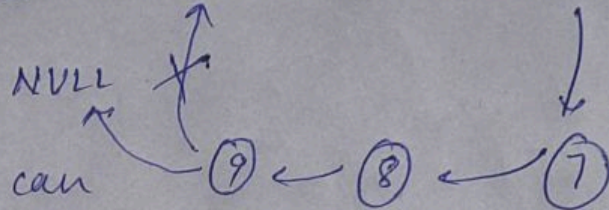
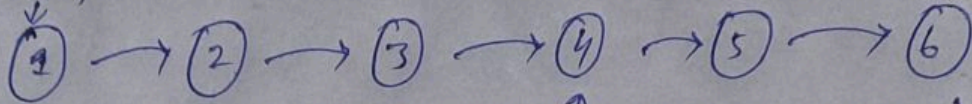
therefore we point slow to head. and allow slow & fast pointers to take 1 step

∴ Through this mathematically fast & slow will meet at starting point



③ Remove loop:

head

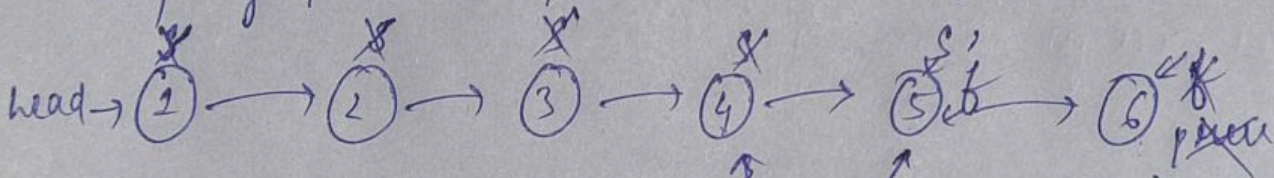


Remove loop we can see that loop is formed

→ To remove loop we will point out last node to the NULL.

→ This can be done through previous pointer.

Assigning previous pointer ^{same as} ~~next~~ to fast pointer.



Assign prev pointer as same fast pointer

• Store prev = fast. Then move fast pointer 1 step ahead.

