REINFORCEMENT LEARNING - CSE564

Homework 1



Q1. The Epsilon Value chosen for the converging case is min(50/t,1) where t = 1,2,3,4..., this choice of epsilon forces the agent to explore its surroundings with probability 1 for atleast the first 50 time steps, this helps in estimating the estimate reward well for all arms atleast for 50 time steps, after which the epsilon decreases and follows equation 2.7.

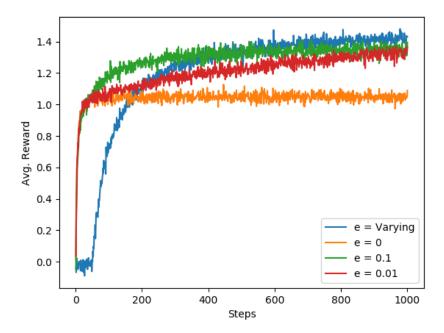


Fig 1.1: Average Reward

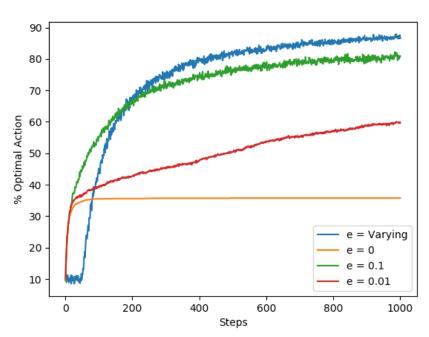


Fig 1.2: Optimal Action

The Varying Epsilon explores for the first 50-time steps and thus picks sub optimal actions in majority of the simulations, but in the long run it outperforms the other choices as it has sufficient knowledge about the estimates given it had exclusively explored during the initial stages. The Error in arms decreases in all cases, except when e = 0, since the first arm that it picks in any simulation, it picks that for the rest of the run, hence not exploring anything, for varying e, the arms are sufficiently and equally explored, hence error reduce is uniform across all arms

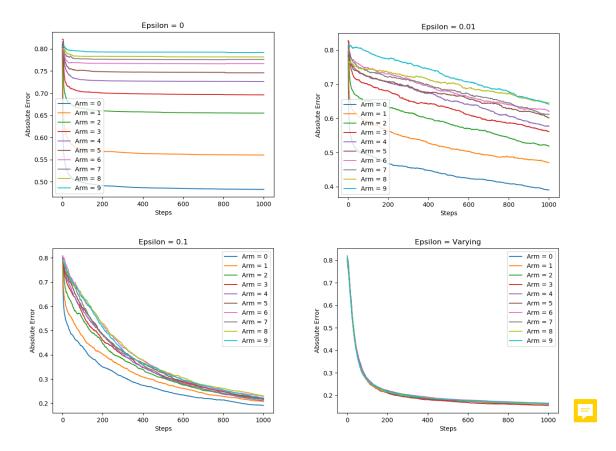


Fig 1.3: Error in Reward Estimate for different epsilon

Q2. As the variance across expected rewards increases, it takes slightly longer for the policies to converge to the Actual expected values, but still the earlier trend follows

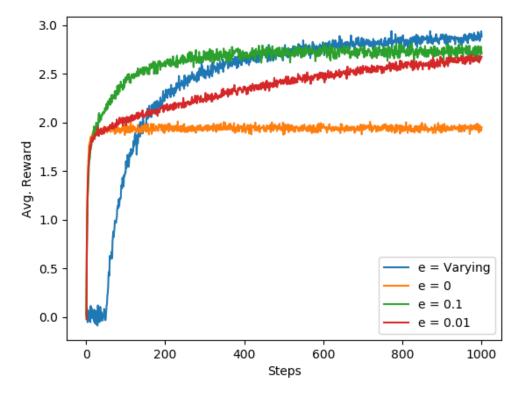


Fig 2.1: Average Reward

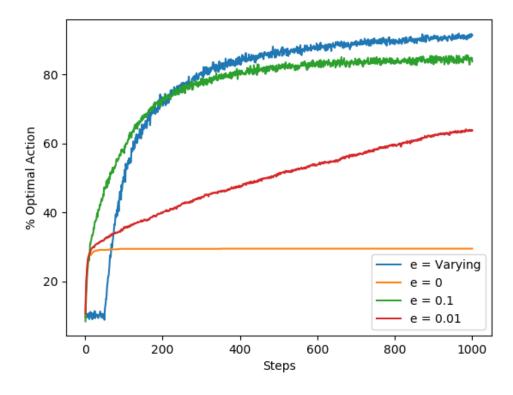


Fig 2.2: Optimal Action

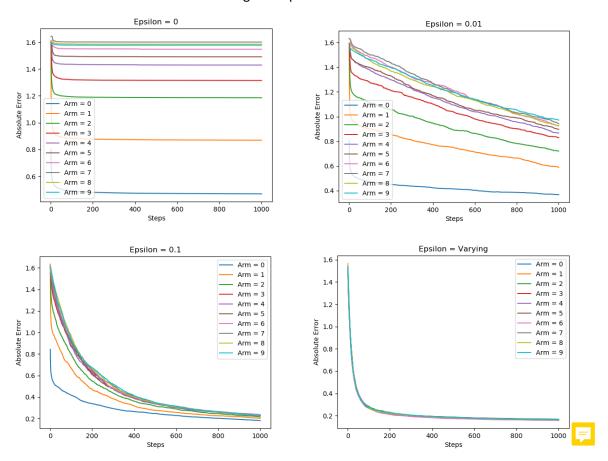


Fig 2.3: Error in Reward Estimate for different epsilon

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Q3. The estimates after a long time would converge to the actual Expected values. at t=00, let estimates (= a ctual values)
be gropt, 81, 92, 29
gi titopt is reward for optimal arm
$E(R) = E(R A = cont greedy) \cdot P(greedy)$
+ E(R A = explore) P(explore)
$= (-\epsilon) \stackrel{?}{=} q_{opt} + \epsilon e_{\cdot} \underline{1}, q_{i}$ $\stackrel{?}{=} 10$
= (1-E) gapt + E. (9, +92+ +99 + gapt)
let Pay be the any reward for all arms
$E(R) = (1 - E) q_{opt} + E \cdot q_{avg}$ $= q_{opt} + E(q_{avg} - q_{opt})$
clearly gropt > gaug
$ \begin{array}{c c} \hline & & & & & & & & & & \\ & & & & & & & & \\ & & & & $
9opt 3 9avg

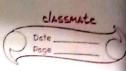
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thus E(R) = 9opt + E(9avg-9opt)
as gavg - gropt & 0 the higher the E, the lower the expected value.
Case(1): $E = 0.1$ $E(R) = q_{opt} + 0.1 (q_{avg} - q_{opt})$ 0.1
Case @ & = 0.01
E(R) = 90pt + 0.01 (garg - 90pt)
Case 10 = 50 = 00 as +-200
Con Con
$\frac{\text{case } 9}{\epsilon} = 0$
we count arrund that estimates converge to actual values as we always pich and added
His only arm that had a societive remained
So the Expeeled value is quing.
Clearly
E > E > E
Thus the best choice is Econ with diff:
0.01 (9opt - 9aug) & 0.1 (9opt - 9aug) for t=0-01



Next we have £ = 0.0L with diff 0.89 (9opt - 9 ang)
with diff 0.011 Topt Tang

	Classmate Page
	84. Sample mean is not influenced by initial chaice of 0,10)
	Inventual update egn: -
	putting @ in O
	$ \frac{9}{n-2} = \left(\frac{n-3}{n-2}\right) \frac{9}{n-2} + \frac{1}{n-2} \frac{R_{n-2}}{n-2} $
	putting 10 in 3
	$Q_{m+1} = {n-3 \choose n} Q_{m-2} + {1 \over m} (R_n + R_{m-1} + R_{m-2})$
-	in General n
	Bn+1= (n-k-1) Bn-k + 1 \(\bar{k} \) h-k
	put n-k=1
	$\frac{9^{n+1}}{n} = \frac{(0)^n 8^n + 1}{n} = \frac{8^n}{1}$
	$= \frac{2}{2}Ri$
	which is independent of choice of By

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when using constant step parameter &
$\mathbb{O} - \mathbb{O}_{n+1} = \mathbb{O}_n + \mathbb{A}(\mathbb{R}_n - \mathbb{O}_n)$
$\mathfrak{D} = \mathfrak{D}_{n-1} + \alpha (\mathfrak{R}_{n-1} - \mathfrak{g}_{n-1})$
3 Bn-1 = Bn-2 + a (R - Dn-2)
put @ in D
(I) Qn+1 = Qn-1 + d(Rn-1-Qn-1)
+ X(Rm-Dn-1+ X(Rn-)
-9 _{n-1})
$\theta_{n+1} = \alpha R_n + (1-\alpha)(\alpha R_{n-1} + (1-\alpha) \theta_{n-1})$
· · · · · · · · · · · · · · · · · · ·
$9_{n+1} = (1-\kappa) 0_1 + \sum_{\alpha=1}^{\infty} \alpha(1-\alpha) R_{\alpha}^{\alpha}$
clearly Q, 13 a function of B,
Mso, the contribution of 0, to 9n+1 is given by
(1-x) Q,



	Date
	Now consider two d: x, 1 dz OS 2; 51
	where d, ede
	$= > 1-\alpha > 1-\alpha $ $= > (1-\alpha)^n > (1-\alpha)^n$
	=> (1-x1)" > (1-x2)"
	(1-x1) 01 > (1-x2) 01 => For a smaller & o the influence of initial values is larger.
	=> For a smaller of the
	influence of initial values is larger.
	larger by :- ((1-d1) - (1-d2)) 01
	. 0
	i) For comprete eliminating influence of B1000 On we can set d=1, thus ex' becomes: B = Rn
(we can set d=1 thus
	egr becomes: B = Rn
	
	Tois although eliminates Q, but is a poor estimate for newards.
	poor estimate for newards
	·

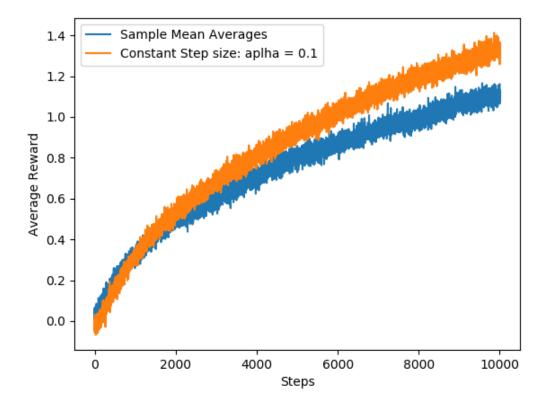


Fig 5.1: Average Reward

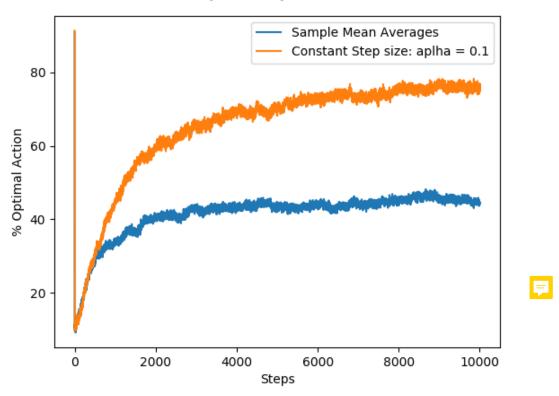


Fig 5.2: Optimal Action

The spikes at the 11th time step are a result of the following: Since N_t(a) for all a is zero, thus all arms are maximising, and whenever an arm is chosen, N_t(a) for that arm a, becomes 1, i.e. that arm no longer remains maximising whilst there is some arm that yet hasn't been picked even once, so for the first ten time steps, all the ten arms are explored randomly once, at the 11th time step, the second term for each arm is same, so the agent picks the arm with the maximum estimate value Q_t, this happens across all 2000 runs, thus the average reward is higher, on the 12th time step, each of the 2000 runs take different independent arms, so the average reward drops, thus we obtain a distinct spike at the 11th time step

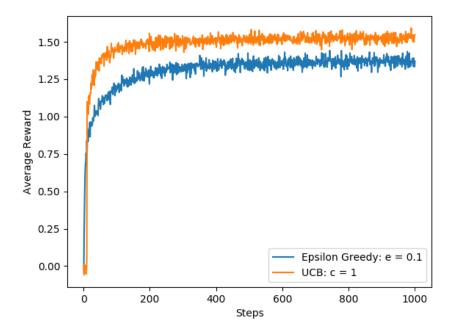


Fig 6.1: c = 1

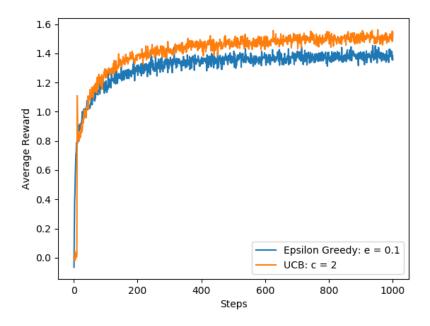


Fig 6.2: c = 2

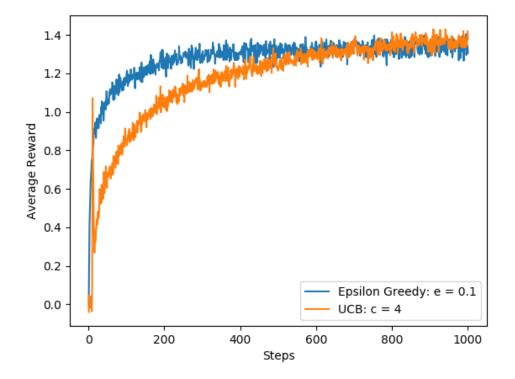


Fig 6.3: c = 4

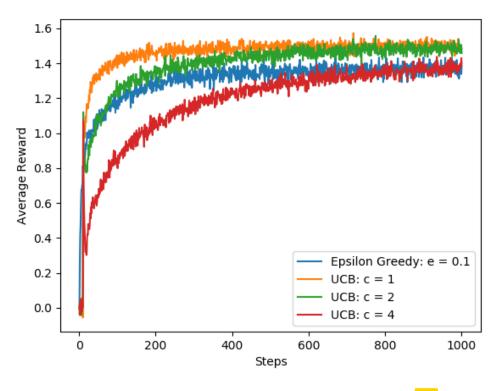


Fig 6.4: Combined

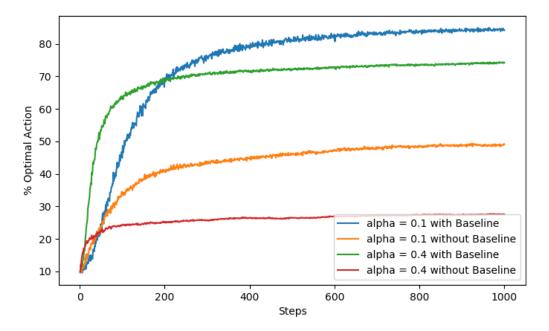


Fig 7.1: Gradient Bandit with alpha = 0.1, 0.4 with/without baseline

