



**RAMAIAH**  
Institute of Technology

# BASICS OF CIVIL ENGINEERING & MECHANICS

Course code:CV14/CV24

Credits:3:0:0

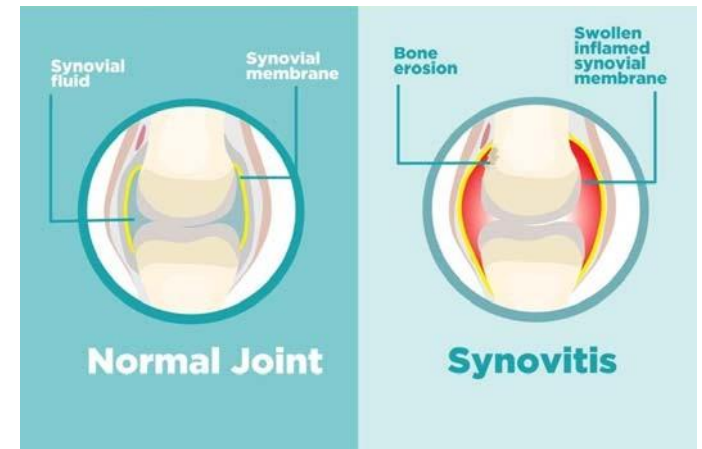
**Topic Covered**  
***Friction***



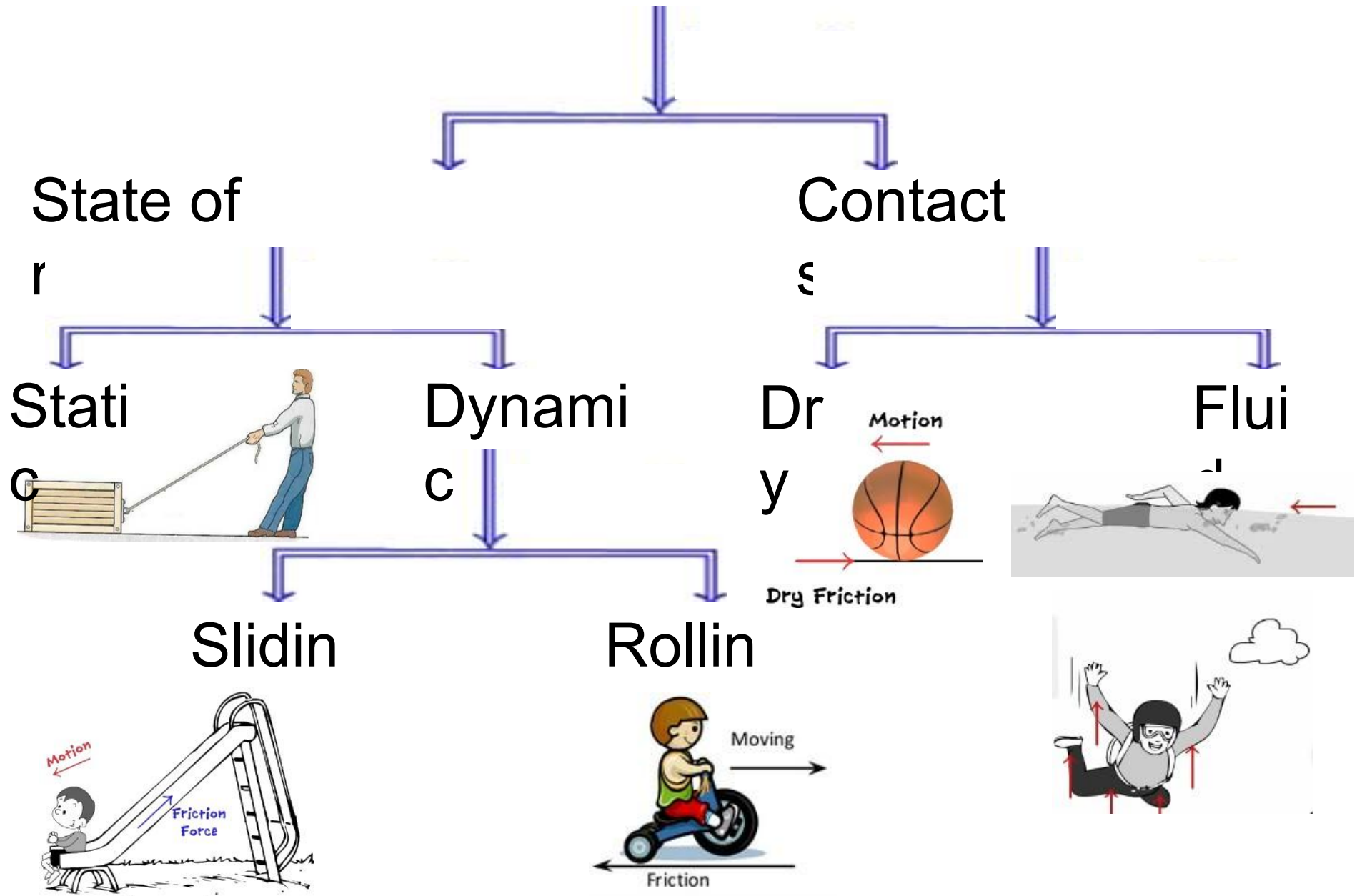
**FRICITION**



**HERO or VILLAIN**



# Types of





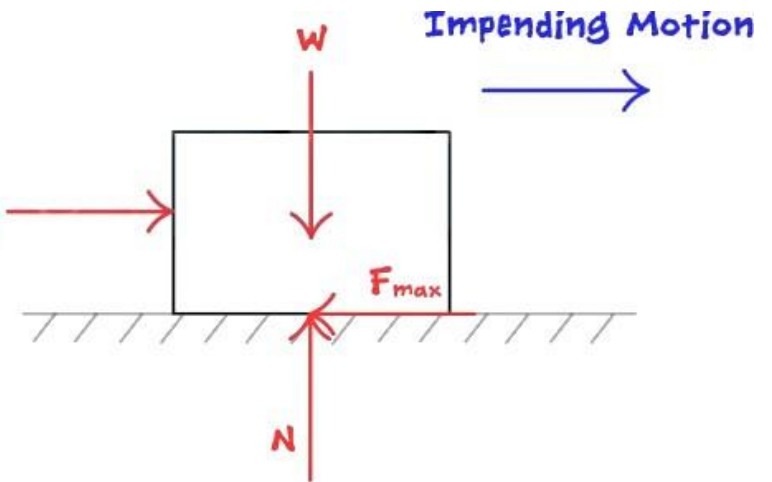


FRICTION



# Law of Static

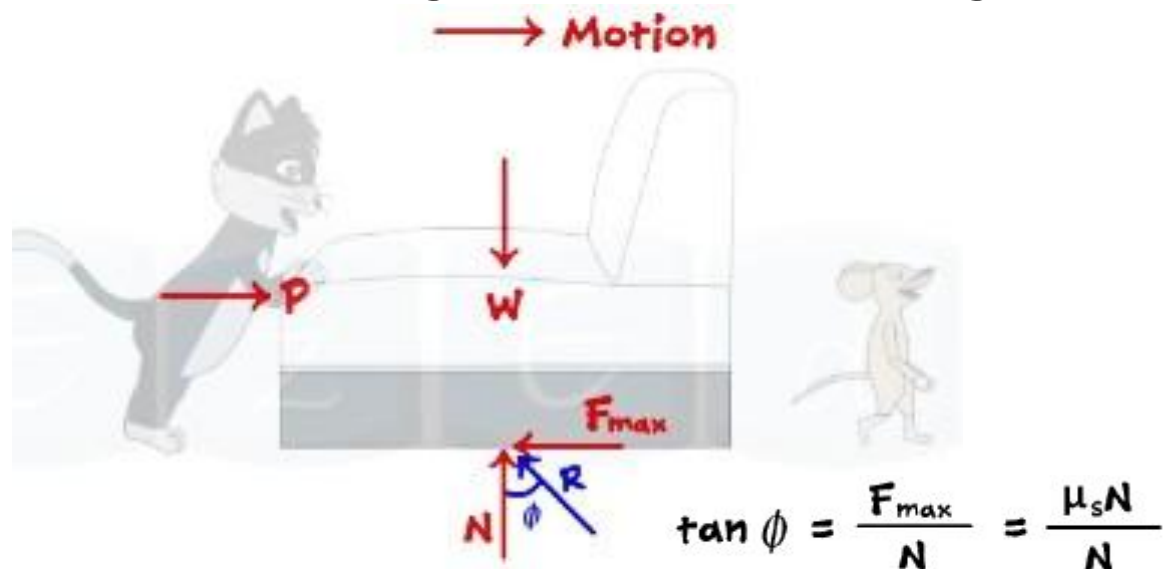
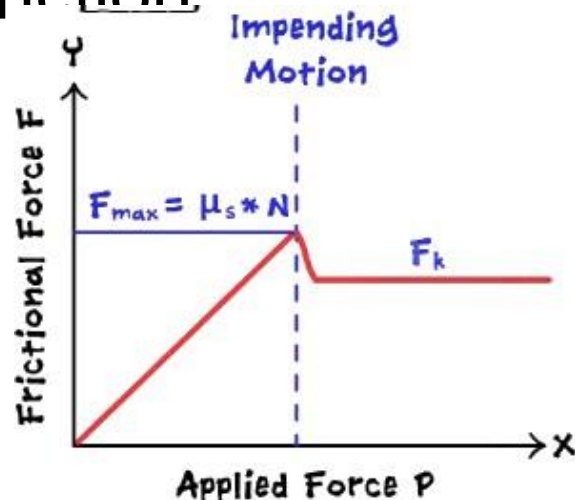
- **Friction** The force of friction always acts in a direction, opposite to that in which the body tends to move.



- The magnitude of the force of friction is exactly equal to the applied force which just moves the body
- The magnitude of the limiting friction bears a constant ratio to the normal reaction between the two surfaces in contact
- The force of friction is independent of the area of contact between the two surfaces.

# Basic Terms in

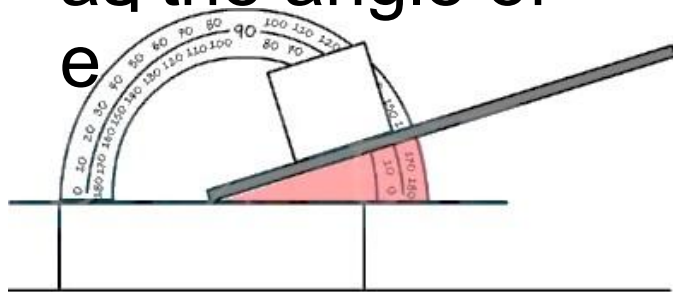
- **Limiting Friction** The maximum static friction after which the body will start moving is called limiting friction.



- **Angle of Friction** The angle of friction for two contacting surfaces is the angle between the resultant  $R$  (of friction force  $F$  and the normal reaction  $N$ ) and the normal reaction  $N$ .

# Basic Terms in Friction

□ **Angle of Repose** The maximum angle made by the inclined plane with the horizontal, when the body placed on that plane is just at the point of sliding down the plane without any external force is known as the angle of



Apply  
COE

$$\mu_s N - W \sin \alpha = 0 \dots (i)$$

$$N = W \cos \alpha \dots (ii)$$

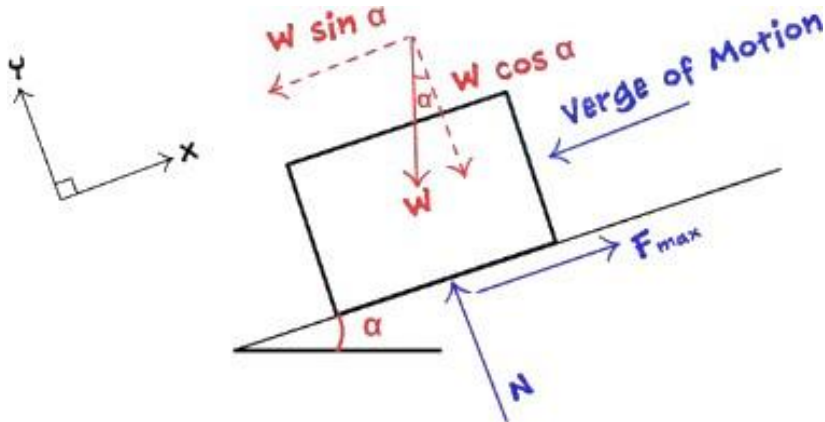
$$\mu_s (W \cos \alpha) - W \sin \alpha = 0$$

$$\tan \alpha = \mu_s \quad \alpha = \tan^{-1} \mu_s$$

$$\phi = \tan^{-1} \mu_s$$

$$\alpha = \phi$$

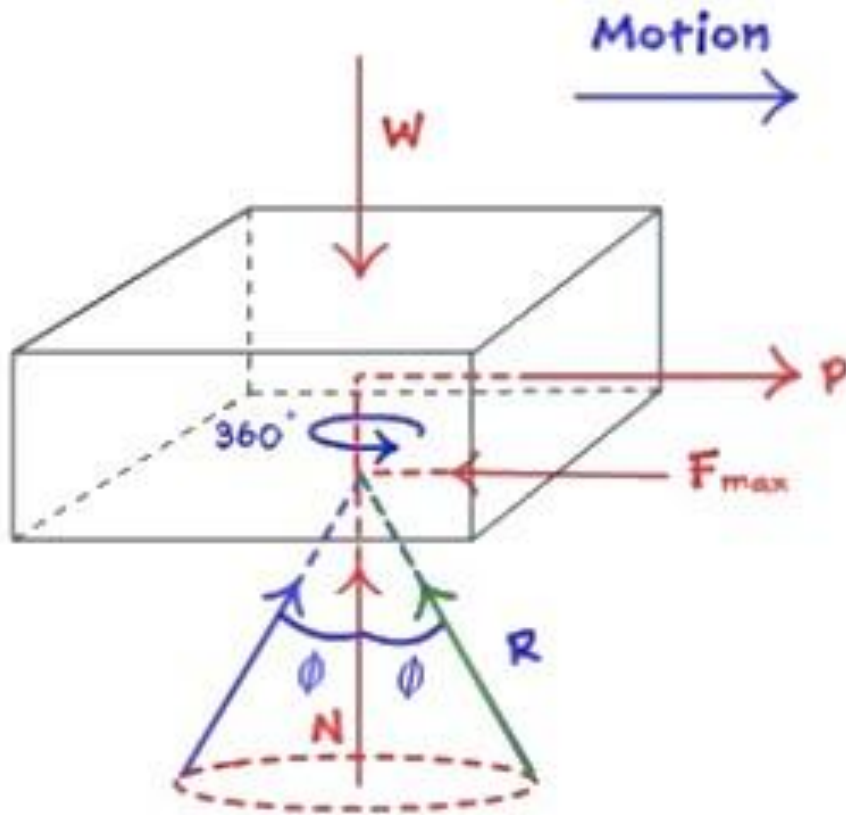
We know  
that,



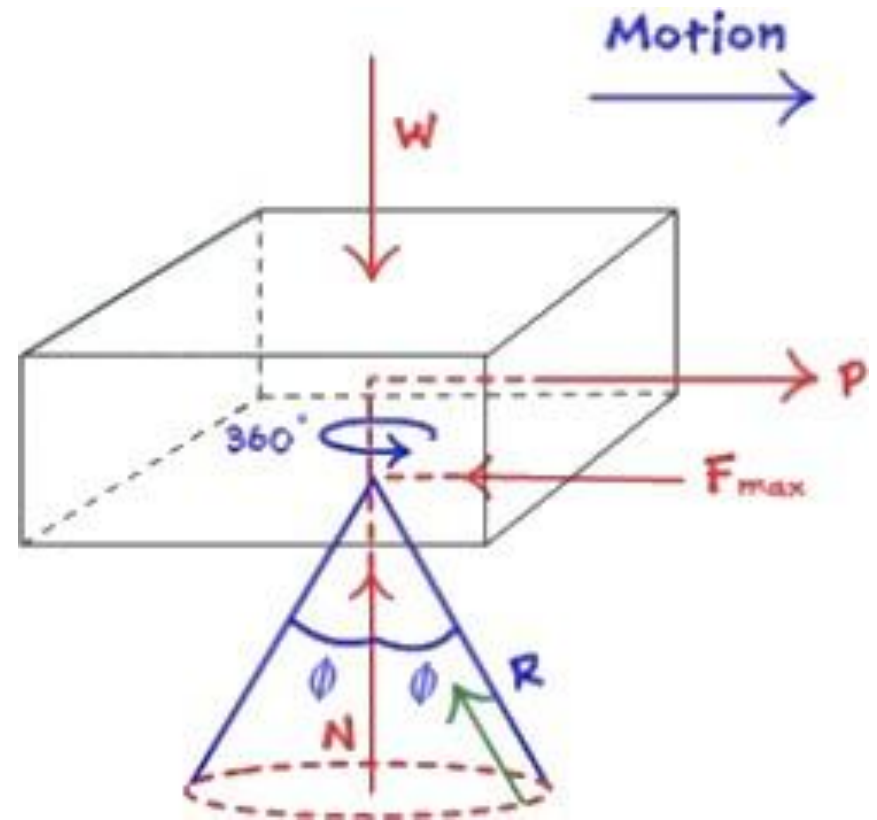


# Basic Terms in Friction

## □ Cone of Friction



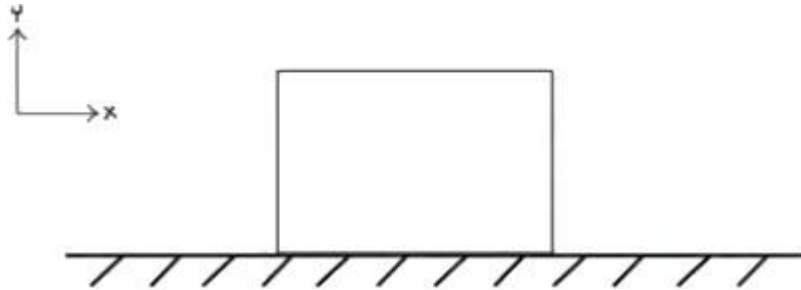
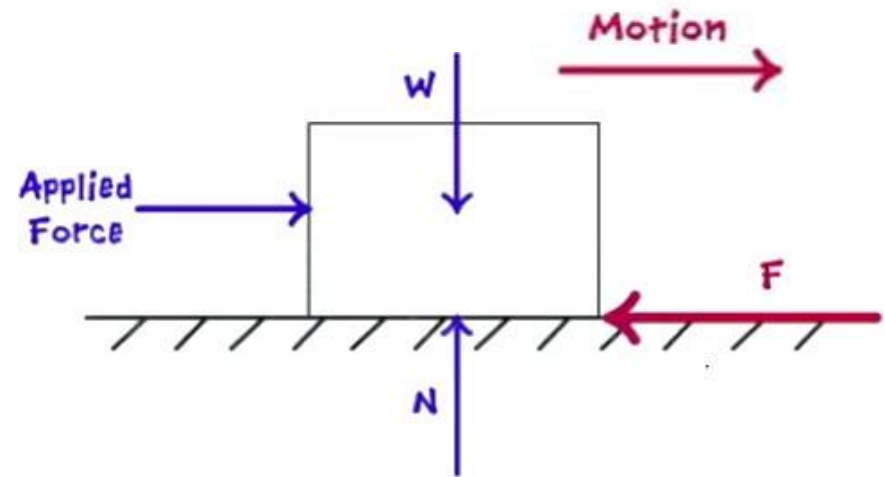
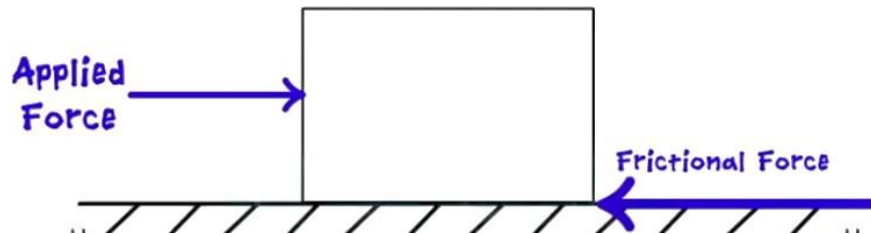
Static body  
under verge  
of motion



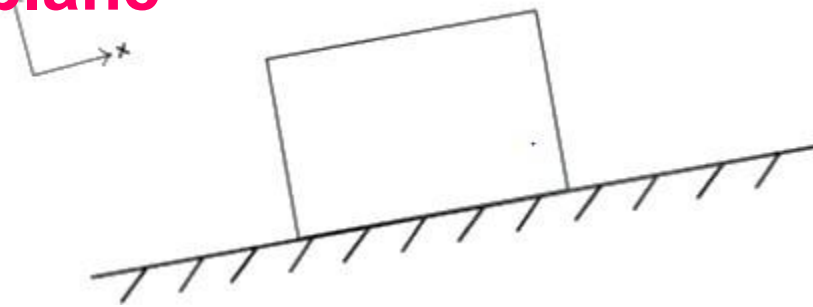
Static body  
under  
Equilibrium



# Block Friction



## Block Friction on Horizontal plane



Apply COE to the system

$$\sum F_x = 0 \Rightarrow \text{ve}$$

$$\sum F_y = 0 \Rightarrow \text{ve}$$

Find Unknowns

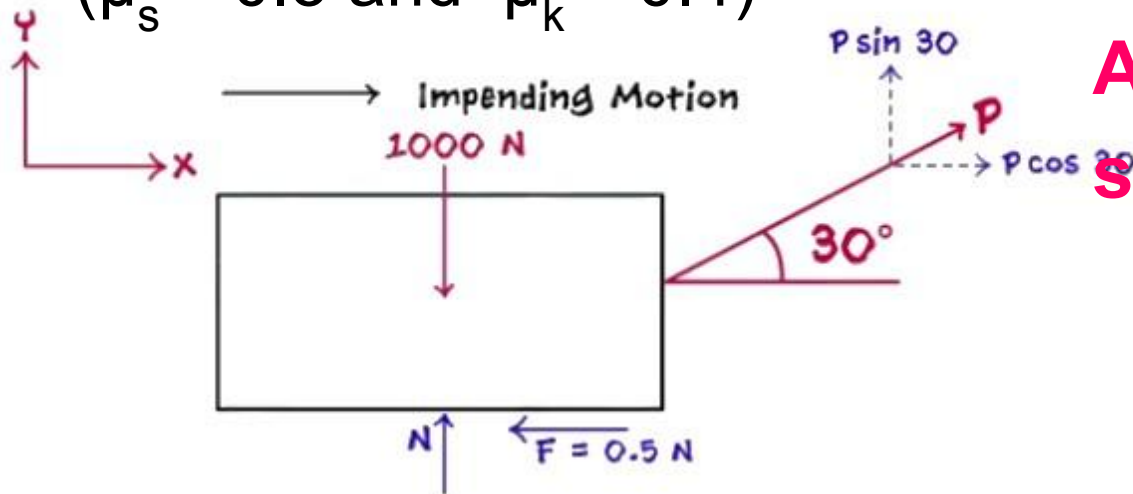
## Block Friction on Inclined plane

# Block Friction on Horizontal

**Plane** A block of weight 1000N is kept on a rough horizontal surface

. A force  $P$  is applied on the block to induce the motion. Find the magnitude of force ' $P$ ' for motion to just impend.

( $\mu_s = 0.5$  and  $\mu_k = 0.4$ )



**Apply COE to the system**

$$\sum F_x = 0 \quad +ve$$

$$P \cos 30^\circ - 0.5N = 0$$

$$N = 1.732P$$

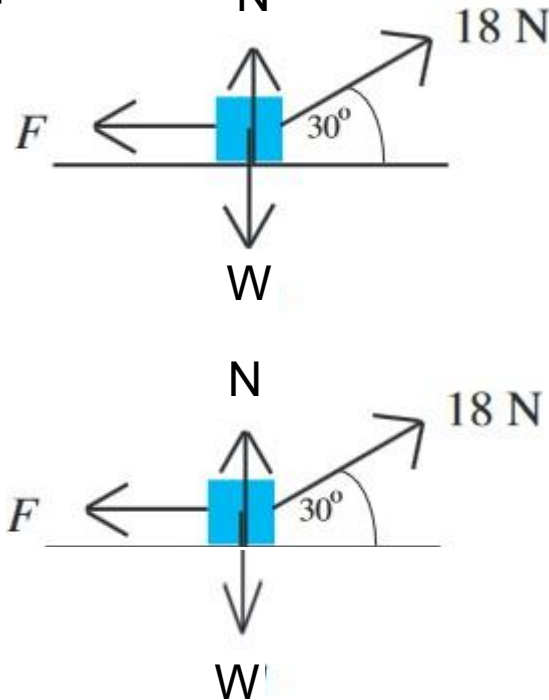
$$N - 1000 + P \sin 30^\circ = 0$$

$$\sum F_y = 0 \quad +ve$$

$$P = 448.02 \text{ N}$$

**FB**  
**D**

2. A force of 18 N acts on a particle, of mass 7.5 kg, at an angle of  $30^\circ$  above the horizontal. The particle is on a rough horizontal plane. Given that the particle is on the point of slipping, what is the coefficient of friction, between the particle and the plane?



**FB**  
**D**

**Apply COE to the system**  $\Rightarrow$

$$\sum F_x = 18 \cos 30^\circ - F = 0$$

$$\sum F_y = N - 7.5 \times 9.81 + 18 \sin 30^\circ = 0$$

$$N = 7.5 \times 9.81 - 18 \sin 30^\circ$$

$$18 \cos 30^\circ = \mu_s (7.5 \times 9.81 - 18 \sin 30^\circ)$$

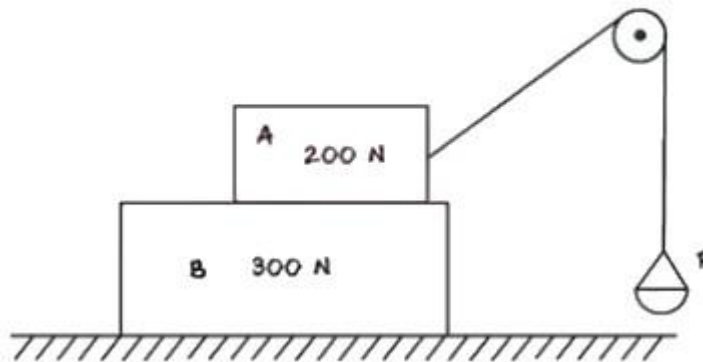
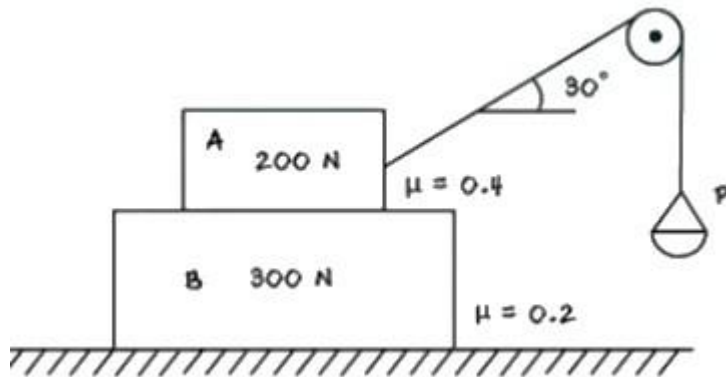
$$\mu_s = 0.24$$

$$ma = 18 \cos 30^\circ - 0.24(7.5 \times 9.81 - 18 \sin 30^\circ)$$

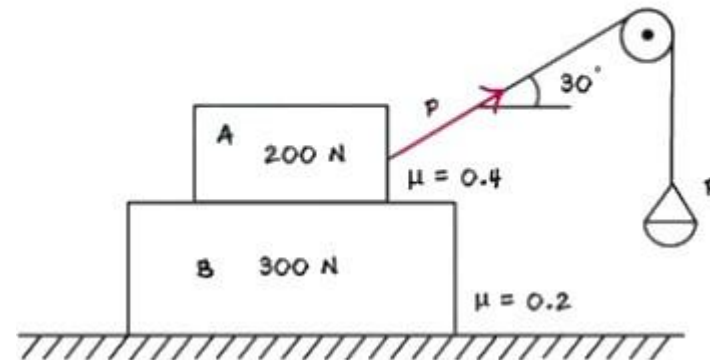
$$a = 0.012 \text{ m/s}^2$$

3. Block A is on block B which is resting on the ground. Block A is attached to a string which is connected to a pan carrying some weight, P. Find the minimum value of weight in the pan so that motion can start. (Ground &

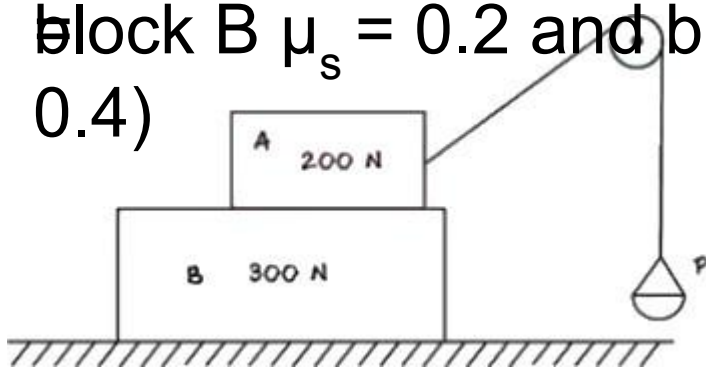
Block A & ①



②



3. Block A is on block B which is resting on the ground. Block A is attached to a string which is connected to a pan carrying some weight, P. Find the minimum value of weight in the pan so that motion can start. (Ground & block B  $\mu_s = 0.2$  and block A & B  $\mu_s = 0.4$ )



Apply COE to the system

$$\Sigma F_x = 0 \dots \rightarrow +ve$$

$$P \cos 30 - 0.4 N_1 = 0$$

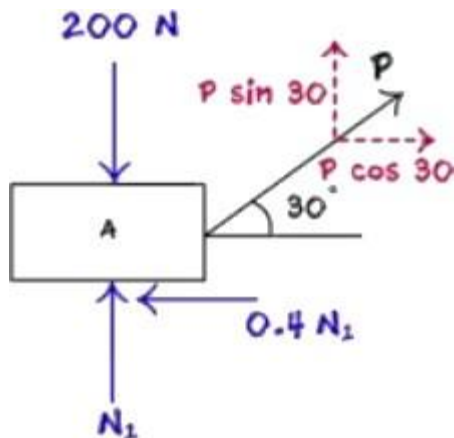
$$N_1 = \frac{P \cos 30}{0.4} \quad N_1 = 2.165 P$$

$$\Sigma F_y = 0 \dots \uparrow +ve$$

$$N_1 - 200 + P \sin 30 = 0$$

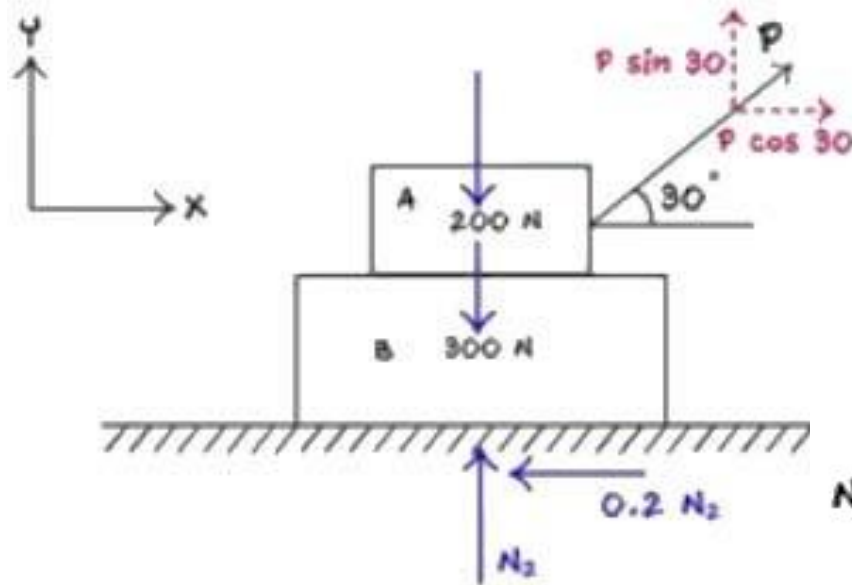
$$2.165 P - 200 + P \sin 30 = 0$$

$$P = 75.05 \text{ N}$$





3. Block A is on block B which is resting on the ground. Block A is attached to a string which is connected to a pan carrying some weight, P. Find the minimum value of weight in the pan so that motion can start. (Ground & block B  $\mu_s = 0.2$  and block A & B  $\mu_s = 0.4$ )



Apply COE to the system

$$\Sigma F_x = 0 \dots \rightarrow +ve$$

$$P \cos 30 - 0.2 N_2 = 0$$

$$N_2 = \frac{P \cos 30}{0.2}$$

$$N_2 = 4.33 P$$

$$\Sigma F_y = 0 \dots \uparrow +ve$$

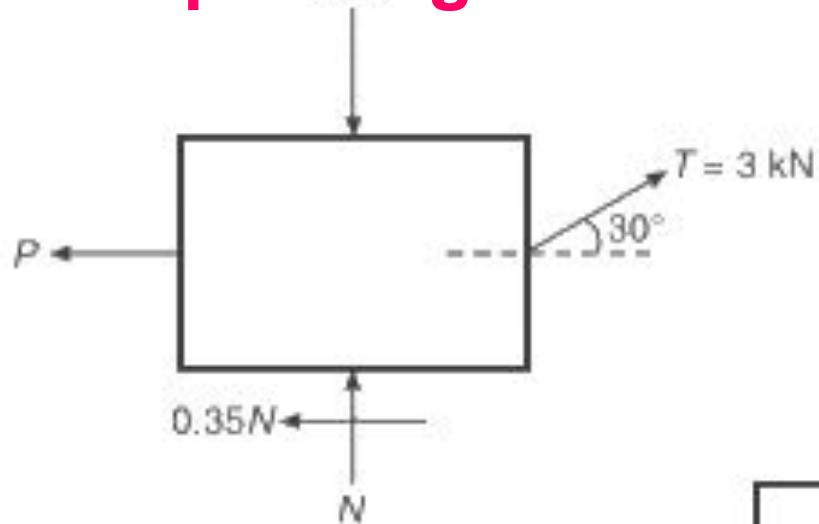
$$N_2 - 200 - 300 + P \sin 30 = 0$$

$$4.33 P - 500 + P \sin 30 = 0$$

$$P = 103.52 \text{ N}$$

4. A block weighing 6 kN is attached to a string, which passes over a frictionless pulley and supports a weight of 3 kN. Determine the value of force  $P$  when the (i) motion is impending towards right. (ii) motion is impending towards left.  $\mu = 0.35$

**Case 1: When motion is impending towards right**



**FB  
D**

**Apply COE to the system**

$$\sum F_y = 0 \quad \uparrow \text{ve}$$

$$3 \sin 30^\circ - 6 + N = 0$$

$$N = 4.5 \text{ kN}$$

$$\sum F_x = 0 \quad \Rightarrow \text{ve}$$

$$-P + 3 \cos 30^\circ - 0.35 N = 0$$

$$P = 1.023 \text{ kN}$$



4. A block weighing 6 kN is attached to a string, which passes over a frictionless pulley and supports a weight of 3 kN. Determine the value of force P when the (i) motion is impending towards right. (ii) motion is impending towards left.  $\mu = 0.35$

**Case 1: When motion is impending towards left**

**Apply COE to the system**

$$\sum F_y = 0 \Rightarrow +ve \uparrow$$

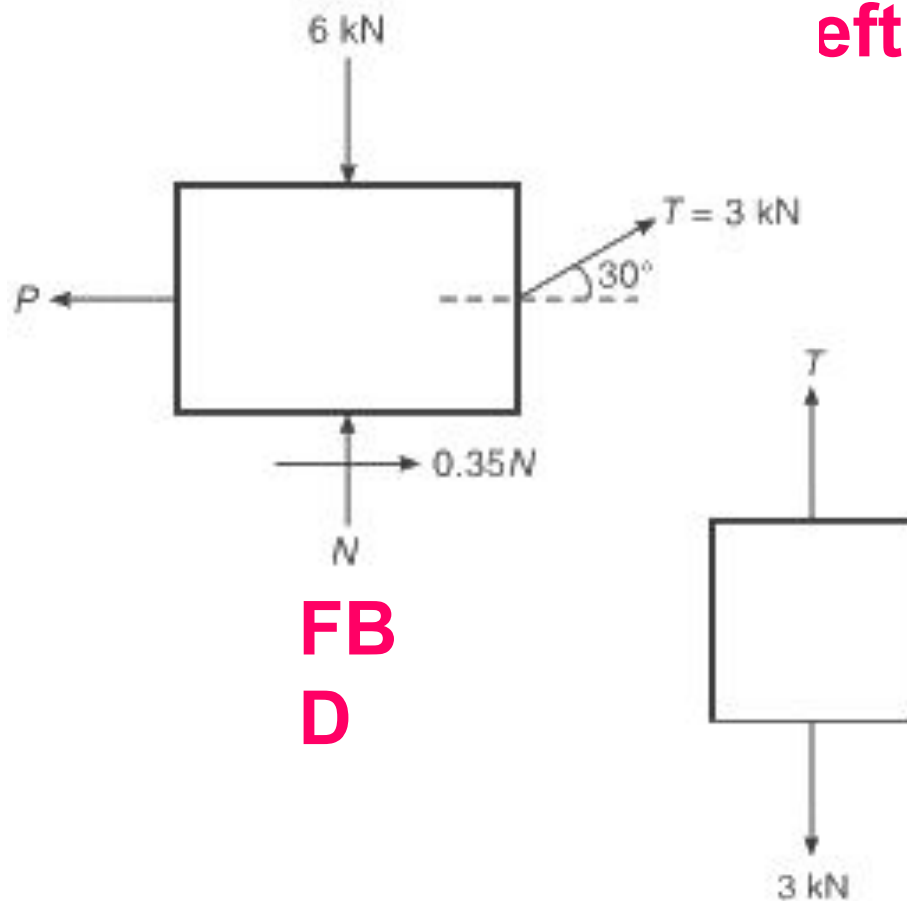
$$3 \sin 30^\circ - 6 + N = 0$$

$$N = 4.5 \text{ kN}$$

$$\sum F_x = 0 \Rightarrow +ve \rightarrow$$

$$-P + 3 \cos 30^\circ + 0.35 N = 0$$

$$P = 4.173 \text{ kN}$$



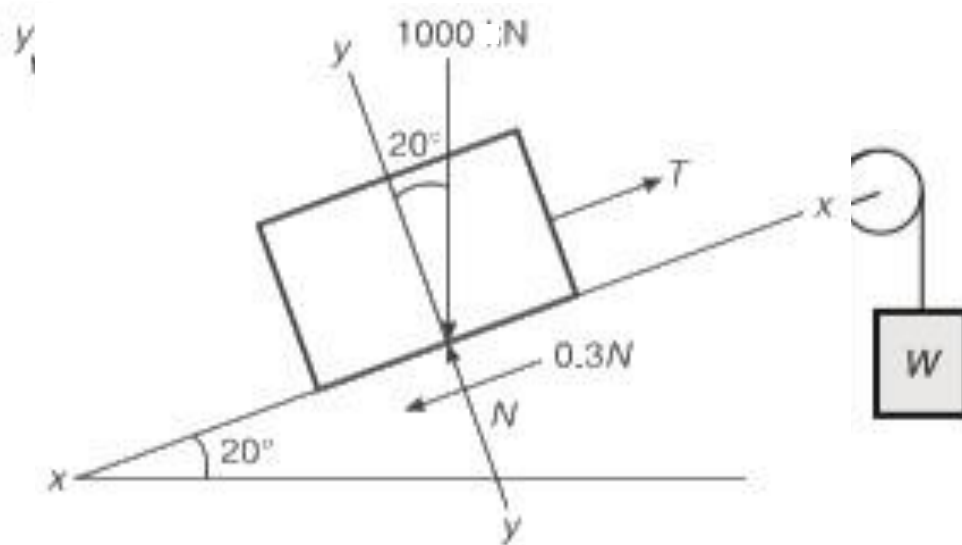
**FB  
D**

# Block Friction on Inclined

**Plane** Calculate the value of  $W$  required for (i) To cause the body to move in the upward direction. (ii) To cause the body to move in the downward direction. Take  $\mu = 0.3$ .

**Case 1: When motion is impending towards upward**

**Apply COE to the system**



**FB**  
**D**

$$\sum F_Y = 0 + \uparrow$$

$$-1000 \cos 20^\circ + N = 0$$

$$N = 939.693 \text{ N}$$

$$\sum F_X = 0 + \rightarrow$$

$$T - 0.3 * 939.693 - 1000 \sin 20^\circ = 0$$

$$T = 623.911 \text{ kN}$$

# Block Friction on Inclined Plane

Calculate the value of  $W$  required for (i) To cause the body to move in the upward direction. (ii) To cause the body to move in the downward direction. Take  $\mu = 0.3$ .

**Case 1: When motion is impending towards downward**

**Apply COE to the system**

$$\sum F_y = 0 \quad \uparrow \text{ve}$$

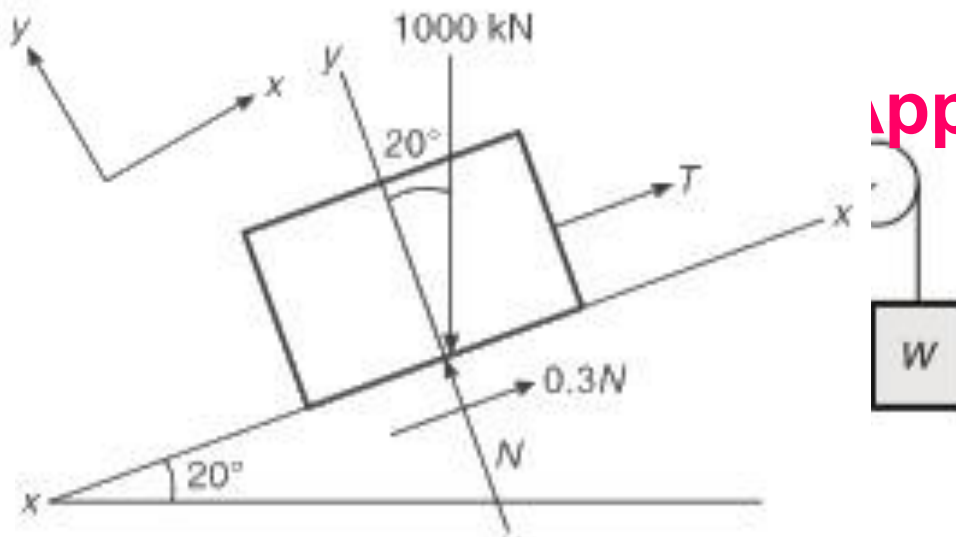
$$-1000 \cos 20^\circ + N = 0$$

$$N = 939.693 \text{ N}$$

$$\sum F_x = 0 \quad \rightarrow \text{ve}$$

$$T + 0.3N - 1000 \sin 20^\circ = 0$$

$$T = 60.112 \text{ kN}$$



**FB**  
**D**

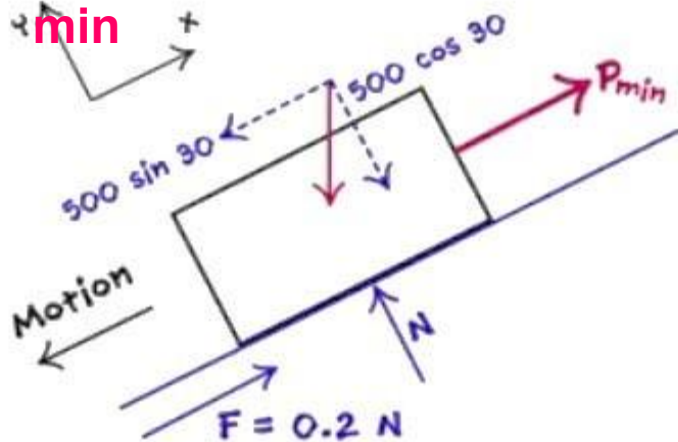


# Block Friction on Inclined

**Plane** A block of weight 500N is placed on a inclined plane. A force  $P$  is applied parallel to inclined plane on the block to keep it in equilibrium. Determine the range of values of force ' $P$ ' for which the block will be in equilibrium. ( $\mu = 0.2$ )

**Case 1:**

**$P_{\min}$**



**FB**  
**D**

**Apply COE to the**

**$\Sigma F_y = 0 \uparrow \text{ve}$**

$$N - 500 \cos 30 = 0$$

$$N = 433 \text{ N}$$

**$\Sigma F_x = 0 \Rightarrow \text{ve}$**

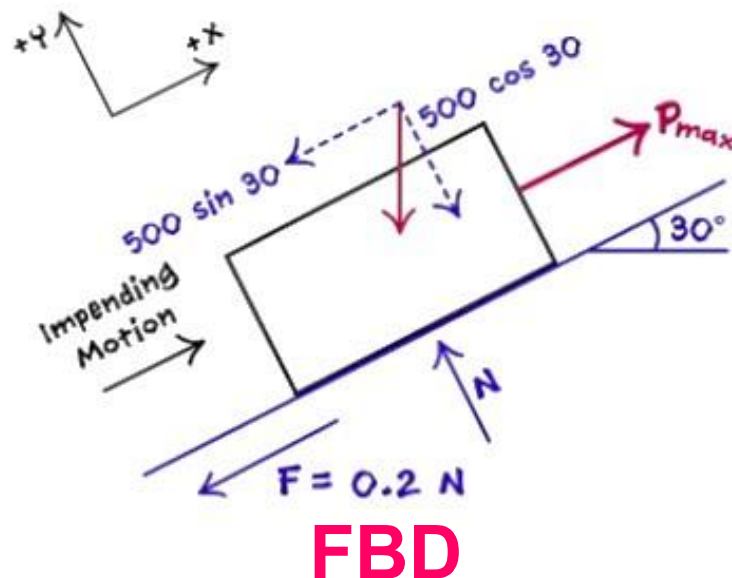
$$P_{\min} - 500 \sin 30 + 0.2N = 0$$

$$P_{\min} = 163.4 \text{ N}$$

# Block Friction on Inclined

**Plane** A block of weight 500N is placed on a inclined plane. A force  $P$  is applied parallel to inclined plane on the block to keep it in equilibrium. Determine the range of values of force ' $P$ ' for which the block will be in equilibrium. ( $\mu = 0.2$ )

**Case 2:**



$$163.4 \text{ N} \leq P \leq 336.6 \text{ N}$$

**Apply COE to the system**

$$\sum F_y = 0 \quad \uparrow \text{ve}$$

$$N - 500 \cos 30 = 0$$

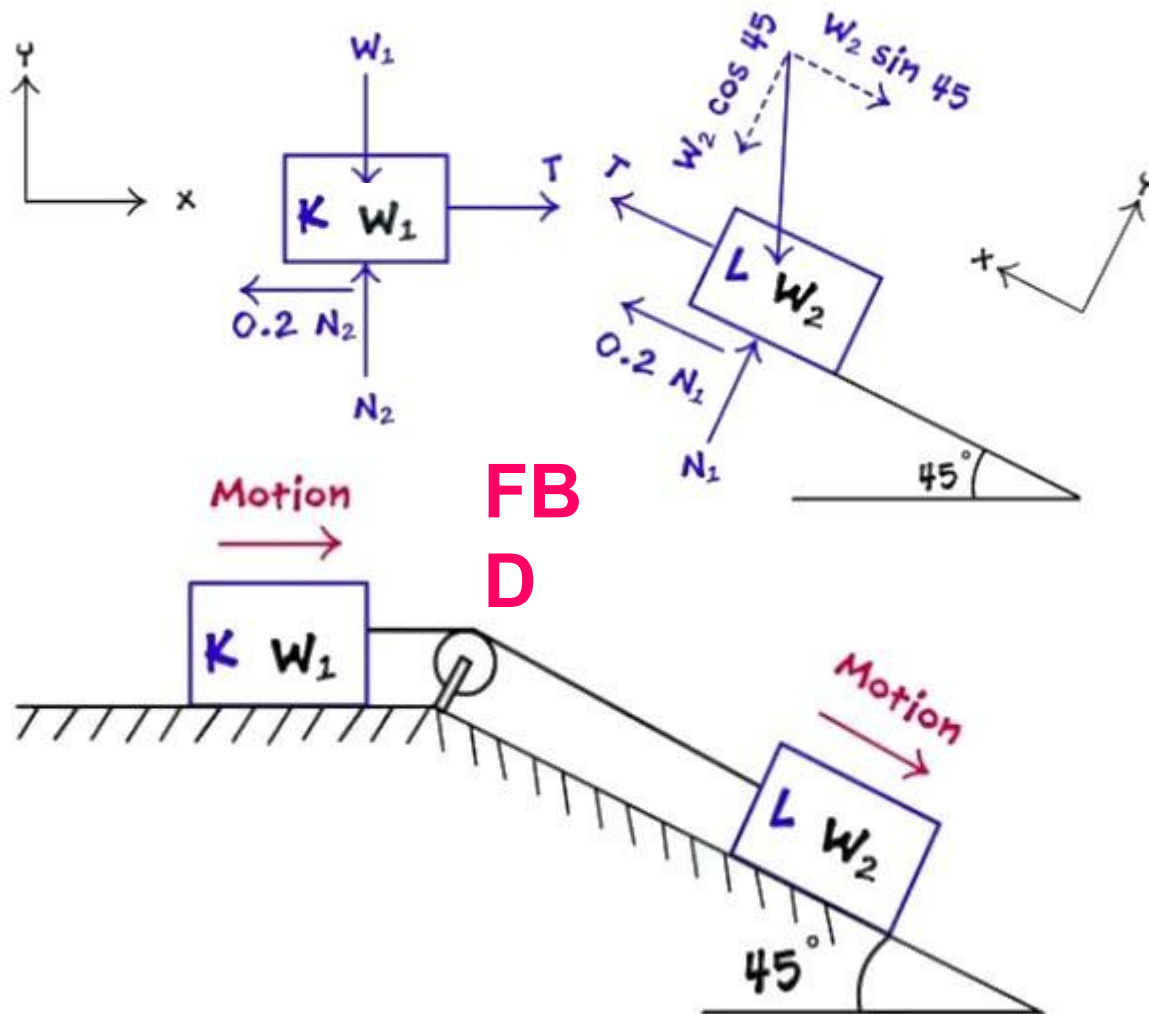
$$N = 433 \text{ N}$$

$$\sum F_x = 0 \quad \Rightarrow \text{ve}$$

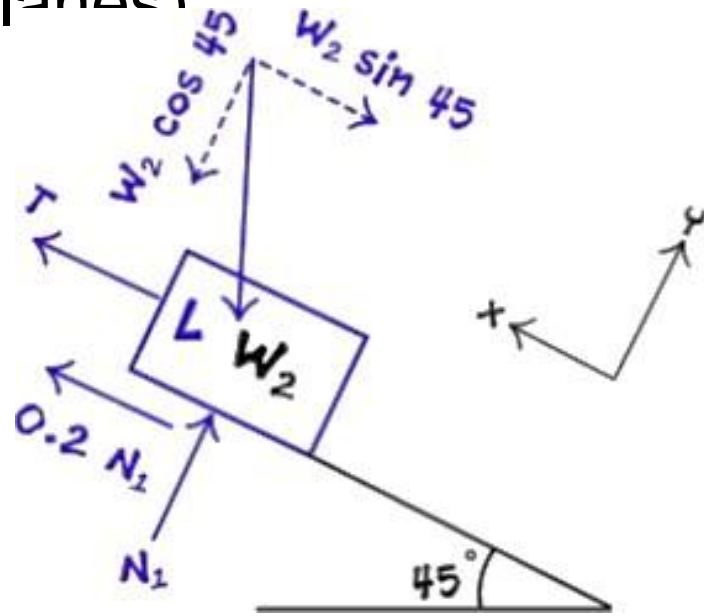
$$P_{\max} - 500 \sin 30 - 0.2N = 0$$

$$P_{\min} = 336.6 \text{ N}$$

3. A string passes through a small pulley connecting 2 blocks (K and L) weighing  $W_1$  and  $W_2$ . One block is on horizontal plane and other on inclined plane. Calculate the min ratio of  $W_1/W_2$  to maintain equilibrium. ( $\mu = 0.2$  for both the planes)



3. A string passes through a small pulley connecting 2 blocks weighing  $W_1$  and  $W_2$ . One block is on horizontal plane and other on inclined plane. Calculate the min ratio of  $W_1/W_2$  to maintain equilibrium. ( $\mu = 0.2$  for both the planes)



**FB  
D**

**Apply COE Inclined  
plane (L)**  $\Uparrow$

$$\sum F_Y = 0 \quad +ve$$

$$N_1 - W_2 \cos 45 = 0$$

$$N_1 = 0.707 W_2$$

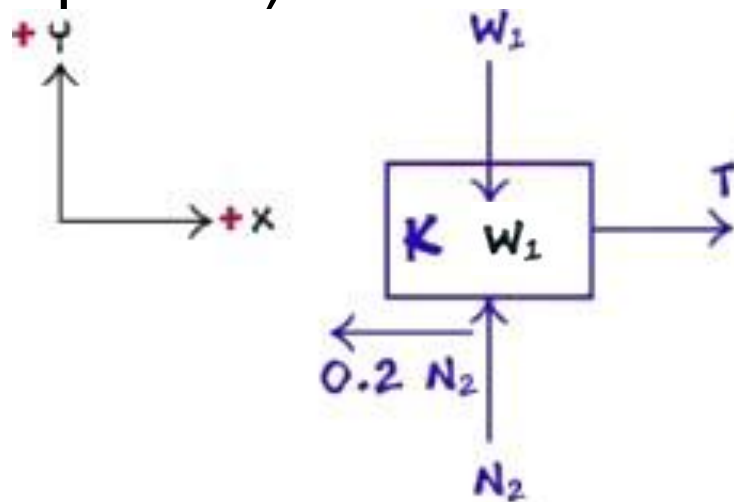
$\Rightarrow$

$$\sum F_X = 0 \quad +ve$$

$$-T - 0.2 N_1 + W_2 \sin 45 = 0$$

$$T = 0.566 W_2$$

3. A string passes through a small pulley connecting 2 blocks weighing  $W_1$  and  $W_2$ . One block is on horizontal plane and other on inclined plane. Calculate the min ratio of  $W_1/W_2$  to maintain equilibrium. ( $\mu = 0.2$  for both the planes)



**FB  
D**

$$N_1 = 0.707 W_2 \quad T = 0.566 W_2$$

**Apply COE Horizontal**

$$\Sigma F_y = 0 \quad \uparrow + \text{ve}$$

$$N_2 - W_1 = 0$$

$$N_2 = W_1$$

$$\Sigma F_x = 0 \Rightarrow + \text{ve}$$

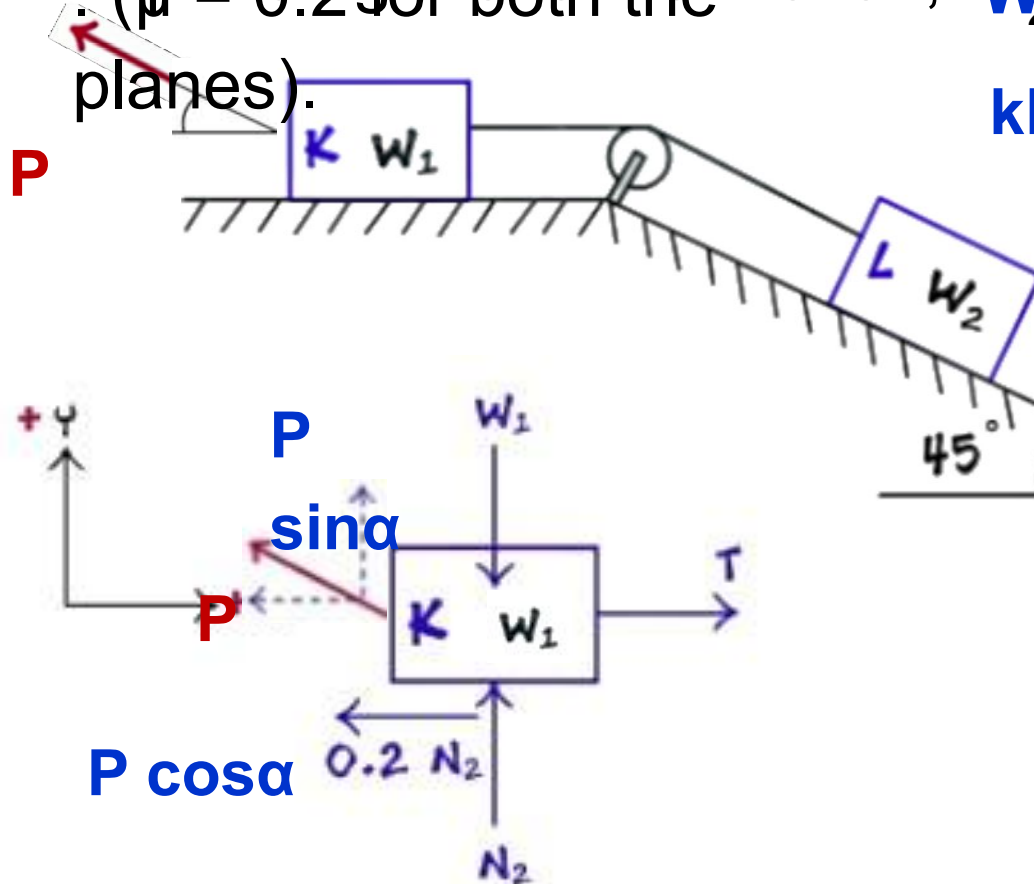
$$T - 0.2 N_2 = 0$$

$$0.556 W_2 - 0.2 W_1 = 0$$

$$W_1 / W_2 = 2.83$$



4. A string passes through a small pulley connecting 2 blocks weighing  $W_1$  and  $W_2$ . One block is on horizontal plane and other on inclined plane. Find the least value of  $P$  required to cause the system of blocks to have impending motion to the left,  $W_1 = 1 \text{ kN}$ ,  $W_2 = 2.83 \text{ kN}$ ,  $N_1 = 0.707 \text{ kN}$  ( $\mu = 0.2$  for both the planes).



$$T = 0.566 \text{ kN}$$

Apply COE Horizontal plane

$$\sum F_Y = 0 + \text{ve}$$

$$N_2 + P \sin \alpha - W_1 = 0$$

$$N_2 = 2.83 - P \sin \alpha$$

$$\sum F_X = 0 + \text{ve}$$

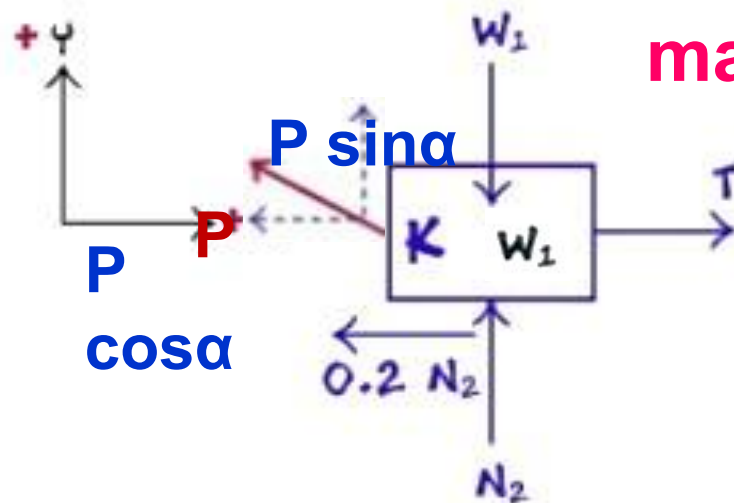
$$0.566 - 0.2N_2 + P \cos \alpha = 0$$

$$P = 1/(\cos \alpha + 0.2 \sin \alpha)$$

FB  
D

2. A string passes through a small pulley connecting 2 blocks weighing  $W_1$  and  $W_2$ . One block is on horizontal plane and other on inclined plane. Find the least value of  $P$  required to cause the system of blocks to have impending motion to the left. ( $\mu = 0.2$  for both the planes).  $W_2 = 1 \text{ kN}$

**P is min, when the denominator is max**



**FB**  
**D**

$$\frac{d}{d\alpha} (\cos \alpha + 0.2 \sin \alpha) = 0$$

$$-\sin \alpha + 0.2 \cos \alpha$$

$$= 0$$

$$\tan \alpha =$$

$$\alpha =$$

$$0.2$$

$$11.31$$

$$P_{\min} = 1 / (\cos \alpha + 0.2 \sin \alpha)$$

$$P_{\min} = 0.98 \text{ kN}$$