

⇒ Implement unification in FOL

Algorithm:  $\text{unity}(\psi_1, \psi_2)$

Step 1: If  $\psi_1$  or  $\psi_2$  is a variable or constant, then:

a) If  $\psi_1$  or  $\psi_2$  are identical, then return NULL.

b) Else if  $\psi_1$  is a variable,

a. then if  $\psi_1$  occurs in  $\psi_2$ , then return fail

b. Else return  $\{(\psi_2/\psi_1)\}$

c. Else if  $\psi_2$  is variable

i. if  $\psi_2$  occurs in  $\psi_1$  return fail

ii. Else return  $\{(\psi_1/\psi_2)\}$

d. Else return fail.

Step 2: If the initial Predicate symbol in  $\psi_1$  and  $\psi_2$  are not same, return fail

Step 3: If  $\psi_1$  and  $\psi_2$  have a different no. of arguments then return fail

Step 4: Set substitution  $\text{set}(\text{SUBST})$  to NULL

Step 5: for  $i=1$  to the no. of elements in  $\psi_1$

a) call unify function with the  $i$ th element of  $\psi_1$  and  $i$ th element of  $\psi_2$  and put result into  $S$

b) If  $S = \text{Failure}$  return Failure

c) If  $S \neq \text{NULL}$  then do

a. apply  $S$  to remaining of both  $\psi_1$  and  $\psi_2$

b.  $\text{subst} = \text{Append}(S, \text{subst})$

Step 6: Return  $\text{SUBST}$

Outputs:

$$S1 = ('P', 'X', ('Y', 'X')), ('Y')$$

$$S2 = ('P', 'a', 'Y', ('Y', 'X'))$$

unification successful.

substitution:  $\{ 'X' : 'a', 'Y' : ('Y', 'X') \}$

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# stfpurcas

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[1]: print("Name:Sudarshan Komar","USN:1BM22CS291",sep="\n")

def unify(s1, s2, theta={}):
    """
    Unifies two first-order logic expressions.

    Args:
        s1: The first expression.
        s2: The second expression.
        theta: The current substitution.

    Returns:
        A substitution that unifies s1 and s2, or None if they cannot be unified.
    """

    if theta is None:
        return None

    if s1 == s2:
        return theta

    if isinstance(s1, str) and s1.islower(): # Variable
        return unify_var(s1, s2, theta)

    if isinstance(s2, str) and s2.islower(): # Variable
        return unify_var(s2, s1, theta)

    if isinstance(s1, tuple) and isinstance(s2, tuple) and len(s1) == len(s2):
        return unify(s1[1:], s2[1:], unify(s1[0], s2[0], theta))

    return None

def unify_var(var, x, theta):
    if var in theta:
        return unify(theta[var], x, theta)
    elif x in theta:
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        return unify(var, theta[x], theta)
    elif occurs_check(var, x, theta):
        return None # Occurs check failed
    else:
        theta[var] = x
        return theta

def occurs_check(var, x, theta):
    if var == x:
        return True
    elif isinstance(x, str) and x.islower() and x in theta:
        return occurs_check(var, theta[x], theta)
    elif isinstance(x, tuple):
        for arg in x:
            if occurs_check(var, arg, theta):
                return True
    return False

s1 = ('p', 'x', ('f', 'x'), ('y'))
s2 = ('p', 'a', 'y', ('f', 'x'))

substitution = unify(s1, s2)

if substitution:
    print("Unification successful:")
    print(f"Substitution: {substitution}")
else:
    print("Unification failed.")

```

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Unification successful:

Substitution: {'x': 'a', 'y': ('f', 'x')}