

## Forward Reasoning Algorithm.

create knowledge base consisting of first order logic statements and prove the given query using forward reasoning

function FOL-FC-Ask(KB,  $\alpha$ ) returns a substitution or false  
 inputs: KB, the knowledge base, a set of first-order definite clauses  $\alpha$ , the query, an atomic sentence.

local variables: new, the new sentences inferred on each iteration

repeat until new is empty

new  $\leftarrow \{\}$

for each rule in KB do

$(p_1 \wedge \dots \wedge p_n \Rightarrow q) \leftarrow \text{standardize-variables}(\text{rule})$

for each  $\theta$  such that  $\text{subst}(\theta, p_1 \wedge \dots \wedge p_n)$

for some  $p'_1, \dots, p'_n$  in KB

$q' \leftarrow \text{subst}(\theta, q)$

if  $q'$  does not unify with some sentence already in KB or new then

add  $q'$  to new

$\phi \leftarrow \text{unify}(q', \alpha)$

if  $\phi$  is not fail then

return  $\phi$

add new to KB

return false

- Q Consider the following problem.
- As per the law, it is a crime for an American to sell weapons to hostile nations. Country A, an enemy of America has some missiles and all the missiles were sold to it by Robert, who is an American citizen.

Prove Robert is criminal.

Knowledge-based

"facts": "American(Robert)": True  
 "Enemy(A, America)": True,  
 "Owns(A, T1)": True,  
 "Missile(T1)": True,

}

"rules": [

{ "if": ["Missile(x)"], "then": ["weapon(x)"] },

{ "if": ["Enemy(x, America)"], "then": ["hostile(x)"] },

{ "if": ["Missile(x)", "owns(A, x)"], "then": ["sells(Robert, x, A)"] },

{ "if": ["American(p)", "weapon(q)", "sells(p, q, r)", "hostile(r)"], "then": ["criminal(p)"] },

}

],

}

output:

# after running forward chaining algo.

Proved: Robert is criminal.



Q Write the FOL for following.

→ Emily is either a surgeon or a lawyer  
 $\text{occupation}(\text{Emily}, \text{surgeon}) \vee$

$\text{occupation}(\text{Emily}, \text{lawyer})$

→ Joe is an actor, but he also holds another job

$\text{occupation}(\text{Joe}, \text{Actor}) \wedge \exists x : \text{occupation}(\text{Joe}, x) \wedge x \neq \text{Actor}$

→ All surgeons are doctors

$\forall p : \text{occupation}(p, \text{surgeon}) \Rightarrow \text{occupation}(p, \text{Doctor})$

→ Joe does not have a lawyer

$\forall p : \neg \text{occupation}(p, \text{lawyer}) \wedge \text{customer}(\text{Joe}, p)$

→ Emily has a boss who is a lawyer

$\exists p : \text{Boss}(p, \text{Emily}) \wedge \text{occupation}(p, \text{lawyer})$

→ There exists a lawyer all of whose customers are doctors

$\exists p : \text{occupation}(p, \text{lawyer}) \wedge \forall c :$

$\text{customer}(p, c) \Rightarrow \text{occupation}(c, \text{Doctor})$

→ Every surgeon has a lawyer

$\forall p : \text{occupation}(p, \text{surgeon}) \Rightarrow \exists l :$

$\text{occupation}(l, \text{lawyer}) \wedge \text{customer}(p, l)$

# fmem3ehyc

December 21, 2024

```
[1]: # Facts in the Knowledge Base
print("Name:Sudarshan Komar","USN:1BM22CS291",sep="\n")
knowledge_base = {
    "facts": {
        "American(Robert)": True,
        "Enemy(A, America)": True,
        "Owns(A, T1)": True,
        "Missile(T1)": True,
    },
    "rules": [
        # Rule 1: Missiles are weapons
        {"if": ["Missile(x)", "then": ["Weapon(x)"]}],

        # Rule 2: Enemy of America is hostile
        {"if": ["Enemy(x, America)", "then": ["Hostile(x)"]}],

        # Rule 3: If a missile is owned by A, Robert sold it
        {"if": ["Missile(x)", "Owns(A, x)", "then": ["Sells(Robert, x, A)"]}],

        # Rule 4: Law: Selling weapons to hostile nations is a crime
        {
            "if": ["American(p)", "Weapon(q)", "Sells(p, q, r)", "Hostile(r)"],
            "then": ["Criminal(p)"],
        },
    ],
}

def forward_chaining(kb):
    # Extract facts and rules
    facts = kb["facts"].copy()
    rules = kb["rules"]

    # Keep track of inferred facts
    inferred = set()

    while True:
```

```

new_inferences = set()

for rule in rules:
    # Check if all conditions of the rule are satisfied
    if_conditions = rule["if"]
    then_conditions = rule["then"]

    # Create a substitution for the rule variables
    substitutions = {}
    all_conditions_met = True

    for condition in if_conditions:
        # Extract the predicate and arguments
        predicate, args = condition.split("(")
        args = args[:-1].split(",") # Remove closing parenthesis and
↪split

        # Check for matching facts
        matched = False
        for fact in facts:
            fact_predicate, fact_args = fact.split("(")
            fact_args = fact_args[:-1].split(",")

            if predicate == fact_predicate and len(args) ==
↪len(fact_args):

                # Match variables or constants
                temp_subs = {}
                for var, val in zip(args, fact_args):
                    if var.islower(): # It's a variable
                        if var in temp_subs and temp_subs[var] != val:
                            break # Conflict in substitution
                        temp_subs[var] = val
                    elif var != val: # Constants must match
                        break

                else:
                    # Valid match
                    matched = True
                    substitutions.update(temp_subs)
                    break

            if not matched:
                all_conditions_met = False
                break

    # If all conditions are met, infer the "then" facts
    if all_conditions_met:
        for condition in then_conditions:

```

```

        # Apply substitutions to the "then" condition
        predicate, args = condition.split("(")
        args = args[:-1].split(",")
        new_fact = predicate + "(" + ",".join(substitutions.
↪get(arg, arg) for arg in args) + ")"
        new_inferences.add(new_fact)

    # Add new inferences to the knowledge base
    if new_inferences - inferred:
        inferred.update(new_inferences)
        facts.update({fact: True for fact in new_inferences})
    else:
        break

    return inferred

# Run forward chaining
result = forward_chaining(knowledge_base)

# Check if Robert is a criminal
if "Criminal(Robert)" in result:
    print("Proved: Robert is a criminal.")
else:
    print("Could not prove that Robert is a criminal.")

```

Name:Sudarshan Komar

USN:1BM22CS291

Proved: Robert is a criminal.