

## \* Resolution

1. Convert all sentences to CNF

Steps to convert logical statement to CNF

(a) Eliminate biconditional &amp; implication

i) eliminate  $\Leftrightarrow$  representing  $\alpha \Leftrightarrow \beta$ to  $\alpha \Rightarrow \beta \wedge \beta \Rightarrow \alpha$ ii) Eliminate  $\Rightarrow$  representing  $\alpha \Rightarrow \beta$   
with  $\neg \alpha \vee \beta$ (b) move  $\neg$  inwardly

i)  $\neg (\forall x p) \equiv \exists x \neg p$

ii)  $\neg (\exists x p) \equiv \forall x \neg p$

iii)  $\neg (\alpha \vee \beta) \equiv \neg \alpha \wedge \neg \beta$

iv)  $\neg (\alpha \wedge \beta) \equiv \neg \alpha \vee \neg \beta$

v)  $\neg \neg \alpha \equiv \alpha$

(c) Standardize variables apart by  
replacing them, each quantifier should  
use a different variable

(d) Skolemize each existential variables

is replaced by a skolem constant or  
skolem function of the enclosing  
universally quantified variableex.  $\exists \text{Rich}(x)$  becomes  $\text{Rich}(c)$ ,  $c$   
a new skolem constant

(e) Drop universal quantifier

 $\forall x \text{ person}(x)$  becomes  $\text{person}(x)$

① Distribute  $\wedge$  over  $\vee$   
 $(\alpha \wedge \beta) \vee \gamma \equiv (\alpha \vee \gamma) \wedge (\beta \vee \gamma)$

2. Negate conclusion  $S$  and convert result to CNF

3. Add negated conclusion  $S$  to the premise clause

4. Repeat until contradiction or no progress is made.

- i) select 2 clauses
- ii) Resolve them together, performing all required unification
- iii) If resolved ~~element~~ is the empty clause, a contradiction has been found.
- iv) If not add resolved to the premise

Ex.

KB or premise

a) John likes all kind of food	a) $\forall x, \text{food}(x) \rightarrow \text{likes}(\text{John}, x)$
b) Apple and vegetable are food	b) $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetable})$
c) Anything anyone eats and not kills are food	c) $\forall x \forall y: \text{eats}(x, y) \wedge \neg \text{killed}(x) \rightarrow \text{food}(y)$
d) Anil eats peanuts and still alive	d) $\text{eats}(\text{Anil}, \text{peanut}) \wedge \text{alive}(\text{Anil})$
e) Harry eats everything that Anil eats	e) $\forall x \text{ eats}(\text{Anil}, x) \rightarrow \text{eats}(\text{Harry}, x)$
f) Anyone who is alive implies not kills	f) $\forall x \text{ alive}(x) \rightarrow \neg \text{killed}(x)$
g) Anyone who is not killed implies alive	g) $\forall x \neg \text{killed}(x) \rightarrow \text{alive}(x)$



prove by resolution that b) John likes peanut  
 (b) likes(John, peanut)

Eliminate implication

- a)  $\forall x \rightarrow \text{food}(x) \vee \text{likes}(\text{John}, x)$
- b)  $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetable})$
- c)  $\forall x \forall y \rightarrow (\text{eats}(x, y) \wedge \neg \text{killed}(x)) \vee \text{food}(y)$
- d)  $\text{eats}(\text{Anil}, \text{peanut}) \wedge \text{alive}(\text{Anil})$
- e)  $\forall x \rightarrow \text{eats}(\text{Anil}, x) \vee \text{eats}(\text{Harry}, x)$
- f)  $\forall x \rightarrow (\neg \text{killed}(x)) \vee \text{alive}(x)$
- g)  $\forall x \rightarrow \text{alive}(x) \vee \neg \text{killed}(x)$
- h)  $\text{likes}(\text{John}, \text{peanut})$

move  $\neg$  inward

$$\forall x \forall y \neg (\text{eats}(x, y) \vee \text{killed}(x) \vee \text{food}(y))$$

standardize variables

- c)  $\forall y \forall z \neg (\text{eats}(y, z) \vee \text{killed}(y) \vee \text{food}(z))$
- e)  $\forall w \neg \text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$
- f)  $\forall g \neg \text{killed}(g) \vee \text{alive}(g)$
- g)  $\forall k \neg \text{alive}(k) \vee \neg \text{killed}(k)$

drop universal quantifiers

- a)  $\neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
- b)  $\text{food}(\text{Apple})$
- c)  $\text{food}(\text{vegetable})$
- d)  $\neg \text{eats}(y, z) \vee \text{killed}(y) \vee \text{food}(z)$
- e)  $\text{eats}(\text{Anil}, \text{peanuts})$
- f)  $\text{alive}(\text{Anil})$
- g)  $\neg \text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$
- h)  $\neg \text{killed}(g) \vee \text{alive}(g)$
- i)  $\neg \text{alive}(k) \vee \neg \text{killed}(k)$
- j)  $\text{likes}(\text{John}, \text{peanut})$

→  $\neg \text{Likes}(\text{John}, \text{Peanut})$

$\neg \text{food}(x) \vee \text{likes}(\text{John}, x)$

$\text{peanut}(x)$

$\neg \text{food}(\text{peanut})$

$\neg \text{eats}(y, z) \vee \text{killed}(y)$

$\vee \text{food}(z)$

$\{\text{peanut} / z\}$

$\neg \text{eats}(y, \text{peanut}) \vee \text{killed}(y)$

$\text{eat}(\text{Anil}, \text{peanut})$

$\{\text{Anil} / y\}$

$\text{killed}(\text{Anil})$

$\neg \text{alive}(k) \vee \text{killed}(k)$

$\{\text{Anil} / k\}$

$\neg \text{alive}(\text{Anil})$

$\text{alive}(\text{Anil})$

$h)$

hence proved

mnaz7lpj4

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[4]: print("Name:Sudarshan Komar", "USN:1BM22CS291", sep="\n")

from sympy import symbols, Or, And, Not
from sympy.logic.inference import satisfiable

def resolution_proof():
    # Define predicates as symbols
    Eats_Anil_Peanuts = symbols('Eats_Anil_Peanuts')
    NotKilled_Anil = symbols('NotKilled_Anil')
    Food_Peanuts = symbols('Food_Peanuts')
    Likes_John_Peanuts = symbols('Likes_John_Peanuts')

    # Step 1: Encode the statements as clauses
    # Fact 1: Anything anyone eats and is not killed is food
    clause1 = Or(Not(Eats_Anil_Peanuts), Not(NotKilled_Anil), Food_Peanuts)

    # Fact 2: Anil eats peanuts and is still alive
    clause2 = And(Eats_Anil_Peanuts, NotKilled_Anil)

    # Fact 3: John likes all kinds of food
    clause3 = Or(Not(Food_Peanuts), Likes_John_Peanuts)

    # Negate the goal: John does NOT like peanuts
    negated_goal = Not(Likes_John_Peanuts)

    # Step 2: Perform resolution
    # Resolve clause1 and clause2 to prove Food_Peanuts
    resolved_clause1 = clause1.subs({Eats_Anil_Peanuts: True, NotKilled_Anil:
↪True})
    print(f"Resolved Clause 1: {resolved_clause1}")

    # Resolve resolved_clause1 to prove Food_Peanuts
    if resolved_clause1 == Food_Peanuts:
        print("Food(Peanuts) is proven.")

    # Resolve Food_Peanuts with clause3 to prove Likes_John_Peanuts
    resolved_clause2 = clause3.subs({Food_Peanuts: True})
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print(f"Resolved Clause 2: {resolved_clause2}")

# Final check
result = satisfiable(And(resolved_clause2, negated_goal))
if result is False:
    print("The goal 'John likes peanuts' is proven using resolution.")
else:
    print("The goal 'John likes peanuts' cannot be proven.")

# Run the proof
resolution_proof()
```

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Resolved Clause 1: Food\_Peanuts

Food(Peanuts) is proven.

Resolved Clause 2: Likes\_John\_Peanuts

The goal 'John likes peanuts' is proven using resolution.