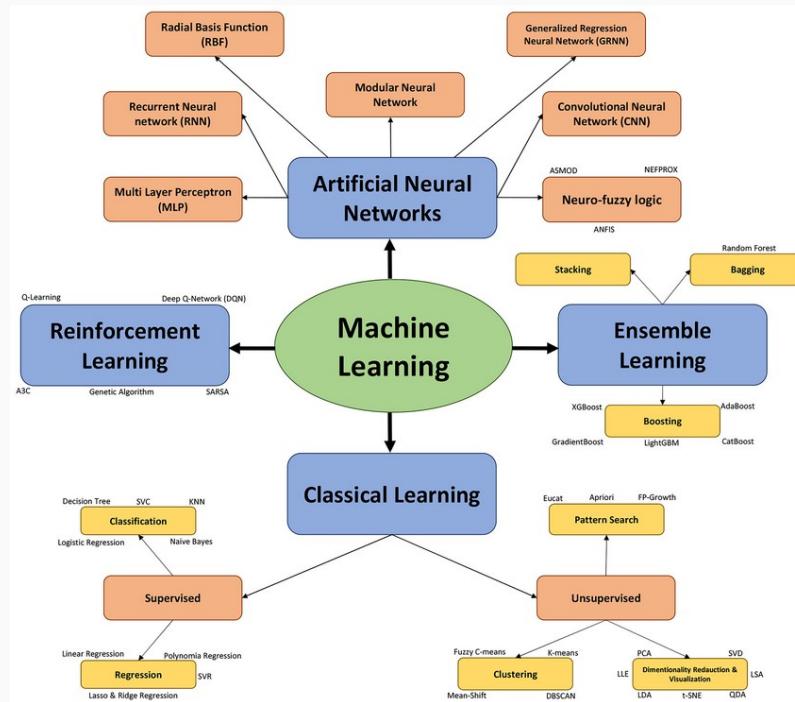


4 Days Workshop on **Artificial Intelligence**



Machine Learning Algorithms



Regression And Classification

What exactly is AI Model ? How does it learn ?

- An AI model is made up of math and numbers that help it make decisions.
- Inside a model, it has **Inputs** (what we give it), **Weights** (how important each input is), **Rules** (math formulas to process the inputs) and **Outputs** (the result or prediction).
- Models try to make predictions.
- They calculate the error between prediction and actual value.
- The model adjusts its weights to reduce this error (training).

Revisiting Linear Regression

The following show the improvement (gain in reading speed) of 8 students in a speed reading program and the number of weeks they have been in program.

Number of weeks	4	5	3	9	7	10	4	5
Speed gain	85	120	48	192	164	234	74	110

2

- b. Find the regression equation of speed gain on number of weeks.
- c. Estimate speed gain of a student who has been in program for 6 weeks and interpret the slope of the line.



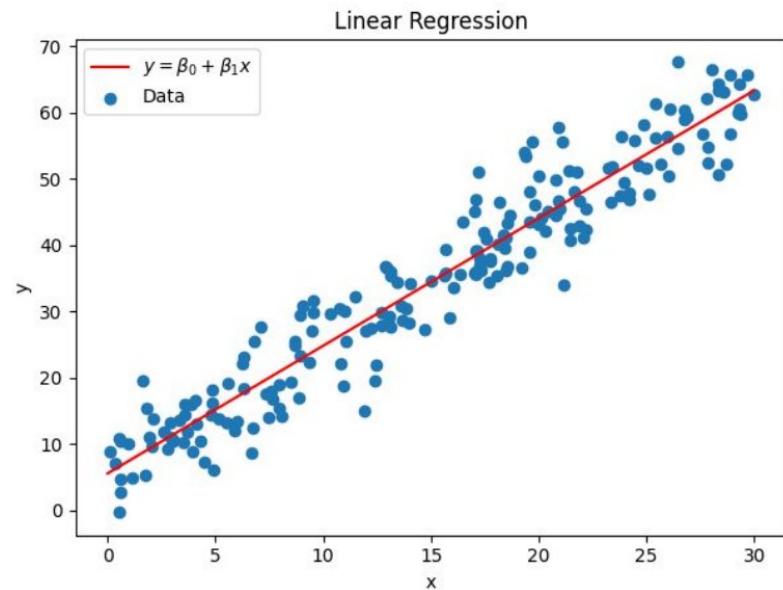
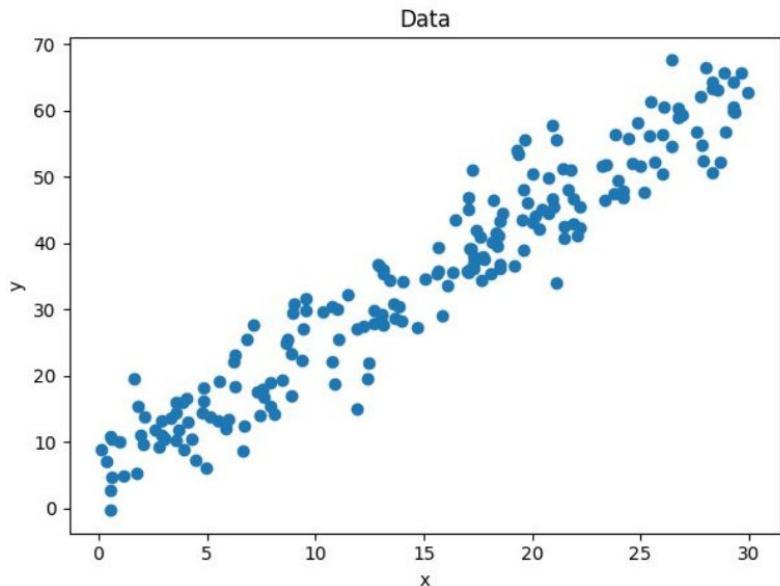
Regression

- Input: **X's** (features, independent, predictors, explanatory variables).
- Output: **y** (outcome, response, dependent variable)
- **Goal:** Find a regression function: $y = f(x, b)$
- Simple Linear Regression: $y = b_0 + b_1 * x$
- Multiple Linear Regression: $y = b_0 + b_1x_1 + b_2x_2 + \dots + b_nx_n$

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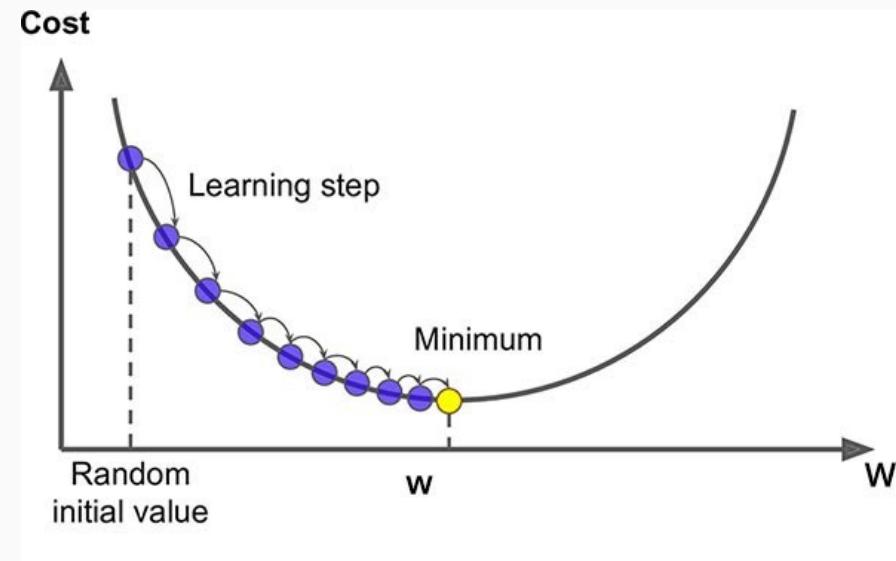
Linear Regression



Ways to solve Linear Regression

- Non-Iterative Method: $\mathbf{B} = (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T \mathbf{y}$

- Gradient Descent method:



Performance Metrics for Regression

$$RSS = \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

$$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i|$$

R-squared:

- how well model performs compared to a “mean model”

Observations $\rightarrow \mathbf{y} \rightarrow (y_1, y_2, \dots, y_n)$

Predictions $\rightarrow \hat{\mathbf{y}} \rightarrow (\hat{y}_1, \hat{y}_2, \dots, \hat{y}_n)$

$$\bar{y} = \frac{1}{n} \sum_{i=1}^n y_i$$

$$SS_{tot} = \sum_{i=1}^n (y_i - \bar{y})^2$$

$$SS_{reg} = \sum_{i=1}^n (\hat{y}_i - \bar{y})^2$$

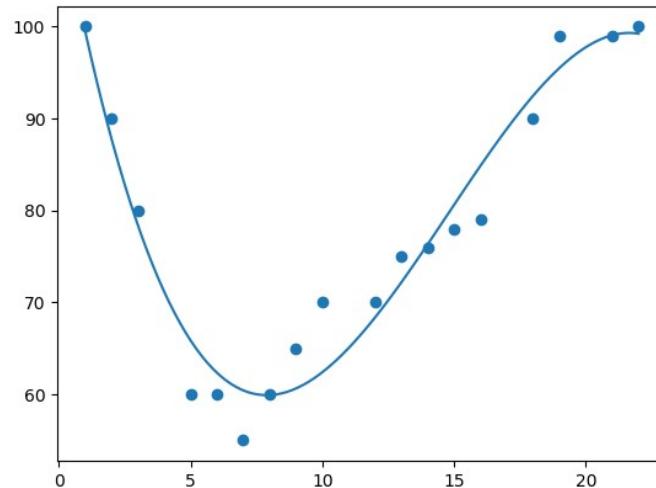
$$SS_{res} = \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

$$R^2 = 1 - \frac{SS_{res}}{SS_{tot}}$$

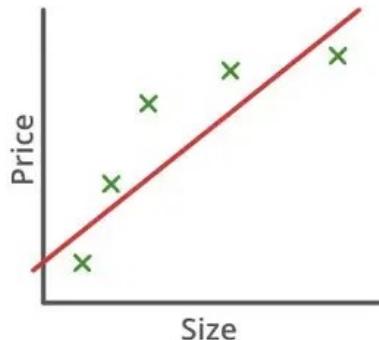
Polynomial Regression

- Polynomial regression: non-linear relationship between x and y

$$Y = ax^2 + bx + c$$

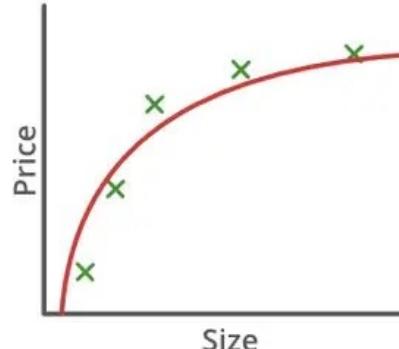


Overfitting vs Underfitting



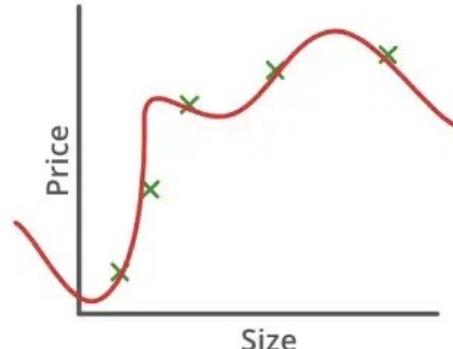
$$\theta_0 + \theta_1 x$$

High Bias
(Underfitting)



$$\theta_0 + \theta_1 x + \theta_2 x^2$$

Low Bias, Low Variance
(Goodfitting)



$$\theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4$$

High Variance
(Overfitting)



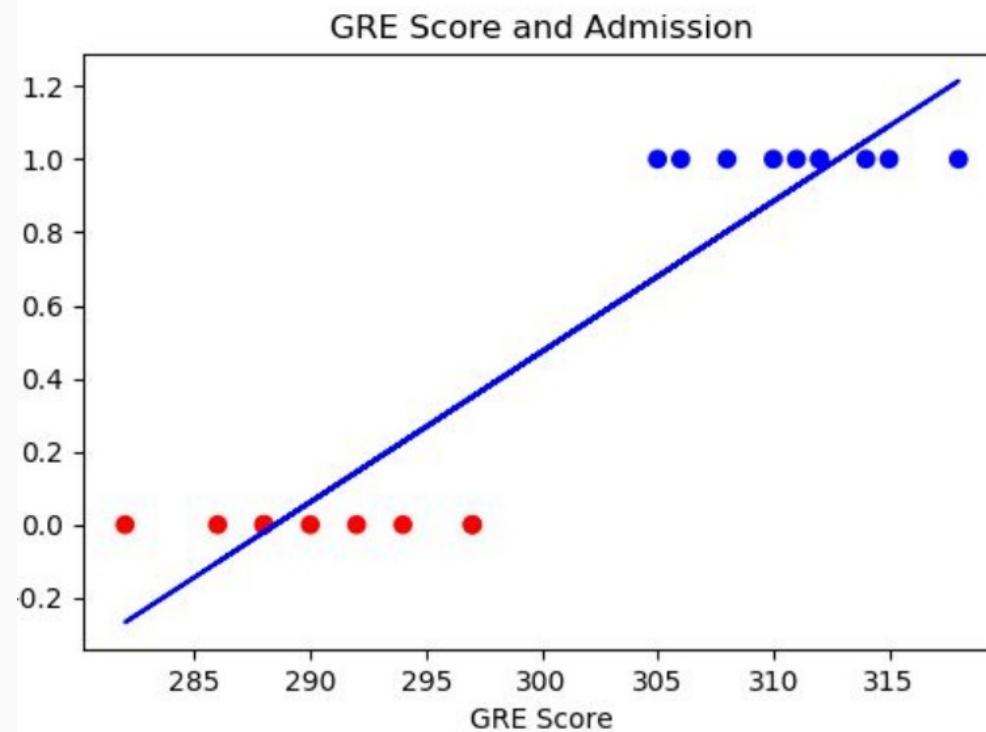


Classification

You have a GRE score of 320. Will you get an admission in a university?

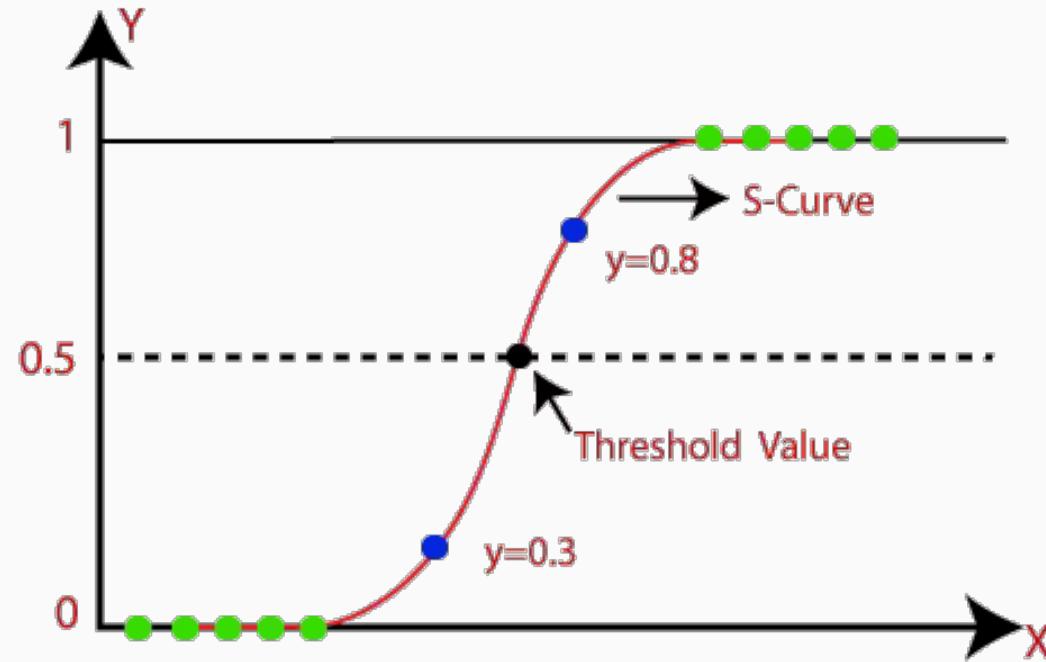
- Get admission – 1
- No admission - 0

Can we use Linear Regression ?

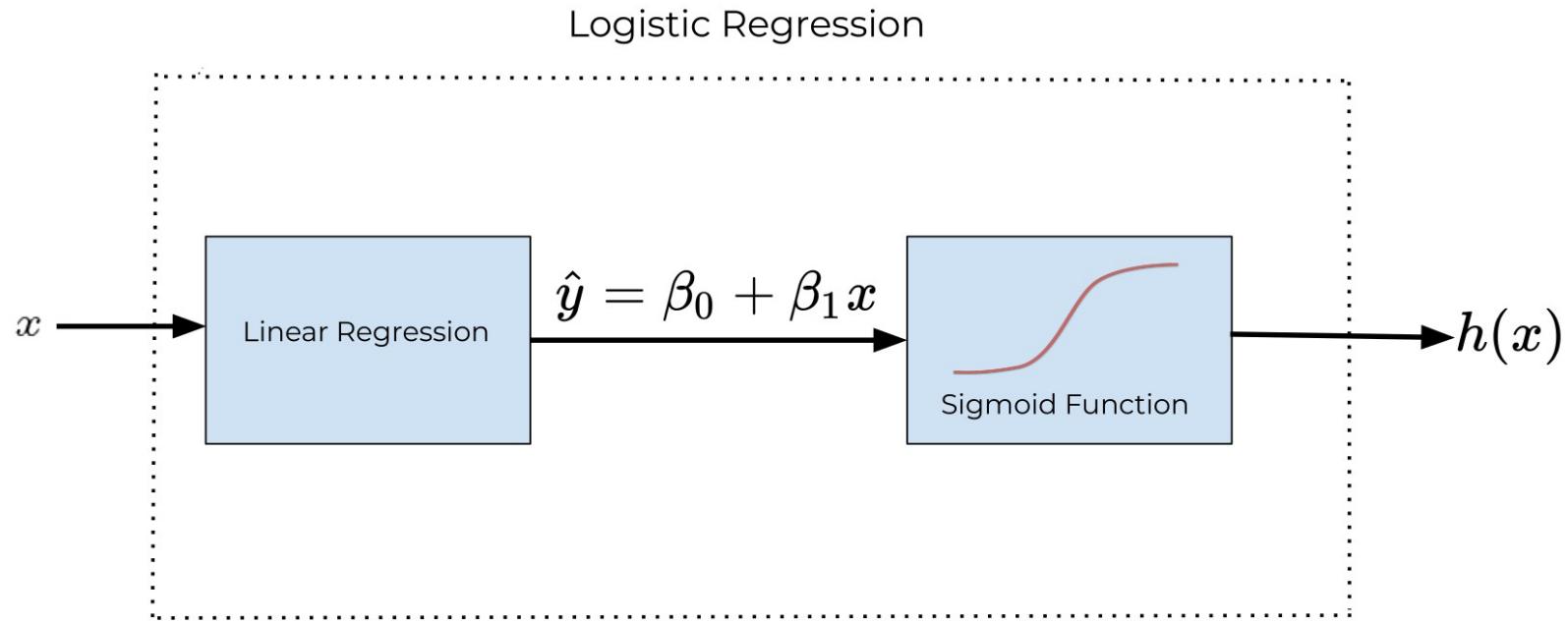


Sigmoid Function

$$A = \frac{1}{1+e^{-x}}$$



Logistic Regression



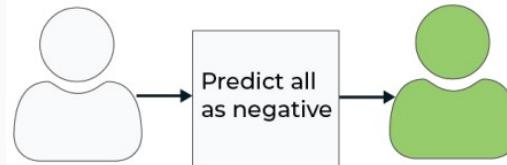
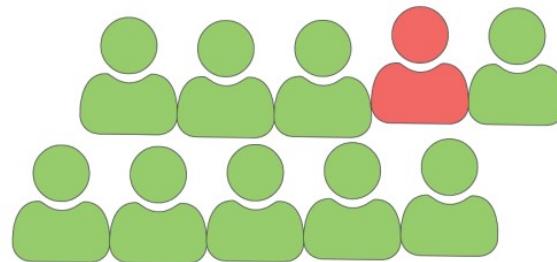
Performance Metrics for Classification

- **Accuracy:** The fraction of predictions that the classifier predicted correctly.

$$\text{Accuracy} = \frac{\text{No. of correct predictions}}{\text{Total no. of predictions}}$$

Accuracy Paradox

Predictive Models
with a high level of
Accuracy always
may not have
greater Predictive
Power than Models
with lower
accuracy.



$$\text{Accuracy} = \frac{9}{10} = 90\%$$

Confusion matrix & F1 Score

ACTUAL VALUES

	POSITIVE	NEGATIVE
POSITIVE	TP	FN
NEGATIVE	FP	TN

$$Precision = \frac{TP}{TP + FP}$$

$$Recall = \frac{TP}{TP + FN}$$

$$Accuracy = \frac{TP + TN}{TP + FP + FN + TN}$$

$$F1\ Score = 2 \times \frac{Precision \times Recall}{Precision + Recall}$$