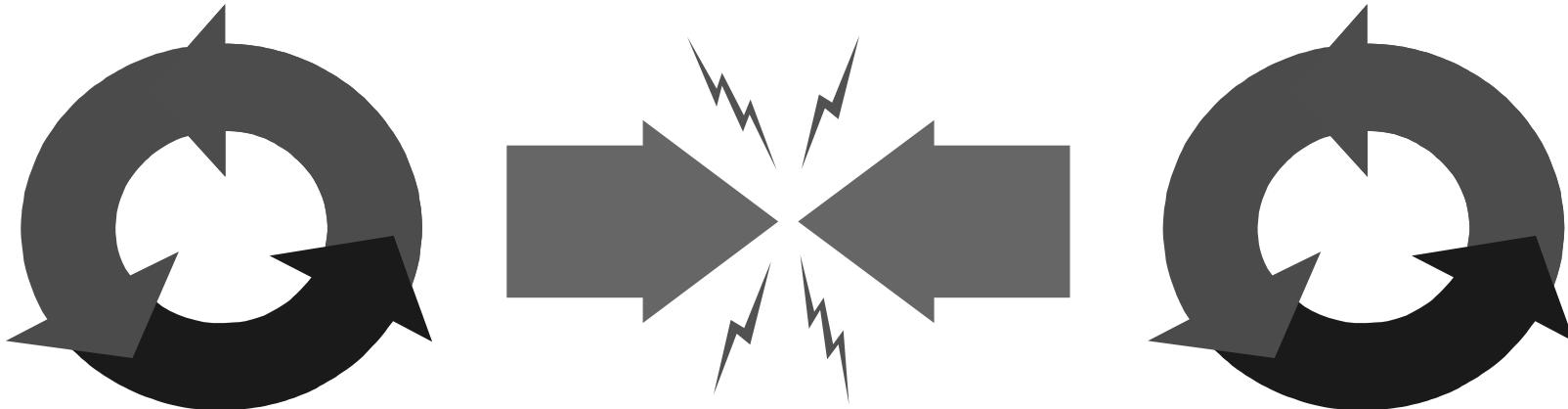


## Concurrency

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# 4 - Shared Objects & Mutual Exclusion



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# Repetition – “Concurrent Execution”

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Concepts: pseudo- vs. real concurrent execution  
concurrent execution and interleaving  
process interaction

Models: parallel composition of asynchronous processes  
- interleaving  
interaction - *shared actions*  
process labeling, action relabeling, and hiding  
structure diagrams

Practice: Multithreaded Java programs

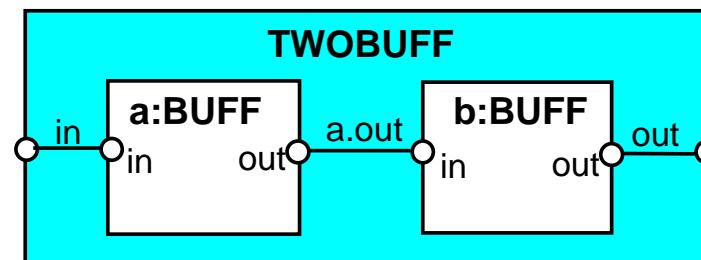
# Repetition (week 06) - Specifically

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## ◆ FSP:

- $P \parallel Q$  // parallel composition
- $a:P$  // action prefixing
- $\{\dots\}:P$  // set prefixing
- $P / \{x/y\}$  // action relabelling
- $P \setminus \{\dots\}$  // hiding
- $P @ \{\dots\}$  // keeping (hide complement)

## ◆ Structure Diagrams:



Concurrency: shared objects & mutual exclusion

©Magee/Kramer

# Shared Objects & Mutual Exclusion

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## ◆ Concepts:

- Process interference
- Mutual exclusion

## ◆ Models:

- Model-checking for interference
- Modelling mutual exclusion

## ◆ Practice:

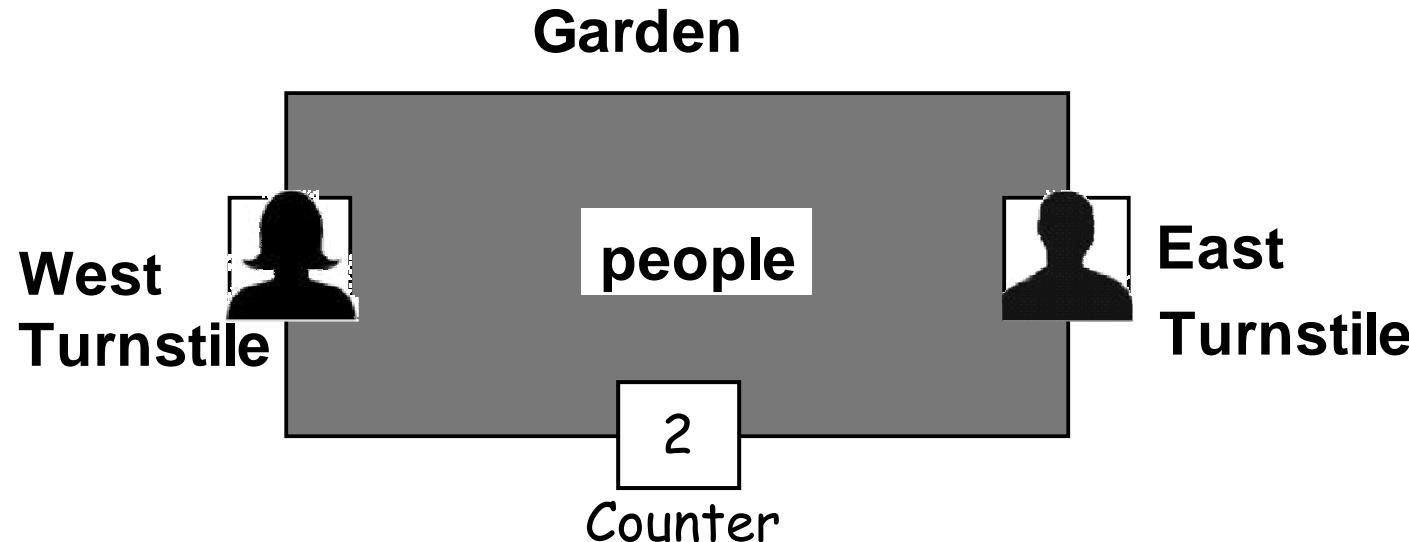
- Thread interference in shared objects in Java
- Mutual exclusion in Java
- synchronized objects, methods, and statements

## 4.1 Interference

---

The "*Ornamental Garden Problem*":

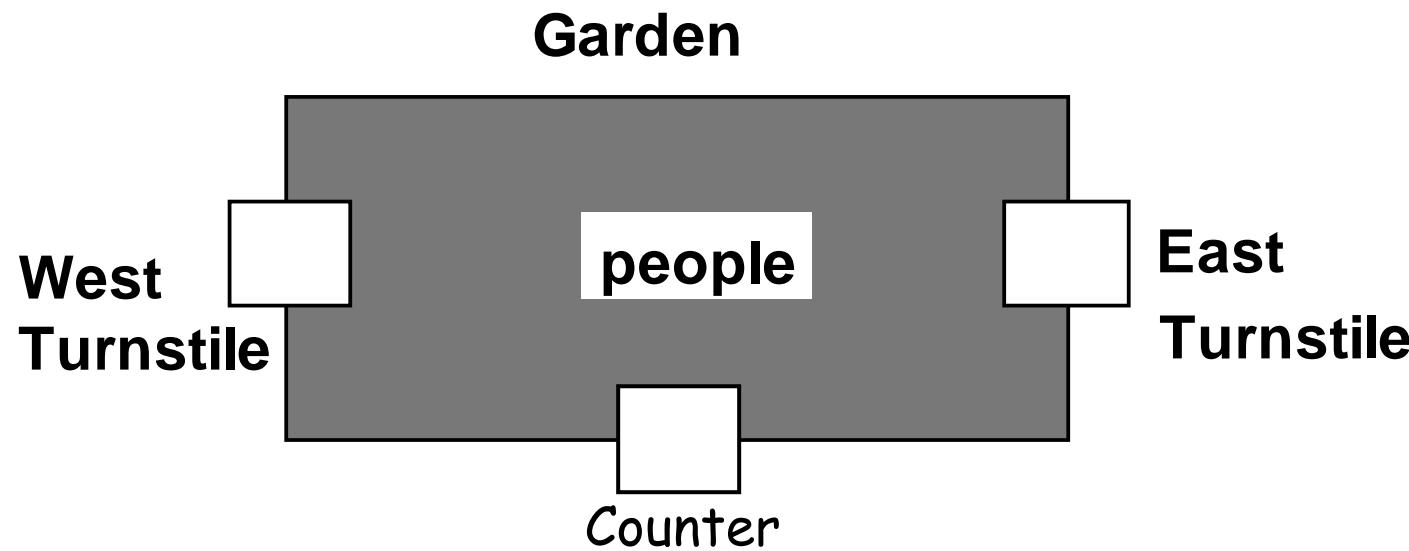
People enter an ornamental garden through either of two turnstiles. Management wishes to know how many are in the garden at any time. (Nobody can exit).



Exercise: variant with Entrance/Exit instead of West/East...

## 4.1 Ornamental Garden Problem (cont'd)

---



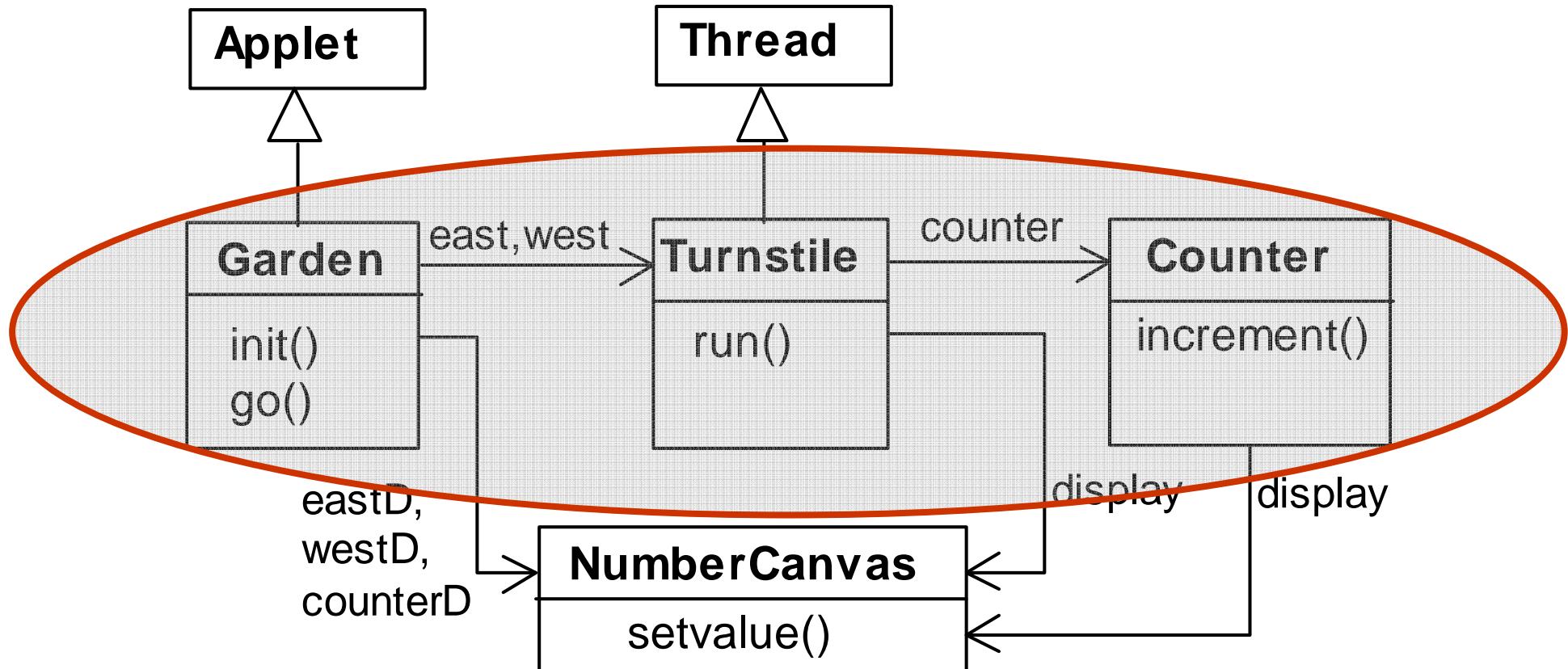
Java implementation:

The concurrent program consists of:

- two concurrent threads (west & east); and
- a shared counter object

# Class Diagram

---



# Ornamental Garden Program

---

The `go()` method of the `Garden` applet...

```
class Garden extends Applet {  
    NumberCanvas counterD, westD, eastD;  
    ...  
    private void go() {  
        counter = new Counter(counterD);  
        west = new Turnstile(westD,counter);  
        east = new Turnstile(eastD,counter);  
        west.start();  
        east.start();  
    }  
}
```

...creates the shared `Counter` object & the `Turnstile` threads.

# The Turnstile Class

---

```
class Turnstile extends Thread {  
    NumberCanvas display;  
    Counter counter;  
  
    public void run() {  
        try {  
            display.setvalue(0);  
            for (int i=1; i<=Garden.MAX; i++) {  
                Thread.sleep(1000);  
                display.setvalue(i);  
                counter.increment();  
            }  
        } catch (InterruptedException _) {}  
    }  
}
```

The Turnstile thread simulates periodic arrival of visitors by invoking the counter object's **increment()** method every second

## The *Shared* Counter Class

---

The `increment()` method of the `Counter` class increments its internal value and updates the display.

```
class Counter {  
    int value;  
    NumberCanvas display;  
  
    void increment() {  
        value = value + 1;  
        display.setvalue(value);  
    }  
}
```

## Counter class – Well, Actually...

```
class Counter {  
    int value=0;  
    NumberCanvas display;  
  
    Counter(NumberCanvas n) {  
        display=n;  
        display.setvalue(value);  
    }  
  
    void increment() {  
        int temp = value;      //read value  
        Simulate.HWinterrupt();  
        value=temp+1;          //write value  
        display.setvalue(value);  
    }  
}
```

Hardware interrupts can occur at **arbitrary** times.

The **counter** simulates a hardware interrupt during an **increment()**, between reading and writing to the shared counter **value**.

Interrupt randomly calls **Thread.yield()** to force a thread switch.

## Running the Applet

---



After the East and West turnstile threads each have incremented the counter 20 times, the garden people counter is not the sum of the counts displayed.

*Why?*

## The *Shared* Counter Class (cont'd)

```
class Counter {  
    int value;  
    NumberCanvas display;  
  
    void increment() {  
        value = value + 1;  
        display.setvalue(value);  
    }  
}
```

Thread switch!

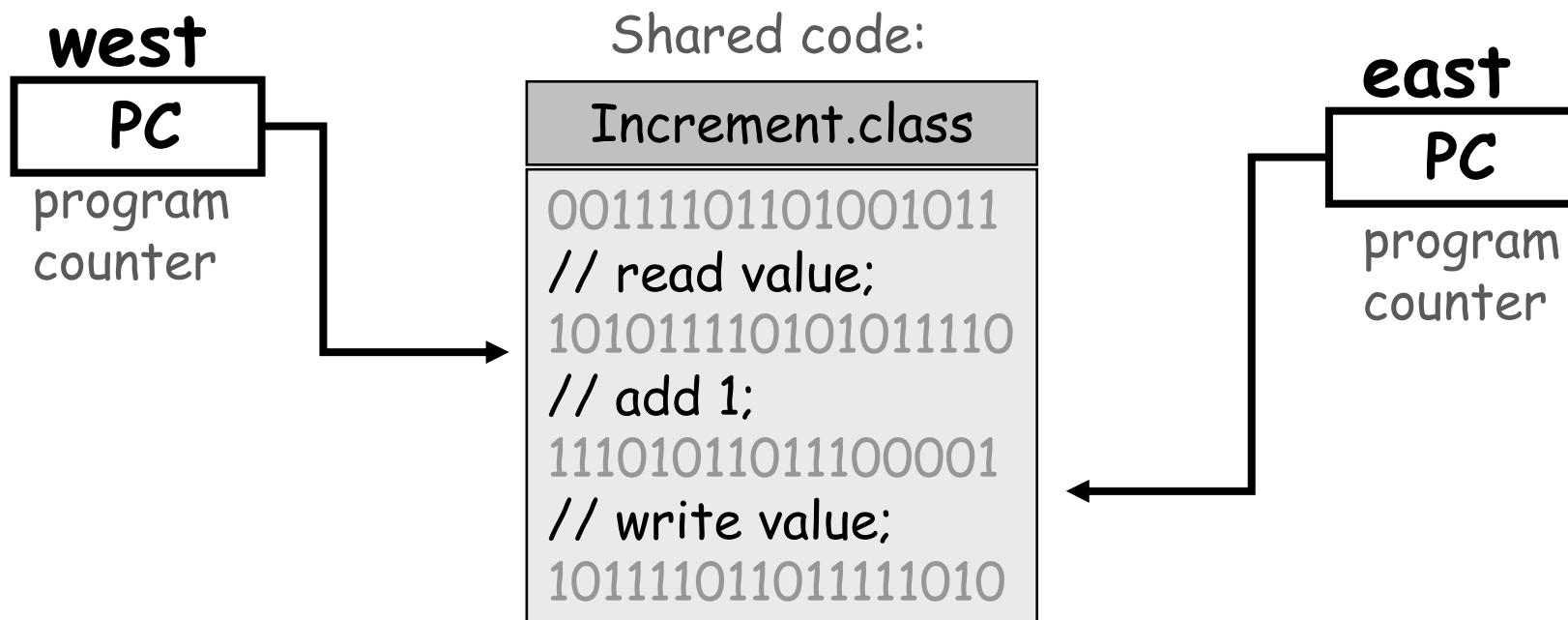
```
value = value + 1;      // 1) read value  
value = value + 1;      // 2) add one  
value = value + 1;      // 3) write result
```

Recall: *thread switching* (or hardware interrupts) can occur at **any** time

# Concurrent Method Activation

Java method activation is not atomic!

Thus, threads `east` and `west` may be executing the code for the increment method at the same time.



# Counter Class: How to Exhibit this Behaviour?

---

```
class Counter {  
    void increment() {  
  
        value = value + 1;  
  
        display.setvalue(value);  
    }  
}
```

# Counter Class: How to Exhibit this Behaviour?

```
class Counter {  
    void increment() {  
        int temp = value; // read  
        Simulate.HWinterrupt();  
        value = temp + 1; // write  
        display.setvalue(value);  
    }  
}
```

The counter simulates a *hardware interrupt* during an `increment()`, between reading and writing to the shared counter `value`.

```
class Simulate { // randomly force thread switch!  
    public static void HWinterrupt() {  
        if (random()<0.5) Thread.yield();  
    }  
}
```

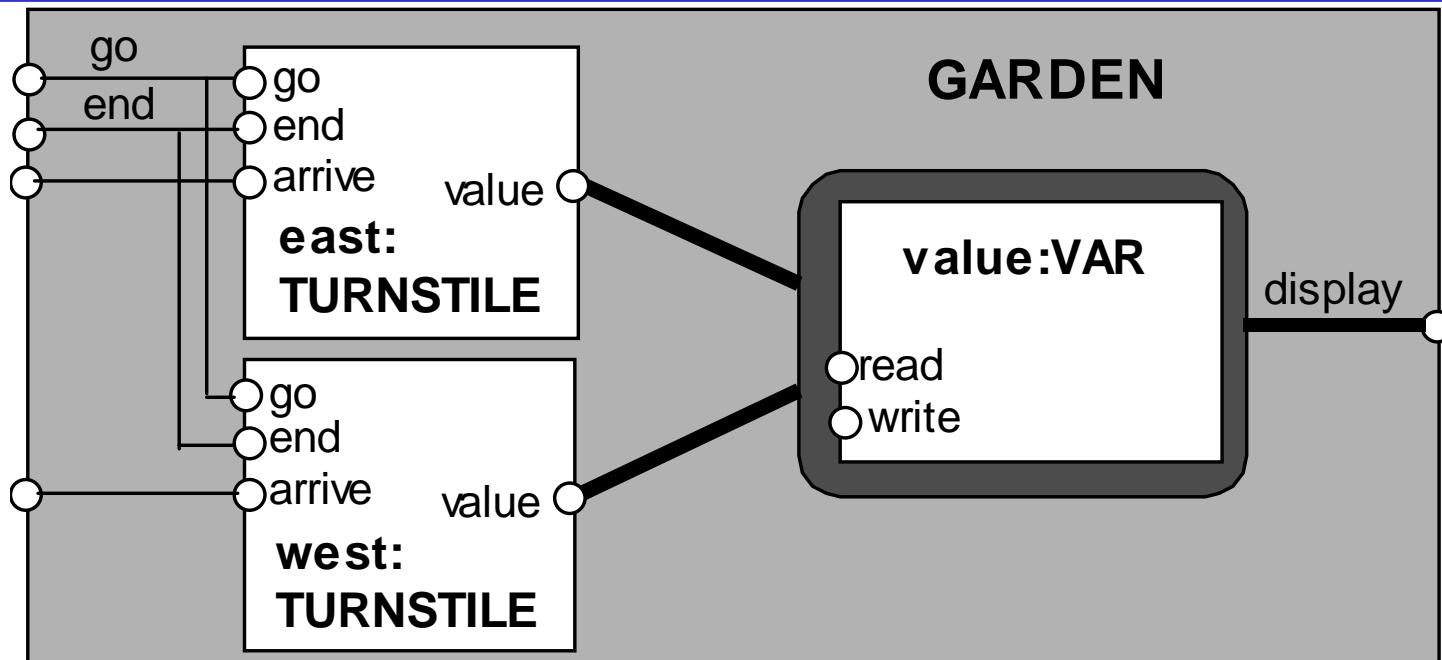
## Running the Applet

---



The erroneous behaviour occurs all the time!

# Ornamental Garden Model (Structure Diagram)



**VAR:**

models read and write access to the shared counter **value**.

**TURNSTILE:**

Increment is modelled inside **TURNSTILE** since Java method activation is not atomic (*i.e.*, thread objects **east** and **west** may interleave their **read** and **write** actions).

# Ornamental Garden Model (FSP)

```
const N = 4
range T = 0..N
set VarAlpha = { value.{read[T],write[T]} }

VAR      = VAR[0],
VAR[u:T] = (read[u]    ->VAR[u]
              | write[v:T]->VAR[v]).

TURNSTILE = (go      -> RUN),
RUN        = (arrive-> INCREMENT
              | end    -> TURNSTILE),
INCREMENT = (value.read[x:T]
              -> value.write[x+1]->RUN
              )+VarAlpha.

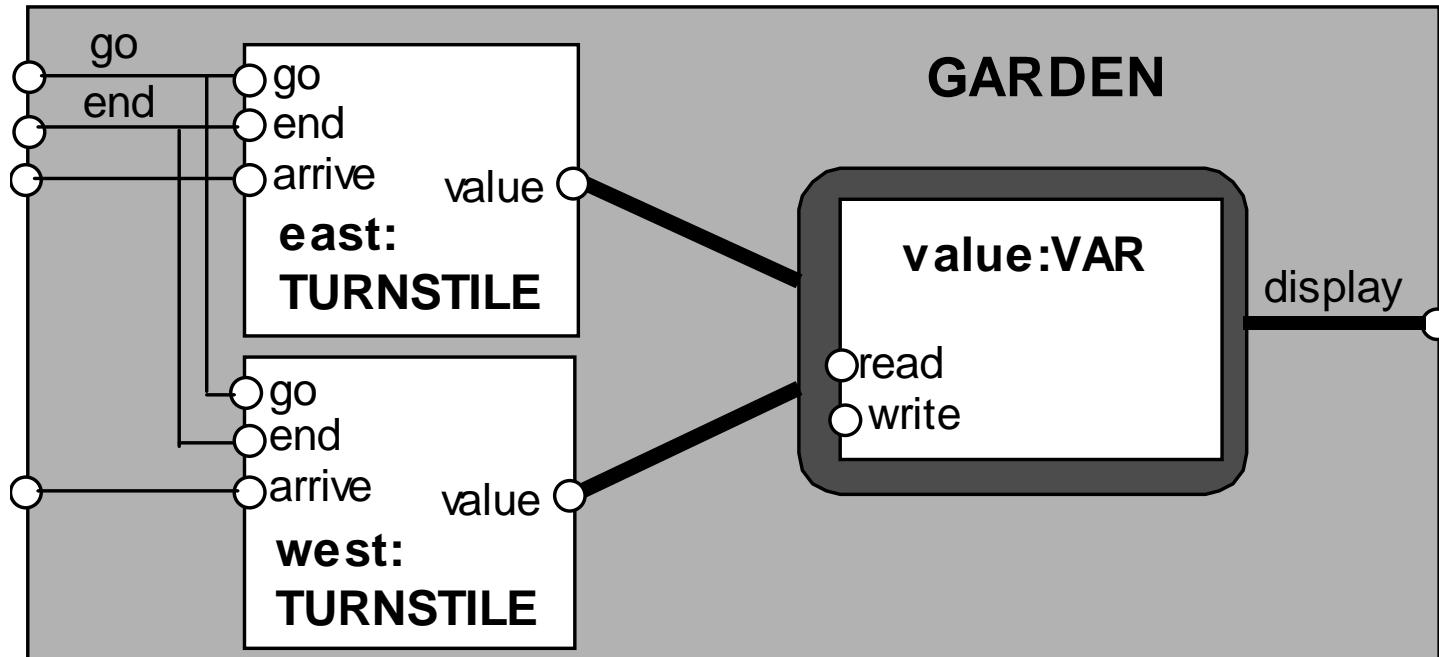
|| GARDEN = (east:TURNSTILE || west:TURNSTILE
              || { east,west,display} ::value:VAR)
              /{ go /{ east,west} .go,
                 end/{ east,west} .end} .
```

The alphabet of process **VAR** is declared explicitly as a **set** constant, **VarAlpha**.

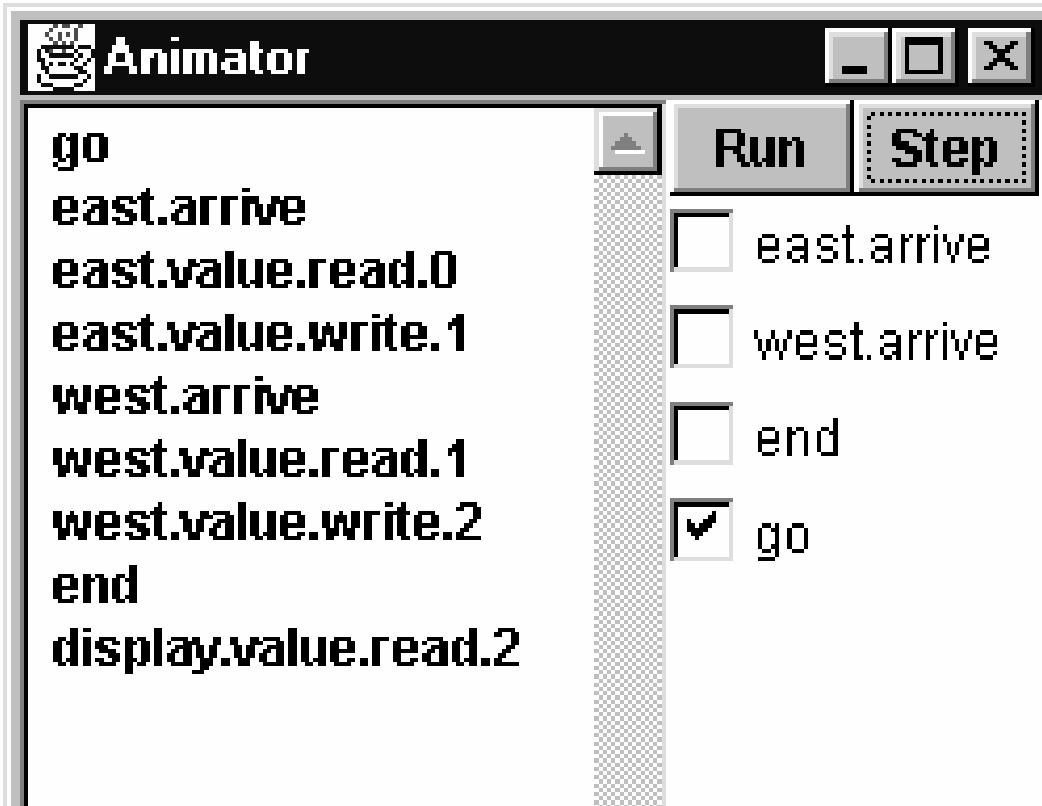
The alphabet of **TURNSTILE** is extended with **VarAlpha** to ensure no unintended free actions in **VAR** ie. all actions in **VAR** must be controlled by a **TURNSTILE**.

# Ornamental Garden Model (Structure Diagram)

```
||GARDEN = (east:TURNSTILE || west:TURNSTILE  
           || {east,west,display}::value:VAR)  
/{ go / {east,west}.go , end / {east,west}.end }.
```



## Checking for Errors - Animation



Scenario checking  
- use animation to produce a trace.

*Is the model correct?*

"Never send a human to do a machine's job"

- Agent Smith (1999)

## Checking for Errors - Compose with Error Detector

Exhaustive checking - compose the model with a TEST process which sums the arrivals and checks against the display value:

```
TEST      = TEST[0],  
TEST[v:T] =  
  (when (v<N){east.arrive,west.arrive}->TEST[v+1]  
   | end->CHECK[v]  
   ),  
CHECK[v:T] =  
  (display.value.read[u:T] ->  
   (when (u==v) right -> TEST[v]  
    | when (u!=v) wrong -> ERROR  
    )  
  )+{display.VarAlpha}.
```

Like STOP, ERROR is a predefined FSP local process (state), numbered -1 in the equivalent LTS.

## Checking for Errors - Exhaustive Analysis

---

```
|| TESTGARDEN = ( GARDEN || TEST ).
```

Use *LTSA* to perform an exhaustive search for **ERROR**:

Trace to property violation in TEST:

```
go
east.arrive
east.value.read.0
west.arrive
west.value.read.0
east.value.write.1
west.value.write.1
end
display.value.read.1
```

wrong

*LTSA* produces  
the shortest  
path to reach  
the **ERROR** state.

# Interference and Mutual Exclusion

---

Destructive update, caused by the arbitrary interleaving of read and write actions, is termed *interference*.

Interference bugs are **extremely difficult** to locate.

The general solution is:

- Give methods *mutually exclusive access* to shared objects.

Mutual exclusion can be modelled as atomic actions.

## 4.2 Mutual Exclusion in Java

---

Concurrent activations of a method in Java can be made *mutually exclusive* by prefixing the method with the keyword **synchronized**.

We correct the Counter class by deriving a class from it and making its increment method synchronized:

```
class SynchronizedCounter extends Counter {  
    SynchronizedCounter(NumberCanvas n) {  
        super(n);  
    }  
    synchronized void increment() {  
        super.increment();  
    }  
}
```

## The Garden Class (revisited)

---

If the **fixit** checkbox is ticked, the **go()** method creates a **SynchronizedCounter**:

```
class Garden extends Applet {  
    private void go() {  
        if (!fixit.getState())  
            counter = new Counter(counterD);  
        else  
            counter = new SynchCounter(counterD);  
        west = new Turnstile(westD,counter);  
        east = new Turnstile(eastD,counter);  
        west.start();  
        east.start();  
    }  
}
```

## Mutual Exclusion - The Ornamental Garden

---



Java associates a *lock* with every object.

The Java compiler inserts code to:

- acquire the lock before executing a synchronized method
- release the lock before the method returns.

Concurrent threads are blocked until the lock is released.

## Java synchronized Statement

---

Access to an object may also be made mutually exclusive by using the **synchronized** statement:

```
synchronized (object) { statements }
```

A less elegant way to correct the example would be to modify the **Turnstile.run()** method:

```
synchronized(counter) {counter.increment();}
```

*Why is this “less elegant”?*

To ensure mutually exclusive access to an object,  
**all object methods** should be synchronized.

# Java synchronized Statement

Synchronized methods:

```
synchronized void increment() {  
    super.increment();  
}
```

Variant - the synchronized *statement*: object reference

```
void increment() {  
    synchronized(semaphore_object) {  
        value = value + 1;  
    }  
    display.setvalue(value);  
}
```

Use synch methods whenever possible.

## 4.3 Modeling Mutual Exclusion

---

Define a mutual exclusion LOCK process:

```
LOCK = (acq -> rel -> LOCK).
```

...and compose it with the shared VAR in the Garden:

```
|| LOCKVAR = (LOCK || VAR).
```

Update the alphabet set:

```
set varAlpha = {value.{read[T],write[T], acq, rel}}.
```

Modify TURNSTILE to *acquire* and *release* the lock:

```
TURNSTILE = (go -> RUN),
RUN        = (arrive -> INCREMENT | end -> TURNSTILE),
INCREMENT = (value.acq
              -> value.read[x:T]
              -> value.write[x+1]
              -> value.rel->RUN )+VarAlpha.
```

# Revised Ornamental Garden Model - Checking for Errors

---

A sample trace:

```
go
east.arrive
east.value.acq
east.value.read.0
east.value.write.1
east.value.rel
west.arrive
west.value.acq
west.value.read.1
west.value.write.2
west.value.rel
end
display.value.read.2
right
```

Use LTSA to perform  
an exhaustive check:  
*"is TEST satisfied?"*

*Yes! No error found!*

# COUNTER: Abstraction Using Action Hiding

```
const N = 4
range T = 0..N

VAR = VAR[0],
VAR[u:T] = ( read[u]->VAR[u]
              | write[v:T]->VAR[v]).

LOCK = (acquire->release->LOCK).

INCREMENT = (acquire->read[x:T]
              -> (when (x<N) write[x+1]
                  ->release->increment->INCREMENT
                  )
              ) + {read[T],write[T]}.

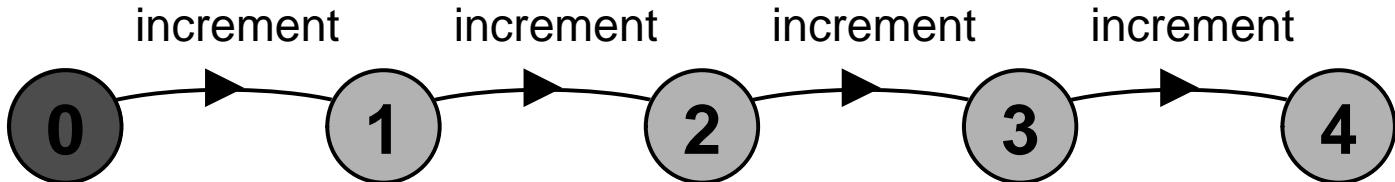
|| COUNTER = (INCREMENT || LOCK || VAR)@{increment}.
```

To model shared objects directly in terms of their synchronized methods, we can abstract the details by hiding.

For `SynchronizedCounter` we hide `read`, `write`, `acquire`, `release` actions.

## COUNTER: Abstraction Using Action Hiding

Minimized  
LTS:



We can give a more abstract, simpler description of a COUNTER which generates the same LTS:

```
COUNTER = COUNTER[ 0 ]
COUNTER[v:T] = (when (v < N) increment -> COUNTER[v+1]).
```

This therefore exhibits "equivalent" behavior i.e. has the same observable behavior.

# Summary

---

## ◆ Concepts

- process interference
- mutual exclusion

## ◆ Models

- model checking for interference
- modeling mutual exclusion

## ◆ Practice

- thread interference in shared Java objects
- mutual exclusion in Java (synchronized objects/methods).