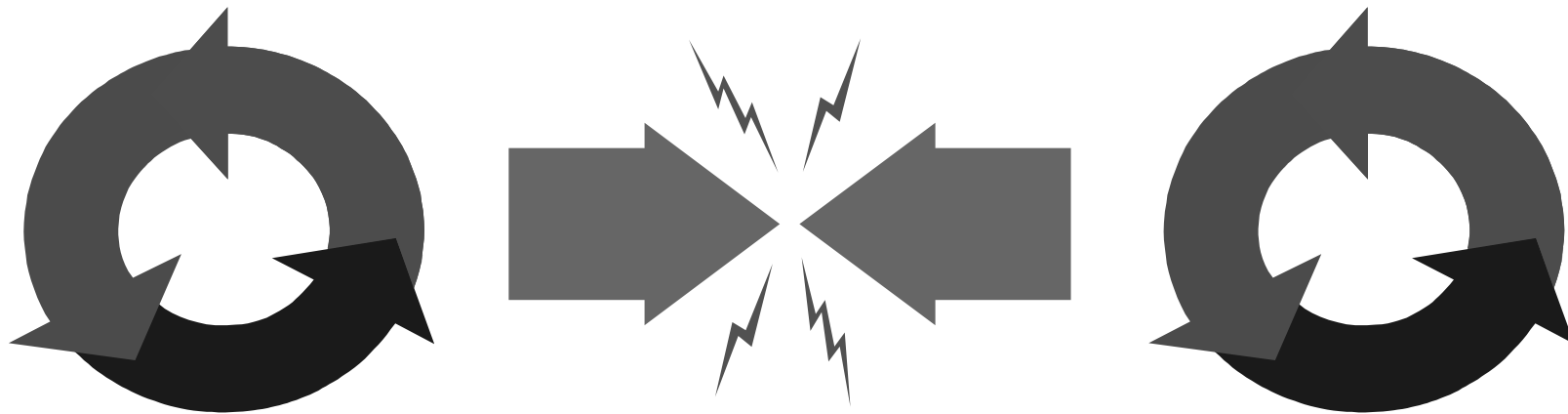


## Concurrency

---

# 4 - Shared Objects & Mutual Exclusion



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## Repetition – “Concurrent Execution”

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Concepts: pseudo- vs. real concurrent execution  
concurrent execution and **interleaving**  
process interaction

Models: **parallel composition** of asynchronous processes  
- interleaving  
**interaction** - *shared actions*  
process labeling, action relabeling, and hiding  
**structure diagrams**

Practice: Multithreaded Java programs

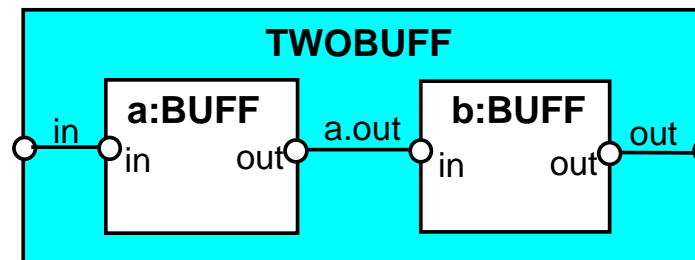
## Repetition (week 06) - Specifically

---

### ◆ FSP:

- $P \parallel Q$  // parallel composition
- $a:P$  // action prefixing
- $\{...\}::P$  // set prefixing
- $P / \{x/y\}$  // action relabelling
- $P \setminus \{...\}$  // hiding
- $P @ \{...\}$  // keeping (hide complement)

### ◆ Structure Diagrams:



# Shared Objects & Mutual Exclusion

---

## ◆ Concepts:

- **Process interference**
- **Mutual exclusion**

## ◆ Models:

- **Model-checking for interference**
- **Modelling mutual exclusion**

## ◆ Practice:

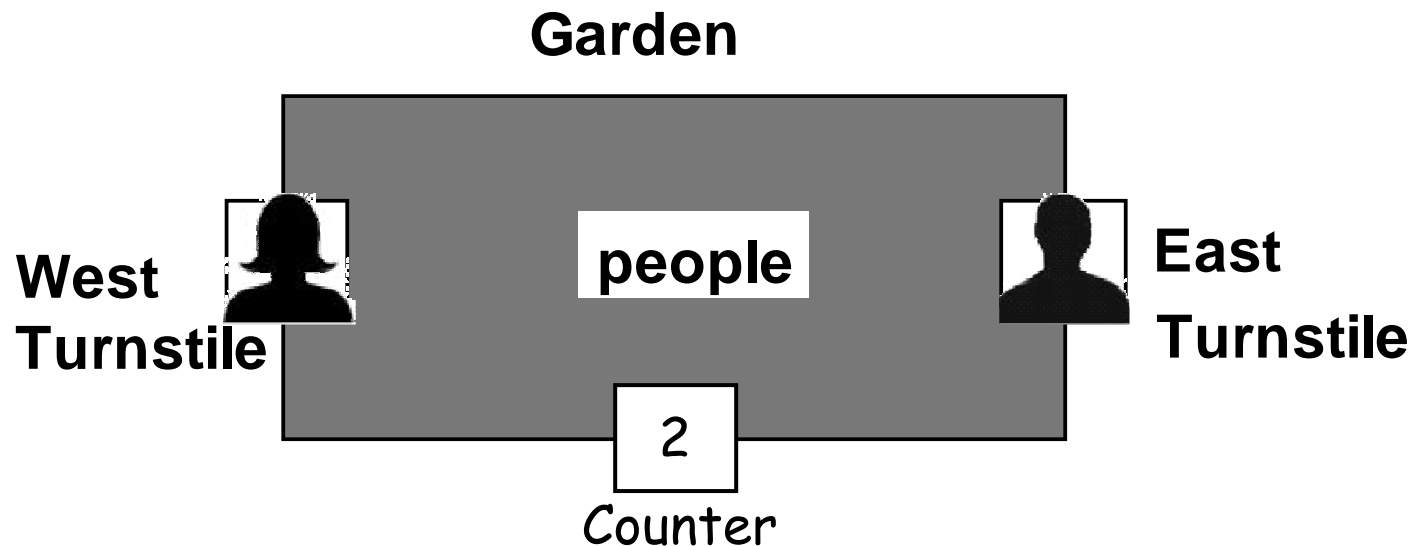
- **Thread interference in shared objects in Java**
- **Mutual exclusion in Java**
- **synchronized objects, methods, and statements**

## 4.1 Interference

---

### The "*Ornamental Garden Problem*":

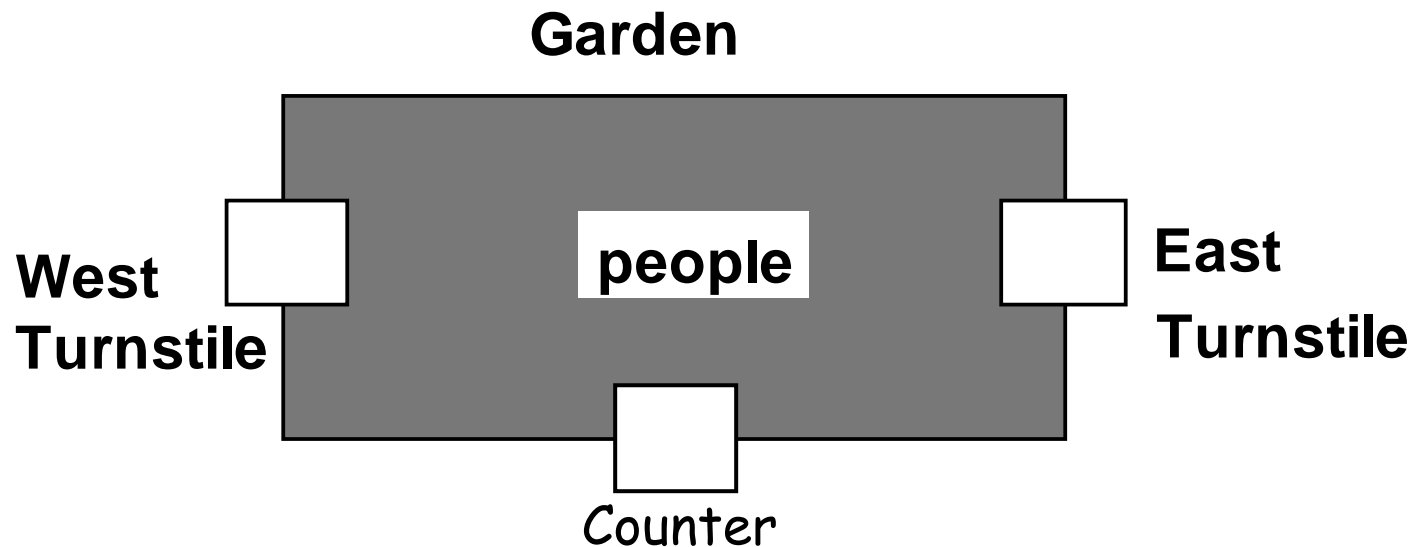
People enter an ornamental garden through either of two turnstiles. Management wishes to know how many are in the garden at any time. (Nobody can exit).



Exercise: variant with Entrance/Exit instead of West/East...

## 4.1 Ornamental Garden Problem (cont'd)

---

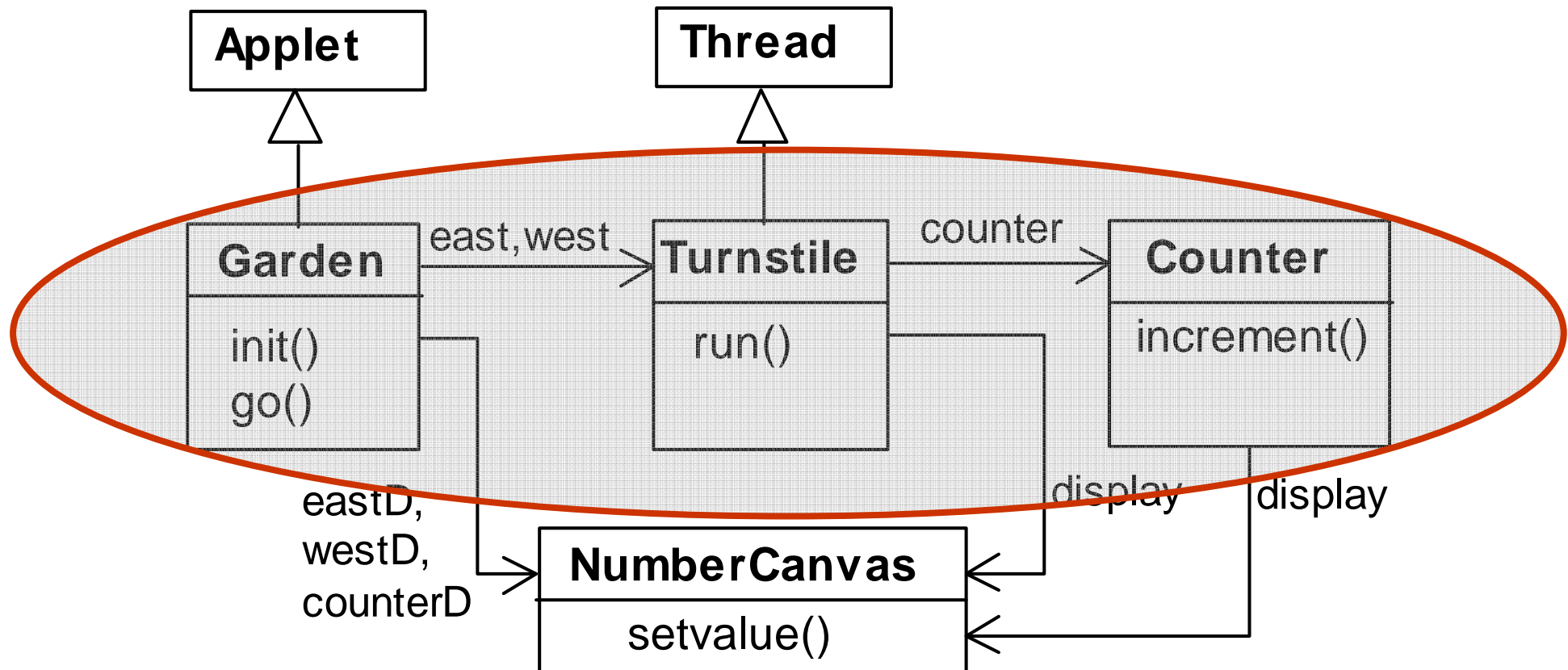


**Java** implementation:

The concurrent program consists of:

- two concurrent threads (west & east); and
- a shared counter object

# Class Diagram



# Ornamental Garden Program

---

The *go()* method of the Garden applet...

```
class Garden extends Applet {  
    NumberCanvas counterD, westD, eastD;  
    ...  
    private void go() {  
        counter = new Counter(counterD);  
        west = new Turnstile(westD, counter);  
        east = new Turnstile(eastD, counter);  
        west.start();  
        east.start();  
    }  
}
```

...creates the shared **Counter** object & the **Turnstile** threads.



# The Turnstile Class

---

```
class Turnstile extends Thread {
    NumberCanvas display;
    Counter counter;

    public void run() {
        try {
            display.setvalue(0);
            for (int i=1; i<=Garden.MAX; i++) {
                Thread.sleep(1000);
                display.setvalue(i);
                counter.increment();
            }
        } catch (InterruptedException _) {}
    }
}
```

The **Turnstile** thread simulates periodic arrival of visitors by invoking the counter object's **increment()** method every second

## The *Shared* Counter Class

---

The **increment()** method of the Counter class increments its internal value and updates the display.

```
class Counter {  
    int value;  
    NumberCanvas display;  
  
    void increment() {  
        value = value + 1;  
        display.setvalue(value);  
    }  
}
```

## Counter class – Well, Actually...

```
class Counter {
    int value=0;
    NumberCanvas display;

    Counter(NumberCanvas n) {
        display=n;
        display.setvalue(value);
    }

    void increment() {
        int temp = value;    //read value
        Simulate.HWinterrupt();
        value=temp+1;        //write value
        display.setvalue(value);
    }
}
```

Hardware interrupts can occur at **arbitrary** times.

The **counter** simulates a hardware interrupt during an **increment()**, between reading and writing to the shared counter **value**.

Interrupt randomly calls **Thread.yield()** to force a thread switch.

## Running the Applet

---



After the East and West turnstile threads each have incremented the counter 20 times, the garden people counter is **not the sum of the counts displayed**.

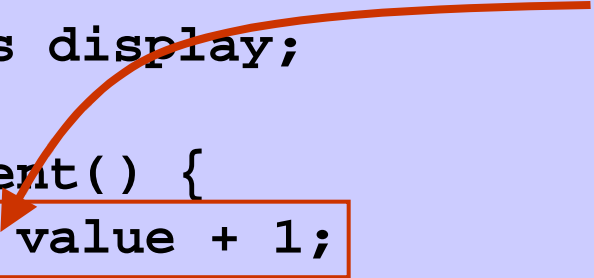
*Why?*

## The *Shared* Counter Class (cont'd)

---

```
class Counter {  
    int value;  
    NumberCanvas display;  
  
    void increment() {  
        value = value + 1;  
        display.setvalue(value);  
    }  
}
```

Thread switch!



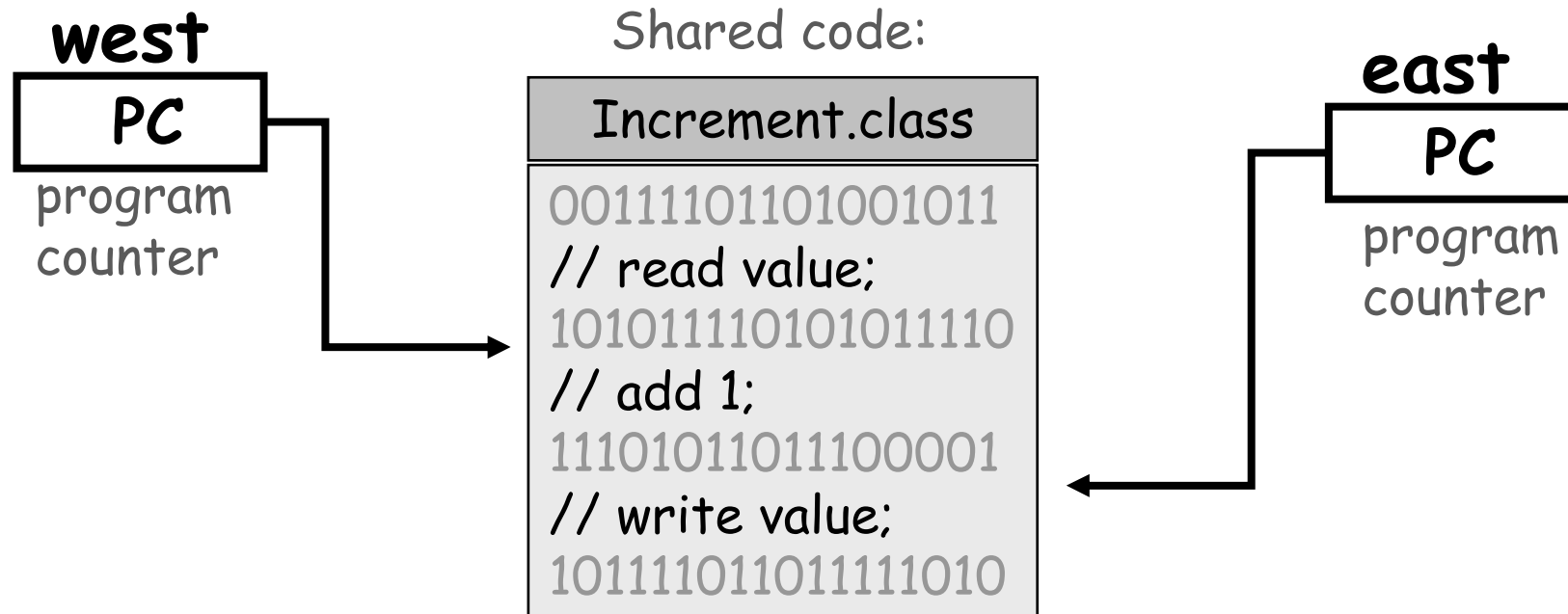
```
value = value + 1;    // 1) read value  
value = value + 1;    // 2) add one  
value = value + 1;    // 3) write result
```

Recall: *thread switching* (or hardware interrupts) can occur at **any** time

# Concurrent Method Activation

Java method activation is **not atomic!**

Thus, threads **east** and **west** may be executing the code for the increment method at the same time.



## Counter Class: How to Exhibit this Behaviour?

---

```
class Counter {  
    void increment() {  
  
        value = value + 1;  
  
        display.setvalue(value);  
    }  
}
```

## Counter Class: How to Exhibit this Behaviour?

---

```
class Counter {  
    void increment() {  
        int temp = value; // read  
        Simulate.HWinterrupt();  
        value = temp + 1; // write  
        display.setvalue(value);  
    }  
}
```

The **counter** simulates a *hardware interrupt* during an **increment()**, between reading and writing to the shared counter **value**.

```
class Simulate { // randomly force thread switch!  
    public static void HWinterrupt() {  
        if (random() < 0.5) Thread.yield();  
    }  
}
```



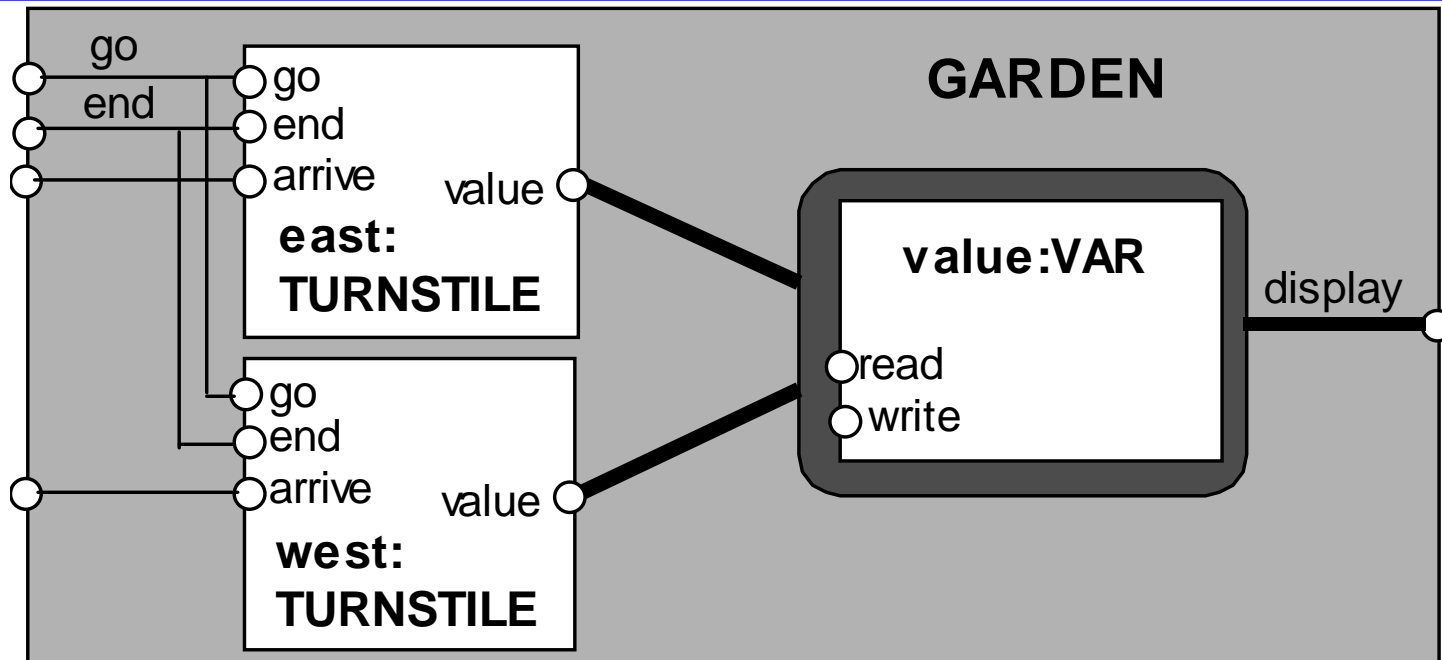
## Running the Applet

---



The erroneous behaviour occurs all the time!

## Ornamental Garden Model (Structure Diagram)



### **VAR:**

models read and write access to the shared counter value.

### **TURNSTILE:**

Increment is modelled inside TURNSTILE since Java method activation is not atomic (*i.e.*, thread objects east and west may interleave their read and write actions).

# Ornamental Garden Model (FSP)

```
const N = 4
range T = 0..N
set VarAlpha = { value.{read[T],write[T]} }

VAR      = VAR[0],
VAR[u:T] = (read[u]    ->VAR[u]
            |write[v:T]->VAR[v]).

TURNSTILE = (go      -> RUN),
RUN        = (arrive-> INCREMENT
            |end     -> TURNSTILE),
INCREMENT  = (value.read[x:T]
            -> value.write[x+1]->RUN
            )+VarAlpha.

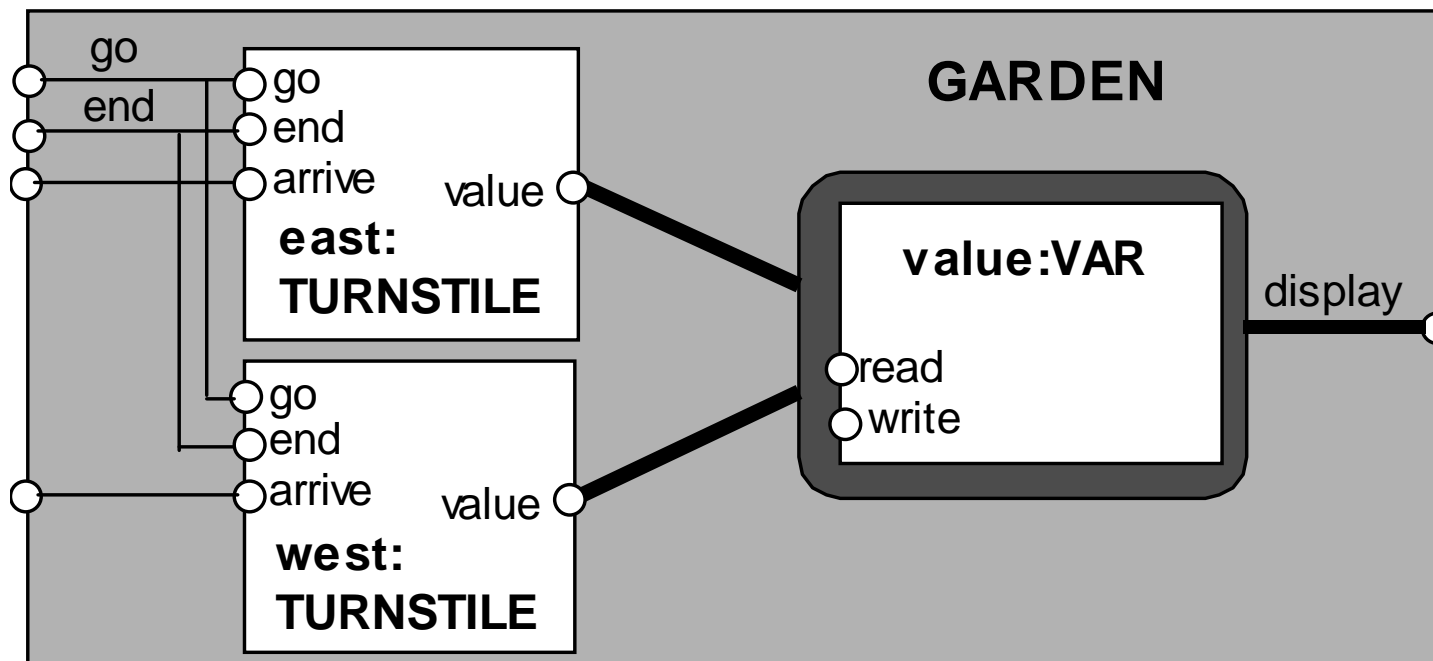
||GARDEN = (east:TURNSTILE || west:TURNSTILE
|| { east,west,display} ::value:VAR)
/{ go /{ east,west} .go,
  end/{ east,west} .end} .
```

The alphabet of process **VAR** is declared explicitly as a **set** constant, **VarAlpha**.

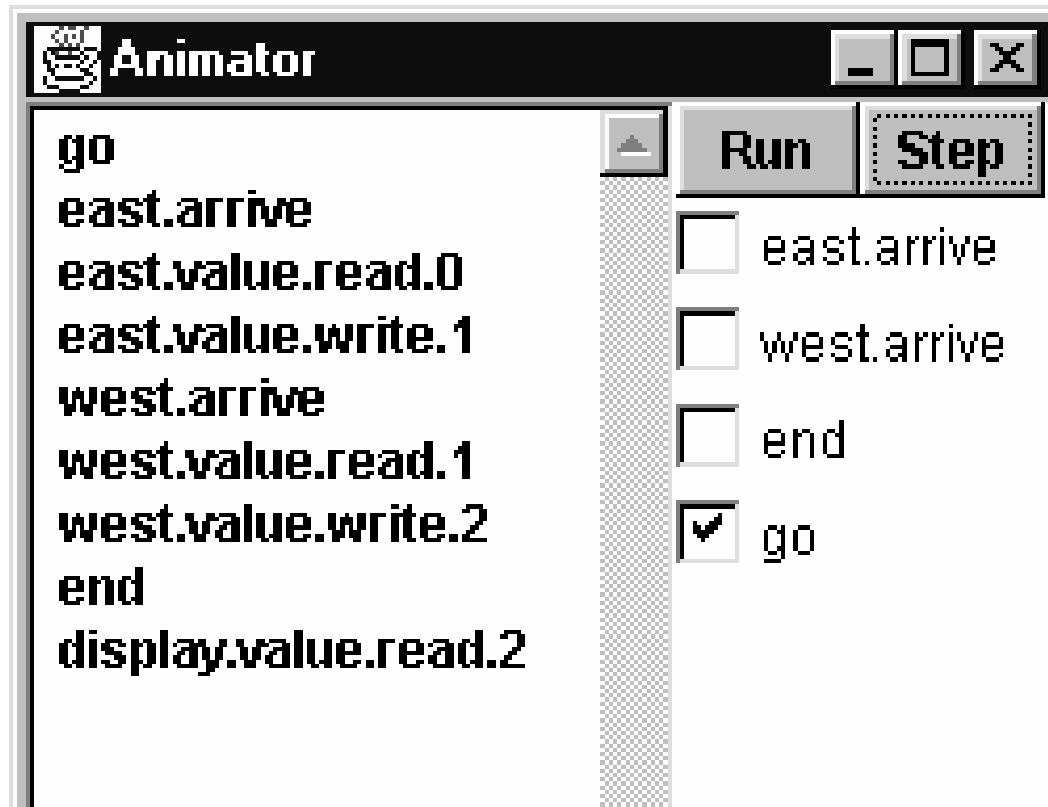
The alphabet of **TURNSTILE** is extended with **VarAlpha** to ensure no unintended free actions in **VAR** ie. all actions in **VAR** must be controlled by a **TURNSTILE**.

# Ornamental Garden Model (Structure Diagram)

```
|| GARDEN = (east:TURNSTILE || west:TURNSTILE
              || {east,west,display}::value:VAR)
            /{ go / {east,west}.go , end / {east,west}.end}.
```



## Checking for Errors - Animation



Scenario checking  
- use animation to  
produce a trace.

*Is the model  
correct?*

"Never send a human to do a machine's job"

- Agent Smith (1999)

## Checking for Errors - Compose with Error Detector

Exhaustive checking - compose the model with a TEST process which sums the arrivals and checks against the display value:

```
TEST          = TEST[0],
TEST[v:T]    =
    (when (v<N){east.arrive,west.arrive}->TEST[v+1]
    |end->CHECK[v]
    ),
CHECK[v:T]   =
    (display.value.read[u:T] ->
    (when (u==v) right -> TEST[v]
    |when (u!=v) wrong -> ERROR
    )
    )+{display.VarAlpha}.
```

Like STOP, ERROR is a predefined FSP local process (state), numbered -1 in the equivalent LTS.

## Checking for Errors - Exhaustive Analysis

---

`|| TESTGARDEN = (GARDEN || TEST).`

Use *LTSA* to perform an exhaustive search for **ERROR**:

Trace to property violation in TEST:

```
go
east.arrive
east.value.read.0
west.arrive
west.value.read.0
east.value.write.1
west.value.write.1
end
display.value.read.1
```

wrong

*LTSA* produces  
the shortest  
path to reach  
the **ERROR** state.

# Interference and Mutual Exclusion

---

Destructive update, caused by the arbitrary interleaving of read and write actions, is termed *interference*.

Interference bugs are **extremely** difficult to locate.

The general solution is:

- Give methods *mutually exclusive* access to shared objects.

Mutual exclusion can be modelled as atomic actions.



## 4.2 Mutual Exclusion in Java

---

Concurrent activations of a method in Java can be made *mutually exclusive* by prefixing the method with the keyword `synchronized`.

We correct the `Counter` class by deriving a class from it and making its `increment` method `synchronized`:

```
class SynchronizedCounter extends Counter {  
    SynchronizedCounter(NumberCanvas n) {  
        super(n);  
    }  
    synchronized void increment() {  
        super.increment();  
    }  
}
```

## The Garden Class (revisited)

---

If the `fixit` checkbox is ticked, the `go()` method creates a **SynchronizedCounter**:

```
class Garden extends Applet {  
    private void go() {  
        if (!fixit.getState())  
            counter = new Counter(counterD);  
        else  
            counter = new SynchCounter(counterD);  
        west = new Turnstile(westD, counter);  
        east = new Turnstile(eastD, counter);  
        west.start();  
        east.start();  
    }  
}
```

## Mutual Exclusion - The Ornamental Garden

---



Java associates a *lock* with every object.

The Java compiler inserts code to:

- acquire the lock before executing a synchronized method
- release the lock before the method returns.

Concurrent threads are blocked until the lock is released.

## Java synchronized Statement

---

Access to an object may also be made mutually exclusive by using the **synchronized** statement:

```
synchronized (object) { statements }
```

A less elegant way to correct the example would be to modify the **Turnstile.run()** method:

```
synchronized(counter) { counter.increment(); }
```

*Why is this “less elegant”?*


To ensure mutually exclusive access to an object, **all object methods** should be synchronized.

# Java synchronized Statement

---

Synchronized methods:

```
synchronized void increment() {  
    super.increment();  
}
```

Variant - the synchronized *statement*:  object reference

```
void increment() {  
    synchronized(semaphore_object) {  
        value = value + 1;  
    }  
    display.setvalue(value);  
}
```

Use synch *methods*  
whenever possible.

## 4.3 Modeling Mutual Exclusion

---

Define a mutual exclusion LOCK process:

```
LOCK = (acq -> rel -> LOCK).
```

...and compose it with the shared VAR in the Garden:

```
||LOCKVAR = (LOCK || VAR).
```

Update the alphabet set:

```
set VarAlpha = {value.{read[T],write[T], acq, rel}}.
```

Modify TURNSTILE to *acquire* and *release* the lock:

```
TURNSTILE = (go -> RUN),  
RUN        = (arrive -> INCREMENT | end -> TURNSTILE),  
INCREMENT  = (value.acq  
              -> value.read[x:T]  
              -> value.write[x+1]  
              -> value.rel->RUN )+VarAlpha.
```

## Revised Ornamental Garden Model - Checking for Errors

---

A sample trace:

```
go
east.arrive
east.value.acq
east.value.read.0
east.value.write.1
east.value.rel
west.arrive
west.value.acq
west.value.read.1
west.value.write.2
west.value.rel
end
display.value.read.2
right
```

Use **LTSA** to perform  
an exhaustive check:

*"is TEST satisfied"?*

*Yes! No error found!*

## COUNTER: Abstraction Using Action Hiding

```
const N = 4
range T = 0..N

VAR = VAR[0],
VAR[u:T] = ( read[u]->VAR[u]
             | write[v:T]->VAR[v] ).

LOCK = (acquire->release->LOCK).

INCREMENT = (acquire->read[x:T]
             -> (when (x<N) write[x+1]
                 ->release->increment->INCREMENT
                )
             )+{read[T],write[T]}.

|| COUNTER = (INCREMENT || LOCK || VAR)@{increment}.
```

To model shared objects directly in terms of their synchronized methods, we can abstract the details by hiding.

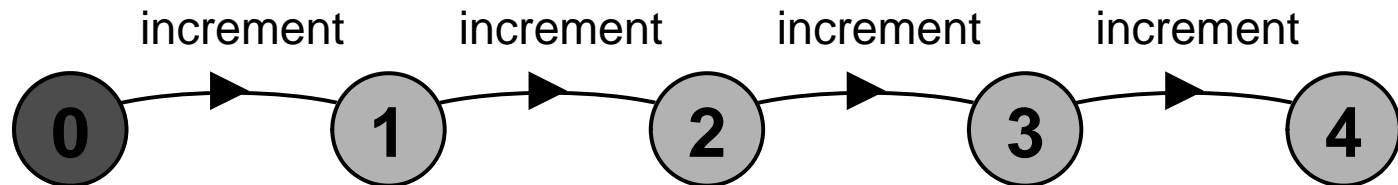
For SynchronizedCounter we hide read, write, acquire, release actions.



## COUNTER: Abstraction Using Action Hiding

---

Minimized  
LTS:



We can give a more abstract, simpler description of a COUNTER which generates the same LTS:

```
COUNTER = COUNTER[0]  
COUNTER[v:T] = (when (v<N) increment -> COUNTER[v+1]).
```

This therefore exhibits “equivalent” behavior i.e. has the same observable behavior.

# Summary

---

## ◆ Concepts

- process interference
- mutual exclusion

## ◆ Models

- model checking for interference
- modeling mutual exclusion

## ◆ Practice

- thread interference in shared Java objects
- mutual exclusion in Java (synchronized objects/methods).