28/02/2024

# GRAPHS CLASS - 6

## 1. Number of Provinces (Leetcode-547)

PROBLEM STATEMENT:

There are **n** cities. Some of them are connected, while some are not. If city **a** is connected directly with city **b**, and city **b** is connected directly with city **c**, then city **a** is connected indirectly with city **c**.

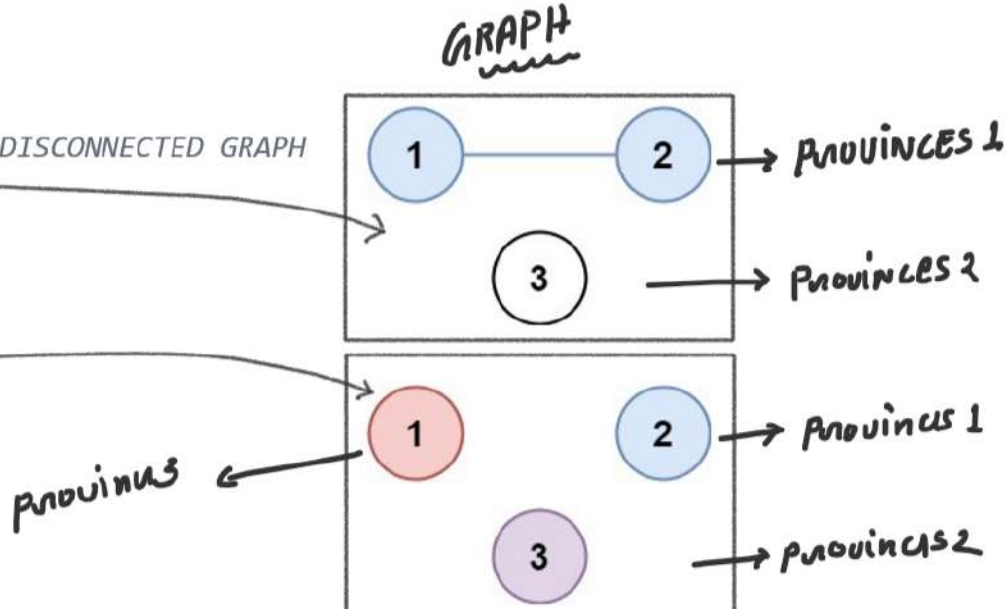
A **province** is a group of directly or indirectly connected **cities** and no other cities outside of the group.
You are given an **n x n** matrix **isConnected** where **isConnected[i][j] = 1** if the **ith** city and the **jth** city are directly connected, and **isConnected[i][j] = 0** otherwise.

**Return the total number of provinces.**

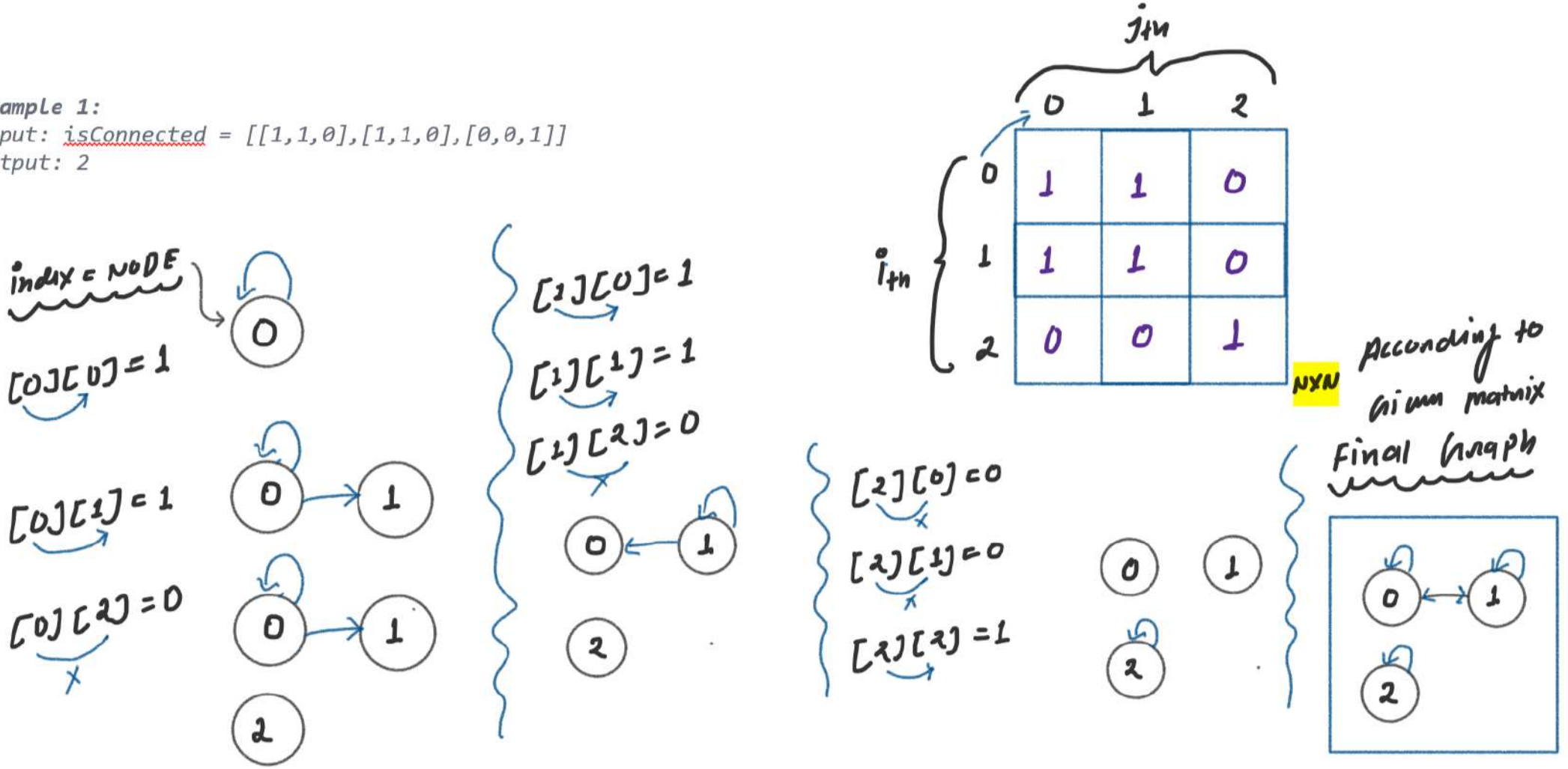

ACTUAL ME **PROVINCES** KA MATLB HAI **COMPONENTS** FIND KARNA FROM DISCONNECTED GRAPH

**Example 1:**
Input: isConnected = [[1,1,0],[1,1,0],[0,0,1]]
Output: 2

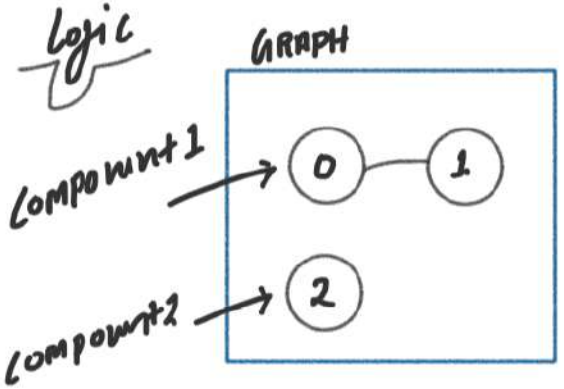
**Example 2:**
Input: isConnected = [[1,0,0],[0,1,0],[0,0,1]]
Output: 3



*Example 1:*
*Input: isConnected = [[1,1,0],[1,1,0],[0,0,1]]*
*Output: 2*

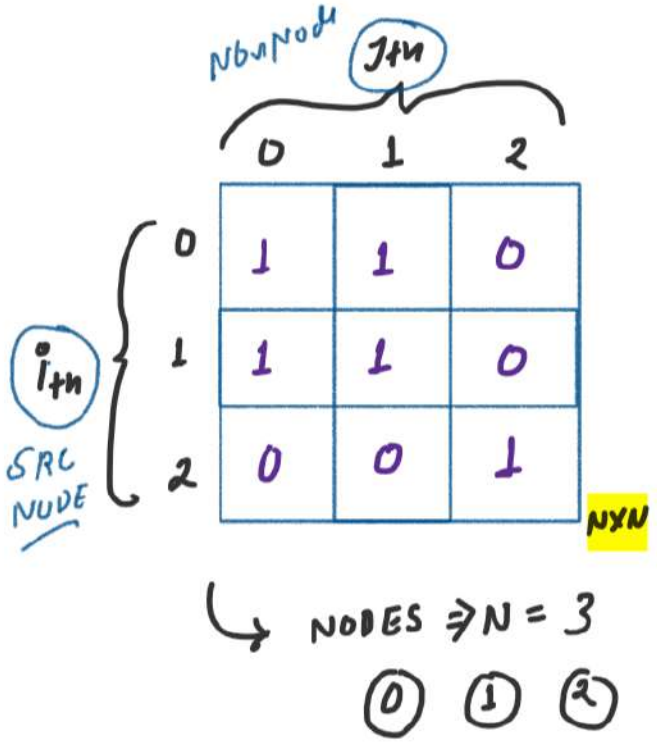


Logic




⇒ FIND NO. of provinces/components using DFS Algorithm

```
Count 0
For( 0 ⟶ N-1 )
{
    if ( ! visited[i] ) {
        ↳ DFS call
        ↳ count ++
    }
}
```



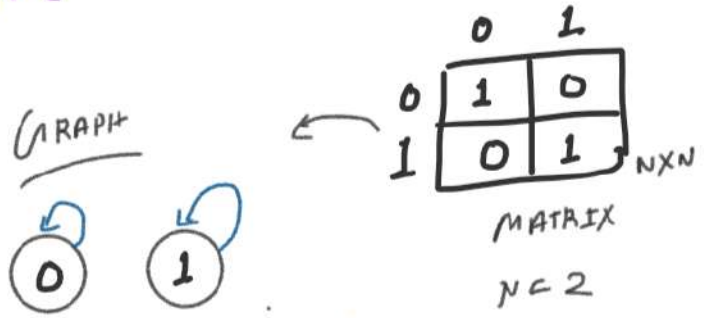

↳ NODES ⇒ N = 3

(0) (1) (2)

```cpp
// 1. Number of Provinces (Leetcode-547)


class Solution {
public:

    void dfs(vector<vector<int>>& isConnected, int &srcNode, unordered_map<int,bool> &visited, int nodes){
        // srcNode ko true visited krdo
        visited[srcNode] = true;

        // ab srcNode ke har ek nbrNode par checkKro ki wo dono ek dusrse se connected hai ya nhi
        for(int nbrNode = 0; nbrNode < nodes; nbrNode++){
            // check both node connected or not
            if(srcNode != nbrNode && isConnected[srcNode][nbrNode] == 1){
                // check krlo nbrNode visited to nhi hai otherwise hum ek inifinite loop me fas jayenge
                if(!visited[nbrNode]){
                    dfs(isConnected, nbrNode, visited, nodes);
                }
            }
        }
    }

    int findCircleNum(vector<vector<int>>& isConnected) {
        // Number of nodes
        int nodes = isConnected.size();
        // Number of provinces
        int count = 0;

        // Traverse from each src node 0, 1, 2, ...
        unordered_map<int,bool> visited;
        for(int srcNode = 0; srcNode < nodes; srcNode++){
            if(!visited[srcNode]){
                dfs(isConnected, srcNode, visited, nodes);
                // province is increasing by 1 when dfs call is completed
                count++;
            }
        }

        return count;
    }
};
```

Why used this condition?

if (srcNode != nbrNode)



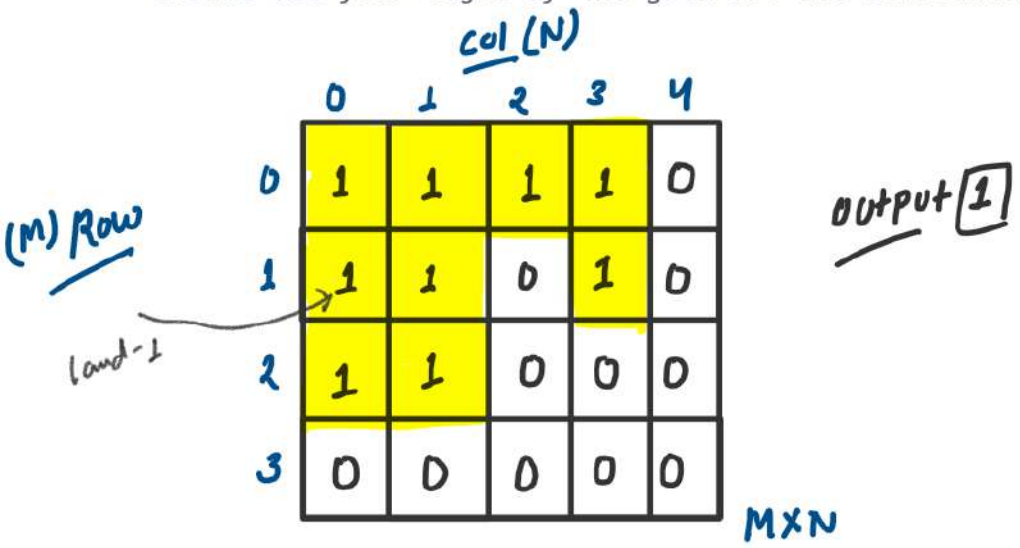

When srcNode == nbrNode
0

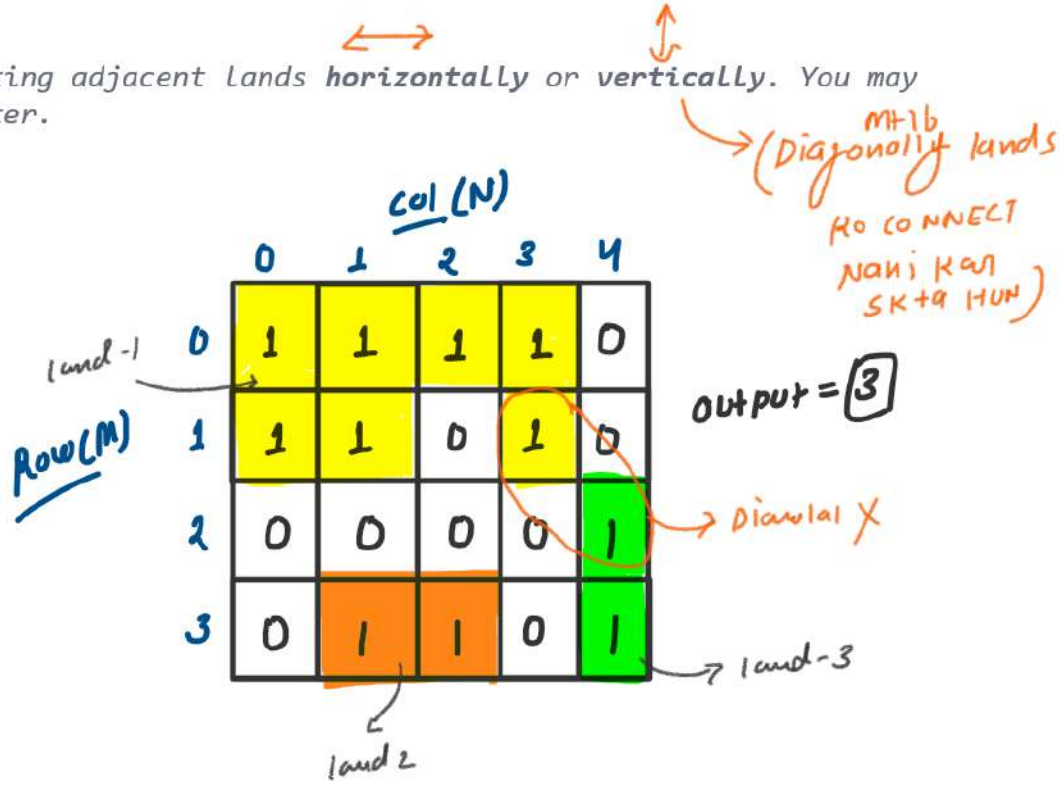
↳ iska matlb hum DFS call one same node par pobara se nahi karna chahte hai. → DFS call only = 2 Hogi in this case

## 2. Number of Islands (Leetcode-200)

**Problem Statement:**
Given an `m x n` 2D binary **grid** which represents a map of **'1's (land)** and **'0's (water)**, return the number of **islands.**

**Important Line:**
An `island` is surrounded by water and is formed by connecting adjacent lands **horizontally** or **vertically.** You may assume all four edges of the grid are all surrounded by water.



**Observation**

0 → water

1 → land

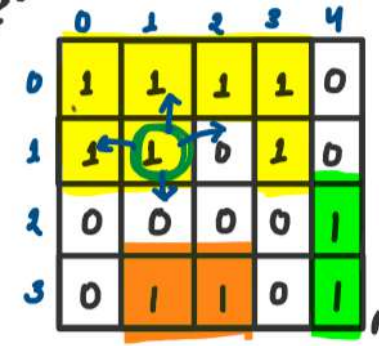
[GRID] ROW x COL

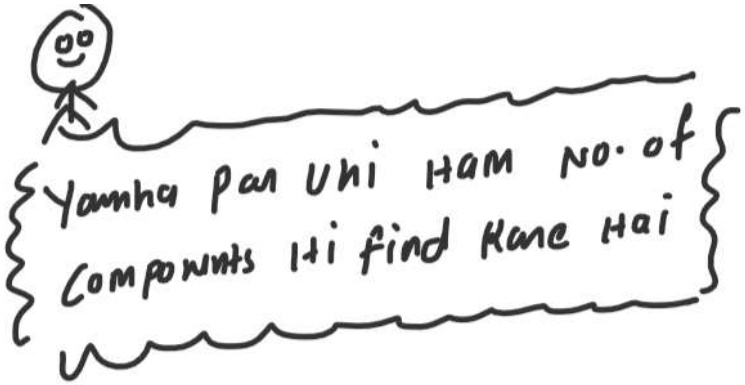
1 ↔ 1 Horizontal

and

1
⇕
1 Vertical

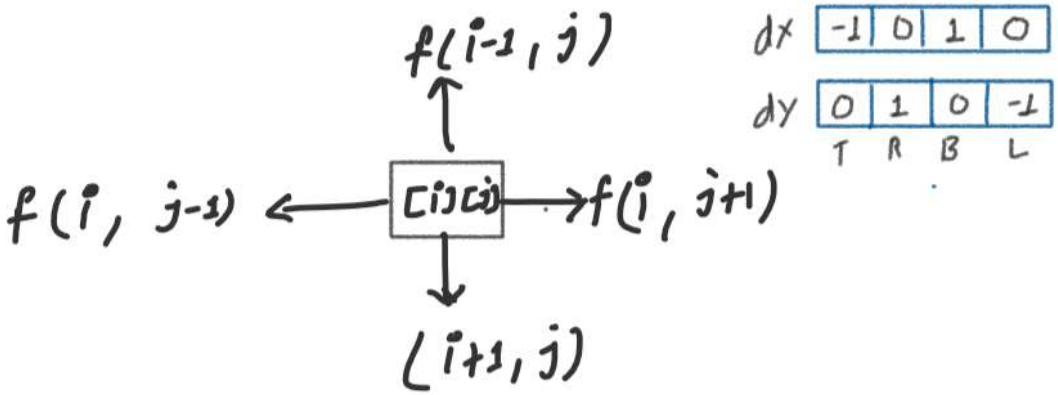
GRID




We have 4 move from each cell of grid jaanha par Hum stand Kar Rhe Hai

1. TopMove
2. BottomMove
3. Right Move
4. Left Move

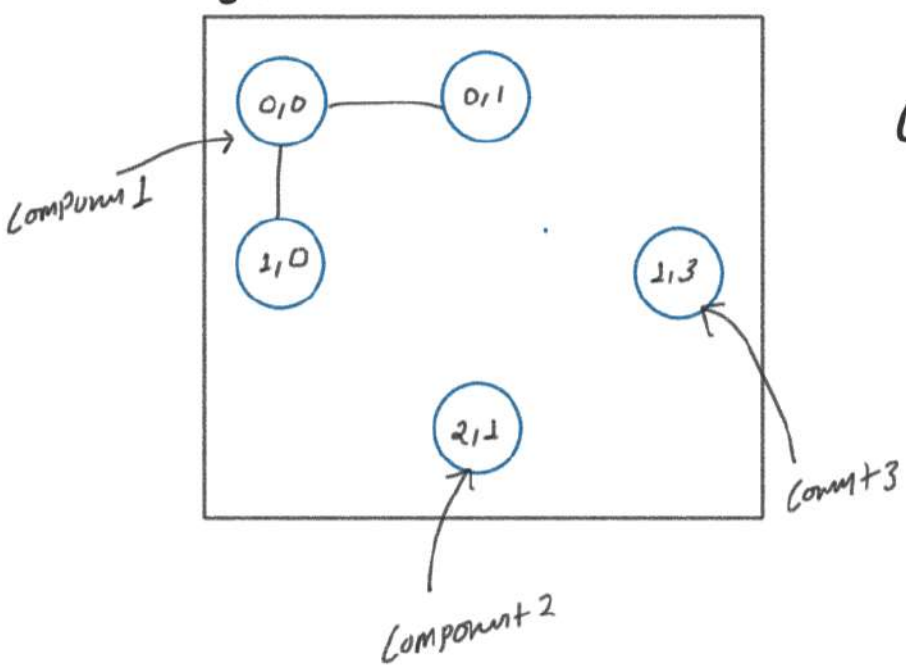


Visit
Graph

**NODE = CELL of GRID**

NODE 1 = [0][0]
NODE 2 = [0][1]
⋮
NODEN = [N-1][M-1]

GRAPH




| Grid | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | 1 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 | 1 |
| 2 | 0 | 1 | 0 | 0 |

N x M

Total Component / Islands = 3

ANS

solve using BFS

visited

| | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | (0,0) F → T | (0,1) F | (0,2) F | (0,3) F |
| 1 | (1,0) F | (1,1) F | (1,2) F | (1,3) F |
| 2 | (2,0) F | (2,1) F | (2,2) F | (2,3) F |

N x M

initial state

Grid

| | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | SRC 1 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 | 1 |
| 2 | 0 | 1 | 0 | 0 |

N x M

Count: 0

Queue: (0,0)

initial state

Situation 1

BSF call [0,0]

STEP1 get frontNode and pop it

(0,0)

STEP2 find safe move [I, R, B, L]

[R] => (0,1)

[B] => (1,0)

STEP3 BFS call completed so count incremented by 1

Count | 0 |

visited

| | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | (0,0) ~~T~~ | (0,1) ~~T~~ | (0,2) F | (0,3) F |
| 1 | (1,0) ~~T~~ | (1,1) F | (1,2) F | (1,3) F |
| 2 | (2,0) F | (2,1) F | (2,2) F | (2,3) F |

N x M

Grid

| | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | SRC 1 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 | 1 |
| 2 | 0 | 1 | 0 | 0 |

N x M

Queue

initial state

| (0,0) | (0,1) | (1,0) | |
|---|---|---|---|

## Situation 1.1

BFS call (0,0)

STEP1 Get frontNode and pop it

(0,1)

STEP2 find safe move (T, R, B, L)

NO safe Mode from (0,1)

STEP3 BFS call completed so count increased by 1

Count 0

visited

| | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | (0,0) ~~F~~ T | (0,1) ~~F~~ T | (0,2) F | (0,3) F |
| 1 | (1,0) ~~F~~ T | (1,2) F | (1,2) F | (1,3) F |
| 2 | (2,0) F | (2,1) F | (2,2) F | (2,3) F |

N x M

Grid

| | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | 1 | (1) | 0 | 0 |
| 1 | 1 | 0 | 0 | 1 |
| 2 | 0 | 1 | 0 | 0 |

N x M

Queue | ~~(0,1)~~ | (1,0) |

## Situation 1.2

BFS call (0,0)

STEP1 Get frontNode and pop it

(1,0)

STEP2 find safe move (L, R, B, L) — X X X X

NO safe Moves from (1,0)

STEP3 BFS call completed so count increased by 1

Now Que is Empty So Increase the Count by 1

Count ~~0~~ 1

Queue (1,0) ~~(1,0)~~ |

visited

| | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | (0,0) ~~F~~ T | (0,1) ~~F~~ T | (0,2) F | (0,3) F |
| 1 | (1,0) ~~F~~ T | (1,1) F | (1,2) F | (1,3) F |
| 2 | (2,0) F | (2,1) F | (2,2) F | (2,3) F |

N x M

Grid

| | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | 1 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 | 1 |
| 2 | 0 | 1 | 0 | 0 |

N x M

## Situation 2

BFS call (1,3)

STEP1 Get frontNode and popit

(1,3)

STEP2 find safe move (T, R, B, L) (X X X X)

NO safe Mode from (1,3)

STEP3 BFS call completed so count incremented by 1

Now Queue is Empty So Increment the Count by 1

Count ~~1~~ 2

visited

| | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | (0,0) ~~T~~ | (0,1) ~~T~~ | (0,2) F | (0,3) F |
| 1 | (1,0) ~~T~~ | (1,2) F | (1,2) F | (1,3) ~~T~~ |
| 2 | (2,0) F | (2,1) F | (2,2) F | (2,3) F |

N x M

Grid

| | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | 1 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 | 1 |
| 2 | 0 | 1 | 0 | 0 |

N x M

Queue (~~1~~,3)

## Situation 3

BFS call (2,1)

STEP1 Get frontNode and pop it
(2,1)

STEP2 find safe move (L, R, B, L)
(X X X X)

No safe moves from (2,1)

STEP3 BFS call completed
so count incremented by 1

Now Queue is Empty
So Increment the Count by 1

Count ~~2~~ 3

Queue (2,1) ~~(2,1)~~ |

Output = 3

visited

| | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | (0,0) ~~T~~ | (0,1) ~~T~~ | (0,2) F | (0,3) F |
| 1 | (1,0) ~~T~~ | (1,2) F | (1,2) F | (1,3) ~~F~~ T |
| 2 | (2,0) F | (2,1) ~~F~~ T | (2,2) F | (2,3) F |

N x M

Grid

| | 0 | 1 | 2 | 3 |
|---|---|---|---|---|
| 0 | 1 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 | 1 |
| 2 | 0 | 1 | 0 | 0 |

N x M

```cpp
// 1. Number of Islands (Leetcode-200)
// Solve Using BFS Traversal

class Solution {
public:

    bool isSafe(int newX, int newY, vector<vector<char>>& grid, map<pair<int,int>,bool> &visited){
        if(newX >= 0 && newY >= 0 && newX < grid.size() && newY < grid[0].size() && !visited[{newX, newY}] && grid[newX][newY] != '0'){
            return true;
        }
        else{
            return false;
        }
    }

    void bfs(vector<vector<char>>& grid, int srcX, int srcY, map<pair<int,int>,bool> &visited){
        queue<pair<int, int> > q;
        // initial state
        q.push({srcX, srcY});
        visited[{srcX, srcY}] = true;

        while(!q.empty()){
            pair<int, int> frontNodePair = q.front();
            q.pop();
            int tempX = frontNodePair.first;
            int tempY = frontNodePair.second;

            // We have four move from each cell janaha par hum khade hue hai
            // TopMove --> RightMove --> BottomMove --> LeftMove
            int dx[] = {-1, 0, 1, 0};
            int dy[] = { 0, 1, 0, -1};
            for(int i=0; i<4; i++){
                int newX = tempX + dx[i];
                int newY = tempY + dy[i];
                if(isSafe(newX, newY, grid, visited)){
                    // Update the initial state
                    q.push({newX, newY});
                    visited[{newX, newY}] = true;
                }
            }
        }
    }

    int numIslands(vector<vector<char>>& grid) {
        int m = grid.size();
        int n = grid[0].size();
        int count = 0;

        map<pair<int,int>,bool> visited;

        for(int i=0; i<m; i++){
            for(int j=0; j<n; j++){
                if(grid[i][j] !='0' && !visited[{i,j}]){
                    bfs(grid, i, j, visited);
                    // islands is increasing by 1 when bfs call is completed
                    count++;
                }
            }
        }
        return count;
    }
};
```

Time and space complexity

= ?

```cpp
// 1. Number of Islands (Leetcode-200)
// Solve Using DFS Traversal

class Solution {
public:
    void dfs(vector<vector<char>>& grid, int i, int j){
        int m = grid.size();
        int n = grid[0].size();
        // Base case
        if(i < 0 || j < 0 || i >= m ||  j >= n || grid[i][j] =='0' || grid[i][j] == 'x'){
            return;
        }

        // 1 case hum solve kar lege:
        // x represents the current cell of grid is visited now
        grid[i][j] = 'x';

        // We have four move from each cell janaha par hum khade hue hai
        // TopMove
        dfs(grid, i-1, j);
        // BottomMove
        dfs(grid, i+1, j);
        // RightMove
        dfs(grid, i, j+1);
        // LeftMove
        dfs(grid, i, j-1);
    }

    int numIslands(vector<vector<char>>& grid) {
        int m = grid.size();
        int n = grid[0].size();
        int ans = 0;

        for(int i=0; i<m; i++){
            for(int j=0; j<n; j++){
                if(grid[i][j] !='0' && grid[i][j] != 'x'){
                    dfs(grid, i, j);
                    ans++;
                }
            }
        }
        return ans;
    }
};
```

Time and space complexity =

?

## 3. Flood Fill (Leetcode-733)

**Problem Statement:**
An image is represented by an **m x n** integer grid **image** where **image[i][j]** represents the pixel value of the image.

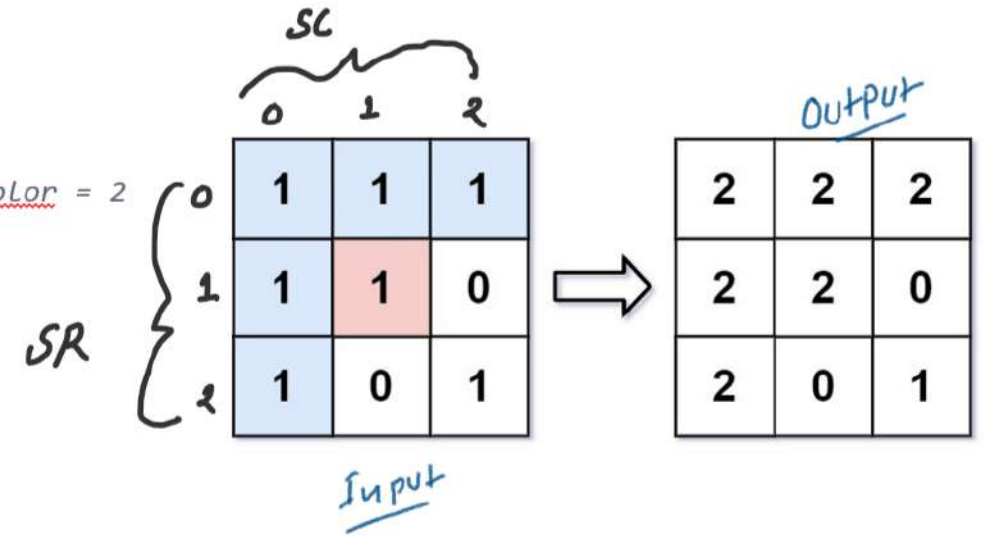
You are also given three integers **sr**, **sc**, and **color**. You should perform a **flood fill** on the image starting from the pixel **image[sr][sc]**.

To perform a **flood fill**, consider the starting pixel, plus any pixels connected **4-directionally** to the starting pixel of the same color as the starting pixel, plus any pixels connected **4-directionally** to those pixels (also with the same color), and so on. Replace the color of all of the aforementioned pixels with **color**.

Return the modified image after performing the flood fill.

**Example 1:**
Input: image = [[1,1,1],[1,1,0],[1,0,1]], sr = 1, sc = 1, color = 2
Output: [[2,2,2],[2,2,0],[2,0,1]]

- oldColour = image[1][1] = 1
- newColour = 2

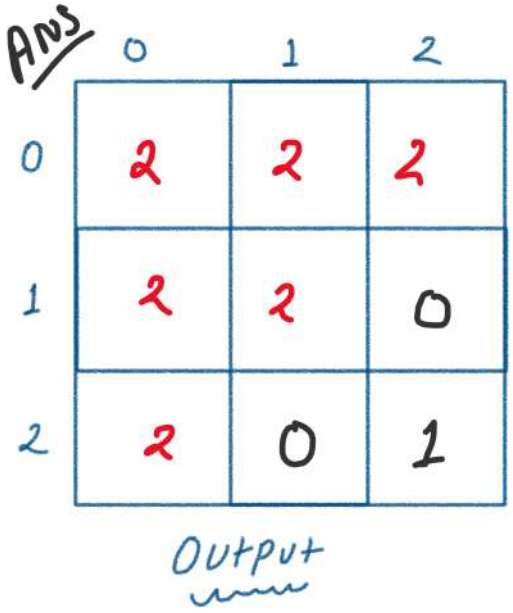


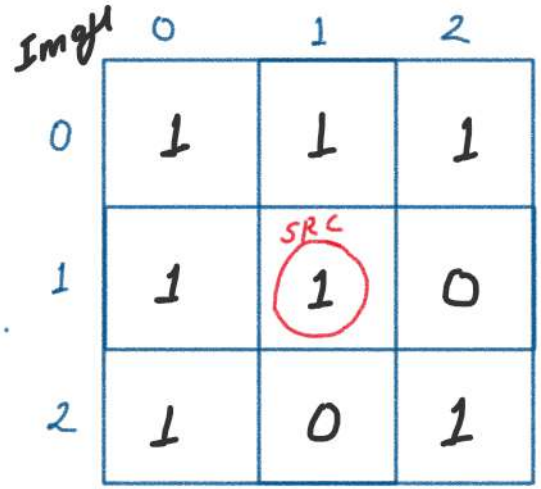
# Solve using DFS Algo

***Example 1:***

*Input: image = [[1,1,1],[1,1,0],[1,0,1]], sr = 1, sc = 1, color = 2*

*Output: [[2,2,2],[2,2,0],[2,0,1]]*




SRC Node = Image[1][1]

Old Colour = 1

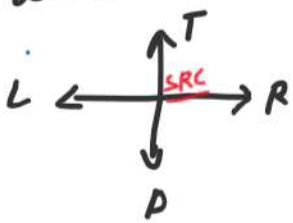
New Colour = 2

DRY RUN

| Key | Value |
|---|---|
| 0,0 | ~~F~~ T |
| 0,1 | ~~F~~ T |
| 0,2 | ~~F~~ T |
| 1,0 | ~~F~~ T |
| 1,1 | ~~F~~ T |
| 1,2 | F |
| 2,0 | ~~F~~ T |
| 2,1 | F |
| 2,2 | F |

visited

we have 4-moves



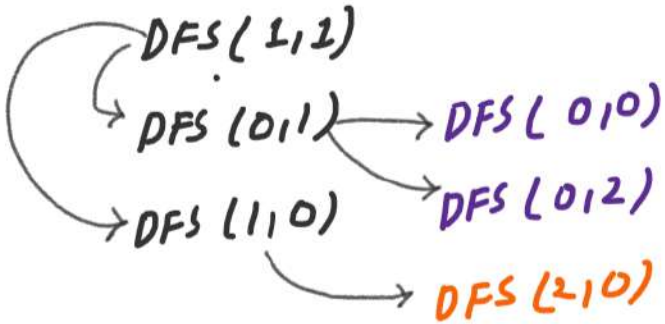

ANS

| | 0 | 1 | 2 |
|---|---|---|---|
| 0 | 2 | 2 | 2 |
| 1 | 2 | 2 | 0 |
| 2 | 2 | 0 | 1 |

Image

| | 0 | 1 | 2 |
|---|---|---|---|
| 0 | 1 | 1 | 1 |
| 1 | 1 | 1 | 0 |
| 2 | 1 | 0 | 1 |

SRC




Src Node = Image[1][1]

Old Colour = 1

New Colour = 2

```cpp
// 3. Flood Fill (Leetcode-733)

class Solution {
public:

    bool isSafe(int newX, int newY, map<pair<int,int>,bool> &visited, vector<vector<int>> &ans, int oldColor){
        if(newX >= 0 &&
           newY >= 0 &&
           newX < ans.size() &&
           newY < ans[0].size() &&
           ans[newX][newY] == oldColor &&
           visited[{newX, newY}] == false)
        {
            return true;
        }
        else
        {
            return false;
        }
    }

    void dfs(int oldColor, int newColor, map<pair<int,int>, bool> &visited, vector<vector<int>> &ans,
             vector<vector<int>>& image, int sr, int sc){.......}

    vector<vector<int>> floodFill(vector<vector<int>>& image, int sr, int sc, int color) {
        vector<vector<int>> ans = image;
        map<pair<int,int>, bool> visited;
        int oldColor = image[sr][sc];
        int newColor = color;

        dfs(oldColor, newColor, visited, ans, image, sr, sc);
        return ans;
    }
};
```

```cpp
void dfs(int oldColor, int newColor, map<pair<int,int>, bool> &visited, vector<vector<int>> &ans,
         vector<vector<int>>& image, int sr, int sc)
{
    // visited true for each cell/node
    visited[{sr,sc}] = true;
    // ans is updated with newColor
    ans[sr][sc] = newColor;

    // We have four move from each cell janaha par hum khade hue hai
    // TopMove --> RightMove --> BottomMove --> LeftMove
    int dx[] = {-1, 0, 1, 0};
    int dy[] = { 0, 1, 0, -1};
    for(int i=0; i<4; i++)
    {
        int newX = sr + dx[i];
        int newY = sc + dy[i];
        if(isSafe(newX, newY, visited, ans, oldColor))
        {
            dfs(oldColor, newColor, visited, ans, image, newX, newY);
        }
    }
}
```

Why single call of DFS ?

↳ Because of SRC Node ke according hame newColor fill karna hai.

## 📂 4. Rotting Oranges (Leetcode-994)

***PROBLEM STATEMENT:***

*You are given an **m x n** grid where each cell can have one of three values:*

- ***0** representing an **empty** cell,*
- ***1** representing a **fresh** orange, or*
- ***2** representing a **rotten** orange.*

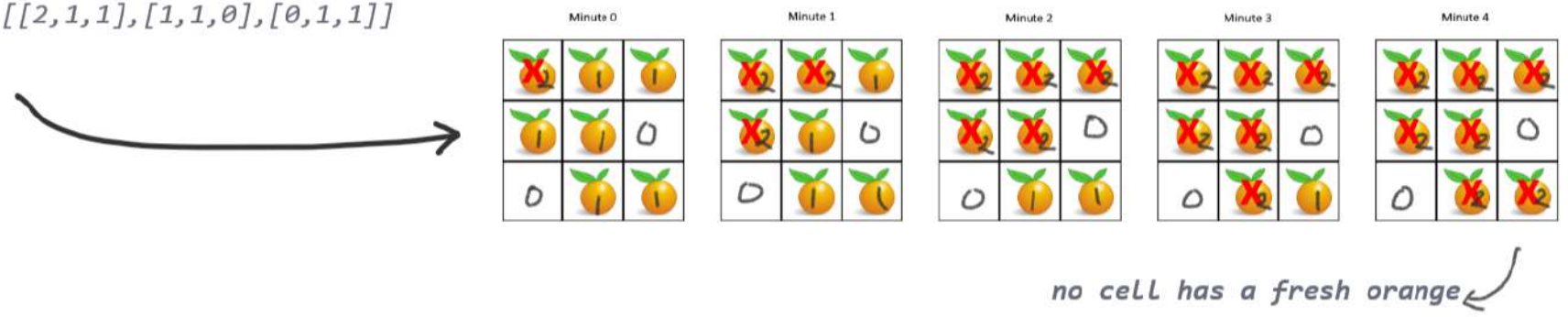
*Every minute, any fresh orange that is 4-directionally adjacent to a rotten orange becomes rotten.*

*Return the **minimum number of minutes** that must elapse until **no cell has a fresh orange**. If this is impossible, return **-1**.*

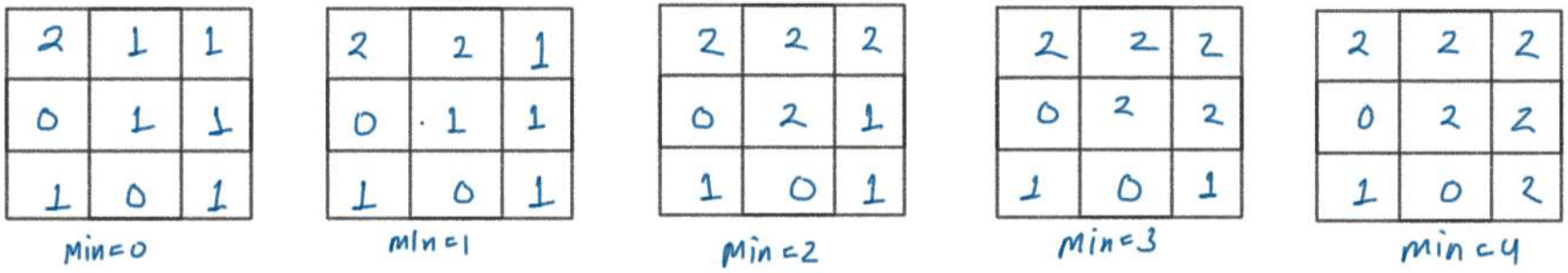
***Example 1:***

*Input: grid = [[2,1,1],[1,1,0],[0,1,1]]*

*Output: 4*



***Example 2:***
*Input: grid = [[2,1,1],[0,1,1],[1,0,1]]*
*Output: -1*

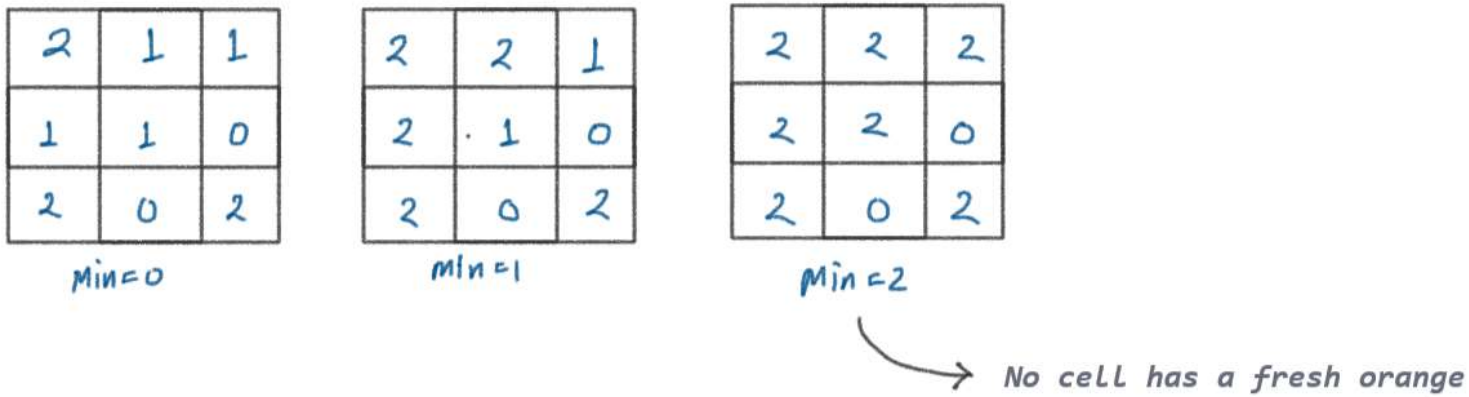



*One cell has a fresh orange so return -1*

***Example 3:***
*Input: grid = [[0,2]]*
*Output: 0*


*No cell has a fresh orange*

***Example 4:***
*Input: grid = [[2,1,1],[1,1,0],[2,0,2]]*
*Output: 2*



Solve using BFS

*Example 4:*
*Input: grid = [[2,1,1],[1,1,0],[2,0,2]]*
*Output: 2*

⇒ initial state

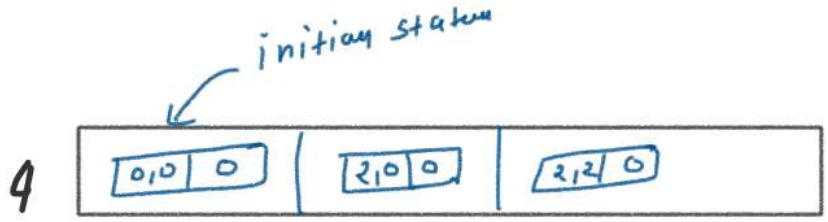
q.push ( coordinates , TIME)

when grid[x][y] == 2

grid

| | 0 | 1 | 2 |
|---|---|---|---|
| 0 | 2 | 1 | 1 |
| 1 | 1 | 1 | 0 |
| 2 | 2 | 0 | 2 |

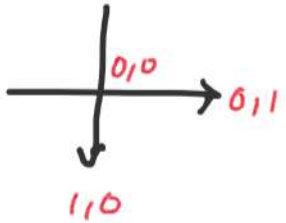
Min=0



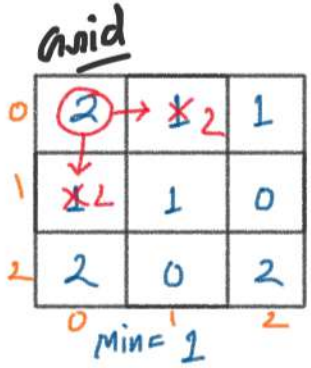
Iteration 1

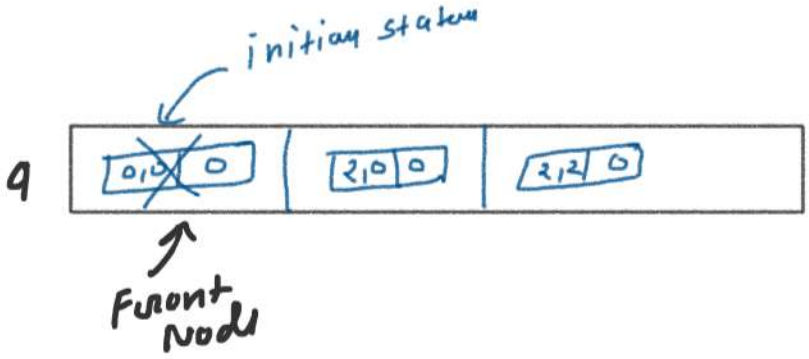
STEP1 Get frontNode and pop it


STEP2 We have four from each node
so go to possible move to make bottom graph

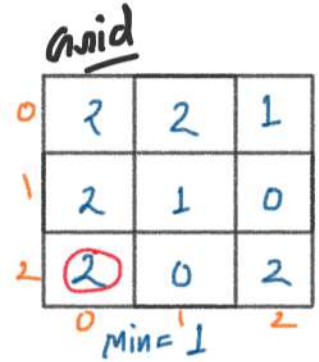



and push bottom graph into queue



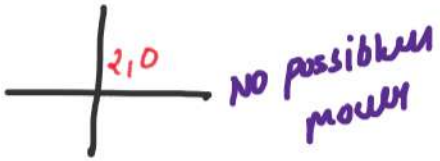



## Iteration 2

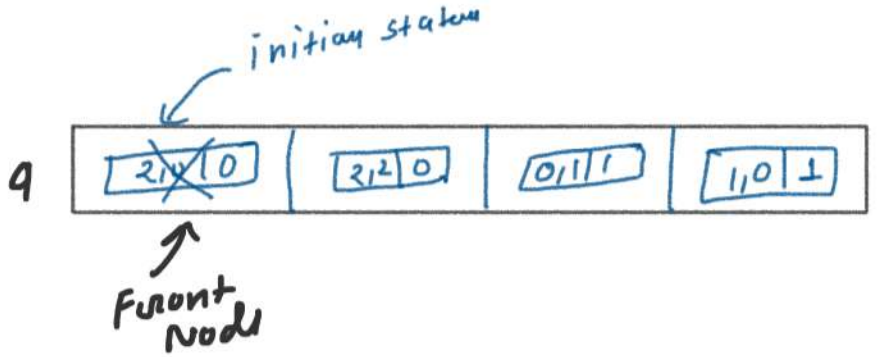



**STEP1** Get frontNode and pop it

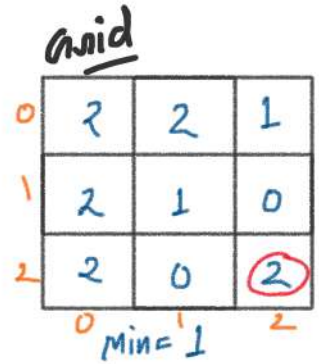

**STEP2** We have four from each node
so go to possible move to make bottom orange




and push bottom orange into queue

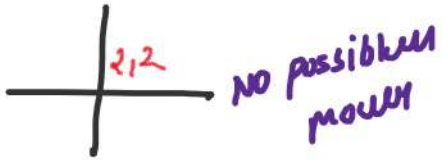


Iteration 3

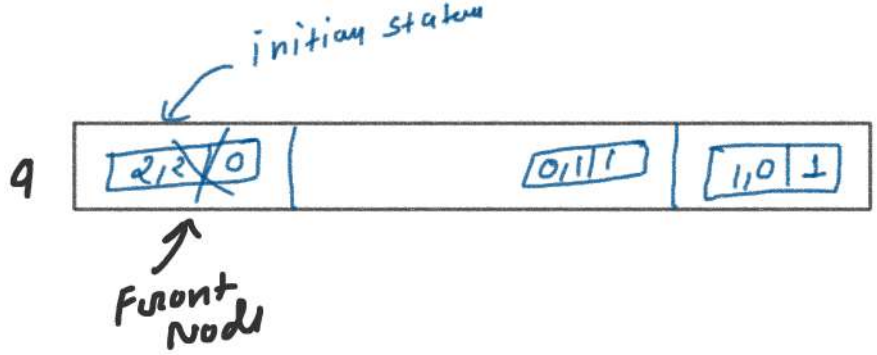



STEP1 Get frontNode and pop it


STEP2 We have four from each node
so go to possible move to mark rotten orange



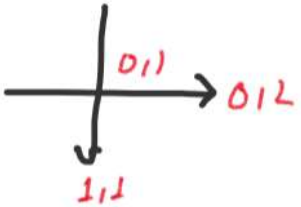

and push rotten orange into queue



## Iteration 4

STEP1 Get frontNode and pop it


STEP2 We have four from each node
so go to possible node to mark rotten orange




and push rotten orange into queue

grid

| | | | |
|---|---|---|---|
| 0 | 2 | 2 | ~~1~~ 2 |
| 1 | 2 | ~~1~~ 2 | 0 |
| 2 | 2 | 0 | 2 |
| | 0 | 1 Min=2 | 2 |

initial state

q


Front Node

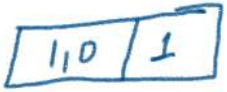
## Iteration 5

grid

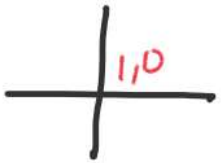
| | 0 | 1 | 2 |
|---|---|---|---|
| 0 | 2 | 2 | 2 |
| 1 | 2 | 2 | 0 |
| 2 | 2 | 0 | 2 |

Min = 2

**STEP1** Get frontNode and pop it

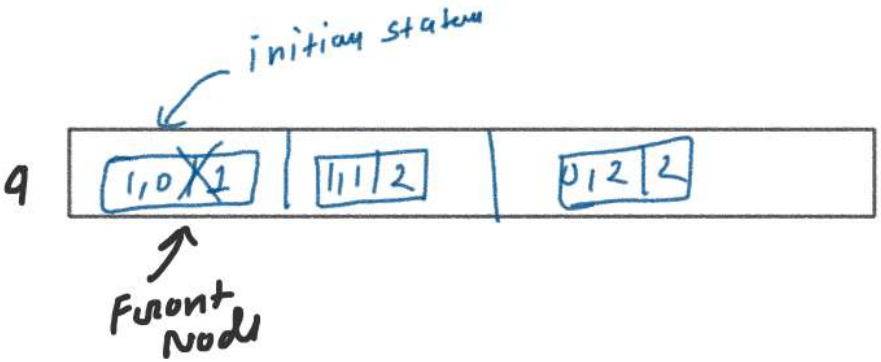



**STEP2** We have four from each node
so go to possible move to mark rotten orange

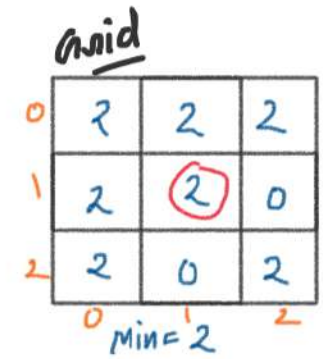



No possible move

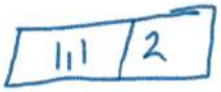
and push rotten orange into queue



## Situation 6



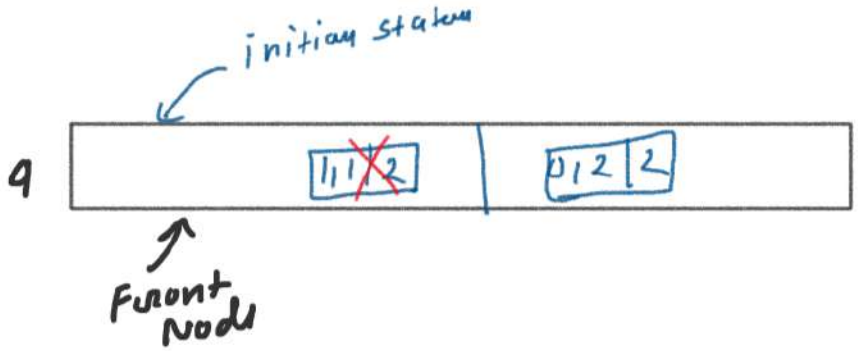

**STEP1** Get frontNode and pop it




**STEP2** We have four from each node
so go to possible move to mark rotten orange

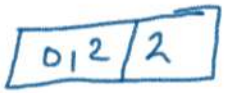

No possible move

and push rotten orange into queue

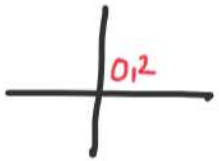


Iteration 7

STEP1 Get frontNode and pop it




STEP2 We have four from each node
so go to possible move to mark rotten orange



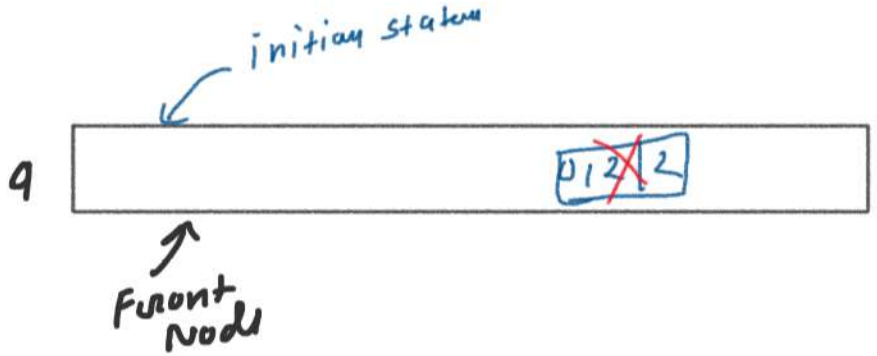

No possible move

and push rotten orange into queue

grid

| | | | |
|---|---|---|---|
| 0 | 2 | 2 | 2 |
| 1 | 2 | 2 | 0 |
| 2 | 2 | 0 | 2 |
| | 0 | 1 | 2 |

Min = 2



Iteration 8

grid

| | | | |
|---|---|---|---|
| 0 | 2 | 2 | 2 |
| 1 | 2 | 2 | 0 |
| 2 | 2 | 0 | 2 |
| | 0 | 1 | 2 |

Minc 2

STEP3 jab queue empty ho jayega it means Humne all possible oranges ko Rotten kar diya Hai ⇒

freshOranges == 1

↳ return -1

freshOranges != 0 = 1

↳ return time

q EMPTY

```cpp
// 4. Rotting Oranges (Leetcode-994)

class Solution {
public:
    bool isSafe(int newX, int newY, vector<vector<int>> &temp){.....}

    int orangesRotting(vector<vector<int>>& grid) {
        vector<vector<int>> temp = grid;
        queue<pair<pair<int,int>, int>> q;
        int minTime = 0;

        // find all rotten oranges and push into the queue
        int n = grid.size();
        int m = grid[0].size();
        for(int i=0; i<n; i++){
            for(int j=0; j<m; j++){
                if(temp[i][j] == 2){
                    // Initial state:
                    // push each src node into the queue with initial time is 0 minute
                    q.push({{i, j}, 0});
                }
            }
        }

        // BFS Logic start
        while(!q.empty()){.....}

        // Step 3: ab queue empty ho chuka hai it means
        // hamne all possible oranges ko rotten bna diya hai
        // check karo ki koi orange fresh to nhi hai agar hai to return -1
        for(int i=0; i<n; i++){
            for(int j=0; j<m; j++){
                if(temp[i][j] == 1){
                    return -1;
                }
            }
        }

        // Koi fresh ornage nhi hai to minTime return krdo
        return minTime;
    }
};
```

```cpp
bool isSafe(int newX, int newY, vector<vector<int>> &temp){
    if(newX >= 0 &&
       newY >= 0 &&
       newX < temp.size() &&
       newY < temp[0].size() &&
       temp[newX][newY] == 1)
    {
        return true;
    }
    else{
        return false;
    }
}
```

```cpp
// BFS Logic start
while(!q.empty()){
    // Step 1: get front node and pop it
    auto frontNodePair = q.front();
    q.pop();

    auto frontNodeCoordinates = frontNodePair.first;
    int frontNodeTime = frontNodePair.second;
    int tempX = frontNodeCoordinates.first;
    int tempY = frontNodeCoordinates.second;

    // Step 2: we have four move from each node so goto
    // each possible move to make rotten orange
    int dx[] = {-1, 0, 1, 0};
    int dy[] = { 0, 1, 0, -1};
    for(int i=0; i<4; i++){
        int newX = tempX + dx[i];
        int newY = tempY + dy[i];
        if(isSafe(newX, newY, temp)){
            // Push rotten orange into queue
            q.push({{newX, newY}, frontNodeTime+1});
            // Mark as rotten orange
            temp[newX][newY] = 2;
            // Update the minTime
            minTime = max(frontNodeTime+1, minTime);
        }
    }
}
```

Time Complexity
$= O(N^2)$