

Find Polygon with the Largest Perimeter (LEETCODE-2971)

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Date: 15-02-2024

Given polygon

- At least 3 sides $\Rightarrow (K \geq 3)$
- longest side (a_k) < sum of other sides
 $\hookrightarrow a_k < a_1 + a_2 + \dots + a_{k-1}$

This condition is applied for checking is polygon or not

where

$$a_1 \leq a_2 \leq a_3 \leq a_4 \dots a_{k-1} \leq a_k$$

\hookrightarrow Given Array ko SORT KARNA PADEGA TO FIND THE Longest side

Ex



sides

$$a_1 = 2$$

$$a_2 = 2$$

$$a_3 = 3$$

perimeter

$$= a_1 + a_2 + a_3$$

$$= 2 + 2 + 3$$

$$= 7$$

Input: `nums = [1, 12, 1, 2, 5, 50, 3]`
 Output: 12

Explanation

a_1	a_2	a_3	a_4	a_5	a_6	a_7
1	1	2	3	5	12	50
0	1	2	3	4	5	6

\nwarrow $a_{k-1} + \text{side} = a_k$

Case 4 $a_4 = 3$ $\text{sum} = 4 \Rightarrow 3 < 4$ ✓

$\rightarrow \text{perimeter} = 3 + 4 = 7$

Case 5 $a_3 = 2$ $\text{sum} = 2 \Rightarrow 2 < 2$ ✗

Case 6 a_2 STOP $[k] = 3$

$2 > 3$ ✗ \rightarrow $\text{output} = \max(7, 12) = 12$

Check polygon OR not

$$a_k < a_1 + a_2 + a_3 + \dots + a_{k-1}$$

Case 1 $a_7 = 50$ $\text{sum} = 24 \Rightarrow 50 < 24$ ✗
 Not polygon

Case 2 $a_6 = 12$ $\text{sum} = 12 \Rightarrow 12 < 12$ ✗
 Not polygon

Case 3 $a_5 = 5$ $\text{sum} = 7 \Rightarrow 5 < 7$ ✓
 This is polygon

$\rightarrow \text{perimeter} = 5 + 7 = 12$

Approach Backward

STEP 1 SORT Array

STEP 2 Get sum of all elements

STEP 3 Traverse the array backwards

STEP 4 check $(sum - \text{largest side}) > \text{largest side}$

STEP 5 This condition is met
→ return perimeter

STEP 6 if no suitable perimeter found
→ return -1

Nums

[SORT]						
1	1	2	3	5	12	50
0	1	2	3	4	5	6

↖ i

$i = 6$

sum = 74
largest side = 50

$$\begin{aligned} \text{sum} &= 74 - 50 \\ &= 24 \\ 24 > 50 &\times \end{aligned}$$

$i = 5$

sum = 24
largest side = 12

$$\begin{aligned} \text{sum} &= 24 - 12 \\ &= 12 \\ 12 > 12 &\times \end{aligned}$$

$i = 4$

sum = 12
largest side = 5

$$\begin{aligned} \text{sum} &= 12 - 5 \\ &= 7 \\ 7 > 5 &\checkmark \end{aligned}$$

→ return (sum + largest side)
 $= 7 + 5$
 $= 12$

```

/*
Approach 1( With Backward Iteration):
Time complexity: O(N Log N)
Space complexity: O(1)
Author: github.com/BCAPATHSHALA
*/

class Solution {
public:
    long long largestPerimeter(vector<int>& nums) {
        // Step1: Sort the array first
        sort(nums.begin(), nums.end());

        // Step2: Sum all the elements in the nums array
        long long sum = 0;
        for(auto i : nums) {
            sum += i;
        }

        // Step3: Traverse the array backwards
        int n = nums.size();
        for(int i = n - 1; i >= 2; i--){
            // Step4: Check if the sum minus the current element is greater than the current element
            sum -= nums[i];

            // Step5: If the condition is met, return the sum plus the current element as the perimeter
            if(sum > nums[i]){
                return sum + nums[i];
            }
        }
        // Step6: If no suitable perimeter is found, return -1
        return -1;
    }
};

```

T.C. $\Rightarrow O(\log N)$ for sorting

T.C. $\Rightarrow O(N)$ for loop

Overall T.C. $\Rightarrow O(N \log N)$

S.C. $\Rightarrow O(1)$

where N is length of input Array.