

When to use the DIJKSTRA ALGORI. With PROOF

LinkedIn @manojofficialmj

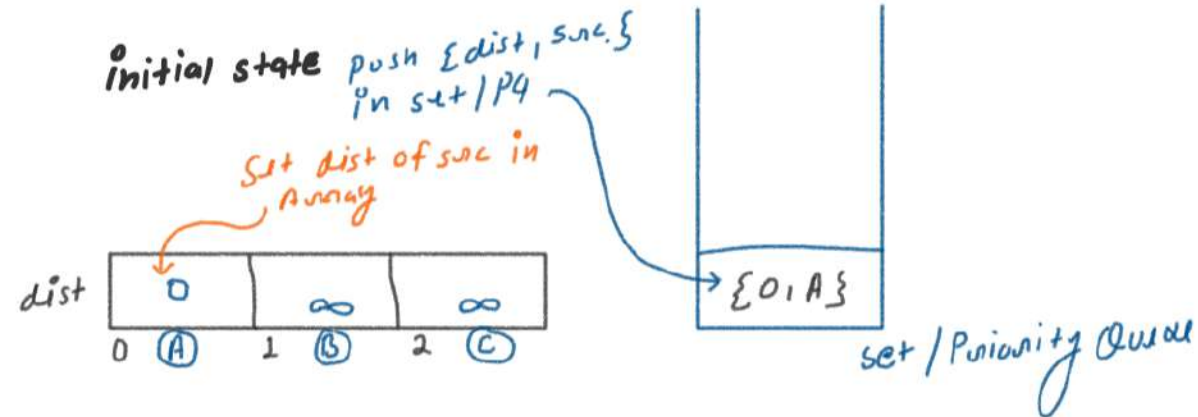
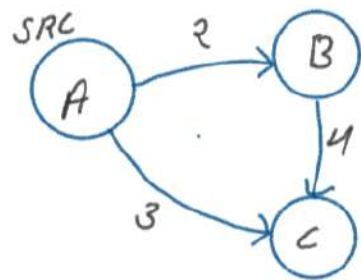
1. Dijkstra Algorithm

 Dijkstra Algorithm: Source, Destination, Minimum

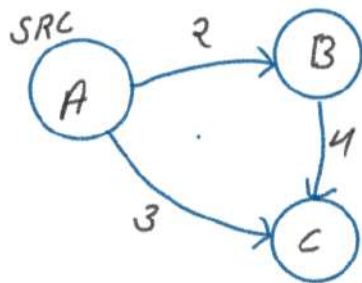
Note 1: It is used to find all shortest path from source to all nodes in a negative and positive weighted, directed or undirected graph.

Note 2: It is not used to when a graph have the negative cycle because of occurring the infinite loop

Example 1: positive weighted directed graph



DRY RUN



Iteration 1

STEP 1 Get shortest dist node from sst/pq and pop it
 $\{0, A\}$

STEP 2 update dist array and create new entry in sst when

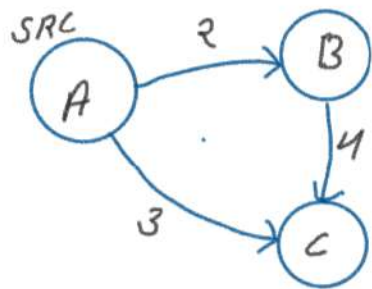


dist

0	1	2
A	B	C

$\{3, C\}$
$\{2, B\}$
$\{0, A\}$

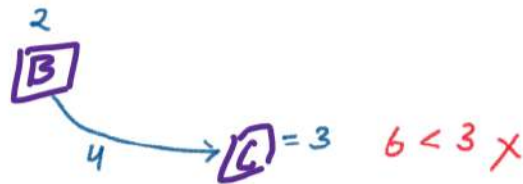
set / Priority Queue



Iteration 2

STEP 1 Get shortest dist node from sst/pq and pop it
 $\{2, B\}$

STEP 2 update dist array and create new entry in sst array

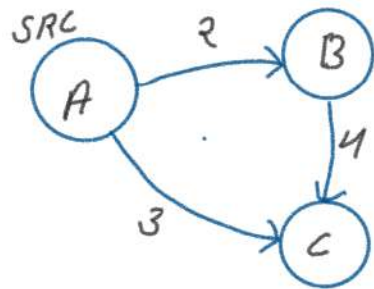


dist

0	2	3
A	B	C



set / Priority Queue



Iteration 3

STEP 1 Get shortest dist node from sst/pq and pop it
 $\{3, C\}$

STEP 2 update dist array and create new entry in sst array

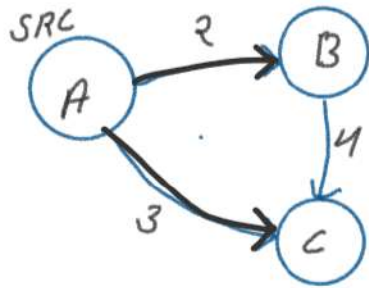
³
C → yanna se kahi ja
 hi nahi sakte hai

dist	0	2	3
	0 (A)	1 (B)	2 (C)



set / Priority Queue

Iterations



STEP 1 Get shortest dist node from set/pq and pop it
↳ Ab set/pq empty ho chuka hai, so stop the loop

All shortest path from **SRC**

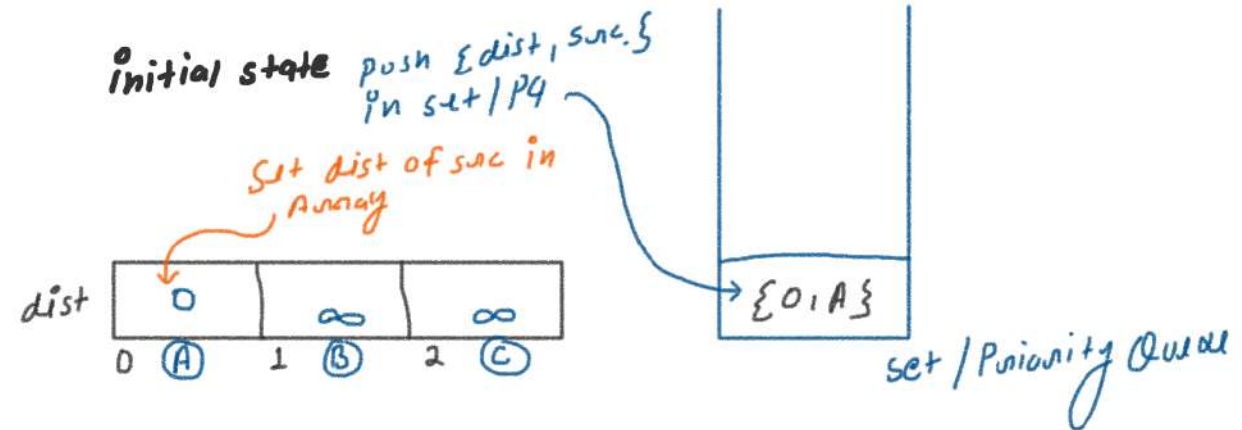
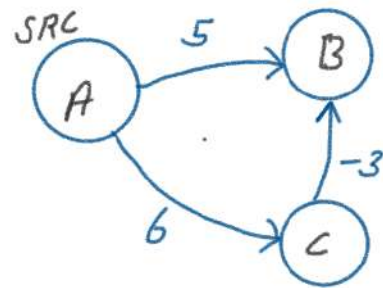
dist

0	1	2
A	B	C

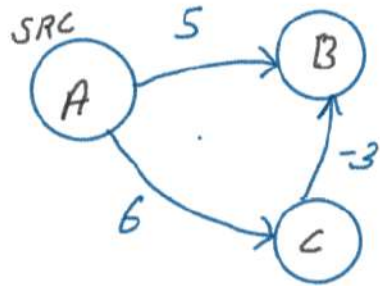
Empty

set / Priority Queue

Example 2: negative weighted directed graph



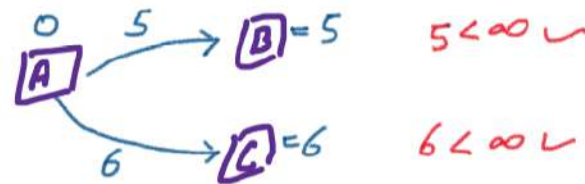
DRY RUN



Iteration 1

STEP 1 Get shortest dist node from set/pq and pop it
 $\{0, A\}$

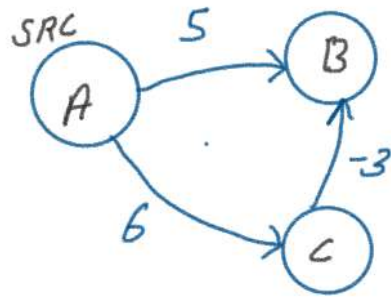
STEP 2 update dist array and create new entry in set array



dist	0	5	6
	0	1	2
	A	B	C

$\{5, C\}$
$\{6, B\}$
$\{0, A\}$

set / Priority Queue



STEP 1 Get shortest dist node from sst/pq and pop it
 $\{5, C\}$

STEP 2 update dist array and create new entry in sst when

$$\boxed{C} \xrightarrow{-3} \boxed{B} = 3 \quad 3 < 5 \quad \checkmark$$

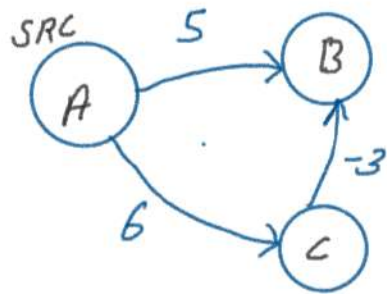
Iteration 2

dist

0	3	6
(A)	(B)	(C)

$\{5, C\}$
$\{6, B\}$

set / Priority Queue



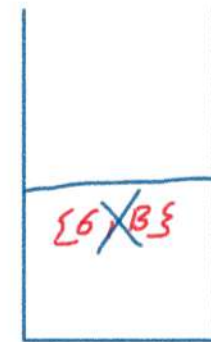
Iteration 3

- STEP 1 Get shortest dist node from set/PQ and pop it
 $\{6, B\}$
- STEP 2 update dist array and create new entry in set and

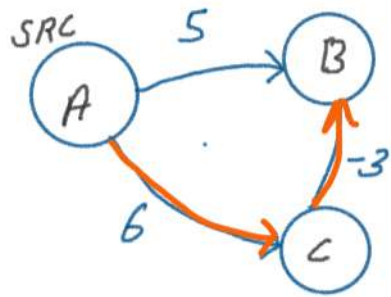
³
B → Yanna se kahi ja
 hi nahi sakte hai

dist

0	1	2
0	3	6
A	B	C



set / Priority Queue



Iteration 4

STEP 1 Get shortest dist node from set/PQ and pop it
 ↳ As set/PQ empty ho chuka hai, so stop the loop

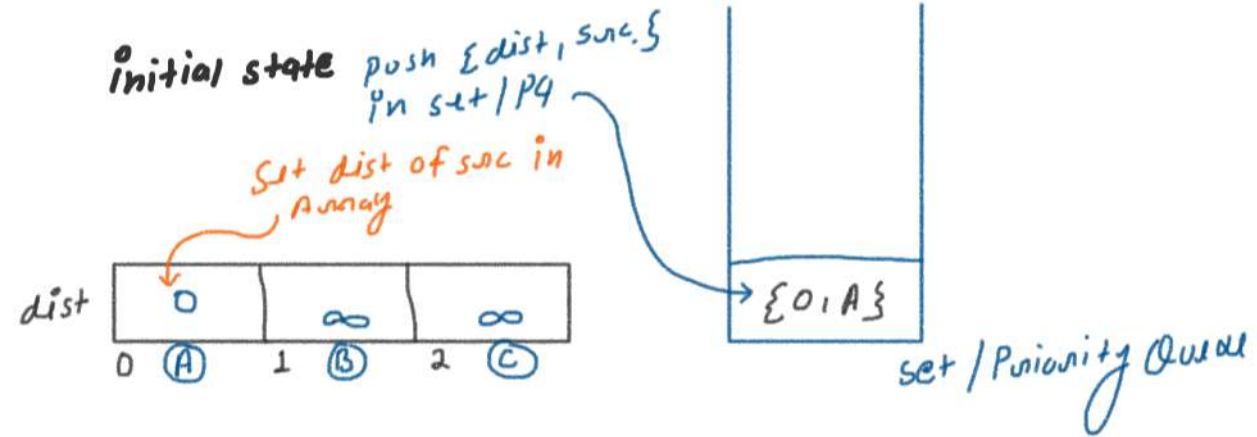
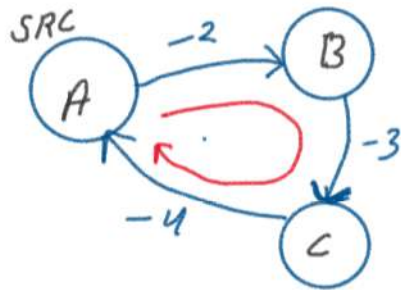
All shortest path from SRC

dist	0	3	6
	0 (A)	1 (B)	2 (C)

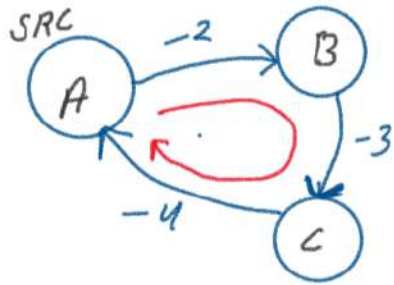
Empty

set / Priority Queue

Example 3: negative cycle in directed graph



DRY RUN



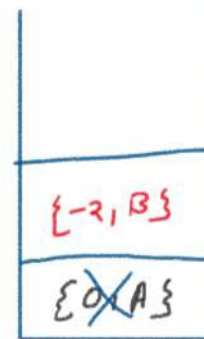
Iteration 1

STEP 1 Get shortest dist node from set/pq and pop it
 $\{0, A\}$

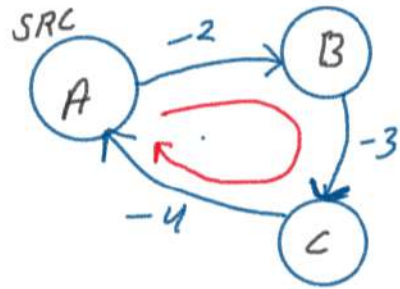
STEP 2 update dist array and create new entry in set and



dist	0	-2	∞
	0	1	2
	A	B	C



set / Priority Queue



Iteration 2

STEP 1 Get shortest dist node from sst/pq and pop it
 $\{-2, B\}$

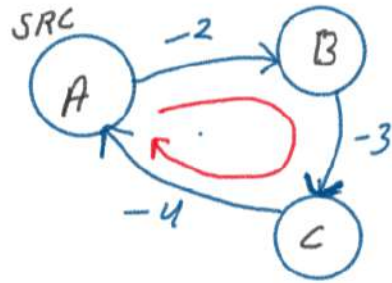
STEP 2 update dist array and create new entry in sst array

$$\boxed{B} \xrightarrow{-3} \boxed{C} = -5 \quad -5 < \infty$$

dist	0	-2	-5
	0 (A)	1 (B)	2 (C)

$\{-5, C\}$
$\{-2, B\}$

set / Priority Queue



STEP 1 Get shortest dist node from set/PQ and pop it
 $\{-5, C\}$

STEP 2 update dist array and create new entry in set when

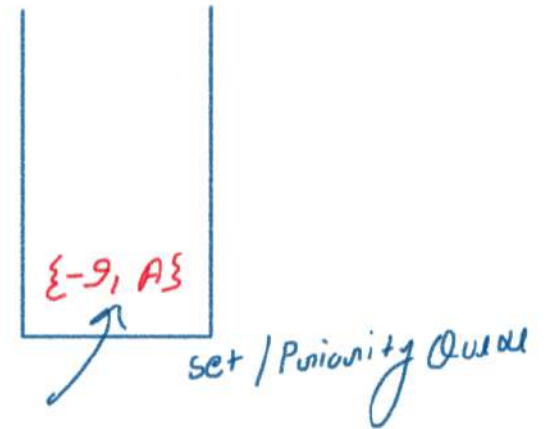
$$\boxed{C} \xrightarrow{-4} \boxed{A} = -9 \quad -9 < 0$$

Iteration 3

∞ Infinite loop me
 Loop Fas jayenge

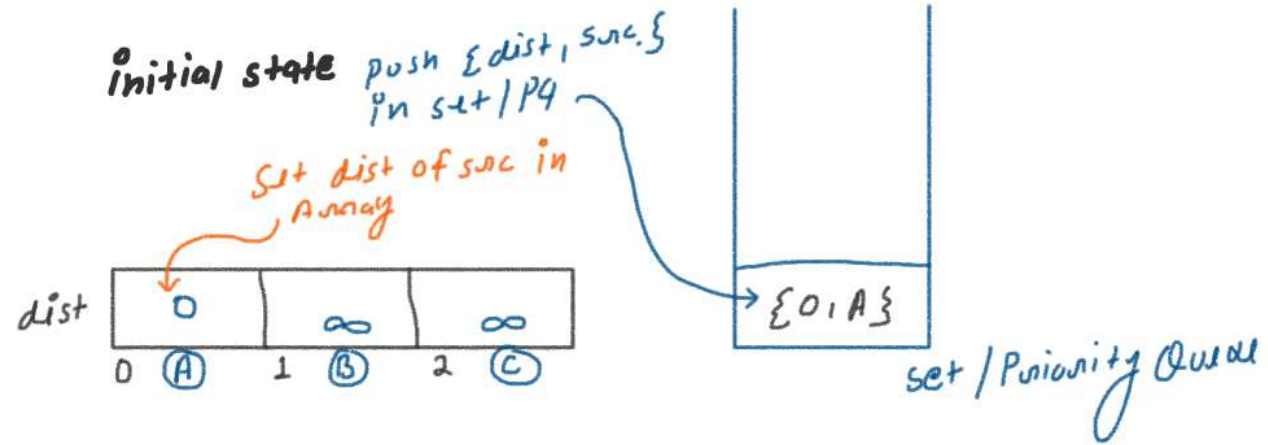
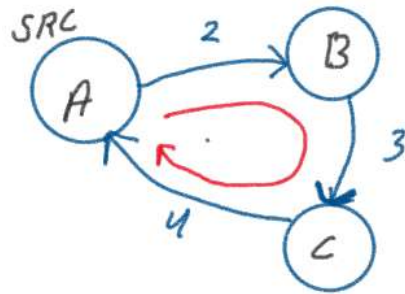
dist

-9	-2	-5
0 (A)	1 (B)	2 (C)

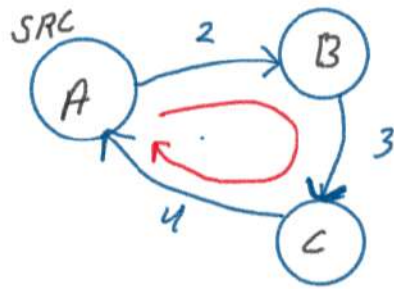


{ Jab $(-u) + (-u)$ to Hamish smallest distan mita
 Ranga as comane to jo dist array me pahle se Rakha
 Huaa hai to Iss Rangan Set/PQ Empty Nahi Ho payega }

Example 4: positive cycle in directed graph



DRY RUN



Iteration 1

STEP 1 Get shortest dist node from set/pq and pop it
 $\{0, A\}$

STEP 2 update dist array and create new entry in set when

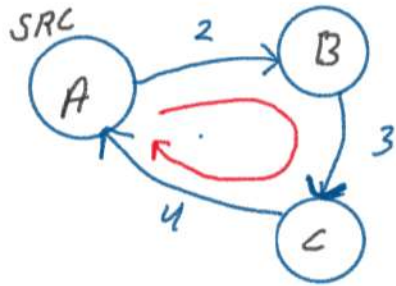


dist	0	2	∞
	0 (A)	1 (B)	2 (C)



set / Priority Queue

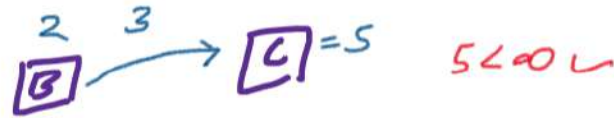
DRY RUN



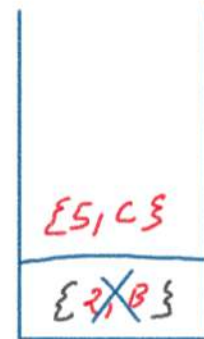
Iteration 2

STEP 1 Get shortest dist node from sst/pq and pop it
 $\{2, B\}$

STEP 2 update dist array and create new entry in sst when

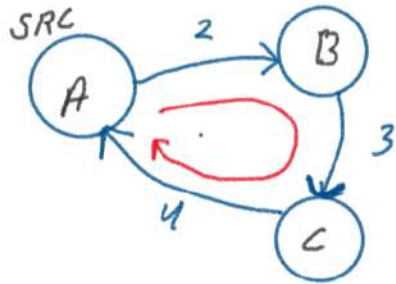


dist	0	2	5
	A	B	C



set / Priority Queue

DRY RUN



Iteration 3

- STEP 1 Get shortest dist node from set/pq and pop it
 $\{5, C\}$
- STEP 2 update dist array and create new entry in set when

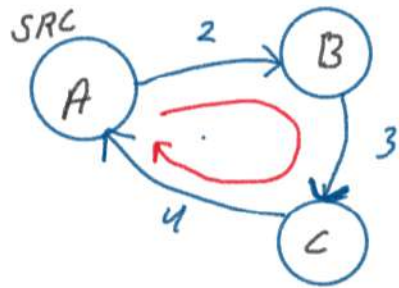


dist

0	2	5
0 (A)	1 (B)	2 (C)



set / Priority Queue



Iteration 4

STEP 1 Get shortest dist node from set/pq and pop it

Now set/pq is Empty so stop the loop.

All shortest path from SRC

dist	0	2	5
	0 (A)	1 (B)	2 (C)

Empty

set / Priority Queue