



Subject Name: **Theory of Computation**

Subject Code: **IT-5001**

Semester: **5<sup>th</sup>**



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## Notes on Left Factoring and Left Recursion

### 2.12 Left Factoring

In a CFG more than one productions contain common prefix substring it is called Left Factoring.

$$A \rightarrow \alpha \beta \mid \alpha \gamma \mid \alpha Z$$

Left factoring has to be eliminated from the grammar. It can be done by rewriting left factoring production as follows

$$\begin{aligned} A &\rightarrow \alpha D \\ D &\rightarrow \beta \mid \gamma \mid Z \end{aligned}$$

( A new variable D is introduced )

### Example of elimination of Left Factoring

Consider productions of CFG

$$S \rightarrow aBD \mid aBbD \mid aBbE$$

$$B \rightarrow a$$

$$D \rightarrow b$$

$$E \rightarrow a$$

In S productions aB are common prefix substring

Therefore new productions can be created with new variable F

$$S \rightarrow aBF$$

$$F \rightarrow D \mid bD \mid bE$$

$$B \rightarrow a$$

$$D \rightarrow b$$

$$E \rightarrow a$$

Now F productions has common prefix sub string b, Therefore new productions can be created with new variable H

$$S \rightarrow aBF$$

$$F \rightarrow D \mid bH$$

$$H \rightarrow D \mid E$$

$$B \rightarrow a$$

$$D \rightarrow b$$

$$E \rightarrow a$$

### 2.13 Direct Left Recursion

Left recursion is a case when the left-most variable in a production of a variable is the variable itself is known as direct left recursion.

Consider production  $A \rightarrow A \alpha \mid \beta$ . In this production  $A \rightarrow A \alpha$  is direct left recursion.

In building of parser ( component of Compiler ) Left recursion have to be removed.

### Elimination of Left Recursion

Consider  $A \rightarrow A \alpha \mid \beta$ . Left Recursion can be eliminated by introducing a new variable Z as follows

$$A \rightarrow \beta \mid \beta Z$$
$$Z \rightarrow \alpha \mid \alpha Z$$

### Example on Elimination of Left Recursion

$$A \rightarrow AB \mid BA \mid a$$
$$B \rightarrow b \mid c$$

### Solution

$$A \rightarrow BA \mid a \mid BAZ \mid aZ$$
$$Z \rightarrow B \mid BZ$$
$$B \rightarrow b \mid c$$




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