CSE 601 – Homework 2 Mining Association Rules from Gene Expression Data

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Part 1

Task

Implement the Apriori algorithm to find all frequent itemsets. Report the number of frequent itemsets for support of 30%, 40%, 50%, 60%, and 70%, respectively.

Implementation Details about Apriori Algorithm

The input data is taken from gene_expression.txt file. We read the file from the .txt file using a BufferedReader in Java. Each line is read one at a time and we split the terms with a tab delimiter. In each line the first term is considered to be the symptom and the rest are the geneset for the symptom. In the input file the genes are given as up and down. We append "G" and the position of it to the value of term to generate our itemset. The Apriori algorithm is performed on this itemset. In our implementation we called the itemset as transactions. Transactions are generated by the function parse and stores as an ArrayList.

The program takes the text file and the Minimum support count as the input. There are two steps in our implementation of this algorithm. We first generate the candidate itemset using the function generateCandidateItemset. This generates the combination of size N depending on the stage of the call and populates the ArrayList candidateItemset. This itemset is then pruned to get the frequent item set. To perform pruning, the number of occurrences of each combination in the given transaction is recorded in a HashMap frequentItemsetMap. If the count(value of itemset in map) is less than the minimum support count, then the combination is eliminated. This is performed by generateFrequentItemset. The process of forming combination of size N is stopped when no further combination can be produces. Following the requirement the output at each minimum support count is the number of itemsets at each possible length that can be generated and the total of number of itemsets at each stage.

Result

Support is set to be: 70%

number of length-1 frequent itemset: 7

Total:7

Support is set to be: 60%

number of length-1 frequent itemset: 34 number of length-2 frequent itemset: 2

Total:36

Support is set to be: 50%

number of length-1 frequent itemset: 109 number of length-2 frequent itemset: 63 number of length-3 frequent itemset: 2

Total:174

Support is set to be: 40%

number of length-1 frequent itemset: 167 number of length-2 frequent itemset: 753 number of length-3 frequent itemset: 149 number of length-4 frequent itemset: 7 number of length-5 frequent itemset: 1

Total:1077

Support is set to be: 50

number of length-1 frequent itemset: 109

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number of length-2 frequent itemset: 63
{[G72 UP]}->{[G32 Down]}
{[G32\_Down]} -> {[G72\_UP]}
\{[G97\_Down]\} -> \{[G82\_Down]\}
\{[G82\_Down]\} -> \{[G97\_Down]\}
{[G88\_Down]} -> {[G24\_Down]}
{[G24\_Down]} -> {[G88\_Down]}
\{[G94\_UP]\} -> \{[G38\_Down]\}
{[G38\_Down]} -> {[G94\_UP]}
{[G52\_Down]} -> {[G28\_Down]}
\{[G28\_Down]\} -> \{[G52\_Down]\}
\{[G41\_Down]\} -> \{[G38\_Down]\}
\{[G38 Down]\} -> \{[G41 Down]\}
\{[G59\_UP]\} -> \{[G38\_Down]\}
{[G38\_Down]} -> {[G59\_UP]}
\{[G28 Down]\} -> \{[G10 Down]\}
{[G10\_Down]} -> {[G28\_Down]}
{[G6\_UP]}->{[G38\_Down]}
{[G38\_Down]} -> {[G6\_UP]}
{[G88\_Down]} -> {[G41\_Down]}
{[G41\_Down]} -> {[G88\_Down]}
{[G6\_UP]}->{[G28\_Down]}
\{[G28\_Down]\} -> \{[G6\_UP]\}
{[G96\_Down]} -> {[G59\_UP]}
{[G59_UP]}->{[G96_Down]}
{[G97\_Down]} -> {[G72\_UP]}
\{[G72\_UP]\} -> \{[G97\_Down]\}
\{[G67\_UP]\} -> \{[G1\_UP]\}
{[G1_UP]}->{[G67_UP]}
\{[G32\_Down]\} -> \{[G28\_Down]\}
{[G28\_Down]} -> {[G32\_Down]}
{[G38\_Down]}->{[G2\_Down]}
\{[G2\_Down]\} -> \{[G38\_Down]\}
{[G47 UP]}->{[G28 Down]}
\{[G28\_Down]\} -> \{[G47\_UP]\}
\{[G88\_Down]\} -> \{[G38\_Down]\}
{[G38\_Down]} -> {[G88\_Down]}
\{[G94\_UP]\} -> \{[G10\_Down]\}
\{[G10\_Down]\} -> \{[G94\_UP]\}
{[G41\_Down]} -> {[G28\_Down]}
\{[G28\_Down]\} -> \{[G41\_Down]\}
{[G6_UP]}->{[G59_UP]}
{[G59\_UP]}->{[G6\_UP]}
\{[G67\_UP]\} -> \{[G38\_Down]\}
{[G38\_Down]} -> {[G67\_UP]}
{[G72 UP]}->{[G1 UP]}
\{[G1\_UP]\} -> \{[G72\_UP]\}
{[G72\_UP]}->{[G13\_Down]}
{[G13\_Down]} -> {[G72\_UP]}
\{[G59\_UP]\} -> \{[G13\_Down]\}
{[G13\_Down]} -> {[G59\_UP]}
{[G72\_UP]}->{[G38\_Down]}
{[G38\_Down]} -> {[G72\_UP]}
{[G38\_Down]} -> {[G10\_Down]}
{[G10\_Down]} -> {[G38\_Down]}
{[G82\_Down]}->{[G72\_UP]}
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{[G72_UP]}->{[G82_Down]}
{[G88_Down]}->{[G54_UP]}
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{[G54_UP]}->{[G88_Down]}

{[G2_Down]}->{[G28_Down]}

{[G28_Down]}->{[G2_Down]}

{[G59_UP]}->{[G32_Down]}

{[G32_Down]}->{[G59_UP]}

 ${[G6_UP]} -> {[G32_Down]}$

 ${[G32_Down]}->{[G6_UP]}$

 ${[G88_Down]} -> {[G28_Down]}$

 ${[G28_Down]} -> {[G88_Down]}$

 $\{[G82_Down]\} -> \{[G59_UP]\}$

 ${[G59_UP]} \rightarrow {[G82_Down]}$

 ${[G59_UP]}->{[G10_Down]}$

 ${[G10_Down]} -> {[G59_UP]}$

 ${[G88_Down]} -> {[G10_Down]}$

 ${[G10_Down]}->{[G88_Down]}$

 ${[G54_UP]}->{[G1_UP]}$

 ${[G1_UP]} \rightarrow {[G54_UP]}$

 ${[G87_UP]} \rightarrow {[G28_Down]}$

 ${[G28_Down]} \rightarrow {[G87_UP]}$

 ${[G8_UP]}->{[G88_Down]}$

 ${[G88_Down]}->{[G8_UP]}$

 ${[G96_Down]} -> {[G72_UP]}$

{[G72_UP]}->{[G96_Down]}

 $\{[G47_UP]\} - \{[G38_Down]\}$

{[G38_Down]}->{[G47_UP]}

{[G52_Down]}->{[G38_Down]}

{[G38_Down]}->{[G52_Down]}

{[G88_Down]}->{[G87_UP]}

 ${[G87_UP]}->{[G88_Down]}$

{[G72_UP]}->{[G59_UP]}

{[G59_UP]}->{[G72_UP]}

 ${[G54_UP]} \rightarrow {[G24_Down]}$

 ${[G24_Down]} -> {[G54_UP]}$

{[G70_Down]}->{[G1_UP]}

{[G1_UP]}->{[G70_Down]}

 ${[G91_UP]}->{[G38_Down]}$

{[G38_Down]}->{[G91_UP]}

 ${[G65_Down]} -> {[G38_Down]}$

 ${[G38_Down]} -> {[G65_Down]}$

 $\{[G70_Down]\} -> \{[G38_Down]\}$

 ${[G38_Down]}->{[G70_Down]}$

{[G88_Down]}->{[G59_UP]} {[G59_UP]}->{[G88_Down]}

 ${[G82_Down]}->{[G13_Down]}$

 ${[G13_Down]} -> {[G82_Down]}$

 $\{[G96_Down]\} -> \{[G82_Down]\}$

 ${[G82_Down]}->{[G96_Down]}$

{[G87_UP]}->{[G59_UP]}

{[G59_UP]}->{[G87_UP]}

 ${[G59_UP]}->{[G1_UP]}$

{[G1_UP]}->{[G59_UP]}

 ${[G70_Down]} -> {[G10_Down]}$

{[G10_Down]}->{[G70_Down]}

 ${[G47_UP]}->{[G10_Down]}$

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{[G10\_Down]} \rightarrow {[G47\_UP]}
{[G38 Down]}->{[G28 Down]}
{[G28\_Down]}->{[G38\_Down]}
{[G38\_Down]} -> {[G1\_UP]}
{[G1 UP]}->{[G38 Down]}
{[G28\_Down]} -> {[G13\_Down]}
\{[G13\_Down]\} -> \{[G28\_Down]\}
\{[G59\_UP]\} -> \{[G28\_Down]\}
{[G28\_Down]} -> {[G59\_UP]}
{[G1\_UP]}->{[G10\_Down]}
{[G10\_Down]} -> {[G1\_UP]}
{[G6\_UP]}->{[G13\_Down]}
{[G13 Down]}->{[G6 UP]}
{[G38\_Down]} -> {[G32\_Down]}
{[G32\_Down]} -> {[G38\_Down]}
{[G72 UP, G82 Down]}->{[G59 UP]}
{[G59_UP, G82_Down]}->{[G72_UP]}
{[G59_UP, G72_UP]}->{[G82_Down]}
{[G82 Down]}->{[G59 UP, G72 UP]}
{[G59_UP]}->{[G72_UP, G82_Down]}
{[G72_UP]}->{[G59_UP, G82_Down]}
{[G72 UP, G96 Down]}->{[G59 UP]}
{[G59_UP, G96_Down]}->{[G72_UP]}
{[G59_UP, G72_UP]}->{[G96_Down]}
{[G96 Down]}->{[G59 UP, G72 UP]}
{[G59_UP]}->{[G72_UP, G96_Down]}
{[G72_UP]}->{[G59_UP, G96_Down]}
number of length-3 frequent itemset: 2
Total:174
Total number of rules generated: 138
Number of rules generated from query(RULE HAS ANY OF G6_UP): 10
{[G6\_UP]}->{[G38\_Down]}
{[G38\_Down]} -> {[G6\_UP]}
{[G6\_UP]}->{[G28\_Down]}
\{[G28\_Down]\} -> \{[G6\_UP]\}
{[G6_UP]}->{[G59_UP]}
{[G59_UP]}->{[G6_UP]}
{[G6\_UP]}->{[G32\_Down]}
\{[G32\_Down]\} -> \{[G6\_UP]\}
{[G6\_UP]}->{[G13\_Down]}
{[G13\_Down]} -> {[G6\_UP]}
Number of rules generated from query(RULE HAS 1 OF G1_UP): 14
{[G67_UP]}->{[G1_UP]}
{[G1_UP]}->{[G67_UP]}
{[G72_UP]}->{[G1_UP]}
{[G1 UP]}->{[G72 UP]}
{[G54_UP]}->{[G1_UP]}
{[G1_UP]}->{[G54_UP]}
{[G70\_Down]} -> {[G1\_UP]}
\{[G1\_UP]\} -> \{[G70\_Down]\}
{[G59_UP]}->{[G1_UP]}
{[G1_UP]}->{[G59_UP]}
{[G38\_Down]} -> {[G1\_UP]}
{[G1\_UP]}->{[G38\_Down]}
{[G1\_UP]}->{[G10\_Down]}
{[G10\_Down]} -> {[G1\_UP]}
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Number of rules generated from query(RULE HAS 1 OF (G1_UP, G10_DOWN)): 26
\{[G28 Down]\} - \{[G10 Down]\}
{[G10\_Down]} -> {[G28\_Down]}
{[G67 UP]}->{[G1 UP]}
{[G1 UP]}->{[G67 UP]}
\{[G94\_UP]\} -> \{[G10\_Down]\}
{[G10\_Down]} -> {[G94\_UP]}
{[G72_UP]}->{[G1_UP]}
{[G1\_UP]}->{[G72\_UP]}
{[G38\_Down]} -> {[G10\_Down]}
\{[G10\_Down]\} -> \{[G38\_Down]\}
{[G59\_UP]} \rightarrow {[G10\_Down]}
{[G10 Down]}->{[G59 UP]}
{[G88\_Down]} -> {[G10\_Down]}
{[G10\_Down]} -> {[G88\_Down]}
{[G54 UP]}->{[G1 UP]}
{[G1_UP]}->{[G54_UP]}
{[G70\_Down]}->{[G1\_UP]}
{[G1\_UP]}->{[G70\_Down]}
{[G59_UP]}->{[G1_UP]}
{[G1_UP]}->{[G59_UP]}
\{[G70 Down]\} -> \{[G10 Down]\}
{[G10\_Down]} -> {[G70\_Down]}
\{[G47\_UP]\} -> \{[G10\_Down]\}
\{[G10 Down]\} -> \{[G47 UP]\}
{[G38\_Down]} -> {[G1\_UP]}
\{[G1\_UP]\} -> \{[G38\_Down]\}
Number of rules generated from query(BODY HAS ANY OF G6 UP): 5
{[G6\_UP]}->{[G38\_Down]}
{[G6\_UP]}->{[G28\_Down]}
{[G6_UP]}->{[G59_UP]}
{[G6\_UP]}->{[G32\_Down]}
{[G6\_UP]}->{[G13\_Down]}
Number of rules generated from query(BODY HAS NONE OF G72_UP): 124
{[G32 Down]}->{[G72 UP]}
{[G97 Down]}->{[G82 Down]}
\{[G82\_Down]\} -> \{[G97\_Down]\}
\{[G88\_Down]\} -> \{[G24\_Down]\}
\{[G24 Down]\} - \{[G88 Down]\}
{[G94\_UP]}->{[G38\_Down]}
\{[G38\_Down]\} -> \{[G94\_UP]\}
\{[G52\_Down]\} -> \{[G28\_Down]\}
{[G28\_Down]} -> {[G52\_Down]}
\{[G41\_Down]\} -> \{[G38\_Down]\}
{[G38\_Down]} -> {[G41\_Down]}
{[G59 UP]}->{[G38 Down]}
{[G38 Down]}->{[G59 UP]}
\{[G28 Down]\} -> \{[G10 Down]\}
{[G10\_Down]} -> {[G28\_Down]}
{[G6 UP]}->{[G38 Down]}
{[G38\_Down]} -> {[G6\_UP]}
{[G88\_Down]} -> {[G41\_Down]}
\{[G41\_Down]\} -> \{[G88\_Down]\}
{[G6\_UP]}->{[G28\_Down]}
{[G28\_Down]}->{[G6\_UP]}
\{[G96\_Down]\} -> \{[G59\_UP]\}
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{[G59_UP]}->{[G96_Down]}
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- $\{[G97_Down]\} -> \{[G72_UP]\}$
- {[G67_UP]}->{[G1_UP]}
- {[G1_UP]}->{[G67_UP]}
- $\{[G32_Down]\} -> \{[G28_Down]\}$
- ${[G28_Down]} -> {[G32_Down]}$
- ${[G38_Down]} -> {[G2_Down]}$
- ${[G2_Down]} -> {[G38_Down]}$
- ${[G47_UP]}->{[G28_Down]}$
- $\{[G28_Down]\} -> \{[G47_UP]\}$
- ${[G88_Down]} -> {[G38_Down]}$
- ${[G38_Down]} -> {[G88_Down]}$
- {[G94 UP]}->{[G10 Down]}
- ${[G10_Down]} -> {[G94_UP]}$
- ${[G41_Down]} -> {[G28_Down]}$
- $\{[G28_Down]\} -> \{[G41_Down]\}$
- ${[G6_UP]}->{[G59_UP]}$
- {[G59_UP]}->{[G6_UP]}
- ${[G67_UP]}->{[G38_Down]}$
- ${[G38_Down]} -> {[G67_UP]}$
- ${[G1_UP]} \rightarrow {[G72_UP]}$
- ${[G13_Down]} -> {[G72_UP]}$
- ${[G59_UP]} \rightarrow {[G13_Down]}$
- $\{[G13_Down]\} -> \{[G59_UP]\}$
- ${[G38_Down]}->{[G72_UP]}$
- ${[G38_Down]} -> {[G10_Down]}$
- $\{[G10_Down]\} -> \{[G38_Down]\}$
- ${[G82_Down]}->{[G72_UP]}$
- ${[G88_Down]} -> {[G54_UP]}$
- ${[G54_UP]} \rightarrow {[G88_Down]}$
- ${[G2_Down]} -> {[G28_Down]}$
- ${[G28_Down]} -> {[G2_Down]}$
- ${[G59_UP]} \rightarrow {[G32_Down]}$
- ${[G32_Down]} -> {[G59_UP]}$
- ${[G6_UP]}->{[G32_Down]}$
- ${[G32_Down]} -> {[G6_UP]}$
- ${[G88_Down]} -> {[G28_Down]}$
- $\{[G28_Down]\} -> \{[G88_Down]\}$
- $\{[G82_Down]\} -> \{[G59_UP]\}$
- ${[G59_UP]}->{[G82_Down]}$
- $\{[G59_UP]\} -> \{[G10_Down]\}$
- ${[G10_Down]}->{[G59_UP]}$
- ${[G88_Down]} -> {[G10_Down]}$
- ${[G10_Down]} -> {[G88_Down]}$
- ${[G54_UP]}->{[G1_UP]}$
- ${[G1_UP]} \rightarrow {[G54_UP]}$
- $\{[G87_UP]\} -> \{[G28_Down]\}$
- $\{[G28_Down]\} -> \{[G87_UP]\}$
- $\{[G8_UP]\} -> \{[G88_Down]\}$
- $\{[G88_Down]\} -> \{[G8_UP]\}$
- {[G96_Down]}->{[G72_UP]}
- ${[G47_UP]}->{[G38_Down]}$
- ${[G38_Down]} -> {[G47_UP]}$
- ${[G52_Down]}->{[G38_Down]}$ $\{[G38_Down]\} -> \{[G52_Down]\}$
- ${[G88_Down]} -> {[G87_UP]}$

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{[G87\_UP]} \rightarrow {[G88\_Down]}
{[G59_UP]}->{[G72_UP]}
{[G54\_UP]} \rightarrow {[G24\_Down]}
\{[G24\_Down]\} -> \{[G54\_UP]\}
\{[G70\_Down]\} -> \{[G1\_UP]\}
{[G1\_UP]}->{[G70\_Down]}
{[G91\_UP]} \rightarrow {[G38\_Down]}
{[G38\_Down]} -> {[G91\_UP]}
{[G65\_Down]}->{[G38\_Down]}
{[G38\_Down]} -> {[G65\_Down]}
\{[G70\_Down]\} -> \{[G38\_Down]\}
{[G38\_Down]} -> {[G70\_Down]}
{[G88 Down]}->{[G59 UP]}
{[G59_UP]}->{[G88_Down]}
{[G82\_Down]} -> {[G13\_Down]}
\{[G13\_Down]\} -> \{[G82\_Down]\}
{[G96\_Down]} -> {[G82\_Down]}
{[G82\_Down]} -> {[G96\_Down]}
{[G87_UP]}->{[G59_UP]}
{[G59_UP]}->{[G87_UP]}
{[G59\_UP]} \rightarrow {[G1\_UP]}
{[G1_UP]}->{[G59_UP]}
\{[G70\_Down]\} -> \{[G10\_Down]\}
{[G10\_Down]} -> {[G70\_Down]}
{[G47\_UP]}->{[G10\_Down]}
{[G10\_Down]}->{[G47\_UP]}
\{[G38\_Down]\} -> \{[G28\_Down]\}
{[G28\_Down]} -> {[G38\_Down]}
{[G38\_Down]} -> {[G1\_UP]}
{[G1\_UP]}->{[G38\_Down]}
{[G28\_Down]} -> {[G13\_Down]}
{[G13\_Down]} -> {[G28\_Down]}
{[G59\_UP]} -> {[G28\_Down]}
{[G28\_Down]} -> {[G59\_UP]}
{[G1\_UP]}->{[G10\_Down]}
\{[G10\_Down]\} -> \{[G1\_UP]\}
{[G6\_UP]}->{[G13\_Down]}
\{[G13\_Down]\} -> \{[G6\_UP]\}
{[G38\_Down]} -> {[G32\_Down]}
{[G32\_Down]} -> {[G38\_Down]}
{[G59_UP, G82_Down]}->{[G72_UP]}
{[G82_Down]}->{[G59_UP, G72_UP]}
{[G59\_UP]}->{[G72\_UP, G82\_Down]}
{[G59_UP, G96_Down]}->{[G72_UP]}
{[G96_Down]}->{[G59_UP, G72_UP]}
{[G59_UP]}->{[G72_UP, G96_Down]}
Number of rules generated from query(RULE HAS 1 OF (G1_UP, G10_DOWN)): 15
{[G10\_Down]} -> {[G28\_Down]}
{[G1\_UP]} \rightarrow {[G67\_UP]}
\{[G10\_Down]\} -> \{[G94\_UP]\}
{[G1\_UP]} \rightarrow {[G72\_UP]}
{[G10\_Down]} -> {[G38\_Down]}
{[G10\_Down]} -> {[G59\_UP]}
{[G10\_Down]} -> {[G88\_Down]}
{[G1\_UP]} -> {[G54\_UP]}
{[G1\_UP]}->{[G70\_Down]}
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{[G1_UP]}->{[G59_UP]}
\{[G10 Down]\} -> \{[G70 Down]\}
{[G10\_Down]} -> {[G47\_UP]}
{[G1\_UP]}->{[G38\_Down]}
\{[G1\_UP]\} -> \{[G10\_Down]\}
{[G10\_Down]} -> {[G1\_UP]}
Number of rules generated from query(HEAD HAS ANY OF G6_UP): 5
{[G38\_Down]} -> {[G6\_UP]}
{[G28\_Down]}->{[G6\_UP]}
{[G59_UP]}->{[G6_UP]}
{[G32\_Down]} -> {[G6\_UP]}
{[G13\_Down]} -> {[G6\_UP]}
Number of rules generated from query(HEAD HAS NONE OF G1 UP,G6 UP): 126
{[G72\_UP]}->{[G32\_Down]}
{[G32\_Down]} -> {[G72\_UP]}
\{[G97 Down]\} - \{[G82 Down]\}
{[G82\_Down]} -> {[G97\_Down]}
{[G88\_Down]} -> {[G24\_Down]}
\{[G24\_Down]\} -> \{[G88\_Down]\}
{[G94\_UP]}->{[G38\_Down]}
{[G38\_Down]} -> {[G94\_UP]}
{[G52\_Down]} -> {[G28\_Down]}
\{[G28\_Down]\} -> \{[G52\_Down]\}
\{[G41\_Down]\} -> \{[G38\_Down]\}
{[G38\_Down]} -> {[G41\_Down]}
{[G59\_UP]} \rightarrow {[G38\_Down]}
\{[G38\_Down]\} -> \{[G59\_UP]\}
\{[G28\_Down]\} -> \{[G10\_Down]\}
{[G10\_Down]} \rightarrow {[G28\_Down]}
{[G6\_UP]}->{[G38\_Down]}
{[G88\_Down]} -> {[G41\_Down]}
{[G41\_Down]} -> {[G88\_Down]}
{[G6\_UP]}->{[G28\_Down]}
{[G96\_Down]} -> {[G59\_UP]}
{[G59_UP]}->{[G96_Down]}
\{[G97\_Down]\} -> \{[G72\_UP]\}
\{[G72\_UP]\} -> \{[G97\_Down]\}
{[G1_UP]}->{[G67_UP]}
\{[G32\_Down]\} -> \{[G28\_Down]\}
{[G28\_Down]} -> {[G32\_Down]}
\{[G38\_Down]\} -> \{[G2\_Down]\}
{[G2\_Down]} -> {[G38\_Down]}
{[G47\_UP]} \rightarrow {[G28\_Down]}
\{[G28\_Down]\} -> \{[G47\_UP]\}
{[G88\_Down]} -> {[G38\_Down]}
{[G38\_Down]} -> {[G88\_Down]}
\{[G94\_UP]\} -> \{[G10\_Down]\}
{[G10\_Down]} -> {[G94\_UP]}
{[G41\_Down]} -> {[G28\_Down]}
\{[G28\_Down]\} -> \{[G41\_Down]\}
{[G6\_UP]} \rightarrow {[G59\_UP]}
{[G67\_UP]}->{[G38\_Down]}
{[G38\_Down]} -> {[G67\_UP]}
{[G1\_UP]} \rightarrow {[G72\_UP]}
{[G72\_UP]}->{[G13\_Down]}
{[G13\_Down]} -> {[G72\_UP]}
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{[G59_UP]}->{[G13_Down]}
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- ${[G13_Down]} -> {[G59_UP]}$
- ${[G72_UP]}->{[G38_Down]}$
- ${[G38_Down]} \rightarrow {[G72_UP]}$
- ${[G38_Down]} \rightarrow {[G10_Down]}$
- ${[G10_Down]} -> {[G38_Down]}$
- ${[G82_Down]} -> {[G72_UP]}$
- ${[G72_UP]} \rightarrow {[G82_Down]}$
- ${[G88_Down]} -> {[G54_UP]}$
- ${[G54_UP]} \rightarrow {[G88_Down]}$
- ${[G2_Down]}->{[G28_Down]}$
- {[G28_Down]}->{[G2_Down]}
- ${[G59_UP]} \rightarrow {[G32_Down]}$
- ${[G32_Down]} -> {[G59_UP]}$
- ${[G6_UP]}->{[G32_Down]}$
- ${[G88_Down]} -> {[G28_Down]}$
- ${[G28_Down]} -> {[G88_Down]}$
- ${[G82_Down]} -> {[G59_UP]}$
- ${[G59_UP]} \rightarrow {[G82_Down]}$
- ${[G59_UP]}->{[G10_Down]}$
- ${[G10_Down]} -> {[G59_UP]}$
- ${[G88_Down]} -> {[G10_Down]}$
- {[G10_Down]}->{[G88_Down]}
- {[G1_UP]}->{[G54_UP]}
- ${[G87_UP]} \rightarrow {[G28_Down]}$
- ${[G28_Down]}->{[G87_UP]}$
- ${[G8_UP]}->{[G88_Down]}$
- {[G88_Down]}->{[G8_UP]}
- ${[G96_Down]} -> {[G72_UP]}$
- {[G72_UP]}->{[G96_Down]}
- ${[G47_UP]}->{[G38_Down]}$
- ${[G38_Down]} -> {[G47_UP]}$
- ${[G52_Down]} -> {[G38_Down]}$
- ${[G38_Down]} -> {[G52_Down]}$
- ${[G88_Down]} -> {[G87_UP]}$
- ${[G87_UP]} \rightarrow {[G88_Down]}$
- {[G72_UP]}->{[G59_UP]}
- ${[G59_UP]} \rightarrow {[G72_UP]}$
- ${[G54_UP]} \rightarrow {[G24_Down]}$
- ${[G24_Down]} -> {[G54_UP]}$
- {[G1_UP]}->{[G70_Down]}
- {[G91_UP]}->{[G38_Down]}
- {[G38_Down]}->{[G91_UP]}
- {[G65_Down]}->{[G38_Down]}
- ${[G38_Down]} -> {[G65_Down]}$
- {[G70_Down]}->{[G38_Down]}
- {[G38_Down]}->{[G70_Down]}
- $\{[G88_Down]\} -> \{[G59_UP]\}$
- ${[G59_UP]}->{[G88_Down]}$
- ${[G82_Down]}->{[G13_Down]}$
- {[G13_Down]}->{[G82_Down]}
- ${[G96_Down]} -> {[G82_Down]}$
- ${[G82_Down]} -> {[G96_Down]}$
- {[G87_UP]}->{[G59_UP]}
- {[G59_UP]}->{[G87_UP]}
- ${[G1_UP]}->{[G59_UP]}$

```
\{[G70\_Down]\} -> \{[G10\_Down]\}
\{[G10 Down]\} -> \{[G70 Down]\}
\{[G47\_UP]\} -> \{[G10\_Down]\}
\{[G10\_Down]\} -> \{[G47\_UP]\}
\{[G38\_Down]\} -> \{[G28\_Down]\}
\{[G28\_Down]\} -> \{[G38\_Down]\}
{[G1\_UP]}->{[G38\_Down]}
{[G28\_Down]} -> {[G13\_Down]}
{[G13\_Down]} -> {[G28\_Down]}
{[G59\_UP]} \rightarrow {[G28\_Down]}
\{[G28\_Down]\} -> \{[G59\_UP]\}
{[G1\_UP]}->{[G10\_Down]}
{[G6 UP]}->{[G13 Down]}
{[G38\_Down]} -> {[G32\_Down]}
{[G32\_Down]} -> {[G38\_Down]}
{[G72 UP, G82 Down]}->{[G59 UP]}
{[G59_UP, G82_Down]}->{[G72_UP]}
{[G59_UP, G72_UP]}->{[G82_Down]}
{[G82 Down]}->{[G59 UP, G72 UP]}
{[G59\_UP]}->{[G72\_UP, G82\_Down]}
{[G72_UP]}->{[G59_UP, G82_Down]}
{[G72_UP, G96_Down]}->{[G59_UP]}
{[G59_UP, G96_Down]}->{[G72_UP]}
{[G59_UP, G72_UP]}->{[G96_Down]}
{[G96 Down]}->{[G59 UP, G72 UP]}
{[G59_UP]}->{[G72_UP, G96_Down]}
{[G72_UP]}->{[G59_UP, G96_Down]}
Number of rules generated from query(HEAD HAS 1 OF G6_UP,G8_UP): 6
{[G38\_Down]} -> {[G6\_UP]}
{[G28_Down]}->{[G6_UP]}
{[G59\_UP]}->{[G6\_UP]}
{[G32\_Down]}->{[G6\_UP]}
{[G88\_Down]} -> {[G8\_UP]}
{[G13\_Down]}->{[G6\_UP]}
Number of rules generated from query(RULE HAS 1 OF G1_UP, G6_UP, G72_UP): 48
\{[G72\_UP]\} -> \{[G32\_Down]\}
{[G32\_Down]} -> {[G72\_UP]}
\{[G6\_UP]\} - \{[G38\_Down]\}
\{[G38\_Down]\} -> \{[G6\_UP]\}
{[G6\_UP]}->{[G28\_Down]}
{[G28_Down]}->{[G6_UP]}
{[G97\_Down]} -> {[G72\_UP]}
{[G72\_UP]}->{[G97\_Down]}
{[G67_UP]}->{[G1_UP]}
{[G1\_UP]}->{[G67\_UP]}
{[G6 UP]}->{[G59 UP]}
{[G59 UP]}->{[G6 UP]}
{[G72\_UP]}->{[G13\_Down]}
{[G13\_Down]} -> {[G72\_UP]}
\{[G72\_UP]\} -> \{[G38\_Down]\}
{[G38\_Down]} -> {[G72\_UP]}
{[G82\_Down]} -> {[G72\_UP]}
{[G72\_UP]} \rightarrow {[G82\_Down]}
{[G6\_UP]}->{[G32\_Down]}
{[G32_Down]}->{[G6_UP]}
{[G54\_UP]}->{[G1\_UP]}
```

```
{[G1_UP]}->{[G54_UP]}
{[G96 Down]}->{[G72 UP]}
{[G72\_UP]}->{[G96\_Down]}
{[G72_UP]}->{[G59_UP]}
{[G59_UP]}->{[G72_UP]}
{[G70\_Down]} -> {[G1\_UP]}
{[G1\_UP]}->{[G70\_Down]}
{[G59_UP]}->{[G1_UP]}
{[G1_UP]}->{[G59_UP]}
{[G38\_Down]} -> {[G1\_UP]}
{[G1\_UP]}->{[G38\_Down]}
{[G1\_UP]}->{[G10\_Down]}
\{[G10 Down]\} -> \{[G1 UP]\}
{[G6\_UP]}->{[G13\_Down]}
{[G13\_Down]} -> {[G6\_UP]}
{[G72 UP, G82 Down]}->{[G59 UP]}
{[G59\_UP, G82\_Down]}->{[G72\_UP]}
{[G59_UP, G72_UP]}->{[G82_Down]}
{[G82\_Down]} \rightarrow {[G59\_UP, G72\_UP]}
{[G59\_UP]}->{[G72\_UP, G82\_Down]}
{[G72_UP]}->{[G59_UP, G82_Down]}
{[G72_UP, G96_Down]}->{[G59_UP]}
{[G59_UP, G96_Down]}->{[G72_UP]}
{[G59_UP, G72_UP]}->{[G96_Down]}
{[G96 Down]}->{[G59 UP, G72 UP]}
{[G59_UP]}->{[G72_UP, G96_Down]}
{[G72_UP]}->{[G59_UP, G96_Down]}
Number of rules generated from query(RULE HAS ANY OF G1_UP, G6_UP, G72_UP) : 50
{[G72\_UP]} \rightarrow {[G32\_Down]}
\{[G32\_Down]\} -> \{[G72\_UP]\}
{[G6\_UP]}->{[G38\_Down]}
{[G38\_Down]} -> {[G6\_UP]}
{[G6\_UP]}->{[G28\_Down]}
{[G28\_Down]}->{[G6\_UP]}
{[G97\_Down]} -> {[G72\_UP]}
{[G72\_UP]}->{[G97\_Down]}
{[G67_UP]}->{[G1_UP]}
{[G1_UP]}->{[G67_UP]}
{[G6_UP]}->{[G59_UP]}
{[G59_UP]}->{[G6_UP]}
{[G72_UP]}->{[G1_UP]}
{[G1\_UP]}->{[G72\_UP]}
{[G72\_UP]} \rightarrow {[G13\_Down]}
\{[G13\_Down]\} -> \{[G72\_UP]\}
{[G72\_UP]}->{[G38\_Down]}
{[G38\_Down]} -> {[G72\_UP]}
\{[G82\_Down]\} -> \{[G72\_UP]\}
{[G72\_UP]}->{[G82\_Down]}
{[G6\_UP]}->{[G32\_Down]}
\{[G32\_Down]\} -> \{[G6\_UP]\}
{[G54\_UP]}->{[G1\_UP]}
{[G1\_UP]} -> {[G54\_UP]}
{[G96\_Down]} -> {[G72\_UP]}
{[G72\_UP]}->{[G96\_Down]}
{[G72_UP]}->{[G59_UP]}
{[G59_UP]}->{[G72_UP]}
```

```
{[G70\_Down]}->{[G1\_UP]}
{[G1 UP]}->{[G70 Down]}
{[G59_UP]}->{[G1_UP]}
{[G1 UP]}->{[G59 UP]}
{[G38 Down]}->{[G1 UP]}
\{[G1\_UP]\} -> \{[G38\_Down]\}
{[G1\_UP]}->{[G10\_Down]}
\{[G10 Down]\} -> \{[G1 UP]\}
{[G6\_UP]}->{[G13\_Down]}
{[G13\_Down]} -> {[G6\_UP]}
{[G72_UP, G82_Down]}->{[G59_UP]}
{[G59_UP, G82_Down]}->{[G72_UP]}
{[G59 UP, G72 UP]}->{[G82 Down]}
{[G82 Down]}->{[G59 UP, G72 UP]}
{[G59_UP]}->{[G72_UP, G82_Down]}
{[G72 UP]}->{[G59 UP, G82 Down]}
{[G72 UP, G96 Down]}->{[G59 UP]}
{[G59_UP, G96_Down]}->{[G72_UP]}
{[G59 UP, G72 UP]}->{[G96 Down]}
{[G96_Down]}->{[G59_UP, G72_UP]}
{[G59_UP]}->{[G72_UP, G96_Down]}
{[G72 UP]}->{[G59 UP, G96 Down]}
Number of rules generated from query(SIZE OF RULE>=3): 12
{[G72_UP, G82_Down]}->{[G59_UP]}
{[G59 UP, G82 Down]}->{[G72 UP]}
{[G59_UP, G72_UP]}->{[G82_Down]}
{[G82_Down]}->{[G59_UP, G72_UP]}
{[G59 UP]}->{[G72 UP, G82 Down]}
{[G72_UP]}->{[G59_UP, G82_Down]}
{[G72_UP, G96_Down]}->{[G59_UP]}
{[G59_UP, G96_Down]}->{[G72_UP]}
{[G59_UP, G72_UP]}->{[G96_Down]}
{[G96_Down]}->{[G59_UP, G72_UP]}
{[G59_UP]}->{[G72_UP, G96_Down]}
{[G72 UP]}->{[G59 UP, G96 Down]}
Number of rules generated from query(SIZE OF BODY>=2): 6
{[G72 UP, G82 Down]}->{[G59 UP]}
{[G59_UP, G82_Down]}->{[G72_UP]}
{[G59 UP, G72 UP]}->{[G82 Down]}
{[G82_Down]}->{[G59_UP, G72_UP]}
{[G59_UP]}->{[G72_UP, G82_Down]}
{[G72_UP]}->{[G59_UP, G82_Down]}
{[G72_UP, G96_Down]}->{[G59_UP]}
{[G59_UP, G96_Down]}->{[G72_UP]}
{[G59_UP, G72_UP]}->{[G96_Down]}
{[G96 Down]}->{[G59 UP, G72 UP]}
{[G59 UP]}->{[G72 UP, G96 Down]}
{[G72 UP]}->{[G59 UP, G96 Down]}
Number of rules generated from query(SIZE OF HEAD>=2): 6
{[G82 Down]}->{[G59 UP, G72 UP]}
{[G59_UP]}->{[G72_UP, G82_Down]}
{[G72_UP]}->{[G59_UP, G82_Down]}
{[G96_Down]}->{[G59_UP, G72_UP]}
{[G59_UP]}->{[G72_UP, G96_Down]}
{[G72_UP]}->{[G59_UP, G96_Down]}
Number of rules generated from query(BODY HAS ANY OF G1_UP AND HEAD HAS 1 OF G59_UP): 1
```

Number of rules generated from query(BODY HAS 1 of (G59_UP, G96_DOWN) AND SIZE OF RULE >= 3): 7