

Capacitance transducer types, applications and characteristics

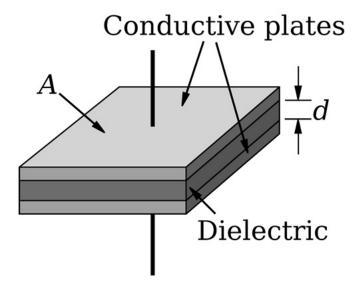
transducer, capacitance

divyasree Oct '18

Capacitance transducers are passive transducers that work on the principle of change of capacitance. Here we will discuss the principle, types, applications and advantages of the capacitance transducers.

Design of a basic capacitance transducer

A capacitor consists of two parallel conducting plates of area A placed at a distance d from each other with any material (insulator) between them. The dielectric constant ϵ is unique for different medium



Principle of a basic capacitance transducer

Capacitance is defined as the function of the geometric quantities, such as the area of the conducting plate and the distance between them, and the permittivity of the dielectric medium between them.

$$C = \frac{\varepsilon A}{d}$$

Where

 ϵ is the dielectric constant, permittivity, of the dielectric medium.

A is the area of the electrode, more specifically overlapping area.

d is the distance between the two parallel electrodes

Capacitance can change with change in any one of the above parameters.

For a capacitor with an insulating material separating the conducting plates, the capacitance is given as

$$C = \frac{\varepsilon_r \varepsilon_0 A}{d}$$

Where, ε_r is the dielectric constant of insulating medium. For air $\,\varepsilon_r\,$ =1

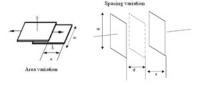
 ε_0 is the permittivity of air or free space (8.85 X 10-12F/m)

In a capacitance transducer, the change in the overlapping area and the distance between the plates is attributed to the movement due to external force, typically used to sense displacement, pressure, force. The change in dielectric medium is often attributed to the displacement of the original medium which is often used in level measurement for fluids.

Depending on the design of the capacitor there is change in the sensitivity which plays a major role in the application .

Types of capacitance transducers

** 1. Parallel plate capacitance with Rectangular plates**



Here one of the plates is fixed while the other is movable, depending on the nature of the movement, there may be variation in the area A or the distance d.

The change in capacitance is given as,

In case of **area variation**, where the capacitance plate moves a distance of x,

$$C = \frac{\varepsilon (A - wx)}{d}$$

In case of **spatial variation**, where the distance between the plates increase by a x,

$$C = \frac{\varepsilon A}{(d+x)}$$

Sensitivity of the Parallel plate capacitance transducer:

Sensitivity of the transducer is given as the change in the output to the change in input.

In this case sensitivity S is dc/dx

$$S = \frac{dC}{dx}$$

Area variation:

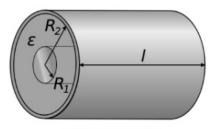
$$S = \frac{\varepsilon wx}{d}$$

Distance variation:

$$S = -\frac{\varepsilon A}{(d+x)^2}$$

2. Cylindrical capacitor transducer

A cylindrical capacitor is two concentric cylinders with a dielectric in between.



CYLINDRICAL CAPACITOR

The surface area of the cylinder of radius x meters and unit length is given as $2\pi x$

The electrical field intensity at a point x meters away from the centre of cylinder is

$$E_x = \frac{Q}{2\pi\epsilon_0\epsilon_r x}$$

The potential difference developed between the cylinders is given as

$$V = \int_{R_1}^{R_2} -E dx$$

$$V = \int_{R_1}^{R_2} \frac{-Qdx}{2\pi\epsilon_0\epsilon_r x}$$

$$V = \frac{-Q}{2\pi\epsilon_0\epsilon_r} \int_{R_1}^{R_2} \frac{dx}{x}$$

$$V = \frac{-Q}{2\pi\epsilon_0\epsilon_r}\log_e R_1 - \log_e R_2$$

$$V = \frac{-Q}{2\pi\epsilon_0\epsilon_r}\log_e\left(\frac{R_1}{R_2}\right)$$

$$\frac{Q}{V} = \frac{2\pi\epsilon_0\epsilon_r}{\log_e\left(\frac{R_2}{R_1}\right)}$$

In that case the capacitance is given as

$$C = \frac{2\pi\epsilon_0\epsilon_r}{\log_e\left(\frac{R_2}{R_1}\right)}F/m$$

Considering a length of the cylinders to be L,

$$C = \frac{2\pi\epsilon_0 \epsilon_r L}{\log_e \left(\frac{R_2}{R_1}\right)} F$$

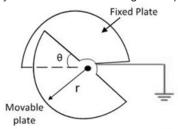
Numerically substituting D instead of R will give the same result.

Sensitivity in this case is S = dC/dL

$$S = \frac{dC}{dL} = \frac{2\pi\varepsilon}{\log_e \frac{R_2}{R_1}}$$

3. Semi circular parallel plate

Mostly used to measure the angular displacement, the capacitance is maximum when the plates completely overlap.



Area of the plate is given as

$$A = \frac{\pi r^2}{2}$$

Therefore, the capacitance is given by

$$C = \frac{\varepsilon \pi r^2}{2d}$$

In case of an angular displacement of $\boldsymbol{\theta}$

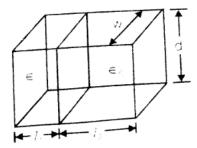
$$C = \frac{\varepsilon \theta r^2}{2d}$$

180 degree is the maximum displacement of the capacitor.

Sensitivity is given by

$$S = \frac{dC}{d\theta} = \frac{\varepsilon r^2}{2d}$$

4. Change of dielectric between parallel plates

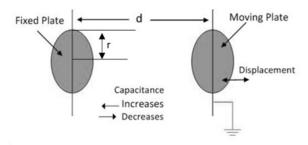


The capacitance of the parallel plate with different dielectric is given as

$$C = \frac{\varepsilon_0}{d} \left(\varepsilon_1.L_1.w + \varepsilon_2.L_2.w \right)$$

This is the principle used in liquid level measurement.

5. Change in distance between circular plates



The capacitance is given by:

$$C = \frac{\varepsilon \pi r^2}{d}$$

When the plates move a distance of x

$$C = \frac{\varepsilon \pi r^2}{d + x}$$

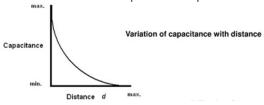
And the sensitivity is given as

$$S = -\frac{\varepsilon \pi r^2}{(d+x)^2}$$

Output characteristics of a capacitor transducer

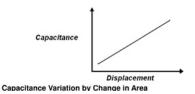
With distance between the plates d

The relation between the input d and output C are in the powers of 2 and inversely proportional. The output is not linear

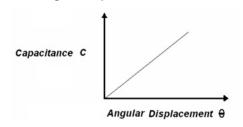


With change in area A due to displacement

The is a linear relationship between the input and output.



With Angular displacement



Advantages of Capacitive transducers

- a. Sensitive is very high
- b. High frequency response
- c. Minimum loading effect
- d. Very good resolution

Disadvantages of capacitive transducer

- a. Non linear behaviour due to edge effect
- b. Temperature sensitive
- c. Affected by stray capacitance

Capacitive transducers have the dynamic characteristics similar to high pass filter

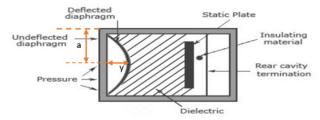
Applications of capacitive transducer

Used in pressure, displacement, force and level measurement.

Special capacitance transducers:

Variable capacitance pressure transducer

Containing a diaphragm instead of one of the fixed plates, the dielectric material is air. The flexible diaphragm is pulled taut but bends into a curve on pressure.



For any radius r, the deflection y is given as

$$y = \frac{3}{16} \frac{(1 - v^2)}{Et^3} (a^2 - r^2)^2 P$$

Where

a = radius of the diaphragm

t = Thickness of the diaphragm

E = Young's modulus

v = Poisson's ratio

The increase in capacitance is given by :

$$\frac{\Delta C}{C} = \frac{(1 - v^2)a^4}{16Edt^3}P$$

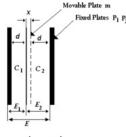
C is the capacitance at zero pressure which is

$$C = \frac{\varepsilon \pi a^2}{d}$$

This is the same principle used in capacitor microphone which converts electrical signal to sound signal.

High precision differential capacitor

This uses a three plate differential (push-pull displacement) sensor consisiting of a movable plate M in between two fixed plates P 1 and 2. X is the displacement of the movable plate, the capacitances is given by,



$$C_1 = \frac{\varepsilon A}{d}, C_2 \frac{\varepsilon A}{d}$$

The voltages across C1 and C2 is

$$E_1 = \frac{EC_2}{C_1 + C_2} = \frac{E}{2}$$

$$E_2 = \frac{EC_1}{C_1 + C_2} = \frac{E}{2}$$

At midpoint, E1 - E2 = 0

With x being the displacement

$$C_1 = \frac{\varepsilon A}{d+x}$$

$$C_2 \frac{\varepsilon A}{d-x}$$

The differential output is

$$\Delta E = E_1 - E_2 = \frac{(d+x)}{2d} E - \frac{(d-x)}{2d} E$$

$$\Delta E = \frac{x}{d}E$$

The sensitivity is given as

$$S = \frac{\Delta E}{E} = \frac{x}{d}$$

The output varies linearly and gives an accuracy of 0.05 %

- **9** What are load cells, types, classifications, calibration
- **𝚱** Micro Electro Mechanical Systems (MEMS)
- **O TYPES OF CAPACITORS AND THEIR APPLICATIONS**

ADVERTISEMENT SPONSORED SEARCHES Q Q Automation PLC Voltage Sensor Level Measurement Q Q Measure Distance Temperature Measurement Force Measurement Q Q Electrician Course **Electrical Circuit** Circuit Schematic **PLC Programming** Q Audio Microphone Q Capacitive Sensor Q Level Transducer Linear Transducer Piezo Transducer

Download PDF [Free]

To View PDF, Download Here ProPDFConverter