

# IIR Filter Design

- Design a Butterworth digital IIR lowpass filter using impulse invariant transformation by taking  $T = 1\text{second}$  to satisfy the given specifications.
- Design a Chebyshev digital IIR lowpass filter using bilinear transformation by taking  $T = 1\text{second}$ , to satisfy the given specifications

- Specification:

Gain at passband edge frequency

Gain at stopband edge frequency

Passband edge digital frequency

Stopband edge digital frequency

Sampling time

Passband attenuation in dB

Stopband attenuation in dB

## Butterworth filter

- `buttord` calculates the minimum order of a digital or analog Butterworth filter required to meet a set of filter design specifications.
- `[n,Wn] = buttord(Wp,Ws,Rp,Rs)` returns the lowest order, `n`, of the digital Butterworth filter with no more than `Rp` dB of passband ripple and at least `Rs` dB of attenuation in the stopband. The scalar (or vector) of corresponding cutoff frequencies, `Wn`, is also returned. Use the output arguments `n` and `Wn` in `butter`.
- `[b,a] = butter(n,Wn)` returns the transfer function coefficients of an `n`th-order lowpass digital Butterworth filter with normalized cutoff frequency `Wn`.

# Chebyshev Filter

- **Cheb1ord: Chebyshev Type I filter order**

`[n,Wp] = cheb1ord(Wp,Ws,Rp,Rs)` returns the lowest order `n` of the Chebyshev Type I filter that loses no more than `Rp` dB in the passband and has at least `Rs` dB of attenuation in the stopband.

The scalar (or vector) of corresponding cutoff frequencies `Wp`, is also returned.

Use the output arguments `n` and `Wp` with the [cheby1](#) function.

- **Cheby1 : Chebyshev Type I filter design**

`[b,a] = cheby1(n,Rp,Wp)` returns the transfer function coefficients of an `n`th-order lowpass digital Chebyshev Type I filter with normalized passband edge frequency `Wp` and `Rp` decibels of peak-to-peak passband ripple.

## Bilinear transformation method for analog-to-digital filter conversion

`[num ,den] = bilinear(num,den,fs)` convert an  $s$ -domain transfer function given by num and den to a discrete equivalent.

## Impulse invariance method for analog-to-digital filter conversion

`[bz,az] =impinvar(b,a,fs)` creates a digital filter with numerator and denominator coefficients bz and az, respectively, whose impulse response is equal to the impulse response of the analog filter with coefficients b and a, scaled by  $1/fs$ .

Digital Transfer Function is,

$$H_z = \text{tf}(\text{num}, \text{den}, T)$$

To get the frequency response

$H = \text{freqz}(\dots, W)$  returns the frequency response at frequencies designated in vector  $W$ , in radians/sample (normally between 0 and  $\pi$ ).

Then get magnitude response