

Chapter 2: DIFFRACTION PATTERNS AND POLARIZATION

Polarization

P 12: Plane-polarized light is incident on a single polarizing disk with the direction of \mathbf{E} parallel to the direction of the transmission axis. Through what angle should the disk be rotated so that the intensity in the transmitted beam is reduced by a factor of (a) 3.00, (b) 5.0, and (c) 10.0 ?

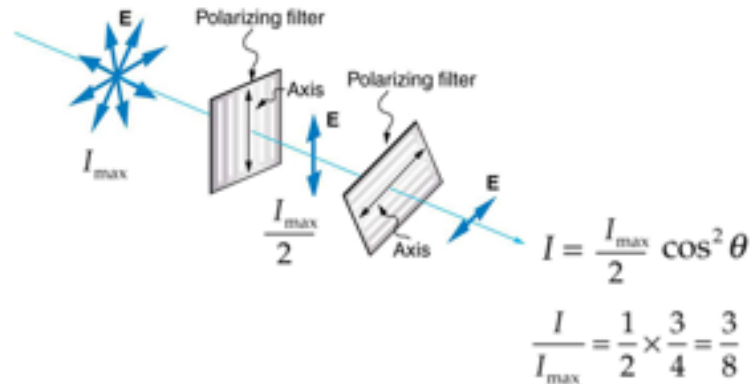
$$I = I_{\max} \cos^2 \theta \quad \text{OR} \quad \theta = \cos^{-1} \sqrt{\frac{I}{I_{\max}}}$$

$$\text{(a) For } I = I_{\max}/3.0, \quad \theta = \cos^{-1} \left(\frac{I}{I_{\max}} \right)^{1/2} = \cos^{-1} \frac{1}{\sqrt{3.00}} = \cos^{-1} 0.577 = 54.7^\circ$$

$$\text{(b) For } I = I_{\max}/5.0, \quad \theta = \cos^{-1} \left(\frac{I}{I_{\max}} \right)^{1/2} = \cos^{-1} \frac{1}{\sqrt{5.00}} = \cos^{-1} 0.447 = 63.4^\circ$$

$$\text{(c) For } I = I_{\max}/10.0, \quad \theta = \cos^{-1} \left(\frac{I}{I_{\max}} \right)^{1/2} = \cos^{-1} \frac{1}{\sqrt{10.0}} = \cos^{-1} 0.316 = 71.6^\circ$$

P 13 : Unpolarized light passes through two ideal Polaroid sheets. The axis of the first is vertical, and the axis of the second is at 30° to the vertical. What fraction of the incident light is transmitted?



Let I_{\max} be the intensity of incident unpolarised light.

The intensity of light passing through the first polarizing filter is reduced by $\frac{1}{2}$. (Transmitted light is polarized, with E parallel to transmission axis)

Hence the intensity of light falling on the second polarizer is $I_{\max}/2$

The second transmits $I = (I_{\max}/2) \cos^2 30^\circ = (I_{\max}/2) \frac{3}{4}$

$$\frac{I}{I_{\max}} = \frac{1}{2} \times \frac{3}{4} = \frac{3}{8} = 0.375$$