

Searching and Sorting

ICT 4303

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Linear Search

Time Complexity?

$O(n)$

```
int search(int arr[], int n, int x)
{
    int i;
    for (i = 0; i < n; i++)
        if (arr[i] == x)
            return i;
}
```

Binary Search: Iterative

Time Complexity?

$O(\log n)$

```
int binarySearch(int arr[], int start, int end, int x)
{
    while (start <= end) {
        int m = start + (end - start) / 2;
        if (arr[m] == x)
            return m;
        if (arr[m] < x)
            start = m + 1;
        else
            end = m - 1;
    }
}
```

Binary Search : Recursive

```
int binarySearch(int arr[], int start, int end, int x)
{
    if (end >= start) {
        int mid = start + (end - start) / 2;
        if (arr[mid] == x)
            return mid;
        if (arr[mid] > x)
            return binarySearch(arr, start, mid - 1, x);
        return binarySearch(arr, mid + 1, end, x);
    }
}
```

Insertion Sort

Time Complexity?

$O(n)$: Best Case

$O(n^2)$: Worst Case

```
void insertionSort(int arr[], int n)
{
    int i, key, j;
    for (i = 1; i < n; i++)
    {
        curr = arr[i];
        j = i - 1;

        while (j >= 0 && arr[j] > curr)
        {
            arr[j + 1] = arr[j];
            j = j - 1;
        }
        arr[j + 1] = curr;
    }
}
```

Quick Sort

Time Complexity?

$O(n \log n)$: Best and Average Case

$O(n^2)$: Worst Case

```
quickSort(arr[], low, high)
{
    if (low < high)
    {
        pi = partition(arr, low, high);

        quickSort(arr, low, pi - 1); // Before pi
        quickSort(arr, pi + 1, high); // After pi
    }
}
```

Quick Sort

Partition code Snippet with
last element as the pivot

```
partition (arr[], low, high)
{
    pivot = arr[high];

    i = (low - 1);

    for (j = low; j <= high- 1; j++)
    {
        if (arr[j] < pivot)
        {
            i++;
            swap(&arr[i], &arr[j]);
        }
    }
    swap(&arr[i + 1], &arr[high]);
    return (i + 1);
}
```


Quick Sort

Partition code Snippet with
first element as the pivot

```
partition (arr[], low, high) {  
    pivot = arr[low];  
    j= low;  
    i=high;  
    while (j <i){  
        while(arr[j]<=pivot){  
            j++;  
        }  
        while(arr[i]>pivot){  
            i--;  
        }  
        if(j < i){  
            swap (arr[j], arr[i]);  
        }  
    }  
    swap(arr[low], arr[i]);  
    return i;  
}
```

Merge Sort

Time Complexity?

$O(n \log n)$

MergeSort(a[], lb, ub)

If $ub > lb$

1. Find the middle point to divide the array into two halves:

middle $m = lb + ((ub - lb) / 2)$

2. Call mergeSort for first half:

Call mergeSort(a, lb, m)

3. Call mergeSort for second half:

Call mergeSort(a, m+1, ub)

4. Merge the two halves sorted in step 2 and 3:

Call merge(a, lb, m, ub)

Alternatively: middle $m = (lb + ub) / 2$

Merge Sort

Merge function is at the core of Merge Sort.

```
merge (a, lb, m, ub) {  
    i=lb;  
    j=m+1;  
    k=lb;  
    while (i<=mid && j<=ub) {  
        if(a [i] <= a[j]){  
            b[k] = a[i];  
            i++; k++;  
        } else {  
            b[k] = a[j];  
            j++; k++;  
        }  
    }  
    if (i>mid) {  
        while (j<=ub){  
            b[k] = a[j];  
            j++; k++;  
        }  
    } else{  
        while (i<=m){  
            b[k] = a[i];  
            i++; k++;  
        }  
    }  
}
```

Heap Sort

Heapify () is at the core.

Time Complexity?

$O(n \log n)$

```
void heapSort(int arr[], int n)
{
    // Build heap (rearrange array)
    for (int i = n / 2 - 1; i >= 0; i--)
        heapify(arr, n, i);

    // One by one extract an element from heap
    for (int i = n - 1; i > 0; i--) {

        // Move current root to end
        swap(arr[0], arr[i]);

        // call max heapify on the reduced heap
        heapify(arr, i, 0);
    }
}
```

Heap Sort

Heapify () is at the core.

```
void heapify(int arr[], int n, int i)
{
    int largest = i;
    int l = 2 * i + 1;
    int r = 2 * i + 2;

    // If left child is larger than root
    if (l < n && arr[l] > arr[largest])
        largest = l;

    // If right child is larger than largest so far
    if (r < n && arr[r] > arr[largest])
        largest = r;

    // If largest is not root
    if (largest != i) {
        swap(arr[i], arr[largest]);

        // Recursively heapify the affected sub-tree
        heapify(arr, n, largest);
    }
}
```

Shell Sort

A variation of Insertion Sort.

```
int shellSort(int arr[], int n)
{
    for (int gap = n/2; gap > 0; gap /= 2)
    {
        for (int i = gap; i < n; i += 1)
        {
            int temp = arr[i];

            int j;
            for (j = i; j >= gap && arr[j - gap] > temp; j -= gap)
                arr[j] = arr[j - gap];

            arr[j] = temp;
        }
    }
    return 0;
}
```