

Time Complexity + Recursion

Assignment

Find time complexity of below code blocks :

Problem 1 : ¶

```
def quicksort(arr):  
    if len(arr) <= 1:  
        return arr  
  
    pivot = arr[len(arr) // 2]  
  
    left = [x for x in arr if x < pivot]  
    middle = [x for x in arr if x == pivot]  
    right = [x for x in arr if x > pivot]  
  
    return quicksort(left) + middle + quicksort(right)
```

Average-case time Complexity : $O(n \log n)$

Worst-case time complexity: $O(n^2)$

where n is the length of the array

Problem 2 :

```
def nested_loop_example(matrix):
```

```
rows, cols = len(matrix), len(matrix[0])
```

```
total = 0
```

Time complexity : $O(\text{rows} * \text{cols})$, where rows is number of rows and cols is number of columns in the matrix

Problem 3 :

```
def example_function(arr):  
  
    result = 0  
  
    for element in arr:  
  
        result += element  
  
    return result
```

Time complexity : $O(n)$, where n is the length of the array

Problem 4 :

```
def longest_increasing_subsequence(nums):  
  
    n = len(nums)  
  
    lis = [1] * n  
  
    for i in range(1, n):  
  
        for j in range(0, i):  
  
            if nums[i] > nums[j] and lis[i] < lis[j] + 1:  
  
                lis[i] = lis[j] + 1  
  
    return max(lis)
```

Time complexity: $O(n^2)$, where n is the length of the input array nums

Problem 5 :

```
def mysterious_function(arr):
```

```
n = len(arr)

result = 0

for i in range(n):

    for j in range(i, n):

        result += arr[i] * arr[j]

return result
```

Time complexity: $O(n^2)$, where n is the length of the input array

Solve the following problems on recursion



Problem 6 : Sum of Digits

Write a recursive function to calculate the sum of digits of a given positive integer.

sum_of_digits(123) -> 6

```
In [8]: def sum_of_digits(num):
        if num <= 9:
            return num
        else:
            digit = num % 10
            return digit + sum_of_digits(num // 10)

        ## Example usage
        print(sum_of_digits(123))
```

6

Problem 7: Fibonacci Series

Write a recursive function to generate the first n numbers of the Fibonacci series.

fibonacci_series(6) -> [0, 1, 1, 2, 3, 5]

```
In [12]: def fibobacci_series(n):
    if n <= 0:
        return []
    elif n == 1:
        return [0]
    elif n == 2:
        return [0,1]
    else:
        fibo = fibobacci_series(n-1)
        fibo.append(fibo[-1] + fibo[-2])
        return fibo

    ## Example usage
    print(fibobacci_series(6))
```

[0, 1, 1, 2, 3, 5]

Problem 8 : Subset Sum

Given a set of positive integers and a target sum, write a recursive function to determine if there exists a subset of the integers that adds up to the target sum.

subset_sum([3, 34, 4, 12, 5, 2], 9) -> True

```
In [40]: def subset_sum(nums, target):
    # Base case: if the target is 0, an empty subset is valid
    if target == 0:
        return True

    # Base case: if the set is empty and the target is not 0, no subset is
    if not nums:
        return False

    # Recursive case: explore two possibilities - include the current element
    include_current = subset_sum(nums[1:], target - nums[0])
    exclude_current = subset_sum(nums[1:], target)

    # Return True if either of the possibilities leads to a valid subset
    return include_current or exclude_current

    # Example usage:
    nums = [3, 34, 4, 12, 5, 2]
    target_sum = 9
    result = subset_sum(nums, target_sum)
    print(result)
```

True

Problem 9: Word Break

Given a non-empty string and a dictionary of words, write a recursive function to determine if the string can be segmented into a space-separated sequence of dictionary words.

word_break(leetcode , [leet , code]) -> True

```
In [38]: def word_break(wordlist,word):
            if word == "":
                return True
            else:
                wordlen = len(word)
                for i in range(1,wordlen+1):
                    if word[:i] in wordlist and word_break(wordlist,word[i:]):
                        return True
                return False

            #Example usage
            print(word_break(["leet", "code"], "leetcode"))
```

True

Problem 10 : N-Queens

Implement a recursive function to solve the N Queens problem, where you have to place N queens on an N×N chessboard in such a way that no two queens threaten each other.

n_queens(4)

```
[
    [".Q..",
     "...Q",
     "Q...",
     "..Q."],
    [".Q.",
     "Q...",
     "...Q",
     ".Q.."]
]
```

```

In [32]: # Return True if it's safe to place queen on the board
def isSafeToPlaceQueen(board, row, col, n):

    #check in the left side
    for i in range(col):
        if board[row][i] == 1:
            return False
    #check in the upper left diagonal
    for i, j in zip(range(row, -1, -1), range(col, -1, -1)):
        if board[i][j] == 1:
            return False
    #check in the lower left diagonal
    for i, j in zip(range(row, n, 1), range(col, -1, -1)):
        if board[i][j] == 1:
            return False
    return True

## should return true if we are able to place all the queens
def solveNQUtil(board, col, n):
    #Base condition
    if (col >= n):
        return True #means we have been able to put queens in all the column
    #check for all the rows
    for row in range(n):
        if isSafeToPlaceQueen(board, row, col, n):
            board[row][col] = 1 #set the queen
            #recursively try for the next columns
            if solveNQUtil(board, col+1, n):
                return True
            #Backtracking
            board[row][col] = 0 ## Queen can't be set here

    return False #won't be able to place the queen

def printBoard(board, n):
    for i in range(n):
        for j in range(n):
            if board[i][j] == 1:
                print("Q", end = " ")
            else:
                print(".", end = " ")
        print()

def solveNQ(board, n):

    if not solveNQUtil(board, 0, n):
        print("Solution doesn't exist")
        return

    printBoard(board, n)

```

```
In [33]: import numpy as np  
board = np.zeros((4,4),int)  
solveNQ(board,4)
```

```
. . Q .  
Q . . .  
. . . Q  
. Q . .
```