# Title of My Thesis



SUBMITTED BY

Jan-Philipp Anton Konrad Christ

## Titel meiner Arbeit

#### Bachelorarbeit

FAKULTÄT FÜR PHYSIK
QUANTEN VIELTEILCHENSYSTEME/ THEORETISCHE NANOPHYSIK
LUDWIG-MAXIMILIANS-UNIVERSITÄT
MÜNCHEN

VORGELEGT VON

Jan-Philipp Anton Konrad Christ

## Title of My Thesis

#### **Bachelor Thesis**

FACULTY OF PHYSICS

QUANTUM MANY-BODY SYSTEMS/ THEORETICAL NANOPHYSICS GROUP

LUDWIG MAXIMILIAN UNIVERSITY

MUNICH

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ABSTRACT

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#### DETAILED CALCULATIONS

### A.1 Deriving the flow equations in the case of no ndependence

First the canonical generator  $\hat{\eta}$  has to be evaluated:

$$\hat{\eta} := \hat{\eta}(\lambda) := \left[\hat{\mathcal{H}}_{0}, \hat{\mathcal{H}}_{int}\right] = \left[\sum_{k} \omega_{k} \hat{a}_{k}^{\dagger} \hat{a}_{k}, \sum_{q \neq q'} V_{q,q'} \hat{a}_{q}^{\dagger} \hat{a}_{q'} + \sum_{p,p'} \left(W_{p,p'} \hat{a}_{p}^{\dagger} \hat{a}_{p'}^{\dagger} + W_{p,p'}^{*} \hat{a}_{p} \hat{a}_{p'}\right)\right]$$

$$= \sum_{k} \sum_{q,q'} \omega_{k} V_{q,q'} \left[\hat{a}_{k}^{\dagger} \hat{a}_{k}, \hat{a}_{q}^{\dagger} \hat{a}_{q'}\right] + \sum_{k} \sum_{p,p'} \left(\omega_{k} W_{p,p'} \left[\hat{a}_{k}^{\dagger} \hat{a}_{k}, \hat{a}_{p}^{\dagger} \hat{a}_{p'}^{\dagger}\right] + \omega_{k} W_{p,p'}^{*} \left[\hat{a}_{k}^{\dagger} \hat{a}_{k}, \hat{a}_{p} \hat{a}_{p'}\right]\right)$$

$$= \sum_{k} \sum_{q,q'} \omega_{k} V_{q,q'} \left(\hat{a}_{k}^{\dagger} \hat{a}_{q'} \delta_{k,q} - \hat{a}_{q}^{\dagger} \hat{a}_{k} \delta_{k,q'}\right)$$

$$+ \sum_{k} \sum_{p,p'} \left(\omega_{k} W_{p,p'} \left(\hat{a}_{k}^{\dagger} \hat{a}_{p}^{\dagger} \delta_{k,p'} + \hat{a}_{k}^{\dagger} \hat{a}_{p'}^{\dagger} \delta_{k,p}\right) - \omega_{k} W_{p,p'}^{*} \left(\hat{a}_{p} \hat{a}_{k} \delta_{k,p'} + \hat{a}_{p'} + \hat{a}_{p'} \hat{a}_{k} \delta_{k,p}\right)\right)$$

$$= \sum_{q \neq q'} V_{q,q'} (\omega_{q} - \omega_{q'}) \hat{a}_{q}^{\dagger} \hat{a}_{q'} + \sum_{p,p'} \left(W_{p,p'} (\omega_{p} + \omega_{p'}) \hat{a}_{p}^{\dagger} \hat{a}_{p'}^{\dagger} - W_{p,p'}^{*} (\omega_{p} + \omega_{p'}) \hat{a}_{p} \hat{a}_{p'}\right)$$

$$(A.2)$$

Since  $\hat{\eta}$  has the same form as  $\hat{\mathcal{H}}_{int}$ ,  $\left[\hat{\eta}, \hat{\mathcal{H}}_{0}\right]$  follows by inspection of A.2:

$$\left[\hat{\eta}, \hat{\mathcal{H}}_{0}\right] = -\sum_{q \neq q'} V_{q,q'} (\omega_{q} - \omega_{q'})^{2} \hat{a}_{q}^{\dagger} \hat{a}_{q'}$$

$$-\sum_{p,p'} \left( W_{p,p'} (\omega_{p} + \omega_{p'})^{2} \hat{a}_{p}^{\dagger} \hat{a}_{p'}^{\dagger} + W_{p,p'}^{*} (\omega_{p} + \omega_{p'})^{2} \hat{a}_{p} \hat{a}_{p'} \right)$$
(A.3)

10 Detailed Calculations

The commutator of the generator and  $\hat{\mathcal{H}}_{int}$  needs more work:

In the following, A.5-A.8 will be evaluated separately:

A.5:

$$\begin{split} & \left[ \sum_{q \neq q'} V_{q,q'}(\omega_{q} - \omega_{q'}) \hat{a}_{q}^{\dagger} \hat{a}_{q'}, \sum_{\bar{q} \neq \bar{q}'} V_{\bar{q},\bar{q}'} \hat{a}_{\bar{q}}^{\dagger} \hat{a}_{\bar{q}'} \right] \\ & = \sum_{q \neq q'} \sum_{\bar{q} \neq \bar{q}'} V_{\bar{q},\bar{q}'} V_{q,q'}(\omega_{q} - \omega_{q'}) \left[ \hat{a}_{q}^{\dagger} \hat{a}_{q'}, \hat{a}_{\bar{q}}^{\dagger} \hat{a}_{\bar{q}'} \right] \\ & = \sum_{q \neq q'} \sum_{\bar{q} \neq \bar{q}'} V_{\bar{q},\bar{q}'} V_{q,q'}(\omega_{q} - \omega_{q'}) \left( \hat{a}_{q}^{\dagger} \hat{a}_{\bar{q}'} \delta_{q',\bar{q}} - \hat{a}_{\bar{q}}^{\dagger} \hat{a}_{q'} \delta_{q,\bar{q}'} \right) \\ & = \sum_{q \neq q'} \sum_{\bar{q}'} V_{q',\bar{q}'} V_{q,q'}(\omega_{q} - \omega_{q'}) \hat{a}_{q}^{\dagger} \hat{a}_{\bar{q}'} - \sum_{q \neq q'} \sum_{\bar{q}} V_{\bar{q},q} V_{q,q'}(\omega_{q} - \omega_{q'}) \hat{a}_{\bar{q}}^{\dagger} \hat{a}_{q'} \\ & = \sum_{q,q'} \sum_{\bar{q}'} V_{q,\bar{q}'} V_{q,q'}(\omega_{q} - \omega_{q'}) \hat{a}_{q}^{\dagger} \hat{a}_{\bar{q}'} - \sum_{q,q'} \sum_{\bar{q}} V_{\bar{q},q} V_{q,q'}(\omega_{q} - \omega_{q'}) \hat{a}_{\bar{q}}^{\dagger} \hat{a}_{q'} \\ & = \sum_{q,q'} \sum_{\bar{q}} V_{\bar{q},q'} V_{q,\bar{q}}(\omega_{q} - \omega_{\bar{q}}) \hat{a}_{q}^{\dagger} \hat{a}_{q'} - \sum_{q,q'} \sum_{\bar{q}} V_{q,\bar{q}} V_{\bar{q},q'}(\omega_{\bar{q}} - \omega_{q'}) \hat{a}_{q}^{\dagger} \hat{a}_{q'} \\ & = \sum_{q \neq q'} \sum_{\bar{q}} V_{\bar{q},q'} V_{q,\bar{q}}(\omega_{q} - \omega_{\bar{q}}) \hat{a}_{q}^{\dagger} \hat{a}_{q'} - \sum_{q \neq q'} \sum_{\bar{q}} V_{q,\bar{q}} V_{\bar{q},q'}(\omega_{\bar{q}} - \omega_{q'}) \hat{a}_{q}^{\dagger} \hat{a}_{q'} \\ & + \sum_{k} \sum_{\bar{q}} V_{\bar{q},q'} V_{q,\bar{q}}(\omega_{q} - \omega_{\bar{q}}) \hat{a}_{q}^{\dagger} \hat{a}_{q'} - \sum_{q \neq q'} \sum_{\bar{q}} V_{q,\bar{q}} V_{\bar{q},q'}(\omega_{\bar{q}} - \omega_{q'}) \hat{a}_{q}^{\dagger} \hat{a}_{q'} \\ & + \sum_{k} \sum_{\bar{q}} V_{\bar{q},q'} V_{q,\bar{q}}(\omega_{q} - \omega_{\bar{q}}) \hat{a}_{q}^{\dagger} \hat{a}_{q'} - \sum_{q \neq q'} \sum_{\bar{q}} V_{q,\bar{q}} V_{\bar{q},q'}(\omega_{\bar{q}} - \omega_{q'}) \hat{a}_{q}^{\dagger} \hat{a}_{q'} \\ & + \sum_{k} \sum_{\bar{q}} V_{\bar{q},q'} V_{q,\bar{q}}(\omega_{q} - \omega_{\bar{q}}) \hat{a}_{q}^{\dagger} \hat{a}_{q'} - \sum_{q \neq q'} \sum_{\bar{q}} V_{q,\bar{q}} V_{\bar{q},q'}(\omega_{\bar{q}} - \omega_{q'}) \hat{a}_{q}^{\dagger} \hat{a}_{q'} \\ & + \sum_{k} \sum_{\bar{q}} 2 V_{\bar{q},k} V_{k,\bar{q}}(\omega_{k} - \omega_{\bar{q}}) \hat{a}_{k}^{\dagger} \hat{a}_{k} \end{split} \tag{A.9}$$

A.6:

$$\begin{split} & \left[ \sum_{q \neq q'} V_{q,q'}(\omega_{q} - \omega_{q'}) \hat{a}_{q}^{\dagger} \hat{a}_{q'}, \sum_{\bar{p},\bar{p}'} \left( W_{\bar{p},\bar{p}'} \hat{a}_{\bar{p}}^{\dagger} \hat{a}_{\bar{p}'}^{\dagger} + W_{\bar{p},\bar{p}'}^{*} \hat{a}_{\bar{p}}^{\dagger} \hat{a}_{\bar{p}'}^{\dagger} \right) \right] \\ & = \sum_{q \neq q'} \sum_{\bar{p},\bar{p}'} V_{q,q'}(\omega_{q} - \omega_{q'}) \left( W_{\bar{p},\bar{p}'} \left[ \hat{a}_{q}^{\dagger} \hat{a}_{q'}, \hat{a}_{\bar{p}}^{\dagger} \hat{a}_{\bar{p}'}^{\dagger} \right] + W_{\bar{p},\bar{p}'}^{*} \left[ \hat{a}_{q}^{\dagger} \hat{a}_{q'}, \hat{a}_{\bar{p}}^{\dagger} \hat{a}_{\bar{p}'} \right] \right) \\ & = \sum_{q,q'} \sum_{\bar{p},\bar{p}'} V_{q,q'}(\omega_{q} - \omega_{q'}) \left( W_{\bar{p},\bar{p}'} \left( \hat{a}_{q}^{\dagger} \hat{a}_{\bar{p}}^{\dagger} \delta_{q',\bar{p}'} + \hat{a}_{q}^{\dagger} \hat{a}_{\bar{p}'}^{\dagger} \delta_{q',\bar{p}} \right) - W_{\bar{p},\bar{p}'}^{*} \hat{a}_{\bar{p}} \left( \hat{a}_{\bar{p}'} \hat{a}_{q'} \delta_{q',\bar{p}'} + \hat{a}_{\bar{p}} \hat{a}_{\bar{q}'} \delta_{q',\bar{p}} \right) \right] \\ & = \sum_{q,p'} \sum_{q} V_{q,p'}(\omega_{q} - \omega_{q'}) W_{p,p'}^{*} \hat{a}_{q}^{\dagger} \hat{a}_{p}^{\dagger} + \sum_{p,p'} \sum_{q} V_{q,p}(\omega_{q} - \omega_{p}) W_{p,p'} \hat{a}_{q}^{\dagger} \hat{a}_{p'}^{\dagger} \\ & - \sum_{p,p'} \sum_{q} V_{p,q'}(\omega_{p} - \omega_{q'}) W_{p,p'}^{*} \hat{a}_{p'}^{\dagger} \hat{a}_{p'} + \sum_{p,p'} \sum_{q} V_{p,q}(\omega_{p} - \omega_{q}) W_{q,p'} \hat{a}_{p}^{\dagger} \hat{a}_{p'}^{\dagger} \\ & - \sum_{p,p'} \sum_{q} V_{q,p}(\omega_{q} - \omega_{p}) W_{q,p'}^{*} \hat{a}_{p}^{\dagger} \hat{a}_{p'} + \sum_{p,p'} \sum_{q} V_{q,p'}(\omega_{q} - \omega_{p}) W_{p,q}^{*} \hat{a}_{p}^{\dagger} \hat{a}_{p'} \\ & = \sum_{p,p'} \sum_{q} V_{p,q}(\omega_{p'} - \omega_{q}) W_{p,q} \hat{a}_{p}^{\dagger} \hat{a}_{p'}^{\dagger} + \sum_{p,p'} \sum_{q} V_{p,q}(\omega_{p} - \omega_{q}) W_{q,p'} \hat{a}_{p}^{\dagger} \hat{a}_{p'} \\ & - \sum_{p,p'} \sum_{q} V_{q,p}(\omega_{q} - \omega_{p}) W_{q,p'}^{*} \hat{a}_{p} \hat{a}_{p'} + \sum_{p,p'} \sum_{q} V_{q,p'}(\omega_{q} - \omega_{p}) W_{p,q}^{*} \hat{a}_{p}^{\dagger} \hat{a}_{p'} \\ & - \sum_{p,p'} \sum_{q} V_{q,p}(\omega_{q} - \omega_{p}) W_{q,p'}^{*} \hat{a}_{p} \hat{a}_{p'} - \sum_{p,p'} \sum_{q} V_{q,p'}(\omega_{q} - \omega_{p'}) W_{p,q}^{*} \hat{a}_{p}^{\dagger} \hat{a}_{p'} \\ & - \sum_{p,p'} \sum_{q} V_{q,p}(\omega_{p} - \omega_{q}) (W_{q,p'} + W_{p',q}) \hat{a}_{p}^{\dagger} \hat{a}_{p'} \\ & + \sum_{p,p'} \sum_{q} V_{q,p}(\omega_{p} - \omega_{q}) (W_{q,p'} + W_{p',q}) \hat{a}_{p}^{\dagger} \hat{a}_{p'} \end{aligned} \tag{A.10}$$

A.7:

$$\begin{split} & \left[ \sum_{p,p'} \left( W_{p,p'}(\omega_{p} + \omega_{p'}) \hat{a}_{p}^{\dagger} \hat{a}_{p'}^{\dagger} - W_{p,p'}^{*}(\omega_{p} + \omega_{p'}) \hat{a}_{p} \hat{a}_{p'} \right), \sum_{\vec{q} \neq \vec{q}'} V_{\vec{q},\vec{q}'} \hat{a}_{\vec{q}}^{\dagger} \hat{a}_{\vec{q}'} \right] \\ & = \sum_{p,p'} \sum_{\vec{q} \neq \vec{q}'} V_{\vec{q},\vec{q}'}(\omega_{p} + \omega_{p'}) \left( W_{p,p'} \left[ \hat{a}_{p}^{\dagger} \hat{a}_{p'}^{\dagger}, \hat{a}_{\vec{q}}^{\dagger} \hat{a}_{\vec{q}'} \right] - W_{p,p'}^{*} \left[ \hat{a}_{p} \hat{a}_{p'}, \hat{a}_{\vec{q}}^{\dagger} \hat{a}_{\vec{q}'} \right] \right) \\ & = -\sum_{p,p'} \sum_{q \neq q'} V_{q,q'}(\omega_{p} + \omega_{p'}) W_{p,p'}^{*} \left( \hat{a}_{q}^{\dagger} \hat{a}_{p}^{\dagger} \delta_{q',p'} + \hat{a}_{q}^{\dagger} \hat{a}_{p'}^{\dagger} \delta_{q',p} \right) \\ & - \sum_{p,p'} \sum_{q \neq q'} V_{q,q'}(\omega_{p} + \omega_{p'}) W_{p,p'}^{*} \left( \hat{a}_{p} \hat{a}_{q'} \delta_{q,p'} + \hat{a}_{p'} \hat{a}_{q'} \delta_{q,p} \right) \\ & = -\sum_{p,p'} \sum_{q} V_{q,p'}(\omega_{p} + \omega_{p'}) W_{p,p'}^{*} \hat{a}_{q}^{\dagger} \hat{a}_{p}^{\dagger} - \sum_{p,p'} \sum_{q} V_{q,p}(\omega_{p} + \omega_{p'}) W_{p,p'}^{*} \hat{a}_{q}^{\dagger} \hat{a}_{p'} \\ & - \sum_{p,p'} \sum_{q'} V_{p',q'}(\omega_{p} + \omega_{p'}) W_{p,p'}^{*} \hat{a}_{p} \hat{a}_{q'} - \sum_{p,p'} \sum_{q'} V_{p,q'}(\omega_{p} + \omega_{p'}) W_{p,p'}^{*} \hat{a}_{p}^{\dagger} \hat{a}_{p'} \\ & - \sum_{p,p'} \sum_{q'} V_{p',q}(\omega_{p} + \omega_{q'}) W_{p,q}^{*} \hat{a}_{p}^{\dagger} \hat{a}_{p'} - \sum_{p,p'} \sum_{q'} V_{p,q}(\omega_{q} + \omega_{p'}) W_{q',p'}^{*} \hat{a}_{p} \hat{a}_{p'} \\ & - \sum_{p,p'} \sum_{q'} V_{p,q}(\omega_{q} + \omega_{q'}) W_{p,q}^{*} \hat{a}_{p}^{\dagger} \hat{a}_{p'} - \sum_{p,p'} \sum_{q'} V_{q',p}(\omega_{q'} + \omega_{p'}) W_{q',p'}^{*} \hat{a}_{p} \hat{a}_{p'} \\ & - \sum_{p,p'} \sum_{q'} V_{p,q}(\omega_{q} + \omega_{p'}) (W_{p',q} + W_{q,p'}) \hat{a}_{p}^{\dagger} \hat{a}_{p'}^{\dagger} \\ & - \sum_{p,p'} \sum_{q} V_{p,p}(\omega_{q} + \omega_{p'}) (W_{p',q} + W_{q,p'}) \hat{a}_{p}^{\dagger} \hat{a}_{p'} \end{aligned} \tag{A.11}$$

12 Detailed Calculations

**A.8**:

$$\begin{split} & \left[ \sum_{p,p'} \left( W_{p,p'}(\omega_p + \omega_{p'}) \hat{a}_p^{\dagger} \hat{a}_{p'}^{\dagger} - W_{p,p'}^{*}(\omega_p + \omega_{p'}) \hat{a}_p \hat{a}_{p'} \right), \sum_{\vec{p},\vec{p'}} \left( W_{\vec{p},\vec{p'}} \hat{a}_p^{\dagger} \hat{a}_{\vec{p'}}^{\dagger} + W_{\vec{p},\vec{p'}}^{*} \hat{a}_p \hat{a}_{\vec{p'}} \right) \right] \\ & = \sum_{p,p'} \sum_{\vec{p},\vec{p'}} W_{p,p'}(\omega_p + \omega_{p'}) W_{\vec{p},\vec{p'}}^{*} \left[ \hat{a}_p^{\dagger} \hat{a}_{\vec{p'}}^{\dagger}, \hat{a}_p \hat{a}_{\vec{p'}} \right] - \sum_{p,p'} \sum_{\vec{p},\vec{p'}} W_{p,p'}^{*}(\omega_p + \omega_{p'}) \left[ \hat{a}_p \hat{a}_{p'}, \hat{a}_p^{\dagger} \hat{a}_{\vec{p'}} \right] \\ & = -\sum_{p,p'} \sum_{\vec{p},\vec{p'}} W_{p,p'}(\omega_p + \omega_{p'} + \omega_{\vec{p'}} + \omega_{\vec{p'}}) W_{\vec{p},\vec{p'}}^{*} \hat{a}_p^{\dagger} \hat{a}_p^{\dagger} \hat{a}_{p'} \right] \\ & = -\sum_{p,p'} \sum_{\vec{p},\vec{p'}} W_{p,p'}(\omega_p + \omega_{p'} + \omega_{\vec{p'}} + \omega_{\vec{p'}}) W_{\vec{p},\vec{p'}}^{*} \hat{a}_p^{\dagger} \hat{a}_p^{\dagger} \hat{a}_{p'} \right] \\ & = -\sum_{p,p'} \sum_{\vec{p},\vec{p'}} W_{p,p'}(\omega_p + \omega_{p'} + \omega_{\vec{p'}} + \omega_{\vec{p'}}) W_{\vec{p},\vec{p'}}^{*} \hat{a}_p^{\dagger} \hat{a}_p^{\dagger} \hat{a}_{p'} \right] \\ & = -\sum_{p,p'} \sum_{\vec{p},\vec{p'}} W_{p,p'}(\omega_p + \omega_{p'} + \omega_{\vec{p'}} + \omega_{\vec{p'}}) W_{\vec{p},\vec{p'}}^{*} \hat{a}_p^{\dagger} \hat{a}_p^{\dagger} \hat{a}_{p'} \hat{a}_{p'} \right] \\ & = -\sum_{p,p'} \sum_{\vec{p},\vec{p'}} W_{p,p'}(\omega_p + \omega_{p'} + \omega_{\vec{p}} + \omega_{\vec{p'}}) W_{\vec{p},\vec{p'}}^{*} \hat{a}_p^{\dagger} \hat{a}_p^{\dagger} \hat{a}_{p'} \hat{a}_{p'} \hat{a}_{p'} \\ & - \sum_{p,p'} \sum_{\vec{p},\vec{p'}} W_{p,p'}(\omega_p + 2\omega_{p'} + \omega_{\vec{p}}) W_{\vec{p},\vec{p'}}^{*} \hat{a}_p^{\dagger} \hat{a}_p^{\dagger} \hat{a}_p^{\dagger} \hat{a}_p^{\dagger} \hat{a}_p^{\dagger} \hat{a}_{p'} - \sum_{p,p'} \sum_{\vec{p}} W_{p,p'}(2\omega_p + \omega_{p'} + \omega_{\vec{p}}) W_{\vec{p},\vec{p'}}^{*} \hat{a}_p^{\dagger} \hat{a}_{p'} \hat{a}_p^{\dagger} \hat{a}_p^{\dagger} - \sum_{p,p'} \sum_{\vec{p}} W_{p,p'}(2\omega_p + \omega_{p'} + \omega_{\vec{p}}) W_{\vec{p},\vec{p'}}^{*} \hat{a}_p^{\dagger} \hat{a}_p^{\dagger} \hat{a}_p^{\dagger} \hat{a}_p^{\dagger} \hat{a}_p^{\dagger} - \sum_{p,p'} \sum_{\vec{p}} W_{p,p'}(2\omega_p + \omega_{p'} + \omega_{\vec{p}}) W_{\vec{p},\vec{p'}}^{*} \hat{a}_p^{\dagger} \hat{a}_p^$$

Using the expressions for the commutators of the generator and  $\hat{\mathcal{H}}_0$  respectively  $\hat{\mathcal{H}}_{int}$  derived above, the flow  $\partial_{\lambda}\hat{\mathcal{H}}(\lambda) = [\hat{\eta}(\lambda), \hat{\mathcal{H}}(\lambda)]$  yields the following flow equations:

$$\partial_{\lambda}\omega_{k} = \sum_{\tilde{q}} 2V_{\tilde{q},k}V_{k,\tilde{q}}(\omega_{k} - \omega_{\tilde{q}}) - 2\sum_{\tilde{p}} (W_{k,\tilde{p}} + W_{\tilde{p},k})(\omega_{k} + \omega_{\tilde{p}})(W_{\tilde{p},k}^{*} + W_{k,\tilde{p}}^{*})$$
(A.13a)

$$\partial_{\lambda} V_{q,q'} = -V_{q,q'} (\omega_q - \omega_{q'})^2 - \sum_{\tilde{p}} (W_{q,\tilde{p}} + W_{\tilde{p},q}) (\omega_q + 2\omega_{\tilde{p}} + \omega_{q'}) (W_{\tilde{p},q'}^* + W_{q',\tilde{p}}^*)$$

$$+\sum_{\tilde{q}} V_{\tilde{q},q'} V_{q,\tilde{q}}(\omega_q - \omega_{\tilde{q}}) - \sum_{\tilde{q}} V_{q,\tilde{q}} V_{\tilde{q},q'}(\omega_{\tilde{q}} - \omega_{q'})$$
(A.13b)

$$\partial_{\lambda}W_{p,p'} = -W_{p,p'}(\omega_p + \omega_{p'})^2 - \sum_{q} V_{p,q}(\omega_q + \omega_{p'})(W_{p',q} + W_{q,p'})$$

$$+\sum_{q} V_{p,q}(\omega_p - \omega_q)(W_{q,p'} + W_{p',q})$$
(A.13c)

$$\partial_{\lambda} W_{p,p'}^{*} = -W_{p,p'}^{*} (\omega_{p} + \omega_{p'})^{2} - \sum_{q} V_{q,p} (\omega_{q} + \omega_{p'}) (W_{p',q}^{*} + W_{q,p'}^{*})$$

$$+\sum_{q} V_{q,p}(\omega_p - \omega_q)(W_{q,p'}^* + W_{p',q}^*)$$
(A.13d)

$$\partial_{\lambda}\varepsilon = -2\sum_{p,p'} (W_{p,p'} + W_{p',p})(\omega_p + \omega_{p'})W_{p,p'}^*$$
(A.13e)

Obviously, equations A.13c and A.13d are not independent from each other, since they are related by complex conjugation. It is nevertheless a good consistency check to see that the two independently derived equations are equivalent.

14 Detailed Calculations

APPENDIX B	
I	
	THE SECOND APPENDIX

Here comes the second appendix.

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18 BIBLIOGRAPHY

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Munich, 22.06.2023 .....