

Matrix Exponentiation

We can find n'th Fibonacci Number in $O(\log n)$ time using Matrix Exponentiation

Same like the binary exponentiation we need to form the initial matrix and same logic

```
public class MatrixExponentiation {
```

```
    // Function to multiply two matrices
    static int[][] multiply(int[][] a, int[][] b) {
        int n = a.length;
        int[][] result = new int[n][n];

        for (int i = 0; i < n; i++) {
            for (int j = 0; j < n; j++) {
                for (int k = 0; k < n; k++) {
                    result[i][j] += a[i][k] * b[k][j];
                }
            }
        }

        return result;
    }

    // Function to raise a matrix to the power of p using recursion
    static int[][] power(int[][] matrix, int p) {
        if (p == 1) {
            return matrix;
        }
        int[][] result;
        if (p % 2 == 0) {
            int[][] halfPower = power(matrix, p / 2);
            result = multiply(halfPower, halfPower);
        } else {
            int[][] halfPower = power(matrix, (p - 1) / 2);
            result = multiply(matrix, multiply(halfPower, halfPower));
        }
        return result;
    }
}
```

```

public static void main(String[] args) {
    int[][] matrix = {{1, 1}, {1, 0}}; // Example matrix
    int exponent = 5; // Example exponent

    int[][] result = power(matrix, exponent);

    // Printing the result
    for (int i = 0; i < result.length; i++) {
        for (int j = 0; j < result[0].length; j++) {
            System.out.print(result[i][j] + " ");
        }
        System.out.println();
    }
}

```

`}

The initial matrix in this example is a 2x2 matrix. It's a common example used in demonstrating matrix exponentiation because it's associated with the Fibonacci sequence.

The matrix in question is:

$\begin{Bmatrix} 1 & 1 \\ 1 & 0 \end{Bmatrix}$

$\begin{bmatrix} F(n) & F(n-1) \\ F(n-1) & F(n-2) \end{bmatrix}$

$\begin{bmatrix} F(n) & F(n-1) \\ F(n-1) & F(n-2) \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix} * \begin{bmatrix} F(n-1) & F(n-2) \\ F(n-2) & F(n-3) \end{bmatrix}$