DATA_621_HW1

Chi Pong, Euclid Zhang, Jie Zou, Joseph Connolly, LeTicia Cancel

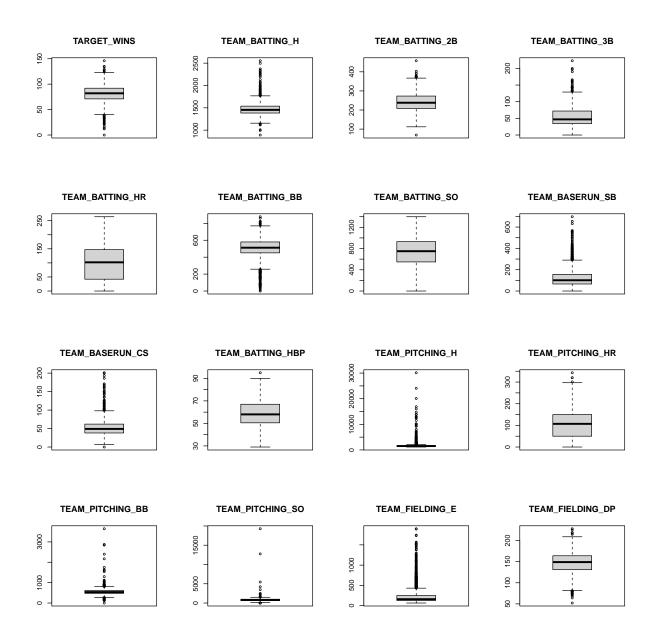
1/30/2022

DATA EXPLORATION

```
##
     TARGET_WINS
                      TEAM_BATTING_H TEAM_BATTING_2B TEAM_BATTING_3B
##
    Min.
           : 0.00
                             : 891
                                      Min.
                                             : 69.0
                                                       Min.
                                                              : 0.00
                      Min.
    1st Qu.: 71.00
##
                      1st Qu.:1383
                                      1st Qu.:208.0
                                                       1st Qu.: 34.00
##
    Median: 82.00
                      Median:1454
                                      Median :238.0
                                                       Median: 47.00
           : 80.79
##
    Mean
                      Mean
                             :1469
                                      Mean
                                             :241.2
                                                       Mean
                                                               : 55.25
##
    3rd Qu.: 92.00
                      3rd Qu.:1537
                                      3rd Qu.:273.0
                                                       3rd Qu.: 72.00
##
    Max.
           :146.00
                      Max.
                             :2554
                                      Max.
                                             :458.0
                                                       Max.
                                                               :223.00
##
                      TEAM_BATTING_BB TEAM_BATTING_SO
##
    TEAM_BATTING_HR
                                                         TEAM_BASERUN_SB
##
    Min.
           : 0.00
                      Min.
                             : 0.0
                                       Min.
                                              :
                                                  0.0
                                                         Min.
                                                                : 0.0
##
    1st Qu.: 42.00
                      1st Qu.:451.0
                                       1st Qu.: 548.0
                                                         1st Qu.: 66.0
##
    Median :102.00
                      Median :512.0
                                       Median: 750.0
                                                         Median :101.0
          : 99.61
                             :501.6
                                              : 735.6
##
    Mean
                      Mean
                                       Mean
                                                         Mean
                                                                 :124.8
##
    3rd Qu.:147.00
                      3rd Qu.:580.0
                                       3rd Qu.: 930.0
                                                         3rd Qu.:156.0
           :264.00
                             :878.0
                                              :1399.0
##
    Max.
                      Max.
                                       Max.
                                                         Max.
                                                                 :697.0
                                                                 :131
##
                                       NA's
                                              :102
                                                         NA's
##
    TEAM BASERUN CS TEAM BATTING HBP TEAM PITCHING H TEAM PITCHING HR
##
    Min.
           : 0.0
                             :29.00
                                              : 1137
                     Min.
                                       Min.
                                                        Min.
                                                                : 0.0
##
    1st Qu.: 38.0
                     1st Qu.:50.50
                                       1st Qu.: 1419
                                                        1st Qu.: 50.0
    Median: 49.0
                                       Median: 1518
##
                     Median :58.00
                                                        Median :107.0
##
    Mean
           : 52.8
                     Mean
                            :59.36
                                       Mean
                                              : 1779
                                                        Mean
                                                                :105.7
##
    3rd Qu.: 62.0
                     3rd Qu.:67.00
                                       3rd Qu.: 1682
                                                        3rd Qu.:150.0
##
    Max.
           :201.0
                             :95.00
                                              :30132
                                                        Max.
                                                                :343.0
                     Max.
                                       Max.
##
    NA's
           :772
                     NA's
                             :2085
    TEAM_PITCHING_BB TEAM_PITCHING_SO
                                         TEAM_FIELDING E
                                                           TEAM FIELDING DP
##
                                                                   : 52.0
##
    Min.
               0.0
                      Min.
                                   0.0
                                         Min.
                                                 : 65.0
                                                           Min.
##
    1st Qu.: 476.0
                      1st Qu.:
                                615.0
                                         1st Qu.: 127.0
                                                           1st Qu.:131.0
    Median: 536.5
                                813.5
                                         Median: 159.0
##
                      Median:
                                                           Median :149.0
                                                 : 246.5
##
    Mean
           : 553.0
                      Mean
                                817.7
                                                           Mean
                                                                   :146.4
                             :
                                         Mean
##
    3rd Qu.: 611.0
                      3rd Qu.:
                                968.0
                                         3rd Qu.: 249.2
                                                           3rd Qu.:164.0
##
    Max.
           :3645.0
                      Max.
                             :19278.0
                                         Max.
                                                 :1898.0
                                                           Max.
                                                                   :228.0
##
                      NA's
                              :102
                                                           NA's
                                                                   :286
```

* Outliers

From the summaries The maximum values for TEAM_PITCHING_H, TEAM_PITCHING_BB, TEAM_PITCHING_SO and TEAM_FIELDING_E seem abnormally large. There may be outliers in the columns. We can confirm this finding by checking the distributions of the values:



From the boxplots, there are indeed values in TEAM_PITCHING_H, TEAM_PITCHING_BB, TEAM_PITCHING_SO and TEAM_FIELDING_E that are extremly off from the majority of the data. We would handle these outliers later with the other problems.

* Missing values

From the summaries, we see that are missing values for TEAM_BATTING_SO, TEAM_BASERUN_SB, TEAM_BASERUN_CS, EAM_BATTING_HBP, TEAM_PITCHING_SO, and TEAM_FIELDING_DP. Now we check the portion of missing data in each field:

##	TARGET_WINS	TEAM_BATTING_H	TEAM_BATTING_2B	TEAM_BATTING_3B
##	0.00000000	0.00000000	0.0000000	0.00000000
##	TEAM_BATTING_HR	TEAM_BATTING_BB	TEAM_BATTING_SO	TEAM_BASERUN_SB
##	0.00000000	0.00000000	0.04481547	0.05755712

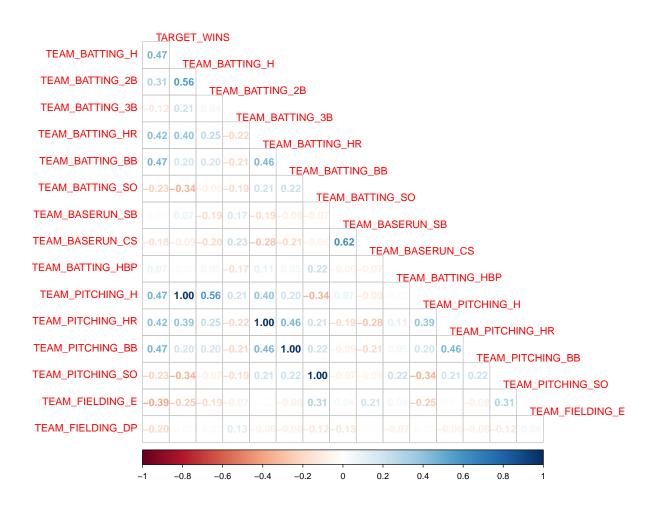
```
##
   TEAM_BASERUN_CS TEAM_BATTING_HBP
                                       TEAM PITCHING H TEAM PITCHING HR
##
         0.33919156
                          0.91608084
                                            0.00000000
                                                             0.0000000
##
  TEAM PITCHING BB TEAM PITCHING SO
                                      TEAM FIELDING E TEAM FIELDING DP
         0.00000000
                          0.04481547
                                            0.00000000
                                                             0.12565905
##
```

91.6% of the data in TEAM_BATTING_HBP are missing. Since the minimum of TEAM_BATTING_HBP is 29, it is not plausible that the missing values are all 0. We will drop this field from our analysis as there are too many missing values and there is no good way of imputing the values.

For TEAM_BATTING_SO, TEAM_BASERUN_SB, TEAM_BASERUN_CS, TEAM_PITCHING_SO, and TEAM FIELDING DP, we will do imputation and may be handled with other problems.

* Correlations

Now let's look at the correlations between the variables



The following variables are nearly perfectly correlated

- TEAM BATTING H and TEAM PITCHING H
- TEAM BATTING HR and TEAM PITCHING HR
- TEAM_BATTING_BB and TEAM_PITCHING_BB
- \bullet TEAM_BATTING_SO and TEAM_PITCHING_SO

We take a more careful look at the correlation between the TARGET_WINS and other variables, and compare it with the theoretical effects

##		${\tt correlation_with_TARGET_WINS}$	${\tt Theoretical_Effect}$
##	TEAM_BATTING_H	0.4699	Positive
##	TEAM_BATTING_2B	0.3130	Positive
##	TEAM_BATTING_3B	-0.1243	Positive
##	TEAM_BATTING_HR	0.4224	Positive
##	TEAM_BATTING_BB	0.4687	Positive
##	TEAM_BATTING_SO	-0.2289	Negative
##	TEAM_BASERUN_SB	0.0148	Positive
##	TEAM_BASERUN_CS	-0.1788	Negative
##	TEAM_BATTING_HBP	0.0735	Positive
##	TEAM_PITCHING_H	0.4712	Negative
##	TEAM_PITCHING_HR	0.4225	Negative
##	TEAM_PITCHING_BB	0.4684	Negative
##	TEAM_PITCHING_SO	-0.2294	Positive
##	TEAM_FIELDING_E	-0.3867	Negative
##	TEAM_FIELDING_DP	-0.1959	Positive

^{**}The following variables do not have correlation matching with the theoretical effect:

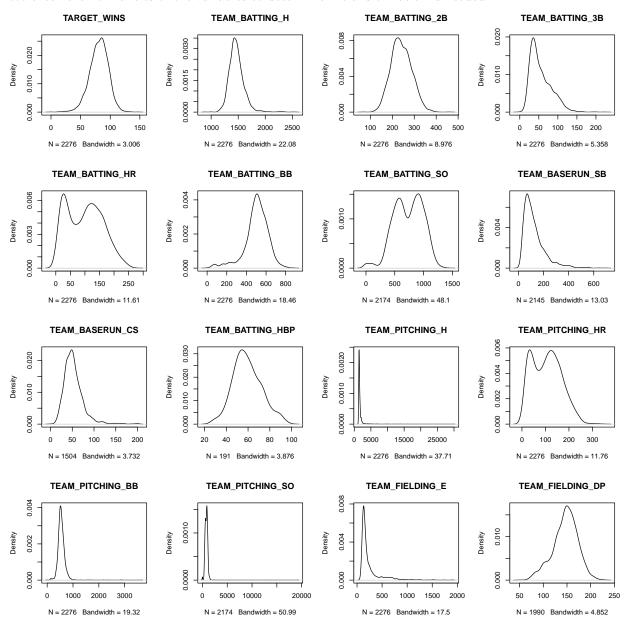
- TEAM_BATTING_3B
- TEAM_PITCHING_H
- TEAM_PITCHING_HR
- TEAM_PITCHING_BB
- TEAM PITCHING SO
- TEAM_FIELDING_DP

For TEAM_BATTING_3B and TEAM_FIELDING_DP, we would need to perform deeper analysis on this finding.

For TEAM_PITCHING_H, TEAM_PITCHING_HR, TEAM_PITCHING_BB, TEAM_PITCHING_SO, we may consider dropping the variables since they are amlost perfectly correlated with one other variable. Also, TEAM_PITCHING_H, TEAM_PITCHING_BB and TEAM_PITCHING_SO have outlier problem as found above.

* normalities

We check the normalities of the variables to determine if transformation is needed.



TEAM_PITCHING_H, TEAM_PITCHING_BB, TEAM_PITCHING_SO and TEAM_FIELDING_E are largely right skewed because of the outliers. We will check the distributions later again when the outliers are handled.

TEAM_BATTING_HR, TEAM_BATTING_SO, TEAM_PITCHING_HR are bimodal that may need to be transformed.

There are some variables such as TEAM_BASERUN_SB that are slightly right skewed. We may keep them as it for easier interpretation of the result.

DATA PREPARATION

* Dropping variables

TEAM_BATTING_HBP is dropped for the following reason(s)

• 91.6% of the data are missing

TEAM_PITCHING_HR is dropped for the following reason(s)

- nearly perfectly correlated with one other variable
- do not have correlation matching with the theoretical effect

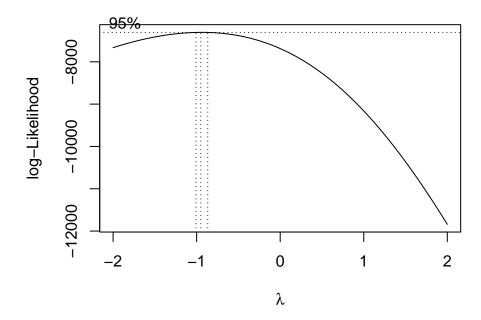
TEAM_PITCHING_H,TEAM_PITCHING_BB,TEAM_PITCHING_SO are dropped for the following reason(s)

- nearly perfectly correlated with one other variable
- do not have correlation matching with the theoretical effect
- large outliers

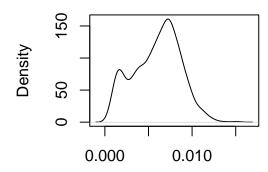
* Transforming variables

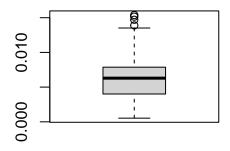
Since **TEAM_FIELDING_E** is extremely right skewed, we will transform the variable using Box-Cox transformation

The optimal lamba from the following result plot is near -1, so we will transform the variable using the power of -1



The following density plot and box plot show that the distribution is closer to normal and there are no extreme



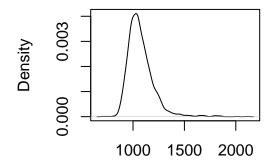


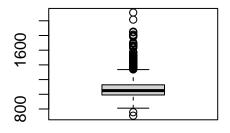
ourliers.

Since TEAM_BATTING_H also counts the number of TEAM_BATTING_2B, TEAM_BATTING_3B and TEAM_BATTING_3B.

Instead of using TEAM_BATTING_H, we will create a new variable TEAM_BATTING_1B by subtracting TEAM_BATTING_2B, TEAM_BATTING_3B and TEAM_BATTING_3B from TEAM_BATTING_H

The distribution of the new variable is slightly right skewed. We will keep it as it for now unless transformation is necessary when developing a model.





* Imputation for Missing Values

The only problem now is the missing values in TEAM_BATTING_SO, TEAM_BASERUN_SB, TEAM_BASERUN_CS and TEAM_FIELDING_DP

We will impute the missing values by using linear regression models. We will not go deep into evaluating these models in this project. The purpose here is to impute missing values have better explained variance

than simply using the means or medians.

In the imputation models, **TARGET_WINS** is not included as an independent variable since the values are not provided in the test data set. We will need to use the same models to impute missing values in the test data set.

We will perform separate imputations in the following order, based on the number of missing values: 1. TEAM_BATTING_SO 2. TEAM_BASERUN_SB 3. TEAM_FIELDING_DP 4. TEAM_BASERUN_CS

Variables that are already imputed are included in the models after and un-imputed variables are not included. We will keep the trained models and use them to impute missing values in the test data set.

The R-squared values of the models are:

```
## [1] "TEAM_BATTING_SO - R-squared:0.7045"
## [1] "TEAM_BASERUN_SB - R-squared:0.1571"
## [1] "TEAM_BASERUN_CS - R-squared:0.599"
## [1] "TEAM_FIELDING_DP - R-squared:0.1227"
```

The numbers in the summary of our prepared data set all look plausible, we are ready for our model development

```
##
     TARGET_WINS
                     TEAM_BATTING_2B TEAM_BATTING_3B
                                                       TEAM_BATTING_HR
   Min.
##
          : 0.00
                            : 69.0
                                     Min.
                                             : 0.00
                                                       Min.
                                                             : 0.00
                     Min.
   1st Qu.: 71.00
                     1st Qu.:208.0
                                      1st Qu.: 34.00
                                                       1st Qu.: 42.00
   Median: 82.00
                     Median :238.0
                                     Median : 47.00
                                                       Median :102.00
##
   Mean
          : 80.79
                     Mean
                            :241.2
                                      Mean
                                             : 55.25
                                                       Mean
                                                             : 99.61
##
   3rd Qu.: 92.00
                     3rd Qu.:273.0
                                      3rd Qu.: 72.00
                                                       3rd Qu.:147.00
##
  Max.
           :146.00
                     Max.
                            :458.0
                                      Max.
                                             :223.00
                                                       Max.
                                                              :264.00
   TEAM_BATTING_BB TEAM_BATTING_SO
                                     TEAM_BASERUN_SB TEAM_BASERUN_CS
##
##
   Min.
           : 0.0
                    Min.
                          :
                               0.0
                                      Min.
                                             : 0.0
                                                      Min.
                                                             : 0.00
                                      1st Qu.: 67.0
##
   1st Qu.:451.0
                    1st Qu.: 542.0
                                                      1st Qu.: 43.00
##
  Median :512.0
                    Median: 732.0
                                     Median :101.0
                                                      Median: 57.00
           :501.6
                           : 727.6
                                             :123.4
                                                             : 69.27
##
  Mean
                    Mean
                                     Mean
                                                      Mean
   3rd Qu.:580.0
                    3rd Qu.: 925.0
                                      3rd Qu.:152.0
##
                                                      3rd Qu.: 86.89
## Max.
           :878.0
                           :1399.0
                                             :697.0
                    Max.
                                     Max.
                                                      Max.
                                                             :272.21
  TEAM FIELDING DP TEAM FIELDING E Transformed TEAM BATTING 1B
## Min.
           : 52.0
                     Min.
                            :0.0005269
                                                  Min.
                                                         : 709.0
##
   1st Qu.:130.0
                     1st Qu.:0.0040120
                                                  1st Qu.: 990.8
##
  Median :146.0
                     Median: 0.0062893
                                                  Median :1050.0
                            :0.0059708
  Mean
           :144.9
                     Mean
                                                  Mean
                                                         :1073.2
##
   3rd Qu.:162.0
                     3rd Qu.:0.0078740
                                                  3rd Qu.:1129.0
   Max.
           :228.0
                     Max.
                            :0.0153846
                                                  Max.
                                                         :2112.0
```

BUILD MODELS

* 1. Full model:

TEAM_BATTING_1B, TEAM_BATTING_2B, TEAM_BATTING_3B, TEAM_BATTING_HR, TEAM_BATTING_BB, TEAM_BATTING_SO, TEAM_BASERUN_SB, TEAM_BASERUN_CS, TEAM_FIELDING_DP, TEAM_FIELDING_E_Transformed

```
##
## Call:
  lm(formula = TARGET_WINS ~ ., data = train_prepared_df)
##
## Residuals:
##
                1Q Median
                                3Q
       Min
                                       Max
   -68.884
            -8.302
                     0.085
                             8.208
                                    66.698
##
## Coefficients:
##
                                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                1.222e+01
                                           5.369e+00
                                                        2.277 0.022887 *
                                           7.396e-03
## TEAM_BATTING_2B
                                2.067e-02
                                                        2.795 0.005240 **
## TEAM_BATTING_3B
                                1.437e-01
                                           1.713e-02
                                                        8.389
                                                              < 2e-16 ***
## TEAM_BATTING_HR
                                8.623e-02
                                           9.275e-03
                                                        9.297
                                                              < 2e-16 ***
## TEAM_BATTING_BB
                                2.181e-02
                                           2.942e-03
                                                        7.414 1.72e-13 ***
## TEAM_BATTING_SO
                                -9.109e-03
                                           2.383e-03
                                                       -3.823 0.000136 ***
## TEAM_BASERUN_SB
                                1.534e-02
                                           8.865e-03
                                                        1.730 0.083685
## TEAM BASERUN CS
                                1.215e-02
                                           2.325e-02
                                                        0.522 0.601455
                               -1.368e-01
## TEAM_FIELDING_DP
                                           1.369e-02
                                                       -9.993
                                                               < 2e-16 ***
                                                       11.232
## TEAM FIELDING E Transformed 2.373e+03
                                           2.113e+02
                                                               < 2e-16 ***
## TEAM_BATTING_1B
                                4.254e-02 3.716e-03
                                                      11.450
                                                              < 2e-16 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.1 on 2265 degrees of freedom
## Multiple R-squared: 0.3109, Adjusted R-squared:
## F-statistic: 102.2 on 10 and 2265 DF, p-value: < 2.2e-16
```

In the full model, The sign of **TEAM_BASERUN_CS** and **TEAM_FIELDING_DP** do not match with the theoretical effects.

By looking at the below confidence intervals with 5% significance level, The positive sign for **TEAM_BASERUN_CS** may just happen by chance. The high p-value of **TEAM_BASERUN_CS** also indicates that the variable is not significant here. With the fact that more than 30% of the values of **TEAM_BASERUN_CS** are imputed. We suggest to drop this variable from our model.

For TEAM_FIELDING_DP, confidence interval is below 0 and the correlation between TAR-GET_WINS and TEAM_FIELDING_DP is -0.2. In the correlation matrix, it doesn't show any strong correlation with any other variables. One explanation is that double play happens when there is already a runner on a base. So a higher TEAM_FIELDING_DP means the team let the an opponent player stay on a base more frequently. A good team will get their opponents out before double play can happen. We may need to observe the behaviors of the baseball players directly to find out the true reason of the negative correlation, but in this analysis, We will compare the performance of the models with or without TEAM_FIELDING_DP using the test data set to determine whether we should keep this variable in our model.

```
##
                                        2.5 %
                                                     97.5 %
## (Intercept)
                                1.695863e+00
                                               2.275411e+01
## TEAM_BATTING_2B
                                6.165689e-03
                                               3.517413e-02
## TEAM_BATTING_3B
                                1.101057e-01
                                               1.772853e-01
## TEAM BATTING HR
                                6.804495e-02
                                               1.044223e-01
                                1.604367e-02 2.758226e-02
## TEAM_BATTING_BB
## TEAM BATTING SO
                               -1.378154e-02 -4.435984e-03
## TEAM_BASERUN_SB
                               -2.043957e-03 3.272634e-02
## TEAM_BASERUN_CS
                               -3.345244e-02 5.774641e-02
## TEAM_FIELDING_DP
                               -1.636101e-01 -1.099324e-01
```

```
## TEAM_FIELDING_E_Transformed 1.958557e+03 2.787093e+03 ## TEAM_BATTING_1B 3.525880e-02 4.983134e-02
```

* 2. Adjusted model 1:

exclude TEAM_BASERUN_CS

```
##
## Call:
## lm(formula = TARGET_WINS ~ . - TEAM_BASERUN_CS, data = train_prepared_df)
## Residuals:
      Min
               10 Median
                               3Q
                                      Max
## -68.884 -8.330
                   0.106
                            8.252
                                   66.698
##
## Coefficients:
##
                                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                               1.315e+01 5.068e+00
                                                     2.595 0.009519 **
## TEAM_BATTING_2B
                               2.029e-02 7.360e-03
                                                      2.757 0.005876 **
## TEAM_BATTING_3B
                               1.463e-01 1.637e-02
                                                      8.938 < 2e-16 ***
                               8.526e-02 9.083e-03
## TEAM_BATTING_HR
                                                      9.386 < 2e-16 ***
## TEAM BATTING BB
                               2.184e-02
                                          2.941e-03
                                                      7.428 1.55e-13 ***
## TEAM_BATTING_SO
                              -9.211e-03 2.374e-03
                                                     -3.879 0.000108 ***
## TEAM BASERUN SB
                               1.937e-02 4.353e-03
                                                      4.451 8.97e-06 ***
## TEAM_FIELDING_DP
                              -1.373e-01
                                         1.365e-02 -10.056 < 2e-16 ***
## TEAM_FIELDING_E_Transformed 2.357e+03
                                          2.091e+02 11.274 < 2e-16 ***
## TEAM_BATTING_1B
                               4.225e-02 3.672e-03 11.505 < 2e-16 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.1 on 2266 degrees of freedom
## Multiple R-squared: 0.3109, Adjusted R-squared: 0.3081
## F-statistic: 113.6 on 9 and 2266 DF, p-value: < 2.2e-16
```

The significance of **TEAM_BASERUN_SB** increases and the Adjusted R-squared increases. Dropping **TEAM_BASERUN_CS** gives us a better result. We will also verify this in our test data set.

* 3. Adjusted model 2:

exclude TEAM_BASERUN_CS and TEAM_FIELDING_DP

```
##
## Call:
## lm(formula = TARGET_WINS ~ . - TEAM_BASERUN_CS - TEAM_FIELDING_DP,
##
       data = train_prepared_df)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                        Max
## -70.701 -8.440
                    0.110
                             8.463 64.470
##
## Coefficients:
                                  Estimate Std. Error t value Pr(>|t|)
##
```

```
## (Intercept)
                                1.731e+00 5.047e+00
                                                       0.343
                                                               0.7316
                                                               0.0110 *
## TEAM_BATTING_2B
                                1.915e-02 7.520e-03
                                                       2.546
                                1.527e-01
                                                       9.136 < 2e-16 ***
## TEAM BATTING 3B
                                           1.672e-02
                                7.170e-02
## TEAM_BATTING_HR
                                           9.179e-03
                                                       7.811 8.59e-15 ***
## TEAM_BATTING_BB
                                1.560e-02
                                           2.937e-03
                                                       5.310 1.20e-07 ***
## TEAM BATTING SO
                               -7.351e-03
                                           2.419e-03
                                                      -3.039
                                                               0.0024 **
## TEAM BASERUN SB
                                3.324e-02
                                           4.219e-03
                                                       7.880 5.06e-15 ***
## TEAM_FIELDING_E_Transformed 2.160e+03
                                           2.127e+02
                                                      10.152
                                                             < 2e-16 ***
## TEAM BATTING 1B
                                3.671e-02
                                           3.710e-03
                                                       9.893 < 2e-16 ***
## ---
## Signif. codes:
                  0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 13.39 on 2267 degrees of freedom
## Multiple R-squared: 0.2801, Adjusted R-squared: 0.2776
## F-statistic: 110.3 on 8 and 2267 DF, p-value: < 2.2e-16
```

The significance of **TEAM_BATTING_2B** and **TEAM_BATTING_SO** decreases and the Adjusted R-squared also decreases. It seems that it is better to keep **TEAM_FIELDING_DP** in our model.

* 4. Adjusted model 3:

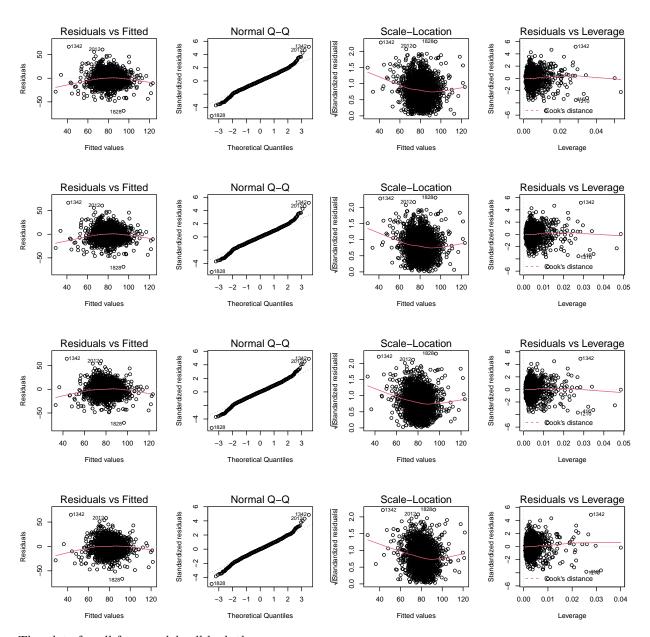
exclude all variables with imputed values (TEAM_BATTING_SO, TEAM_BASERUN_SB, TEAM_BASERUN_CS and TEAM_FIELDING_DP)

```
##
## Call:
## lm(formula = TARGET_WINS ~ . - TEAM_BATTING_SO - TEAM_BASERUN_SB -
       TEAM_BASERUN_CS - TEAM_FIELDING_DP, data = train_prepared_df)
##
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -66.320
           -8.342
                     0.075
                             8.584
                                    64.966
##
## Coefficients:
##
                                 Estimate Std. Error t value Pr(>|t|)
                                                      -1.882
## (Intercept)
                               -6.779e+00
                                           3.601e+00
                                                               0.0599
## TEAM_BATTING_2B
                                1.457e-02
                                           7.590e-03
                                                       1.919
                                                               0.0551 .
## TEAM_BATTING_3B
                                1.923e-01
                                           1.608e-02
                                                      11.960
                                                             < 2e-16 ***
## TEAM BATTING HR
                                                       6.502 9.72e-11 ***
                                5.544e-02
                                           8.527e-03
                                                       7.901 4.27e-15 ***
## TEAM_BATTING_BB
                                2.237e-02
                                           2.831e-03
## TEAM_FIELDING_E_Transformed 1.816e+03
                                           2.082e+02
                                                       8.722
                                                              < 2e-16 ***
## TEAM_BATTING_1B
                                4.272e-02 3.085e-03 13.848 < 2e-16 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 13.56 on 2269 degrees of freedom
## Multiple R-squared: 0.2604, Adjusted R-squared: 0.2584
## F-statistic: 133.1 on 6 and 2269 DF, p-value: < 2.2e-16
```

As expected, including less variables produce a model with lower R-squared value. The Adjusted R-squared is also lower in this case. However, this model is much simpler and all the variables have no missing values. We will compare the performance of this model to the other ones we have built using the test data set.

SELECT MODELS

* Inference Plots



The plots for all four models all look the same.

The residual plots and standardized residual plots show that the residuals are independent and approximately constant with mean 0 within the cloud of data.

The Q-Q plots show that the residuals are approximately normal except the two tails but the problem is mild.

The Residuals vs Leverage plots show no point outside of the Cook's distance. There is no strong influence point.

We conclude that all four models follow the assumptions of OLS regression and so they are valid.

* Adjusted R-squared

The R-squared or Adjusted R-squared is used to measure how well a model fit in the train data. Since our models have different number of predictor variables, it is better to compare the Adjusted R-squared of the 4 models

```
## [1] "Full model: 0.30790710214898"

## [1] "Exclude TEAM_BASERUN_CS: 0.308129181431121"

## [1] "EXclude TEAM_BASERUN_CS and TEAM_FIELDING_DP: 0.277569542766465"

## [1] "Exclude variables with missing values: 0.258422632152477"
```

All models have Adjusted R-squared less than 0.31, we may have omitted variables that are not recorded in our data set. The second model performs the best fitting the train data set. However, it doesn't mean that it will do well in predicting unseen data. We will test the performance of the models using a test data set.

* RMSD (Root Mean Square Deviation)

The RMSD (Root Mean Square Deviation) is a measurement for the difference between a model's predicted values and the actual values. We will use the RMSD to compare the 4 models performance.

First, let's look at the summary of our test data set:

```
##
    TEAM_BATTING_H TEAM_BATTING_2B TEAM_BATTING_3B
                                                       TEAM_BATTING_HR
                           : 44.0
##
                                             : 14.00
    Min.
           : 819
                    Min.
                                     Min.
                                                       Min.
                                                               : 0.00
    1st Qu.:1387
                    1st Qu.:210.0
                                     1st Qu.: 35.00
                                                       1st Qu.: 44.50
    Median:1455
                    Median :239.0
                                     Median : 52.00
                                                       Median :101.00
##
##
    Mean
           :1469
                    Mean
                            :241.3
                                     Mean
                                             : 55.91
                                                       Mean
                                                               : 95.63
##
    3rd Qu.:1548
                    3rd Qu.:278.5
                                     3rd Qu.: 72.00
                                                       3rd Qu.:135.50
                           :376.0
                                             :155.00
                                                               :242.00
##
           :2170
                    Max.
                                     Max.
                                                       Max.
##
##
    TEAM BATTING BB TEAM BATTING SO
                                       TEAM BASERUN SB TEAM BASERUN CS
##
           : 15.0
                     Min.
                                 0.0
                                       Min.
                                               : 0.0
                                                        Min.
                                                                : 0.00
##
    1st Qu.:436.5
                     1st Qu.: 545.0
                                       1st Qu.: 59.0
                                                        1st Qu.: 38.00
    Median :509.0
                     Median: 686.0
                                       Median: 92.0
                                                        Median: 49.50
##
##
    Mean
           :499.0
                             : 709.3
                                       Mean
                                               :123.7
                                                                : 52.32
                     Mean
                                                        Mean
##
    3rd Qu.:565.5
                     3rd Qu.: 912.0
                                       3rd Qu.:151.8
                                                        3rd Qu.: 63.00
##
    Max.
           :792.0
                     Max.
                             :1268.0
                                       Max.
                                               :580.0
                                                        Max.
                                                                :154.00
##
                     NA's
                             :18
                                       NA's
                                               :13
                                                        NA's
                                                                :87
##
    TEAM_BATTING_HBP TEAM_PITCHING_H TEAM_PITCHING_HR TEAM_PITCHING_BB
##
           :42.00
                      Min.
                              : 1155
                                               : 0.0
                                                                 : 136.0
                                                         1st Qu.: 471.0
##
    1st Qu.:53.50
                      1st Qu.: 1426
                                       1st Qu.: 52.0
##
    Median :62.00
                      Median: 1515
                                       Median :104.0
                                                         Median : 526.0
   Mean
##
                                               :102.1
                                                                 : 552.4
           :62.37
                      Mean
                              : 1813
                                       Mean
                                                         Mean
    3rd Qu.:67.50
                      3rd Qu.: 1681
                                       3rd Qu.:142.5
                                                         3rd Qu.: 606.5
##
                                       Max.
##
   Max.
           :96.00
                      Max.
                              :22768
                                               :336.0
                                                         Max.
                                                                 :2008.0
    NA's
           :240
##
##
    TEAM_PITCHING_SO TEAM_FIELDING_E
                                        TEAM_FIELDING_DP
           :
               0.0
                      Min.
                              : 73.0
                                        Min.
                                                : 69.0
    1st Qu.: 613.0
                      1st Qu.: 131.0
                                        1st Qu.:131.0
```

```
## Median: 745.0
                     Median : 163.0
                                      Median :148.0
## Mean
          : 799.7
                     Mean
                            : 249.7
                                      Mean
                                             :146.1
## 3rd Qu.: 938.0
                     3rd Qu.: 252.0
                                      3rd Qu.:164.0
## Max.
           :9963.0
                            :1568.0
                     Max.
                                      Max.
                                             :204.0
## NA's
           :18
                                      NA's
```

First, let's transform and impute the variables in the test data set.

* F-Statistic

The F-statistic is used to measure the significance of one or more variables if they are added to a base model.

The base model is our model with TEAM_BATTING_SO, TEAM_BASERUN_SB, TEAM_BASERUN_CS and TEAM_FIELDING_DP excluded

We compare it with the model with **TEAM_BATTING_SO** and **TEAM_BASERUN_SB** added

```
## Analysis of Variance Table
##
## Model 1: TARGET_WINS ~ (TEAM_BATTING_2B + TEAM_BATTING_3B + TEAM_BATTING_HR +
       TEAM_BATTING_BB + TEAM_BATTING_SO + TEAM_BASERUN_SB + TEAM_BASERUN_CS +
##
##
       TEAM_FIELDING_DP + TEAM_FIELDING_E_Transformed + TEAM_BATTING_1B) -
       TEAM_BATTING_SO - TEAM_BASERUN_SB - TEAM_BASERUN_CS - TEAM_FIELDING_DP
## Model 2: TARGET_WINS ~ (TEAM_BATTING_2B + TEAM_BATTING_3B + TEAM_BATTING_HR +
       TEAM_BATTING_BB + TEAM_BATTING_SO + TEAM_BASERUN_SB + TEAM_BASERUN_CS +
##
       TEAM_FIELDING_DP + TEAM_FIELDING_E_Transformed + TEAM_BATTING_1B) -
##
##
       TEAM_BASERUN_CS - TEAM_FIELDING_DP
##
     Res.Df
               RSS Df Sum of Sq
                                          Pr(>F)
## 1
       2269 417514
      2267 406375
                          11138 31.068 4.885e-14 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

The F-value with degree of freedom 2 is 31.068, indicating that adding **TEAM_BATTING_SO** and **TEAM_BASERUN_SB** does make an improvement to the model.

Next use our improved model as our new base model check if adding **TEAM_FIELDING_DP** will make another improvement.

```
## Analysis of Variance Table
## Model 1: TARGET_WINS ~ (TEAM_BATTING_2B + TEAM_BATTING_3B + TEAM_BATTING_HR +
       TEAM_BATTING_BB + TEAM_BATTING_SO + TEAM_BASERUN_SB + TEAM_BASERUN_CS +
##
##
       TEAM_FIELDING_DP + TEAM_FIELDING_E_Transformed + TEAM_BATTING_1B) -
##
       TEAM_BASERUN_CS - TEAM_FIELDING_DP
## Model 2: TARGET_WINS ~ (TEAM_BATTING_2B + TEAM_BATTING_3B + TEAM_BATTING_HR +
       TEAM_BATTING_BB + TEAM_BATTING_SO + TEAM_BASERUN_SB + TEAM_BASERUN_CS +
##
       TEAM_FIELDING_DP + TEAM_FIELDING_E_Transformed + TEAM_BATTING_1B) -
##
       TEAM BASERUN CS
##
              RSS Df Sum of Sq
##
    Res.Df
                                          Pr(>F)
## 1
       2267 406375
## 2
      2266 389014 1
                         17362 101.13 < 2.2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

The result shows that the effect of **TEAM_FIELDING_DP** is significant Last, let's check if adding **TEAM_BASERUN_CS** will help

```
## Analysis of Variance Table
## Model 1: TARGET_WINS ~ (TEAM_BATTING_2B + TEAM_BATTING_3B + TEAM_BATTING_HR +
       TEAM_BATTING_BB + TEAM_BATTING_SO + TEAM_BASERUN_SB + TEAM_BASERUN_CS +
##
       TEAM_FIELDING_DP + TEAM_FIELDING_E_Transformed + TEAM_BATTING_1B) -
       TEAM BASERUN CS
##
## Model 2: TARGET_WINS ~ TEAM_BATTING_2B + TEAM_BATTING_3B + TEAM_BATTING_HR +
       TEAM_BATTING_BB + TEAM_BATTING_SO + TEAM_BASERUN_SB + TEAM_BASERUN_CS +
##
       TEAM_FIELDING_DP + TEAM_FIELDING_E_Transformed + TEAM_BATTING_1B
##
##
    Res.Df
               RSS Df Sum of Sq
                                     F Pr(>F)
       2266 389014
## 1
                         46.862 0.2729 0.6015
       2265 388967 1
```

The variable **TEAM_BASERUN_CS** insignificant as we have checked before using the p-value of the coefficient.