# DATA 621 HW3

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train\_df <- read.csv("https://raw.githubusercontent.com/ezaccountz/DATA\_621/main/HW3/crime-training-dat
test\_df <- read.csv("https://raw.githubusercontent.com/ezaccountz/DATA\_621/main/HW3/crime-evaluation-dat</pre>

## DATA EXPLORATION

# \* Data Summary

#### summary(train\_df)

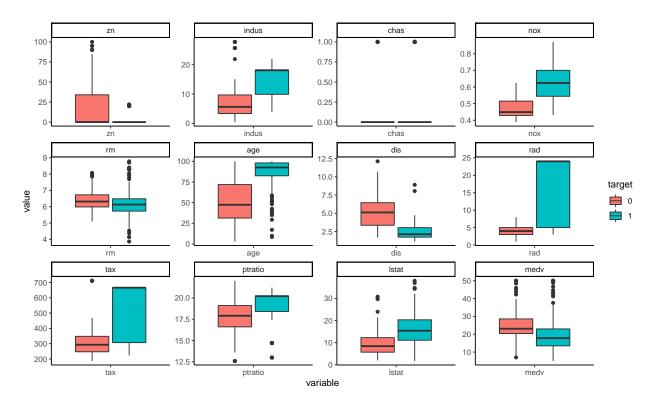
```
##
                          indus
          zn
                                             chas
                                                               nox
    Min.
           : 0.00
                     Min.
                             : 0.460
                                       Min.
                                              :0.00000
                                                          Min.
                                                                 :0.3890
    1st Qu.:
              0.00
                     1st Qu.: 5.145
                                       1st Qu.:0.00000
                                                          1st Qu.:0.4480
##
    Median: 0.00
                     Median : 9.690
                                       Median :0.00000
                                                          Median :0.5380
##
   Mean
          : 11.58
                     Mean
                            :11.105
                                       Mean
                                              :0.07082
                                                          Mean
                                                                 :0.5543
    3rd Qu.: 16.25
                     3rd Qu.:18.100
                                       3rd Qu.:0.00000
                                                          3rd Qu.:0.6240
##
    Max.
           :100.00
                     Max.
                             :27.740
                                       Max.
                                              :1.00000
                                                          Max.
                                                                  :0.8710
##
                                           dis
          rm
                          age
                                                             rad
##
   Min.
           :3.863
                    Min.
                           : 2.90
                                      Min.
                                             : 1.130
                                                        Min.
                                                              : 1.00
    1st Qu.:5.887
                    1st Qu.: 43.88
                                      1st Qu.: 2.101
                                                        1st Qu.: 4.00
    Median :6.210
                    Median : 77.15
                                      Median : 3.191
                                                        Median: 5.00
##
   Mean
           :6.291
                    Mean
                           : 68.37
                                      Mean
                                            : 3.796
                                                        Mean
                                                              : 9.53
    3rd Qu.:6.630
                    3rd Qu.: 94.10
                                      3rd Qu.: 5.215
                                                        3rd Qu.:24.00
##
    Max.
           :8.780
                            :100.00
                                      Max.
                                             :12.127
                                                        Max.
                                                               :24.00
                    Max.
                       ptratio
##
         tax
                                        lstat
                                                           medv
##
                                           : 1.730
   Min.
           :187.0
                    Min.
                            :12.6
                                    Min.
                                                      Min.
                                                             : 5.00
    1st Qu.:281.0
                    1st Qu.:16.9
                                    1st Qu.: 7.043
                                                      1st Qu.:17.02
   Median :334.5
##
                    Median:18.9
                                    Median :11.350
                                                      Median :21.20
    Mean
           :409.5
##
                    Mean
                            :18.4
                                    Mean
                                           :12.631
                                                      Mean
                                                             :22.59
##
    3rd Qu.:666.0
                    3rd Qu.:20.2
                                    3rd Qu.:16.930
                                                      3rd Qu.:25.00
##
    Max.
           :711.0
                    Max.
                            :22.0
                                    Max.
                                           :37.970
                                                      Max.
                                                             :50.00
##
        target
##
  Min.
           :0.0000
   1st Qu.:0.0000
## Median :0.0000
   Mean
           :0.4914
##
    3rd Qu.:1.0000
## Max.
           :1.0000
```

#### From the summary:

- We see that there is **no missing value**
- All numeric variables, except **zn**, the max value is not significantly off from the third quartile. This indicates that they have no extream outliers. We will need to look at the distribution of **zn** to check the outliers.

## \* Box Plots

```
data.m <- melt(train_df, id.vars = 'target')%>% mutate(target = as.factor(target))
ggplot(data.m, aes(x = variable, y = value, fill = target)) + geom_boxplot() +
facet_wrap(~ variable, scales = 'free') + theme_classic()
```



From the boxplots, the following predictors seem to be good candidates differentiating target = 0 and target = 1: \*  $\mathbf{zn}$  \*  $\mathbf{indus}$  \*  $\mathbf{nox}$  \*  $\mathbf{age}$  \*  $\mathbf{dis}$  \*  $\mathbf{rad}$  \*  $\mathbf{tax}$ 

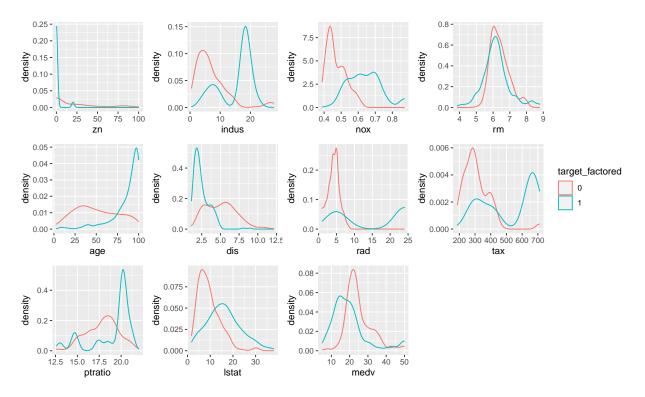
Most of the predictors seem to have a different distribution for target = 0 and target = 1. Let's check the distributions of the predictors:

# \* Distribution plots

```
target_factored <- as.factor(train_df$target)

plot_zn <- ggplot(train_df, aes(x=zn, color=target_factored)) + geom_density()
plot_indus <- ggplot(train_df, aes(x=indus, color=target_factored)) + geom_density()
plot_nox <- ggplot(train_df, aes(x=nox, color=target_factored)) + geom_density()</pre>
```

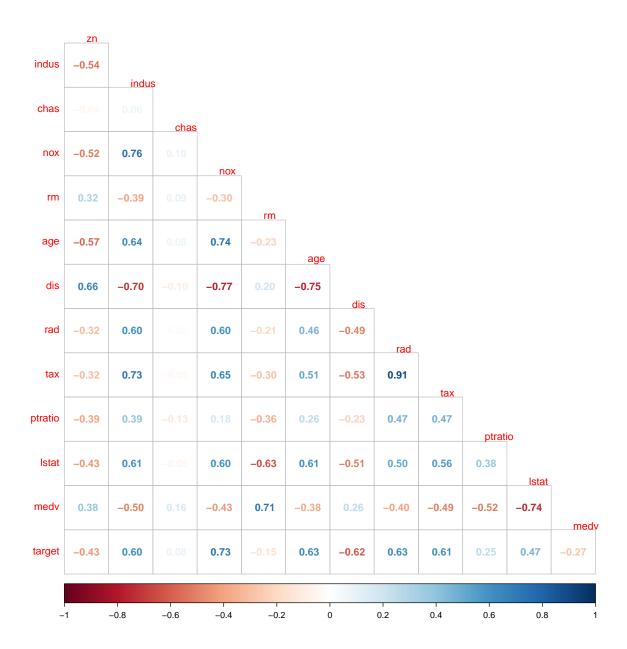
```
plot_rm <- ggplot(train_df, aes(x=rm, color=target_factored)) + geom_density()
plot_age <- ggplot(train_df, aes(x=age, color=target_factored)) + geom_density()
plot_dis <- ggplot(train_df, aes(x=dis, color=target_factored)) + geom_density()
plot_rad <- ggplot(train_df, aes(x=rad, color=target_factored)) + geom_density()
plot_tax <- ggplot(train_df, aes(x=tax, color=target_factored)) + geom_density()
plot_prtatio <- ggplot(train_df, aes(x=ptratio, color=target_factored)) + geom_density()
plot_lstat <- ggplot(train_df, aes(x=lstat, color=target_factored)) + geom_density()
plots_medv <- ggplot(train_df, aes(x=medv, color=target_factored)) + geom_density()
plot_zn+plot_indus+plot_nox+plot_rm+plot_age+plot_dis+plot_rad+plot_tax+
    plot_prtatio+plot_lstat+plots_medv+plot_layout(ncol = 4, guides = "collect")</pre>
```



zn is zero-inflated for target = 1. We may want to add or transform it into a dummy variable indicating zn is greater than 0 or not. **lstat** and medv are right-skewed for both target = 0 and target = 1, we may consider a log-transformation. For other numeric variables, we may check later if transformations are needed.

### \* Correlations

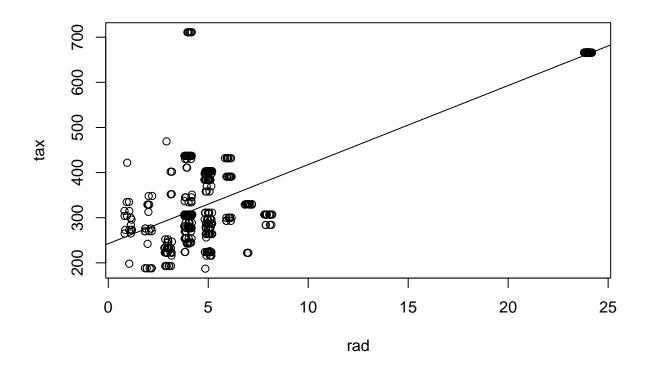
Now let's look at the correlations between the variables



We see that  ${f rad}$  and  ${f tax}$  have strong correlation.

Let's take a look at the linear plot of the two variables

```
plot(jitter(train_df$rad), jitter(train_df$tax), xlab="rad", ylab="tax")
abline(lm (train_df$tax ~ train_df$rad))
```



We can see that the correlation is strongly influenced by one point, where rad = 24.

Without rad, the correlation is only,

```
cor(train_df[train_df$rad < 20,"rad"],train_df[train_df$rad < 20,"tax"])</pre>
```

## [1] 0.1799913

In this case, we will not remove **rad** or **tax** from our model, but we will need to be cautious of the t-statistics of the two in our models.

# DATA PREPARATION

From the density plot of **zn**, we know that the variable is zero-inflated. The percentage of 0 values is

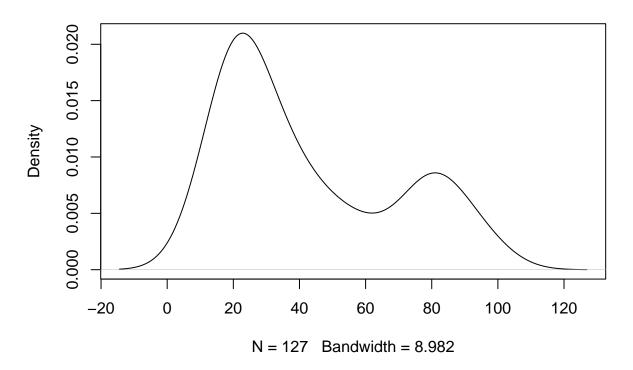
```
nrow(train_df[train_df$zn==0,])/nrow(train_df)
```

## [1] 0.7274678

Let's check the distribution of the  ${\bf zn}$  without the 0 values

```
plot(density(train_df[train_df$zn>0,]$zn,na.rm=TRUE), main = "zn > 0")
```

### zn > 0



The distribution looks a lot better.

We will add a new dummy variable  $zn_y$  indicating if zn is >0. The interaction  $zn_x zn_y = zn$  so we don't need to do anything to it. If  $zn_y$  is deemed to be insignificant by our models, then we can simply drop it.

```
train_df$zn_y <- 0
train_df$zn_y[train_df$zn>0] <- 1</pre>
```

According to the text book A Modern Approach To Regression With R, "when the predictor variable X has a Poisson distribution, the log odds are a linear function of x". Let's check if any of the predictors follows a Poisson distribution

#Method of possion distribution test is from https://stackoverflow.com/questions/59809960/how-do-i-know
#two tail test
p\_poisson <- function(x) {
 return (1-2 \* abs((1 - pchisq((sum((x - mean(x))^2)/mean(x)), length(x) - 1))-0.5))
}

predictors <- colnames(train\_df)
predictors <- predictors[!predictors %in% c("target","chas","zn\_y")]

data.frame(mean\_target0 = round(apply(train\_df[train\_df\$target==0,predictors],2,mean),2),
 variance\_target0 = round(apply(train\_df[train\_df\$target==0,predictors],2,var),2),
 p\_poisson\_target0 = round(apply(train\_df[train\_df\$target==0,predictors],2,p\_poisson),2),
 mean\_target1 = round(apply(train\_df[train\_df\$target==1,predictors],2,mean),2),</pre>

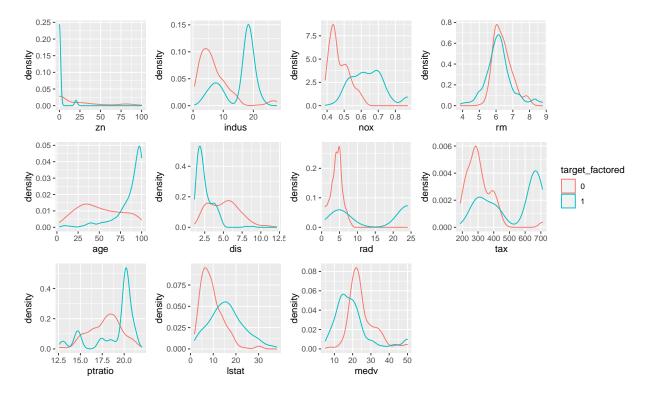
```
variance_target1 = round(apply(train_df[train_df$target==1,predictors],2,var),2),
p_poisson_target1 = round(apply(train_df[train_df$target==1,predictors],2,p_poisson),2))
```

```
##
           mean_target0 variance_target0 p_poisson_target0 mean_target1
## zn
                                    850.75
                                                          0.00
                                                                       15.31
                    7.04
                                     30.27
                                                          0.00
## indus
                    0.47
                                      0.00
                                                          0.00
                                                                        0.64
## nox
## rm
                    6.40
                                       0.31
                                                          0.00
                                                                        6.18
                   50.84
                                    665.13
                                                          0.00
                                                                       86.50
## age
                                       4.27
                                                          0.07
                                                                        2.47
## dis
                    5.08
                    4.17
                                       2.54
                                                          0.00
                                                                       15.07
## rad
                                                          0.00
## tax
                  308.75
                                   7956.24
                                                                      513.77
## ptratio
                   17.86
                                      3.35
                                                          0.00
                                                                       18.96
                    9.36
                                     23.86
                                                          0.00
                                                                       16.02
## 1stat
                                                          0.00
                                                                       20.05
## medv
                   25.04
                                     53.83
##
           variance_target1 p_poisson_target1
## zn
                       25.28
## indus
                       29.28
                                               0
## nox
                        0.01
                                               0
                                               0
## rm
                         0.66
                      297.90
                                               0
## age
## dis
                         1.16
                                               0
                                               0
## rad
                       90.53
## tax
                    27786.70
                                               0
                        5.75
                                               0
## ptratio
                       55.52
                                               0
## lstat
## medv
                                               0
                      105.65
```

The null hypothesis in the tests is that the variable follows a poision distribution. Based on the p-values, we reject the null hypothesis for all predictors. None of the predictors follows a poisson distribution for both target = 0 and target = 1

Let's look at the distributions plots again.

```
plot_zn+plot_indus+plot_nox+plot_rm+plot_age+plot_dis+plot_rad+plot_tax+
    plot_prtatio+plot_lstat+plots_medv+plot_layout(ncol = 4, guides = "collect")
```



The distributions for rm with target = 0 and target = 1 are approximately normal with the same variance. Hence would not transform the variable The distributions for lstat and medv are skewed for both target = 0 and target = 1, we will add a log-transformed variable for each of them.

```
train_df$log_lstat <- log(train_df$lstat)
train_df$log_medv <- log(train_df$medv)</pre>
```

The distributions for indus, nox, age, dis, tax, ptratio look significantly different for the target values. Let perform a anova tests on the single predictor models to see if adding a log transformed or a quadratic transformed variable will improve the performance.

#### Quadratic transformation test:

```
model_compare[i,3] <- anova_test$Df[2]
model_compare[i,4] <- round(anova_test$Deviance[2],2)
model_compare[i,5] <- round(anova_test$`Pr(>Chi)`[2],6)
}
model_compare
```

```
##
                                        model_2 Diff_DF Diff_Deviance Pr_Gt_Chi
            model_1
## 1
      target~indus
                        target~indus+I(indus^2)
                                                                31.13 0.000000
                                                      1
                                                                 0.29 0.587879
## 2
        target~nox
                            target~nox+I(nox^2)
                                                      1
## 3
        target~age
                            target~age+I(age^2)
                                                      1
                                                                 7.63 0.005748
## 4
        target~dis
                            target~dis+I(dis^2)
                                                      1
                                                                 3.64 0.056401
## 5
                            target~tax+I(tax^2)
         target~tax
                                                                 0.44 0.505781
                                                                98.71 0.000000
## 6 target~ptratio target~ptratio+I(ptratio^2)
                                                      1
```

#### Log transformation test:

```
predictors <- c("indus", "nox", "age", "dis", "tax", "ptratio")</pre>
n <- length(predictors)</pre>
model_compare <- data.frame(</pre>
    model_1 = paste0("target~",predictors),
    model_2 = paste0("target~",predictors,"+I(log(",predictors,"))"),
    Diff_DF = rep(0,n),
    Diff Deviance = rep(0.0000,n),
    Pr_Gt_Chi = rep(0.0000,n)
)
for (i in (1:n)) {
    test_model_1 <- glm(target~train_df[,predictors[i]],family = binomial, train_df)</pre>
    test_model_2 <- glm(target~train_df[,predictors[i]]+</pre>
                            I(log(train_df[,predictors[i]])), family = binomial, train_df)
    anova_test <- anova(test_model_1,test_model_2,test="Chi")</pre>
    model_compare[i,3] <- anova_test$Df[2]</pre>
    model_compare[i,4] <- round(anova_test$Deviance[2],2)</pre>
    model_compare[i,5] <- round(anova_test$`Pr(>Chi)`[2],6)
}
model_compare
```

```
##
                                           model_2 Diff_DF Diff_Deviance Pr_Gt_Chi
           model 1
      target~indus
## 1
                        target~indus+I(log(indus))
                                                                   13.91 0.000192
                                                         1
## 2
                            target~nox+I(log(nox))
                                                                    0.63 0.427570
         target~nox
                                                         1
                            target~age+I(log(age))
## 3
        target~age
                                                         1
                                                                    6.37 0.011603
## 4
         target~dis
                            target~dis+I(log(dis))
                                                         1
                                                                    5.15 0.023182
         target~tax
                            target~tax+I(log(tax))
                                                         1
                                                                    1.00 0.317895
## 6 target~ptratio target~ptratio+I(log(ptratio))
                                                                   98.09 0.000000
                                                         1
```

For indus, the improvement is bigger by adding the squared term. For ptratio, since the distribution is left-skewed, it may be better to add the squared term. For other variables, no transformation is added.

```
train_df$indus_squared <- train_df$indus^2
train_df$ptratio_squared <- train_df$ptratio^2</pre>
```

#### Interaction term test:

**chas** is a dummy variable. We will perform a anova tests on the single predictor models to see if adding an interaction between **chas** and a predictor will improve the model.

interaction\_test

```
##
     Preditor Interaction Pr_Gt_Chi
## 1
                   zn:chas
                              0.0645
           zn
        indus indus:chas
## 2
                               0.954
## 3
          nox
                  nox:chas
                              0.6638
## 4
                  rm:chas
                              0.6647
           rm
## 5
                  age:chas
                              0.0719
          age
                              0.0681
## 6
          dis
                  dis:chas
## 7
                  rad:chas
                              0.0191
          rad
## 8
                   tax:chas
                                   0
          tax
## 9
      ptratio ptratio:chas
                              0.3917
## 10
         lstat
                lstat:chas
                              0.1006
## 11
                 medv:chas
                              0.1555
         medv
```

From the result, we will add an interaction between **tax** and **chas** and an interaction between **rad** and **chas** to our preditor candidates.

```
train_df$tax_chas <- train_df$tax * train_df$chas
train_df$rad_chas <- train_df$rad * train_df$chas</pre>
```

## BUILD MODELS

#### \* 1. Full model:

The full model includes all original and the transformed verson of the predictors

```
full_model <- glm(target~.,family = binomial, train_df)</pre>
#store the model formulas for building models for cross validation
model_formulas <- c(paste(deparse(formula(full_model), width.cutoff = 500), collapse=""))</pre>
summary(full_model)
##
## glm(formula = target ~ ., family = binomial, data = train_df)
## Deviance Residuals:
      Min
                 10
                     Median
                                   3Q
                                           Max
## -2.6227 -0.0932
                     0.0000
                               0.0001
                                        3.7950
##
## Coefficients:
##
                     Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                    5.352e+01 2.666e+01
                                           2.008 0.044688 *
                    1.010e-02 3.979e-02
                                           0.254 0.799658
## zn
## indus
                   1.342e+00 4.258e-01
                                           3.152 0.001623 **
## chas
                   -7.255e+02 5.172e+04
                                         -0.014 0.988806
                   3.688e+01 8.993e+00
                                           4.100 4.13e-05 ***
## nox
## rm
                  -1.801e+00 9.893e-01 -1.820 0.068699 .
## age
                   3.642e-02 1.562e-02
                                           2.332 0.019712 *
                   6.235e-01 2.946e-01
                                           2.116 0.034323 *
## dis
                   1.219e+00 3.188e-01
                                           3.824 0.000131 ***
## rad
## tax
                  -2.145e-02 7.854e-03 -2.731 0.006311 **
## ptratio
                  -6.900e+00 2.303e+00 -2.996 0.002732 **
## 1stat
                   2.391e-01 1.681e-01
                                           1.422 0.154981
## medv
                   5.679e-01 2.286e-01
                                           2.484 0.012980 *
## zn_y
                  -2.085e+00 1.398e+00 -1.491 0.136052
## log_lstat
                  -3.186e+00 2.269e+00
                                         -1.404 0.160181
## log_medv
                   -8.051e+00 4.937e+00
                                          -1.631 0.102965
## indus_squared
                  -4.242e-02 1.329e-02 -3.191 0.001418 **
## ptratio_squared 2.027e-01 6.390e-02
                                           3.172 0.001516 **
## tax_chas
                   2.868e+00 2.052e+02
                                           0.014 0.988849
## rad_chas
                   -1.707e+01 1.429e+03 -0.012 0.990469
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 645.88 on 465
                                     degrees of freedom
## Residual deviance: 148.14 on 446 degrees of freedom
## AIC: 188.14
##
## Number of Fisher Scoring iterations: 22
```

### \* 2. Backward Elimination by AIC:

Starting with our full model, perform backward elimination by comparing the AIC of the models.

The result model is:

```
summary(model_AIC)
```

```
##
## Call:
##
  glm(formula = target ~ indus + chas + nox + rm + age + dis +
       rad + tax + ptratio + lstat + medv + zn_y + log_lstat + log_medv +
##
       indus_squared + ptratio_squared + tax_chas, family = binomial,
##
       data = train_df)
##
## Deviance Residuals:
##
      Min
                 10
                     Median
                                   3Q
                                           Max
## -2.6018 -0.0948
                     0.0000
                               0.0001
                                        3.7829
##
## Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                    5.453e+01 2.645e+01
                                           2.061 0.039262 *
                    1.325e+00 4.199e-01
## indus
                                           3.156 0.001601 **
## chas
                   -5.397e+03 3.651e+05 -0.015 0.988205
## nox
                   3.637e+01 8.744e+00
                                           4.160 3.18e-05 ***
                   -1.813e+00 9.855e-01 -1.840 0.065813 .
## rm
## age
                   3.602e-02 1.550e-02
                                           2.324 0.020109 *
                   6.136e-01 2.945e-01
                                           2.083 0.037218 *
## dis
                   1.210e+00 3.177e-01
                                           3.810 0.000139 ***
## rad
## tax
                  -2.117e-02 7.793e-03
                                         -2.716 0.006603 **
                  -6.908e+00 2.298e+00
                                         -3.006 0.002649 **
## ptratio
                   2.396e-01 1.684e-01
                                           1.423 0.154768
## lstat
## medv
                   5.748e-01 2.267e-01
                                           2.535 0.011244 *
## zn_y
                  -1.864e+00 1.097e+00
                                         -1.699 0.089327
                  -3.227e+00 2.267e+00
## log_lstat
                                          -1.424 0.154519
## log_medv
                   -8.226e+00 4.900e+00
                                          -1.679 0.093179
## indus_squared
                   -4.183e-02 1.306e-02
                                          -3.202 0.001365 **
## ptratio_squared 2.029e-01 6.378e-02
                                           3.181 0.001468 **
## tax chas
                    1.949e+01 1.318e+03
                                           0.015 0.988204
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
##
       Null deviance: 645.88 on 465
                                     degrees of freedom
## Residual deviance: 148.20 on 448 degrees of freedom
## AIC: 184.2
## Number of Fisher Scoring iterations: 25
```

# \* 3. Backward Elimination with Chi-square test:

Starting with our full model, perform backward elimination with Chi-square test.

```
#Define a function to perform backward elimination with Chi-square test
#using the significancy / alpha as one of the parameters
backward_chi <- function (train_df, significancy) {</pre>
  glm_string <- "target~."</pre>
  glm_formula <- as.formula(glm_string)</pre>
    drop1_chi <- drop1(glm(glm_formula, family=binomial, train_df), test="Chi")</pre>
    chi_result <- data.frame(preditors = rownames(drop1_chi)[-1],</pre>
              p_{value} = drop1_{chi}[-1,5]
    chi_result <- chi_result[order(chi_result$p_value,decreasing=TRUE),]</pre>
    if(chi_result[1,2] < significancy){</pre>
        break
    }
    else {
        glm_string <- paste0(glm_string,"-",chi_result[1,1])</pre>
        glm_formula <- as.formula(glm_string)</pre>
    }
  }
  return(glm_formula)
}
```

#### model with alpha 0.1 (based on Chi-square test)

```
model_chi_0.1 <- backward_chi(train_df, 0.1)
model_formulas <- c(model_formulas, model_chi_0.1)
model_chi_0.1 <- glm(model_chi_0.1, family=binomial, train_df)
summary(model_chi_0.1)
##</pre>
```

```
## Call:
## glm(formula = model_chi_0.1, family = binomial, data = train_df)
## Deviance Residuals:
##
      Min
                1Q Median
                                 3Q
                                         Max
## -2.7406 -0.0828 0.0000 0.0001
                                      3.7127
##
## Coefficients:
##
                    Estimate Std. Error z value Pr(>|z|)
                   5.201e+01 2.542e+01
                                         2.046 0.040793 *
## (Intercept)
## indus
                   1.359e+00 4.286e-01
                                         3.171 0.001521 **
## chas
                  -5.510e+03 3.890e+05 -0.014 0.988699
                  3.631e+01 8.729e+00 4.160 3.18e-05 ***
## nox
                  -1.622e+00 8.247e-01 -1.966 0.049273 *
## rm
                   3.496e-02 1.462e-02
                                         2.391 0.016786 *
## age
## dis
                  6.704e-01 2.935e-01
                                         2.284 0.022385 *
                  1.224e+00 3.178e-01 3.851 0.000118 ***
## rad
                 -2.186e-02 7.821e-03 -2.795 0.005195 **
## tax
```

```
## ptratio
                  -6.725e+00 2.261e+00 -2.974 0.002935 **
                   7.044e-01 2.064e-01
## medv
                                         3.412 0.000645 ***
## zn y
                  -1.858e+00 1.078e+00 -1.724 0.084774 .
## log_medv
                  -1.090e+01 4.489e+00 -2.428 0.015167 *
## indus_squared
                  -4.276e-02 1.335e-02 -3.203 0.001358 **
## ptratio_squared 1.978e-01 6.285e-02
                                          3.148 0.001643 **
## tax chas
                   1.989e+01 1.404e+03
                                         0.014 0.988698
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 645.88 on 465 degrees of freedom
## Residual deviance: 150.31 on 450 degrees of freedom
## AIC: 182.31
##
## Number of Fisher Scoring iterations: 25
model with alpha 0.05 (based on Chi-square test)
model_chi_0.05 <- backward_chi(train_df, 0.05)</pre>
model_formulas <- c(model_formulas, model_chi_0.05)</pre>
model_chi_0.05 <- glm(model_chi_0.05, family=binomial, train_df)</pre>
summary(model_chi_0.05)
##
## Call:
## glm(formula = model_chi_0.05, family = binomial, data = train_df)
##
## Deviance Residuals:
##
       Min
                  1Q
                        Median
                                      3Q
                                               Max
## -2.36990 -0.09297
                       0.00000
                                 0.00003
                                           3.05262
##
## Coefficients:
                    Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                   6.020e+01 2.251e+01 2.674 0.007490 **
## indus
                   1.407e+00 3.722e-01
                                        3.780 0.000157 ***
                  -5.411e+03 2.712e+05 -0.020 0.984082
## chas
## nox
                   3.217e+01 6.979e+00
                                         4.610 4.02e-06 ***
                  -6.657e-01 6.996e-01 -0.952 0.341302
## rm
## rad
                   1.311e+00 2.903e-01
                                         4.517 6.26e-06 ***
                  -2.429e-02 6.625e-03 -3.667 0.000246 ***
## tax
## ptratio
                  -6.620e+00 2.173e+00 -3.046 0.002319 **
                  6.507e-01 2.025e-01
                                         3.212 0.001316 **
## medv
## log medv
                  -1.315e+01 4.484e+00 -2.933 0.003358 **
## indus_squared
                 -4.418e-02 1.160e-02 -3.808 0.000140 ***
## ptratio_squared 1.950e-01 6.093e-02 3.200 0.001375 **
                   1.954e+01 9.790e+02 0.020 0.984078
## tax_chas
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
```

```
Null deviance: 645.88 on 465 degrees of freedom
## Residual deviance: 160.19 on 453 degrees of freedom
## AIC: 186.19
##
## Number of Fisher Scoring iterations: 24
model with alpha 0.001 (based on Chi-square test)
model_chi_0.001 <- backward_chi(train_df, 0.001)</pre>
model_formulas <- c(model_formulas, model_chi_0.001)</pre>
model_chi_0.001 <- glm(model_chi_0.001, family=binomial, train_df)</pre>
summary(model_chi_0.001)
##
## Call:
## glm(formula = model chi 0.001, family = binomial, data = train df)
## Deviance Residuals:
##
        Min
                         Median
                                       3Q
                   10
                                                Max
## -2.30930 -0.10815
                        0.00000
                                  0.00013
                                            2.94594
##
## Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                    3.571e+01 2.051e+01
                                          1.741 0.081663 .
                                           3.256 0.001132 **
                    1.188e+00 3.649e-01
## indus
## chas
                   -5.464e+03 2.914e+05
                                         -0.019 0.985041
                                           4.688 2.76e-06 ***
## nox
                    3.285e+01 7.007e+00
## rm
                   -1.518e-01 6.562e-01 -0.231 0.817100
## rad
                   1.165e+00 2.953e-01
                                           3.947 7.92e-05 ***
## tax
                   -2.195e-02 6.597e-03 -3.327 0.000877 ***
## ptratio
                   -7.218e+00 2.213e+00 -3.262 0.001107 **
                   8.703e-02 6.717e-02
                                           1.295 0.195148
## medv
## indus squared
                   -3.794e-02 1.132e-02
                                         -3.353 0.000801 ***
## ptratio_squared 2.110e-01 6.166e-02
                                           3.421 0.000623 ***
## tax_chas
                    1.973e+01 1.052e+03
                                           0.019 0.985036
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
  (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 645.88 on 465 degrees of freedom
## Residual deviance: 169.78 on 454 degrees of freedom
## AIC: 193.78
## Number of Fisher Scoring iterations: 24
```

### \* 4. Backward Elimination based on the t-values of the coefficients:

Starting with our full model, perform backward elimination based on the t-values of the coefficients.

 $\#Define\ a\ function\ to\ perform\ backward\ elimination\ based\ on\ the\ t-values\ of\ the\ coefficients$   $\#using\ the\ significancy\ /\ alpha\ as\ one\ of\ the\ parameters$ 

```
backward_p <- function (train_df, significancy) {</pre>
  glm_string <- "target~."</pre>
  glm_formula <- as.formula(glm_string)</pre>
  repeat{
    model_p <- glm(glm_formula, family=binomial, train_df)</pre>
    p result <- data.frame(preditors = rownames(summary(model p)$coefficients)[-1],</pre>
              p_value = summary(model_p)$coefficients[-1,4])
    p_result <- p_result[order(p_result$p_value,decreasing=TRUE),]</pre>
    if(p_result[1,2] < significancy){</pre>
        break
    }
    else {
         glm_string <- paste0(glm_string,"-",p_result[1,1])</pre>
         glm_formula <- as.formula(glm_string)</pre>
    }
  }
  return(glm_formula)
```

#### model with alpha 0.05 (based on the t-values of the coefficients)

alpha = 0.1 produces the same model as alpha = 0.05 so alpha = 0.1 is not used here.

```
model_p_0.05 <- backward_p(train_df, 0.05)</pre>
model_formulas <- c(model_formulas, model_p_0.05)</pre>
model_p_0.05 <- glm(model_p_0.05, family=binomial, train_df)</pre>
summary(model_p_0.05)
##
## Call:
## glm(formula = model_p_0.05, family = binomial, data = train_df)
## Deviance Residuals:
##
     Min
          1Q Median
                              3Q
                                    Max
## -2.1811 -0.1348 -0.0043 0.0012
                                  3.7040
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                21.565494 21.025464 1.026 0.305040
                          0.270470
                                   2.423 0.015387 *
## indus
                0.655387
## nox
                32.968725
                         8.347166 3.950 7.83e-05 ***
                0.025691
                         0.011714 2.193 0.028298 *
## age
                0.666502
                         0.266970 2.497 0.012541 *
## dis
                0.900580 0.211886 4.250 2.13e-05 ***
## rad
## tax
                ## ptratio
               -6.272631
                          2.063883 -3.039 0.002372 **
                ## 1stat
               ## medv
```

```
-2.617454
                              1.063343 -2.462 0.013834 *
## zn v
                 -0.021730
                              0.008692 -2.500 0.012414 *
## indus_squared
                               0.056883
## ptratio_squared 0.182663
                                         3.211 0.001322 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 645.88 on 465 degrees of freedom
## Residual deviance: 172.68 on 453 degrees of freedom
## AIC: 198.68
## Number of Fisher Scoring iterations: 9
model with alpha 0.01 (based on the t-values of the coefficients)
model_p_0.01 <- backward_p(train_df, 0.01)</pre>
model_formulas <- c(model_formulas, model_p_0.01)</pre>
model_p_0.01 <- glm(model_p_0.01, family=binomial, train_df)</pre>
summary(model_p_0.01)
##
## Call:
## glm(formula = model_p_0.01, family = binomial, data = train_df)
##
## Deviance Residuals:
##
       Min
                  1Q
                        Median
                                       3Q
                                                Max
## -1.88094 -0.18124 -0.00327
                                 0.00014
                                            2.85404
##
## Coefficients:
                   Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                  34.400490 17.446746
                                         1.972 0.048639 *
## indus
                   0.831323
                              0.282877
                                         2.939 0.003295 **
                             6.347383
## nox
                  29.226546
                                        4.605 4.13e-06 ***
## rad
                   1.132391
                              0.224553 5.043 4.59e-07 ***
                              0.005160 -3.420 0.000626 ***
## tax
                   -0.017648
## ptratio
                   -6.515603
                              1.893531
                                        -3.441 0.000580 ***
## indus_squared
                  -0.026394
                               0.008849 -2.983 0.002857 **
## ptratio_squared 0.188472
                               0.052980 3.557 0.000375 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 645.88 on 465 degrees of freedom
## Residual deviance: 193.89 on 458 degrees of freedom
## AIC: 209.89
## Number of Fisher Scoring iterations: 9
```

model with alpha 0.001 (based on the t-values of the coefficients)

```
model_p_0.001 <- backward_p(train_df, 0.001)</pre>
model_formulas <- c(model_formulas, model_p_0.001)</pre>
model_p_0.001 <- glm(model_p_0.001, family=binomial, train_df)</pre>
summary(model_p_0.001)
##
## Call:
## glm(formula = model_p_0.001, family = binomial, data = train_df)
## Deviance Residuals:
       Min
                   10
                         Median
                                       30
                                                Max
## -1.89721 -0.27798 -0.03997
                                  0.00557
                                             2.55954
##
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -19.867422
                           2.368325 -8.389 < 2e-16 ***
                                       7.877 3.35e-15 ***
               35.633515
                            4.523677
## rad
                 0.637643
                            0.119444
                                       5.338 9.38e-08 ***
## tax
                -0.008146
                            0.002332 -3.493 0.000478 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 645.88 on 465 degrees of freedom
## Residual deviance: 224.47 on 462 degrees of freedom
## AIC: 232.47
## Number of Fisher Scoring iterations: 8
```

## SELECT MODELS

First, let's compare different metrics of all models we have built

```
models <- list(full_model, model_AIC, model_chi_0.1, model_chi_0.05, model_chi_0.001,
               model_p_0.05, model_p_0.01, model_p_0.001)
model_names <- list("full_model", "model_AIC", "model_chi_0.1", "model_chi_0.05",</pre>
                     "model_chi_0.001", "model_p_0.05", "model_p_0.01", "model_p_0.001")
model_compare <- data.frame(</pre>
    model = rep("",length(models)),
    Deviance = rep(0.0000,length(models)),
    AIC = rep(0.0000, length(models)),
    Accuracy = rep(0.0000,length(models)),
    Sensitivity = rep(0.0000,length(models)),
    Specificity = rep(0.0000,length(models)),
    Precision = rep(0.0000,length(models)),
    F1 = rep(0.0000, length(models)),
    AUC = rep(0.0000, length(models)),
    Nagelkerke_R_squared = rep(0.0000,length(models))
)
```

```
for (i in c(1:length(models))) {
  predicted_class <- ifelse(models[[i]]$fitted.values>0.5,1,0)
  confusion_matrix <- confusionMatrix(as.factor(predicted_class),</pre>
                                         as.factor(train_df$target),positive = "1")
  model_compare[i,1] <- model_names[i]</pre>
  model_compare[i,2] <- round(models[[i]]$deviance,4)</pre>
  model compare[i,3] <- models[[i]]$aic</pre>
  model_compare[i,4] <- confusion_matrix$overall[1]</pre>
  model_compare[i,5] <- confusion_matrix$byClass[1]</pre>
  model_compare[i,6] <- confusion_matrix$byClass[2]</pre>
  model_compare[i,7] <- confusion_matrix$byClass[3]</pre>
  model_compare[i,8] <- 2*confusion_matrix$byClass[1]*confusion_matrix$byClass[3]/
                          (confusion_matrix$byClass[1]+confusion_matrix$byClass[3])
  model_compare[i,9] <- auc(roc(train_df$target, models[[i]]$fitted.values))</pre>
  model_compare[i,10] <- (1-exp((models[[i]]$dev-models[[i]]$null)/</pre>
                                        length(models[[i]]$residuals)))/
                                (1-exp(-models[[i]]$null/length(models[[i]]$residuals)))
model_compare
```

```
##
               model Deviance
                                        Accuracy Sensitivity Specificity Precision
## 1
          full_model 148.1421 188.1421 0.9356223
                                                    0.9257642
                                                                0.9451477 0.9422222
## 2
           model_AIC 148.1999 184.1999 0.9356223
                                                    0.9257642
                                                                0.9451477 0.9422222
## 3
       model chi 0.1 150.3125 182.3125 0.9442060
                                                    0.9301310
                                                                0.9578059 0.9551570
     model chi 0.05 160.1878 186.1878 0.9420601
                                                    0.9257642
                                                                0.9578059 0.9549550
## 5 model_chi_0.001 169.7788 193.7788 0.9291845
                                                    0.9213974
                                                                0.9367089 0.9336283
## 6
        model_p_0.05 172.6756 198.6756 0.9227468
                                                    0.9170306
                                                                0.9282700 0.9251101
## 7
        model_p_0.01 193.8917 209.8917 0.9163090
                                                    0.9213974
                                                                0.9113924 0.9094828
## 8
       model_p_0.001 224.4719 232.4719 0.8884120
                                                    0.8384279
                                                                0.9367089 0.9275362
##
            F1
                     AUC Nagelkerke R squared
## 1 0.9339207 0.9854808
                                    0.8752040
## 2 0.9339207 0.9856466
                                    0.8751471
## 3 0.9424779 0.9844306
                                    0.8730647
## 4 0.9401330 0.9814457
                                    0.8632040
## 5 0.9274725 0.9794926
                                    0.8534249
## 6 0.9210526 0.9789030
                                    0.8504315
## 7 0.9154013 0.9747572
                                    0.8279318
## 8 0.8807339 0.9594458
                                    0.7936446
```

Since this is **logistic regression with binary data**, Deviance shouldn't be used to judge a model's goodness of fit. We will mainly use AIC and the accuracy. Depending on the business objective, we may use other metrics such as sensitivity and specificity to compare the models' performance. However, the business objective is not defined here so we simply use the accuracy. The Nagelkerke R squared is a pseudo version of the R squared, since R squared can not be used for generalized linear regression. The Nagelkerke R squared should not be used to judge the goodness of fit of a single model. It can be used to compare the fit of different models.

The result shows that model\_chi\_0.1 has the lowest AIC and best performance in predicting the using the training data. The models produced based the t-values of the coefficients are not doing so well. It is reasonable since some of the predictors have high correlation with each other.

The following is the confusion matrix for our best model model chi 0.1:

```
## Confusion Matrix and Statistics
##
##
             Reference
               0 1
## Prediction
##
            0 227 16
            1 10 213
##
##
##
                  Accuracy: 0.9442
                    95% CI: (0.9193, 0.9632)
##
##
       No Information Rate: 0.5086
       P-Value [Acc > NIR] : <2e-16
##
##
##
                     Kappa: 0.8883
##
##
   Mcnemar's Test P-Value: 0.3268
##
##
               Sensitivity: 0.9301
##
               Specificity: 0.9578
##
            Pos Pred Value: 0.9552
##
            Neg Pred Value: 0.9342
##
                Prevalence: 0.4914
##
            Detection Rate: 0.4571
##
     Detection Prevalence: 0.4785
##
         Balanced Accuracy: 0.9440
##
          'Positive' Class: 1
##
##
```

# \* Cross Validation (5 fold)

Let's perform a cross validation on all the models we have to check if they are doing well with unseen data

```
Accuracy_average = rep(0.0000,length(models)),
AIC_1 = rep(0.0000,length(models)),
AIC_2 = rep(0.0000,length(models)),
AIC_3 = rep(0.0000,length(models)),
AIC_4 = rep(0.0000,length(models)),
AIC_5 = rep(0.0000,length(models)),
AIC_average = rep(0.0000,length(models))))

set.seed(14)
cv_df<-train_df[sample(nrow(train_df)),]
folds <- cut(seq(1,nrow(cv_df)),breaks=5,labels=FALSE)</pre>
```

```
#Perform 5 fold cross validation
for(i in 1:5){
    testIndexes <- which(folds==i,arr.ind=TRUE)</pre>
    testData <- cv_df[testIndexes, ]</pre>
    trainData <- cv_df[-testIndexes, ]</pre>
    for (j in c(1:length(models))) {
        test_model <- glm(model_formulas[[j]], family=binomial, trainData)</pre>
        predicted_class <- ifelse(predict(test_model,testData,type="response")>0.5,1,0)
        confusion_matrix <- confusionMatrix(as.factor(predicted_class),</pre>
                                          as.factor(testData$target), positive = "1")
        model_compare[j,1+i] <- confusion_matrix$overall[1]</pre>
        model_compare[j,7+i] <- test_model$aic</pre>
    }
}
model_compare$model <- unlist(model_names)</pre>
model_compare$Accuracy_average <- apply(model_compare[,c(2:6)],1,mean)</pre>
model_compare$AIC_average <- apply(model_compare[,c(8:12)],1,mean)</pre>
```

The following table shows the accuracy of predictions with the test data and the AICs of the trained model.

# model\_compare

```
##
              model Accuracy_1 Accuracy_2 Accuracy_3 Accuracy_4 Accuracy_5
## 1
         full_model 0.9042553 0.8924731 0.9247312 0.9462366 0.9139785
## 2
          model_AIC 0.9042553 0.8924731 0.9247312 0.9462366 0.9139785
## 3
      model_chi_0.1 0.9042553 0.8817204 0.9247312 0.9462366 0.9139785
## 4
     model_chi_0.05 0.8936170
                                0.9247312 0.9462366 0.9354839 0.9139785
## 5 model_chi_0.001 0.8404255
                                0.9032258 0.9247312 0.9354839
                                                                0.8924731
       model_p_0.05  0.8723404  0.8924731  0.9139785  0.9354839  0.8924731
## 6
       model_p_0.01  0.8936170  0.8817204  0.9032258  0.9462366  0.8817204
## 7
## 8
      model_p_0.001 0.7978723 0.9032258 0.9032258 0.9032258 0.8494624
                        AIC 1
                                 AIC_2
                                          AIC 3
                                                   AIC 4
##
    Accuracy_average
                                                           AIC 5 AIC average
## 1
           0.9163349 138.2636 153.1110 154.1078 165.8600 162.2430
                                                                    154.7171
           0.9163349 134.2647 149.1812 150.1884 161.9548 158.3747
## 2
                                                                    150.7928
           0.9141844 131.6432 151.1524 146.5266 160.1229 156.9649
## 3
                                                                    149.2820
```

```
## 4 0.9228094 136.2853 150.3605 153.8125 159.8476 160.0786 152.0769

## 5 0.8992679 141.4014 157.6030 159.1907 165.3722 164.1969 157.5529

## 6 0.9013498 147.3185 158.6745 157.4345 172.7835 166.4235 160.5269

## 7 0.9013040 156.1461 170.6614 169.5861 178.6296 172.1746 169.4396

## 8 0.8714024 168.8905 192.8978 188.4387 193.8342 190.5635 186.9249
```

model\_AIC and model\_chi\_0.1 have the best performance. Since model\_chi\_0.1 is a simpler model with 15 coefficients, we select model\_chi\_0.1 to be our best model as it is a more parsimonious model

```
length(model_chi_0.1$coefficients) - 1 # -1 for the intercept
```

#### ## [1] 15

```
length(model_AIC$coefficients) - 1  # -1 for the intercept
```

#### ## [1] 17

Let's check our final model again.

```
summary(model_chi_0.1)
```

```
##
## Call:
## glm(formula = model_chi_0.1, family = binomial, data = train_df)
##
## Deviance Residuals:
##
       Min
                 1Q
                     Median
                                   3Q
                                          Max
## -2.7406 -0.0828
                     0.0000
                              0.0001
                                       3.7127
##
## Coefficients:
                    Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                   5.201e+01 2.542e+01
                                          2.046 0.040793 *
## indus
                   1.359e+00 4.286e-01
                                          3.171 0.001521 **
## chas
                   -5.510e+03 3.890e+05 -0.014 0.988699
                   3.631e+01 8.729e+00
                                          4.160 3.18e-05 ***
## nox
## rm
                  -1.622e+00 8.247e-01 -1.966 0.049273 *
## age
                   3.496e-02 1.462e-02
                                          2.391 0.016786 *
## dis
                   6.704e-01 2.935e-01
                                          2.284 0.022385 *
## rad
                   1.224e+00 3.178e-01
                                          3.851 0.000118 ***
## tax
                  -2.186e-02 7.821e-03 -2.795 0.005195 **
## ptratio
                   -6.725e+00 2.261e+00 -2.974 0.002935 **
## medv
                   7.044e-01 2.064e-01
                                          3.412 0.000645 ***
                  -1.858e+00 1.078e+00
                                         -1.724 0.084774 .
## zn_y
## log_medv
                  -1.090e+01 4.489e+00
                                         -2.428 0.015167 *
                   -4.276e-02 1.335e-02
## indus_squared
                                         -3.203 0.001358 **
## ptratio_squared 1.978e-01 6.285e-02
                                          3.148 0.001643 **
## tax_chas
                   1.989e+01 1.404e+03
                                          0.014 0.988698
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
```

```
##
## Null deviance: 645.88 on 465 degrees of freedom
## Residual deviance: 150.31 on 450 degrees of freedom
## AIC: 182.31
##
## Number of Fisher Scoring iterations: 25
```

 $zn\_y$  is not so significant. However, from the distribution plots, zn is has strong ability to differentiate target = 0 and target = 1 when zn is 0. It does poorly when zn is 1. We should keep this in our model.

For **chas** and **tax\_chas**, they are highly correlated since  $tax_chas = 0$  when chas = 0. The percentage of 0 in **chas** is

```
nrow(train_df[train_df$chas == 0,])/nrow(train_df)
```

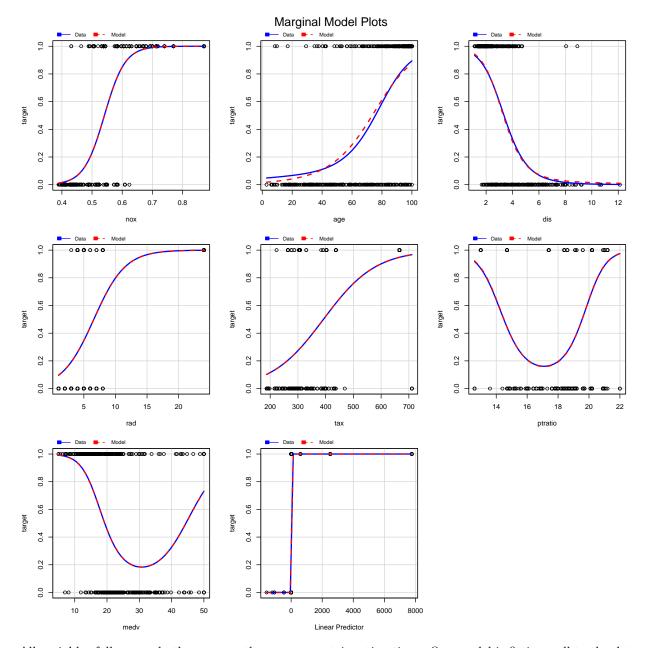
```
## [1] 0.9291845
```

Since they are correlated, we would not judge the two coefficients by the t-value. The Chi-square tests told us that these two variables are important to the model's performance. We will keep **chas** and **tax\_chas** in our model.

# \* model diagnostics

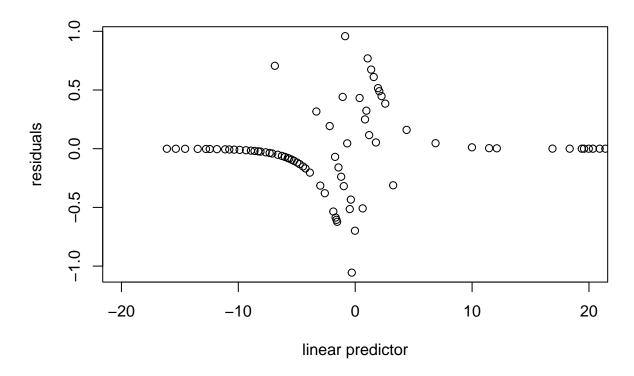
Now let's look at the marginal plots to see if our model is fitting well to the training data

```
marginalModelPlots(model_chi_0.1,~nox+age+dis+rad+tax+ptratio+medv,layout =c(3,3))
```



All variables follow nearly the same as the nonparametric estimations. Our model is fitting well to the data.

### **Residual Plots**



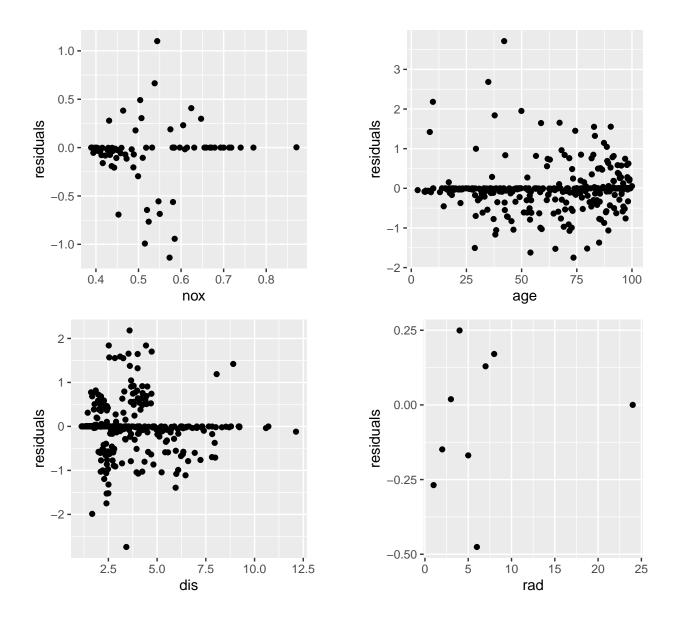
The deviance residual vs linear predictor plot shows that our model is valid. The model is producing accurate predictions at the two ends. The errors around the match point 0 are independent and random.

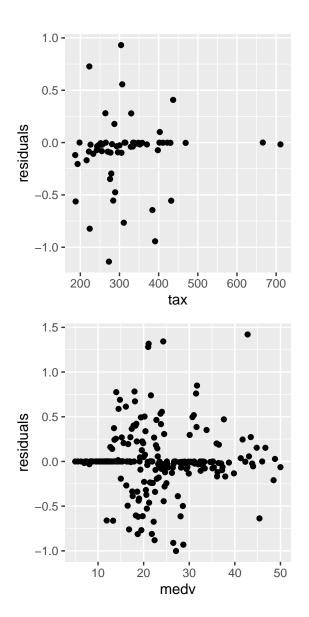
Let's also check the residual plots with individual predictors

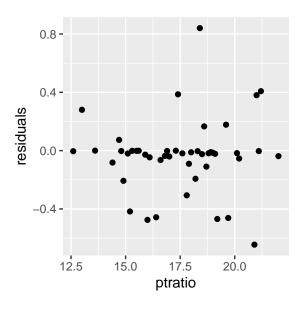
```
predictors <- c("nox", "age", "dis", "rad", "tax", "ptratio", "medv")

residual_df <- mutate(train_df, residuals=residuals(model_chi_0.1, type="deviance"))
gg_plots <- list()

for (i in c(1:length(predictors))) {
    gdf <- group_by(residual_df, .dots = predictors[i])
    diagdf <- summarise(gdf, residuals=mean(residuals))
    print(ggplot(diagdf, aes_string(x=predictors[i], y="residuals")) + geom_point())
}</pre>
```





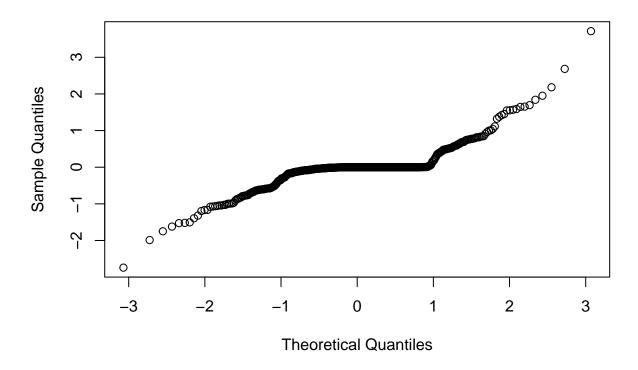


The residuals in each plots are centered at 0, mostly independent and with roughly the same variance, except a few outliers. We conclude that our model does not have notable violation against its validity. The residuals for nox and dis seems to be heteroscedastic. Given this is a logistic regression with binary data, this phenomena is acceptable.

# Q-Q Plot and half normal plot

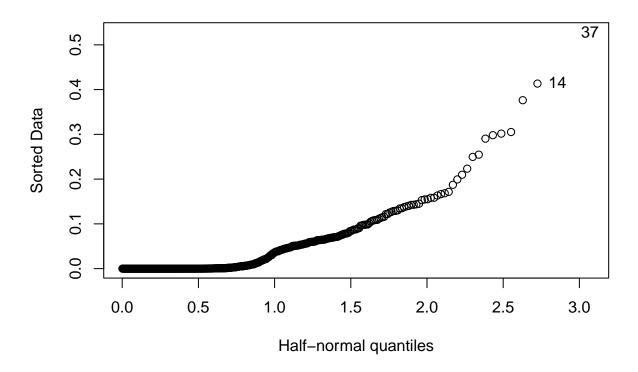
qqnorm(residuals(model\_chi\_0.1))

# Normal Q-Q Plot



The Q-Q plot seems to be fine given it's a logistic regression with binary data

halfnorm(hatvalues(model\_chi\_0.1))



The half normal plots shows case 14 and 37 have high leverage.

By looking at the details of the cases, there is nothing extreme in the values.

```
train_df[c(14,37),]
```

```
##
                                           dis rad tax ptratio lstat medv target zn_y
      zn indus chas
                       nox
                              {\tt rm}
                                   age
## 14 22
          5.86
                   0 0.431 8.259
                                   8.4 8.9067
                                                 7 330
                                                           19.1
                                                                 3.54 42.8
                                                                                 1
                                                                                      1
##
       0
          2.46
                   0 0.488 7.831 53.6 3.1992
                                                 3 193
                                                           17.8
                                                                4.45 50.0
                                                                                      0
##
      log_lstat log_medv indus_squared ptratio_squared tax_chas rad_chas
                                 34.3396
                                                                  0
       1.264127 3.756538
                                                   364.81
                                                                            0
       1.492904 3.912023
                                  6.0516
                                                   316.84
                                                                  0
                                                                            0
```

Additionally, the predicted link values are close to 0, which confirmed they are not outliers. We would keep them in our model training.

```
predict(model_chi_0.1,train_df[c(14,37),], type="link")
```

```
## 14 37
## -0.5557560 -0.8629056
```

# \* Evaluation data prediction

Finally, let's see how our model will predict using the evaluation data set

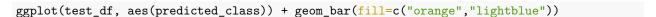
```
test_df$zn_y <- 0
test_df$zn_y[test_df$zn>0] <- 1

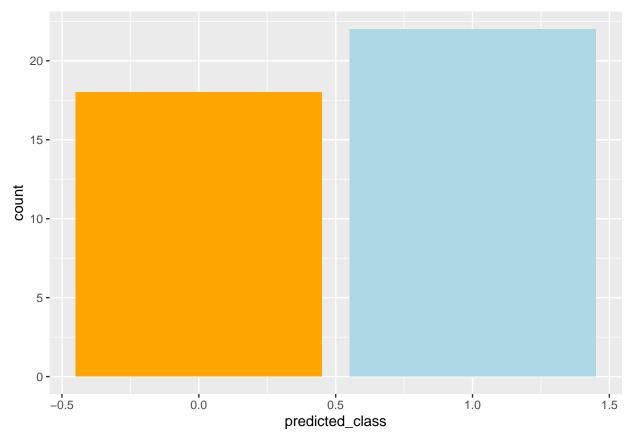
test_df$indus_squared <- test_df$indus^2
test_df$ptratio_squared <- test_df$ptratio^2

test_df$log_lstat <- log(test_df$lstat)
test_df$log_medv <- log(test_df$medv)

test_df$tax_chas <- test_df$tax * test_df$chas
test_df$rad_chas <- test_df$rad * test_df$chas</pre>
```

```
test_df$predicted_class <- ifelse(predict(model_chi_0.1,test_df, type = "response") >0.5,1,0)
```





Both target = 0 and target = 1 are close to 50%, which is a very plausible outcomes. This is the same as we expected since there are 50% of the cases above the median crime rate and 50% of the cases below the median crime rate.