

1. Finite Automata:

- DFA: Deterministic, one path for each input.
- NFA: Non-deterministic, multiple paths.
- epsilon-NFA: Includes epsilon (empty string) transitions.

2. Regular Languages:

- Described using regular expressions.
- Closed under union, concatenation, Kleene star.

3. Context-Free Grammar (CFG):

- Produces context-free languages.
- Used in programming language syntax.

4. Pushdown Automata (PDA):

- Automaton with a stack.
- Recognizes context-free languages.

5. Turing Machine:

- Abstract model of computation.
- Infinite tape, can simulate any algorithm.

6. Decidability:

- Decidable problems have an algorithm.
- Undecidable problems don't (e.g., Halting Problem).

7. Chomsky Hierarchy:

- Type 0: Recursively enumerable (Turing Machines).
- Type 1: Context-sensitive (Linear Bounded Automata).
- Type 2: Context-free (PDA).
- Type 3: Regular (Finite Automata).

8. Regular Expression Identities:

- $(a + b)^* = \text{All strings over } \{a, b\}$
- $a^* = \epsilon + a + aa + aaa + \dots$
- Closure properties: Regular languages closed under:
 - Union, Intersection, Concatenation, Complement, Kleene Star

9. Pumping Lemma:

- Used to prove a language is not regular.
- If a string $s \in L$ and $|s| > p$ (pumping length), then s can be divided into xyz such that:
 - $|xy| \leq p$
 - $|y| > 0$
 - $xy^iz \in L$ for all $i \geq 0$