

//7.1

```
template <typename E>                // base element type
class Position<E> {                  // a node position
public:
    E& operator*();                  // get element
    Position parent() const;         // get parent
    PositionList children() const;   // get node's children
    bool isRoot() const;             // root node?
    bool isExternal() const;         // external node?
};
```

//7.2

```
template <typename E>                // base element type
class Tree<E> {
public:                               // public types
    class Position;                  // a node position
    class PositionList;             // a list of positions
public:                               // public functions
    int size() const;               // number of nodes
    bool empty() const;             // is tree empty?
    Position root() const;          // get the root
    PositionList positions() const; // get positions of all nodes
};
```

//7.4

```
int depth(const Tree& T, const Position& p) {
    if (p.isRoot())
        return 0;                  // root has depth 0
    else
        return 1 + depth(T, p.parent()); // 1 + (depth of parent)
}
```

//7.6

```
int height2(const Tree& T, const Position& p) {
    if (p.isExternal()) return 0; // leaf has height 0
    int h = 0;
    PositionList ch = p.children(); // list of children
    for (Iterator q = ch.begin(); q != ch.end(); ++q)
        h = max(h, height2(T, *q));
}
```

}

```
template <typename E>
```

```
class Position<E> {
```

E& operator*();

Position left() const;

Position right() const;**Position parent() const;**

```
bool isRoot() const;
```

```
bool isExternal() const;
```

}:

```
template <typename E>
```

```
class BinaryTree<E> {
```

public:

```
class Position;
```

```
// a node position
```

```
class PositionList;
```

```
// a list of positions
```

public:

```
// member functions
```

```
int size() const;
```

```
// number of nodes
```

```
bool empty() const;
```

```
// is tree empty?
```

Position root() const;

```
// get the root
```

```
PositionList positions() const;
```

```
// list of nodes
```

}:

```
struct Node {
```

```
// a node of the tree
```

Elem elt;

```
// element value
```

Node* par;

```
// parent
```

Node* left;

```
// left child
```

Node* right;

```
// right child
```

```
Node() : elt(), par(NULL), left(NULL), right(NULL) { } // constructor
```

}:

```
class Position {
```

```
// position in the tree
```

private:

```

    Node* v;                                // pointer to the node
public:
    Position(Node* _v = NULL) : v(_v) { }    // constructor
    Elem& operator*()                        // get element
    { return v->elt; }
    Position left() const                    // get left child
    { return Position(v->left); }
    Position right() const                   // get right child
    { return Position(v->right); }
    Position parent() const                  // get parent
    { return Position(v->par); }
    bool isRoot() const                     // root of the tree?
    { return v->par == NULL; }
    bool isExternal() const                 // an external node?
    { return v->left == NULL && v->right == NULL; }
    friend class LinkedBinaryTree;          // give tree access
};
typedef std::list<Position> PositionList;    // list of positions

```

//7.19

```

typedef int Elem;                            // base element type
class LinkedBinaryTree {
protected:
    // insert Node declaration here...
public:
    // insert Position declaration here...
public:
    LinkedBinaryTree();                      // constructor
    int size() const;                       // number of nodes
    bool empty() const;                     // is tree empty?
    Position root() const;                  // get the root
    PositionList positions() const;         // list of nodes
    void addRoot();                          // add root to empty
tree
    void expandExternal(const Position& p);  // expand external
node
    Position removeAboveExternal(const Position& p); // remove p and parent
    // housekeeping functions omitted...

```



```

        sib->par = NULL;
    }
    else {
        Node* gpar = v->par;                // w's grandparent
        if (v == gpar->left) gpar->left = sib; // replace parent by
sib
        else gpar->right = sib;
        sib->par = gpar;
    }
    delete w; delete v;                    // delete removed
nodes
    n -= 2;                                // two fewer nodes
    return Position(sib);
}

```

//7.23

```

LinkedBinaryTree::PositionList LinkedBinaryTree::positions() const {
    PositionList pl;
    preorder(_root, pl);                    // preorder traversal
    return PositionList(pl);                // return resulting list
}

// preorder traversal
void LinkedBinaryTree::preorder(Node* v, PositionList& pl) const {
    pl.push_back(Position(v));              // add this node
    if (v->left != NULL)                    // traverse left
subtree
        preorder(v->left, pl);
    if (v->right != NULL)                  // traverse right
subtree
        preorder(v->right, pl);
}

```