```
//7.1
template <typename E>
                                  // base element type
 class Position<E> {
                                   // a node position
 public:
   E& operator*();
                                   // get element
   Position parent() const;
                            // get parent
   PositionList children() const; // get node's children
                                  // root node?
   bool isRoot() const;
   bool isExternal() const;
                                // external node?
 };
1/7.2
template <typename E>
                                   // base element type
 class Tree<E> {
 public:
                                    // public types
   class Position:
                             // a node position
   class PositionList:
                                   // a list of positions
 public:
                                   // public functions
                                  // number of nodes
   int size() const;
                                  // is tree empty?
   bool empty() const;
   Position root() const; // get the root
                                         // get positions of all nodes
   PositionList positions() const;
 };
//7.4
int depth(const Tree& T, const Position& p) {
   if (p.isRoot())
     return 0:
                                   // root has depth 0
   else
     return 1 + depth(T, p.parent());// 1 + (depth of parent)
 }
1/7.6
int height2(const Tree& T, const Position& p) {
   if (p.isExternal()) return 0;// leaf has height 0
   int h = 0:
   PositionList ch = p.children(); // list of children
   for (Iterator q = ch.begin(); q != ch.end(); ++q)
     h = max(h, height2(T, *q));
```

```
return 1 + h; // 1 + max height of children
 }
//7.15
                                               // base element type
template <typename E>
 class Position<E> {
                                               // a node position
 public:
   E& operator*();
                                               // get element
   Position left() const;
                                               // get left child
   Position right() const;
                                               // get right child
                                               // get parent
   Position parent() const;
   bool isRoot() const;
                                               // root of tree?
                                               // an external node?
   bool is External() const;
};
//7.16
template <typename E>
                                           // base element type
 class BinaryTree<E> {
                                           // binary tree
 public:
                                           // public types
   class Position:
                                     // a node position
   class PositionList:
                                           // a list of positions
                                           // member functions
 public:
                                           // number of nodes
   int size() const;
   bool empty() const;
                                           // is tree empty?
   Position root() const;
                                           // get the root
   PositionList positions() const;
                                           // list of nodes
 };
//7.17
struct Node {
                                               // a node of the tree
                                                       // element value
     Elem
             elt:
     Node*
              par;
                                                       // parent
     Node* left:
                                                       // left child
     Node*
              right;
                                                       // right child
     Node(): elt(), par(NULL), left(NULL), right(NULL) { } // constructor
   };
//7.18
class Position {
                                               // position in the tree
   private:
```

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Node* v:
                                                        // pointer to the node
   public:
     Position(Node* _v = NULL) : v(_v) \{ \}
                                                       // constructor
     Elem& operator*()
                                                        // get element
       { return v->elt; }
     Position left() const
                                                        // get left child
       { return Position(v->left); }
     Position right() const
                                                        // get right child
       { return Position(v->right); }
     Position parent() const
                                                        // get parent
       { return Position(v->par); }
     bool isRoot() const
                                                        // root of the tree?
       { return v->par == NULL; }
                                                        // an external node?
     bool is External() const
       { return v->left == NULL && v->right == NULL; }
     friend class LinkedBinaryTree;
                                                        // give tree access
   }:
   typedef std::list<Position> PositionList;
                                                       // list of positions
//7.19
typedef int Elem;
                                                       // base element type
 class LinkedBinaryTree {
 protected:
   // insert Node declaration here...
 public:
   // insert Position declaration here...
 public:
   LinkedBinaryTree();
                                                        // constructor
                                                        // number of nodes
   int size() const;
   bool empty() const;
                                                       // is tree empty?
   Position root() const;
                                                       // get the root
   PositionList positions() const;
                                                       // list of nodes
   void addRoot();
                                                       // add root to empty
tree
   void expandExternal(const Position& p);
                                                       // expand external
node
   Position removeAboveExternal(const Position& p);
                                                       // remove p and parent
   // housekeeping functions omitted...
```

```
// local utilities
 protected:
   void preorder(Node* v, PositionList& pl) const;
                                                      // preorder utility
 private:
   Node* _root;
                                                      // pointer to the root
                                                      // number of nodes
   int n:
 };
//7.20
LinkedBinaryTree::LinkedBinaryTree()
                                                      // constructor
   : root(NULL), n(0) { }
 int LinkedBinaryTree::size() const
                                                      // number of nodes
   { return n; }
 bool LinkedBinaryTree::empty() const
                                                      // is tree empty?
   { return size() == 0; }
 LinkedBinaryTree::Position LinkedBinaryTree::root() const // get the root
   { return Position(_root); }
 void LinkedBinaryTree::addRoot()
                                                      // add root to empty
tree
   { _root = new Node; n = 1; }
//7.21
void LinkedBinaryTree::expandExternal(const Position& p) {
   Node* v = p.v;
                                                      // p's node
   v->left = new Node:
                                                              // add a new
left child
   v->left->par = v;
                                                      // v is its parent
   v->right = new Node;
                                                      // and a new right child
                                                      // v is its parent
   v->right->par = v;
   n += 2;
                                                      // two more nodes
 }
//7.22
 Linked Binary Tree :: Position \\
                                                      // remove p and parent
 LinkedBinaryTree::removeAboveExternal(const Position& p) {
   Node* w = p.v; Node* v = w-par;
                                                              // get p's node
and parent
   Node* sib = (w == v->left ? v->right : v->left);
   if (v == _root) {
                                                      // child of root?
     _root = sib;
                                                      // ...make sibling root
```

```
sib->par = NULL;
   else {
     Node* gpar = v->par;
                                                       // w's grandparent
     if (v == gpar->left) gpar->left = sib;
                                                       // replace parent by
sib
     else gpar->right = sib;
     sib->par = gpar;
   delete w; delete v;
                                                       // delete removed
nodes
                                                       // two fewer nodes
   n -= 2;
   return Position(sib);
 }
//7.23
LinkedBinaryTree::PositionList LinkedBinaryTree::positions() const {
 PositionList pl;
                                                       // preorder traversal
 preorder(_root, pl);
 return PositionList(pl);
                                                       // return resulting list
}
                                                       // preorder traversal
void LinkedBinaryTree::preorder(Node* v, PositionList& pl) const {
 pl.push_back(Position(v));
                                                       // add this node
 if (v->left != NULL)
                                                       // traverse left
subtree
   preorder(v->left, pl);
 if (v->right != NULL)
                                                       // traverse right
subtree
   preorder(v->right, pl);
```