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A New Hybrid Machine Learning Method for Stellar Parameter Inference

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ABSTRACT

The advent of machine learning (ML) is revolutionary to numerous scientific disciplines, with a growing number of examples in astronomical spectroscopic inference, as ML is expected to be more powerful than traditional techniques. Here we introduce a hybrid ML (HML) method combining automatic differentiation, interpolation, and Bayesian optimization to infer stellar parameters given stellar spectra. We study T_{eff} , $\log(g)$, and [Fe/H], but this method **could be extended** to other **parameters** such as $[\alpha/\text{Fe}]$ (alpha element abundance), C/O (carbon-oxygen ratio), and f_{sed} (sedimentation efficiency). We first use blase's nontraditional semi-empirical approach, recasting spectra into sets of tunable spectral lines. blase is run on 1,314 spectra from a rectilinear subset of the PHOENIX synthetic spectral model grid ([Fe/H]: [-0.5, 0] dex, T_{eff} : [2300, 12000] K, $\log(g)$: [2, 6], λ : [8038, 12849] Å). For each of the 128,723 lines, we continuously map stellar parameters to spectral line parameters using regular grid linear interpolation. These manifolds are aggregated to create the PHOENIX generator, enabling parallelized reconstruction of spectra given stellar parameters. Gaussian Process minimization is then used to infer stellar parameters by minimizing the root-mean-square (RMS) loss between input and PHOENIX generator spectra. From testing, the inference error in $T_{\rm eff}$ was 185 K, $\log(q)$ was 0.19, and [Fe/H] was 0.12 dex. Our products are an archive of the blase models of the PHOENIX subset, as well as the spectral reconstruction and inference algorithms themselves. This study is a proof of concept showing that semi-empirical HML is a viable alternative to traditional approaches.

1. INTRODUCTION

Stellar spectra are exceedingly rich sources of information about the stars that produce them. Spectra encode fundamental properties such as temperature, surface gravity, and chemical composition via their numerous absorption lines. Extrinsic properties such as the stellar radial velocity or the projected equatorial rotation shift the wavelengths of lines and broaden their widths, respectively. Observing the spectrum alters it again; the resolution, bandwidth, and other properties of the instrument change the fidelity at which we observe the spectrum, and can limit our ability to extract fundamental properties precisely. Observed stellar spectra thus represent extremely complex, data, influenced by multiple parameters, that have gone through multiple transformations before reaching our detectors.

Modern astronomical spectroscopy takes advantage of intuitive, performant spectral models such as

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41 KORG (Wheeler et al. 2023), however it would 42 further benefit from the paradigm of interpretabil-43 ity. The determination of fundamental properties, the 44 creation of Extreme Precision Radial Velocity (EPRV) 45 templates, and the application of composite spectral fit-46 ting could all leverage such an innovation. This am-47 bitious aim may be broadly referred to as a "founda-48 tional spectroscopy model for astrophysics", in reference 49 to the same category of models used for large language 50 models (LLMs) in artificial intelligence (AI). There are 51 many challenges with creating such a foundational spec-52 tral model for astrophysics. Physical inputs into the 53 spectral modeling process are imperfect, and simplify-54 ing assumptions in stellar (and substellar) atmospheres 55 are necessarily inexact due to factors such as asym-56 metries and unknown physics. Computational costs 57 make the training of such models challenging; how-58 ever, advances have been made with attention-59 based (Różański et al. 2023) and transformer-60 based (Leung & Bovy 2024) models, among oth-61 ers. Most prevailing solutions have had to choose ei-62 ther a model driven approach (such as this work), in 63 which precomputed models are taken as gospel, or a data

driven/empirical approach (such as Lux (Horta et al. 2025)), in which our knowledge of stellar physics is ignored or treated phenomenologically, depending on the application. Hybrid solutions exist and have been implemented, such as those presented in Leung & Bovy 2019 and Rains et al. 2024. Although a lingering challenge is always how to ideally balance the fusion of model driven and data driven paradigms.

Spectroscopic surveys such as APOGEE (Majewski et al. 2017) use their own in-house pipelines to ex
tract stellar parameters from spectra (ASPCAP (Gar
fecía Pérez et al. 2016) in the case of APOGEE), and

these pipelines appear effective. The core assumption

for the vast majority of pipelines is that the data to be

analyzed is a list of pixels. Analysis pipelines may be

closed-source or limited to the scope of the survey itself,

causing a sort of siloing effect among surveys. This mo
tivates the development of more universal, instrument
agnostic open-source frameworks that can apply broadly

to a range of spectral observations with relatively little

tuning.

Multiple efforts have been made in this direction, treating spectra in different ways. The standard practice is to treat the wavelength and flux as simply two arrays and use bespoke algorithms tailored to a small number of well-calibrated spectral lines to obtain fundamental stellar parameters and chemical compositions (e.g. the IGRINS YSO Survey (López-Valdivia et al. 2023) and the IRTF Spectral Library (Rayner et al. 2009)). Other whole-spectrum fitting abstractions decompose model spectra into an eigenbasis, implementing the data-model comparison stage as a tractable regression, such as starfish (Czekala et al. 2015).

Ideally, we want a system that can self-consistently 100 learn, a genuine AI foundational spectral model. Such a 101 system would enable the assignment of accurate stellar parameters, and could yield re-usable interpretable spec-103 tral models. blase, first presented in Gully-Santiago 104 & Morley 2022, took an important, albeit limited, step 105 in this direction, treating spectra not as a set of pixels 106 or a set of eigenbasis coefficients but as a set of inter-107 pretable and traceable spectral lines, specifically Voigt profiles. Each of these approaches has tradeoffs, but one 109 key scientific advantage of blase comes from its ability 110 to adapt to new information, while preserving some ad-111 herence to physics-based models. This intelligent capability stems from its ability to fit a theoretically unlim-113 ited number of nonlinear spectral line parameters with 114 automatic differentiation (autodiff). Autodiff is a tech-115 nology that tracks transformations made to data using 116 the chain rule, even being able to differentiate control 117 flow transformations involving if-else blocks, for exam-118 ple. With the gradient obtained from autodiff's chain 119 rule, we can optimize model parameters by just going 120 against the direction of the gradient (because we usu-121 ally want to minimize something such as a loss function, 122 we go in the direction of greatest decrease, which is al-123 ways the negative of the gradient). Autodiff has been 124 used successfully in other astrophysical contexts such as 125 exojax (Kawahara et al. 2022) and wobble (Bedell 126 et al. 2019), but the recasting of spectra into sets of 127 inherently nonlinear spectral lines positions blase as a 128 unique and promising semi-empirical tool. The origi-129 nal blase paper demonstrated the ability to tune spec-130 tral lines with autodiff and 'clone' spectra, recasting 131 them as ML models defined by interpretable sets 132 of tuned spectral lines, however it was restricted 133 to a pre-selected static synthetic model.

Here we introduce the next logical step in the sequence of expanding interpretable spectroscopic machine learning ing from operating on a single grid point and towards an entire 3D grid of precomputed spectra. We rebrand this augmentation as blase3D.

Ideally this process would be monolithic, with the 140 end-to-end spectral inference code powered by a single 141 autodiffable machine learning framework, like PvTorch 142 (Paszke et al. 2019) or JAX (Bradbury et al. 2018). 143 However, here we separate the problem into three pieces, only the first of which is currently differentiable. In section 2, we scale out the blase method to 1,314 precom-146 puted synthetic spectral model clones, yielding a down-147 loadable archive of pretrained machine learning mod-148 els with 128,723 unique spectral lines. In section 3, 149 we then fit manifolds mapping stellar parameters to 150 uniformly-derived spectral line parameters using regular 151 grid linear interpolation. Finally, in section 4, we show 152 how reconstructions of the spectra using said manifolds 153 can be used for inferring stellar fundamental properties 154 from spectra. This final step resembles the aims of "at-155 mospheric retrievals", but in principle should be faster, 156 adaptive, and reusable. An overview of this process is 157 shown in Figure 1.

2. CLONING THE PHOENIX MODEL GRID

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2.1. The PHOENIX Subset

For the purposes of this study, we chose the widely-adopted PHOENIX synthetic spectral model grid (Husser et al. 2013). Our approach can be straightforwardly applied to any other model grid in the future, including substellar atmosphere grids such as Sonora (Marley et al. 2021; Karalidi et al. 2021; Morley et al. 2024; Mukherjee et al. 2024), but for now we limit our

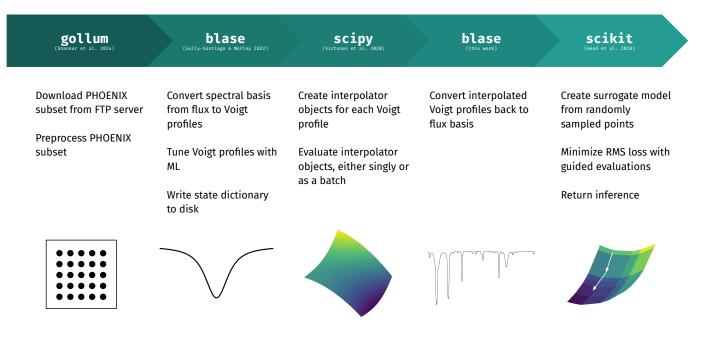


Figure 1. Overview of the process used in this study.

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167 scope to a rectilinear subset of the PHOENIX grid, 168 focusing on near solar metallicities and a broad range of 169 effective temperature and surface gravity, with details 170 given in Table 1. This approach is taken due to the 171 computational cost of interpolation algorithms. 172 Future versions with more advanced models will 173 be able to bypass the limitation of a rectilinear 174 subset.

2.2. Preprocessing with gollum

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First, the PHOENIX subset was programmatically retrieved with gollum (Shankar et al. 2024), which downloaded spectra from the PHOENIX FTP server. The spectra were then put through a three-step preprocessing pipeline similar to that from Gully-Santiago & Morley 2022.

- 1. Blackbody Division: Since the $T_{\rm eff}$ of each spectrum is known, the **corresponding** blackbody spectrum was divided out.
- 2. Percentile Normalization: The spectra were normalized by dividing them by their 99th percentile in order to collapse the dynamic range of flux and only look at relative features.
- 3. Continuum Normalization: The spectra were further normalized by dividing them by a 5^{th} order

polynomial continuum fit using a peak-finding filter in order to eliminate curvature that would inhibit line modeling.

¹⁹⁴ Mathematically, we can express the preprocessing as fol-¹⁹⁵ lows:

$$\bar{\mathsf{S}} = \frac{\mathsf{S}}{\mathsf{BQ}_5 P_{99}} \tag{1}$$

where \bar{S} is the preprocessed spectrum, S is the original spectrum, S is the blackbody spectrum, S is the $n^{\rm th}$ order polynomial continuum fit, and P_n is the $n^{\rm th}$ percentile function. Arithmetic operations between arrays are assumed to be elementwise in all following notation.

2.3. Line Identification with blase

The next step was to convert the PHOENIX subset into a physically interpretable intermediate representation: a table of spectral line properties rather than an array of fluxes. We used blase, which models spectral lines as Voigt profiles and tunes the profiles to mimic the original PHOENIX spectrum with back propagation. Back propagation, put simply, is the process of moving in the autodiff gradient field to update ML model parameters (like mentioned earlier, usually against the gradient because we minimize loss functions). Four parameters were optimized: the line center μ , the log-amplitude $\ln(a)$, the Gaussian width σ , and the Lorentzian width γ .

| Parameter | Symbol | Interval | Sampling |
|-------------------------|-------------------|------------------|--------------------------------|
| Alpha Element Abundance | α | [0] dex | N/A |
| Iron Abundance | $[\mathrm{Fe/H}]$ | [-0.5, 0] dex | $0.5 \mathrm{dex}$ |
| Effective Temperature | $T_{ m eff}$ | [2300, 12000] K | 100 K until 7000 K, then 200 K |
| Surface Gravity | $\log(g)$ | [2, 6] | 0.5 |
| Wavelength | λ | [8038, 12849] Å | $\mathbf{R}=500,000$ |

Table 1. The subset of the PHOENIX grid used in this study. These limits were imposed to reduce the computational cost of the algorithms and to ensure a rectilinear parameter space in order to work with scipy's RegularGridInterpolator (Virtanen et al. 2020). The wavelength limits in particular roughly line up with that of the Habitable Zone Planet Finder (HPF) spectrograph (Mahadevan et al. 2012). This subset is comprised of 1,314 individual spectra: 73 $T_{\rm eff}$ values, 9 $\log(g)$ values, and 2 [Fe/H] values.

²¹⁴ The optimization used the Adam optimizer (Kingma & 215 Ba 2017) with a learning rate of 0.05 over 100 epochs. 216 Gully-Santiago & Morley 2022 recommends this 217 setup as the minimum, and for a proof-of-concept 218 implementation, we found it best to leave it as is. 219 In addition, we limited two custom parameters: wing cut 220 to 6,000 and prominence to 0.005. Wing cut (in pixels) 221 is a parameter that determines the extent of the Voigt 222 profile to evaluate, saving computational resources by 223 not evaluating negligible line wings. Prominence (in 224 normalized flux counts) sets a lower limit for the 225 amplitude of detected lines, which saves resources by 226 disregarding shallow lines, so in our case we disregard $_{227}$ lines with amplitude < 0.05. In short, our choices for 228 wing cut and prominence decrease the computational 229 cost of blase's cloning process at the expense of de-230 creasing its accuracy slightly. blase uses the pseudo-²³¹ Voigt approximation, which saves on computational cost while remaining accurate to about 1% (Ida et al. 2000). The pseudo-Voigt approximation uses a weighted aver-234 age of a Gaussian and Lorentzian as opposed to a con-235 volution. blase's pseudo-Voigt profile implementation 236 uses the following:

$$\tilde{\mathbf{V}}_{\mu}(\lambda) = a \left[\eta \mathbf{L}(\lambda - \mu'; f) + (1 - \eta) \mathbf{G}(\lambda - \mu'; f) \right]$$

$$\eta = \sum_{n=1}^{3} \mathbf{u}_{n} \left(\frac{2\gamma}{f} \right)^{n}$$
(2b)

$$f = 32 \sum_{n=0}^{5} \mathbf{v}_n \left(\sqrt{2 \ln(2)} \sigma \right)^{5-n} (\gamma)^n$$
 (2c)

$$\mathbf{u} = \begin{bmatrix} 1.36603 \\ -0.47719 \\ 0.11116 \end{bmatrix} \quad \mathbf{v} = \begin{bmatrix} 1 \\ 2.69269 \\ 2.42843 \\ 4.47163 \\ 0.07842 \\ 1 \end{bmatrix}$$

²³⁷ where **L** and **G** are abbreviations for Lorentzian and ²³⁸ Gaussian profiles, respectively. Notice that we use μ' ²³⁹ instead of μ in the formula. This is because blase

240 optionally allows the line center to shift slightly dur-241 ing optimization, and it is this shifted center which is 242 used in computation. The individual Voigt profiles are 243 still indexed by μ for cross-model line identification, ex-244 plained in the next section. Once optimization was com-245 plete, the list of identified lines was saved to a 'state 246 dictionary': a common representation for pre-trained 247 machine learning models that can be stored to disk for 248 reuse later. These are stored in the .pt file format for 249 each of the 1,314 PHOENIX subset grid points. The 250 total disk space these files take up is 465 MB (382 MB ²⁵¹ when downloaded as a zip archive). For reference, the 252 storage space the PHOENIX subset takes up on disk is 253 approximately 8.1 GB. This represents a data compres-254 sion factor of around 20 just by recasting the spectrum 255 with blase. The state dictionaries are available on 256 Zenodo at https://zenodo.org/records/11246174 257 (Shankar 2024).

3. INTERPOLATING MANIFOLDS

3.1. Cross-Model Line Identification

As previously mentioned, blase tunes the line centers of detected lines. This means that from one PHOENIX spectrum to the next, the same line could have a slightly different line center. Since the goal of this study is to interpolate the properties of each line, we needed to identify the presence of a particular line across the PHOENIX subset, associating the same line with every occurrence. We decided to do this by using the line centers μ of the detected lines pre-optimization.

Pre-optimized line centers were required to be equal in order to group lines together. The values of μ pre-optimization are recorded by blase to 0.01 Å(picometer) precision; if they instead used the full available floating point precision, this method would likely detect singular (ungroupable) instances of spectral lines across the grid, completely negating the premise of this study. Of course, this method can be confused by species that produce spectral lines at very

279 close wavelengths and other confounding factors, 280 likely resulting in some false positives and nega-281 tives. However, we deem it sufficient to approx-282 imate this way, as an in-depth treatment would 283 be time-consuming and computationally expen-284 sive.

Now with each spectral line indexed by μ , we had four parameters to interpolate: μ' , $\ln(a)$, σ , and γ . Note that since we are dealing with the parameters of Voigt profiles, we can see in Equation 2 that even if the interpolation method is linear, a final spectral reconstruction will vary nonlinearly in flux.

Spectral lines were often only detected in some spectra prom the PHOENIX subset. In Figure 2, we show that different grid points **show** differing counts of detected spectral lines.

The number of detected spectral lines changes as a function of stellar parameter for different reasons. Perhaps for astrophysical reasons: stellar atmospheres genuinely do not produce that line at detectable strength at the given temperature and surface gravity. Alternatively, blase's fitting or our line identification assumptions led to artifacts. Whatever the cause, these missing lines have immediate practical consequences. Rectilinear interpolation schemes break in regions where a line does not appear; you can't interposo late a quantity that simply doesn't exist.

To solve this, we artificially populated missing grid 308 points with log-amplitudes of -1000, which retained interpolator stability while nullifying the evaluated line. 310 Examples of the appearance of missing sections in 311 heatmaps where a line does not appear are shown in Figure 3 and Figure 4. Across the entire PHOENIX subset, blase detected 128,723 spectral lines with unique ₃₁₄ μ . On average, a PHOENIX spectrum has 9,167 315 detected spectral lines, with the minimum being 316 **252** $(T_{\text{eff}} = 12,000, \log(g) = 6, [\text{Fe/H}] = -0.5)$ and 317 the maximum being 34,551 ($T_{\text{eff}} = 2,300, \log(g)$ $_{318} = 3$, [Fe/H] = 0). Every one of these lines can be vi-319 sualized as a manifold mapping a 3D stellar parameter vector to a 4D spectral line parameter vector, and every 321 one was interpolated to map stellar parameters to 323 spectral line properties.

3.2. Continuously Evaluable Manifolds

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For each line, the inputs to the interpolator were the three input parameters $T_{\rm eff}$, $\log(g)$, and [Fe/H], and the output was a list of four parameters, μ' , $\ln(a)$, σ , and For each line, one of these interpolator objects was created using linear interpolation, and these interpolators were aggregated into a single list, which was then written to disk in the .pkl file storage format. These

333 interpolators generate multiple manifolds representing the following mapping:

$$\begin{bmatrix} T_{\text{eff}} \\ \log(g) \\ [\text{Fe/H}] \end{bmatrix} \rightarrow \begin{bmatrix} \mu' \\ \ln(a) \\ \sigma \\ \gamma \end{bmatrix}$$
 (3)

335 These interpolators could now be evaluated at any point 336 lying within the domain of the PHOENIX subset, turn-337 ing a discretely sampled PHOENIX subset into a con-338 tinuously evaluable function, sometimes called a spec-339 tral emulator. With the given size of the PHOENIX 340 subset, the interpolator list takes up 13.2 GB of disk 341 space. This is larger than the original PHOENIX 342 subset by about 63% and than the state dictio-343 nary clone archive by a factor of over 34. This is 344 due to the fact that we are now pickling entire 345 function objects that must memorize the data. 346 Future work with more space-efficient models 347 and clever storage strategies could reduce stor-348 age space requirements in exchange for I/O per-349 formance. This evaluation is able to reconstruct an ex-350 isting PHOENIX spectrum or alternatively interpolate 351 a new spectrum within the domain of the PHOENIX 352 subset, so we call this the PHOENIX generator.

The spectral reconstruction process is done by iterating over the PHOENIX generator, evaluating each insterpolator at the given coordinates, then reshaping the data into the same format that PyTorch uses for state dictionaries. During the iteration, if the interpolated log-amplitude of the line is less than -100, the line is excluded from the state dictionary. We do this to avoid artifacts in the manifolds due to the artifical population of log-amplitudes of -1000 where grid points were missing.

Finally, the state dictionary is fed into blase's
SparseLinearEmulator, which reconstructs the spectrum by constructing a forward model based on the input state dictionary. Any nan values are set to 1 (which
we can do because the spectra are all normalized), and
the spectral reconstruction is complete. We can observe
in Figure 5 that a Fe I line from a reconstructed solar spectrum is not simply a pixel interpolation between
the nearest PHOENIX grid point spectra. It is interpolating the spectral line properties using hundreds
of thousands of manifolds, each representing a nonlinear
parameter in the shape of the spectral line.

3.3. Spectral Reconstruction Time

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A typical use case for the PHOENIX generator may be to batch reconstruct spectra from an array of input stellar parameters. Therefore, there is some motivation

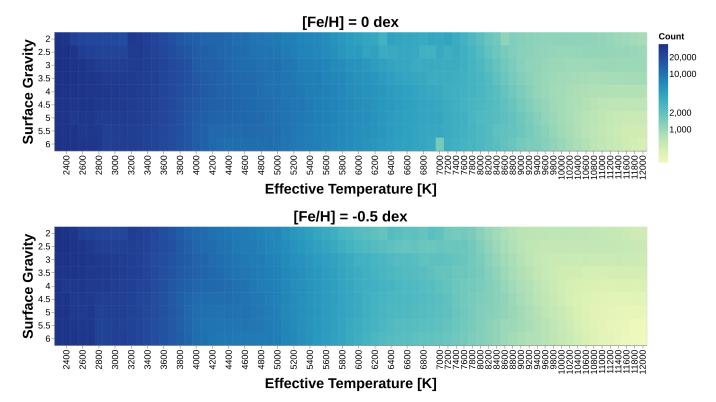


Figure 2. Number of detected spectral lines at each grid point of the PHOENIX subset. We can see that the number of detected lines decreases with increasing $T_{\rm eff}$. Remember that from $T_{\rm eff}=7000~{\rm K}$ onward, PHOENIX's sampling increment changes from 100 K to 200 K. Due to some combination of computational artifacts from our line identification assumptions or innate behavior of PHOENIX grid spectra themselves, outliers such as the obvious one here at $T_{\rm eff}=7000~{\rm K}$ and $\log(g)=6$ appear. Further exploration into why this happens is not in the scope of this study; for inference we are concerned with the lines themselves, not overall grid point behavior.

380 to reduce the computational cost of this procedure to $_{381}$ tractable levels. We evaluate the computational time 382 needed to use the PHOENIX generator in two distinct ways. First, for a single input, which would be relevant 384 in serial applications. Second, for an array of multiple inputs, which would be relevant in parallel applications. 386 scipy's RegularGridInterpolator API allows for the passing in of an entire array of input coordinates to be ³⁸⁸ evaluated at once. However using blase to reconstruct 389 the spectrum from our interpolated state dictionary is 390 always done serially, leading to what is actually more of pseudo-parallel evaluation, but extremely performant 392 nonetheless. Performance results are shown in Figure 6, 393 and we can see that the multi-reconstruction is much faster than a series of single reconstructions. While the 395 generator takes around 15 seconds per spectrum 396 serially, this drops to 1 second per spectrum as 397 soon as 30 reconstructions. The speedup factor between the two methods increases as more spec-399 tra are generated, reaching a factor of 20 at 60 400 reconstructions. The computer used for this test 401 has specifications shown in Table 2 (note that

402 spectral reconstruction does not currently lever-403 age the GPU):

| CPU | AMD EPYC 7513 (32c/64t, 3.65 GHz boost) |
|-----|---|
| RAM | 256 GB |
| GPU | Nvidia A100 40GB (\times 2) |

Table 2. Specifications of the machine used for computations, but not for generating visualizations.

4. BAYESIAN INFERENCE AND TESTING

4.1. Inference Algorithm

The goals of this study's inference algorithm are to infer the stellar parameters $T_{\rm eff}$, $\log(g)$, and [Fe/H] by comparing a spectrum with our reconstructions and solving the optimization problem. We elected to use Bayesian optimization for this component, specifically the gp_minimize function from the scikit-optimize library (Head et al. 2018). This algorithm uses a Gaussian Process to model the objective function, which in this case was the RMS (Root-Mean-Square) loss between the interpolated spectrum M and

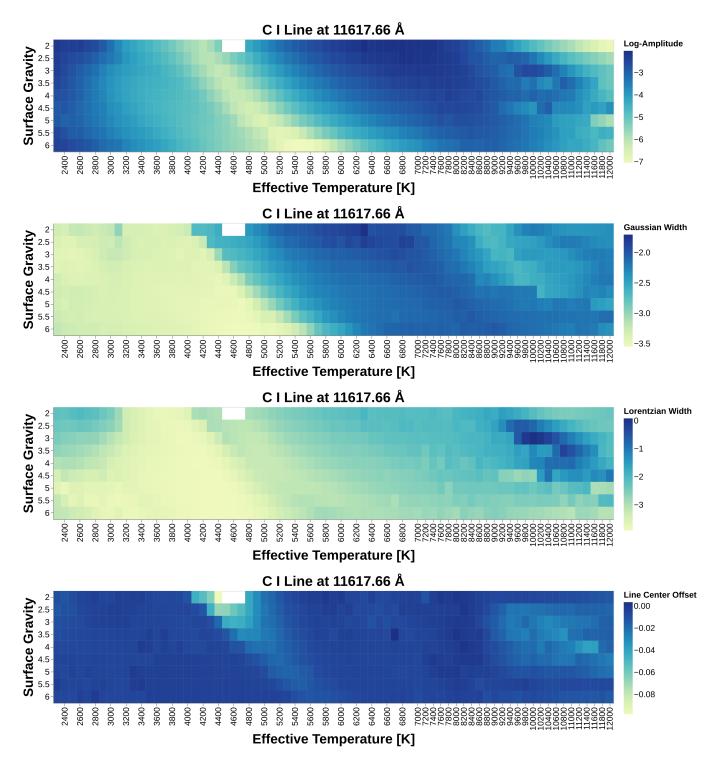


Figure 3. Heatmaps showing how $\ln(a)$, σ , γ , and $\mu' - \mu$ vary over the PHOENIX subset slice at solar metallicity of a **C** I spectral line. Notice the missing chunk in the top left; blase did not detect a spectral line here, so we artificially populate those points with lines that have $\ln(a) = -1000$ during interpolation. This and all spectral lines shown in this paper were identified using the NIST spectral line database (Kramida et al. 2023).

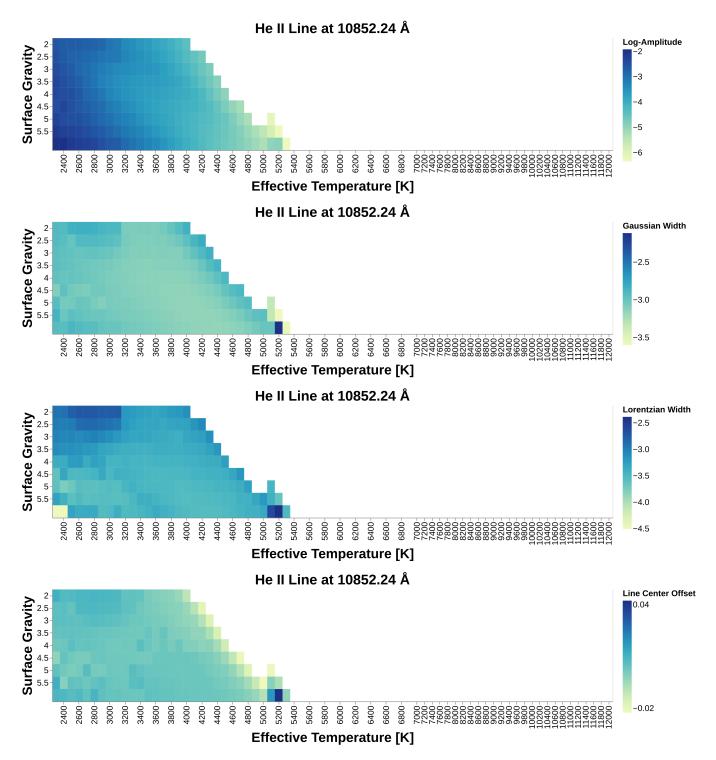


Figure 4. Heatmap showing how $\ln(a)$ and σ vary over the PHOENIX subset slice at solar metallicity of a He II spectral line. We can see that **blase** detects this line at only a select chunk of grid points in PHOENIX, leading to the large amount of missing data for the line.

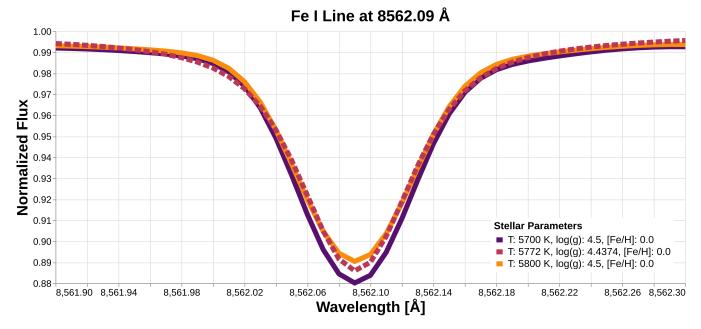


Figure 5. Plot of an Fe I spectral line shown at the closest PHOENIX grid points to the Sun's stellar parameters (solid lines), as well as a solar spectrum reconstructed with the PHOENIX generator (dotted line). We can see the spectral line shape be reconstructed mostly between the two native PHOENIX spectra, being closer to the 5800 K spectrum as the Sun's $T_{\rm eff}$ used here is 5772 K.

418 the true spectrum D, defined as:

$$\mathcal{L} = \left\langle (\mathsf{M} - \mathsf{D})^2 \right\rangle^{1/2} \tag{4}$$

419 The optimizer was configured to first run 100 random 420 evaluations to seed the surrogate model, then run 20 421 more evaluations now guided by the surrogate model. 422 A random evaluation is simply a randomly gen-423 erated tuple of stellar parameters within the 424 parameter space of the PHOENIX generator, 425 which is then evaluated with the generator to 426 get a reconstruction and then compared with the 427 inference target to retrieve its RMS error. The ⁴²⁸ surrogate model is the approximation to the true 429 objective function that the optimizer constructs 430 based on the set of random evaluations (in this case defined by a set of 100 points rather than 432 a fully continuous, infinitely resolved function) 433 Guided evaluations are different, they are not 434 randomly generated tuples of stellar parameters. They use the surrogate model in order to select as new test points for the minimum of the objective function. This totals to 120 evaluations, 100 to cre-438 ate the surrogate model, then 20 guided evaluations, 439 which was deemed sufficient for this study. Fine-tuning 440 these numbers is possible, but simply not warranted for 441 a proof-of concept method. Tweaking these numbers 442 could lead to a more accurate inference, however 443 it would incur additional computational cost as well. One inference run takes on average just under 7.5 minutes to complete.

4.2. Bayesian Optimizer Performance

To test the performance of the inference algorithm,
we used the PHOENIX subset itself. This is possible
for two reasons: first, the PHOENIX generator
has not truly memorized the PHOENIX subset
due to its Voigt profile basis and the ignoring of
weaker features, and secondly, random samples
within the parameter space are extremely unlikely to be PHOENIX grid points themselves,
avoiding any overlap.

We know that in typical observational settings, a coarse estimate for $T_{\rm eff}$ tends to be fairly well-constrained from ancillary data such as photometric color index. So when testing the inference algorithm, we limited its search space to only include $T_{\rm eff}$ which lay within 500 K of the true value on either side. $\log(g)$ and [Fe/H] were allowed to vary freely. The test sample consisted of 9 unique $T_{\rm eff}$ values, 3 unique $\log(g)$ values, and 2 unique [Fe/H] values, totaling 54 unique spectra in the test set. $T_{\rm eff}$ ranged from 3000 K to 11000 K in increments of 1000 K, $\log(g)$ ranged from 2 to 6 in increments of 2, and [Fe/H] ranged from -0.5 to 0 in increments of 0.5.

The results of the inference algorithm are as follows: $_{470}$ $T_{\rm eff}$ differed from the true result by an average of 185 K $_{471}$ or 2.6%. $\log(g)$ differed by an average of 0.19 or 6.8%.

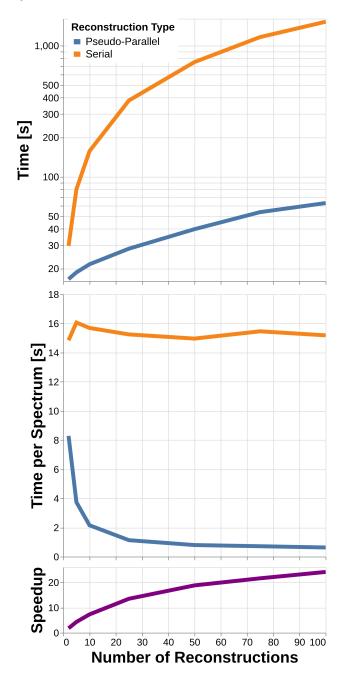


Figure 6. Plots showing the time taken to reconstruct varying numbers of spectra using the PHOENIX generator (lower is better). We can see that the time taken per spectrum for the serial implementation hovers around 15 seconds within run-to-run variance, while the pseudo-parallel implementation continually decreases in time taken per spectrum as the number of inputs increases. The speedup factor (higher is better) increases as more spectra are generated, which is also a desirable outcome.

 $_{472}$ [Fe/H] differed by an average of 0.12 dex, which is 24% $_{473}$ of our search range. From this, we can see that $T_{\rm eff}$

was the most accurately inferred parameter, followed by $\log(g)$, and then [Fe/H].

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5. DISCUSSION

5.1. Scientific Applications

This study's paradigm of spectral inference can enable scientists to adopt self-consistent model grids and analyze their spectral line behavior in an interpretable fashion, which has been fairly uncommon practice thus far. Notably, this system tracks the shifting of spectral lines as a function of stellar parameters, which traditionally has been uncommon for algorithms to assess systematically. We balance rigidity in the Voigt profile basis and flexibility in line parameter tunability, resulting in an interpretable system.

To summarize, we bring to scientists the ability to understand exactly what spectral properties we consider
mathematically and how we expect those properties to
behave on an incredibly detailed level (the 4 line parameters of all spectral lines and their corresponding interpolating manifolds). We treat the PHOENIX precomputed model grid as the ground truth, constructing
the PHOENIX generator that then interfaces with
our inference algorithm.

5.2. Technical Considerations

To reiterate, the manifold fitting steps are not end-499 to-end autodifferentiable. As seen in Figure 1, these 500 steps rely on scipy, which is not equipped with autodiff. 501 Without autodifferentiability, the ability to "machine 502 learn" is significantly reduced compared to a hypothet-503 ical monolithic JAX or PyTorch system. We see three ⁵⁰⁴ reasons for for developing a non-autodifferentiable sys-505 tem. First, the familiar scipy-based system will serve 506 as an easy entry point for most practitioners who are 507 unfamiliar with autodiff, and may still benefit from and 508 modify the code without expert ML knowledge. Second, this non-autodiff version serves as an initial benchmark 510 against which an inevitable autodifferentiable version of 511 blase may be compared. Finally, the inventory of fa-512 miliar interpolation algorithms have not yet been ported 513 to PyTorch or JAX, since machine learning or Gaussian 514 Process fitting schemes are generally preferred within 515 the ML community.

The interpolation scheme presented here represents a proof of concept, showing that leveraging the mapping between synthetic spectral lines and their inputs can yield a semi-empirical basis for data-model comparisons. There are numerous design considerations that could be improved upon with future work. These include but are not limited to the following:

- Limited PHOENIX Subset: The PHOENIX subset used in this study did not include the full PHOENIX grid, which expands the [Fe/H] range to [-4.0, 1.0] dex and the log(g) range to [0, 6], and also includes the alpha element abundance parameter, which we elected to fix at 0 for this study. In addition to the actual stellar parameters, we also took a subset of the PHOENIX wavelength range, with the full [500, 55000] Å wavelength range also being left to future work. Users would be able to fit a greater variety of stellar spectra in many different wavelength regimes.

- Strict Wavelength Range: Currently, the generator only supports inference on spectra whose wavelength limits are either equal to it, or encompass that of the generator and have been truncated to match. However, when the spectrum in question has a smaller wavelength range than the generator, currently there is no functionality to truncate the generator. This would require externally indexing the generator's individual interpolators by line center position and selectively evaluating those to eliminate wasteful computation. This takes burden off the users to truncate their data to the PHOENIX generators, making use simpler.
- Single Model Grid: The PHOENIX grid is not the only model grid of synthetic spectra available, and it does not apply to all types of stars. Future work would extend the reach of this study's algorithm to encompass other model grids such as the Sonora series of substellar models (Marley et al. 2021; Karalidi et al. 2021; Morley et al. 2024; Mukherjee et al. 2024), ATLAS (Kurucz 2005), and coolTLUSTY (Lacy & Burrows 2023), reaching practitioners studying various types of stars and spectra. Future blase versions will be able to have an option for the user to input which model grid they would like to base the inference on, and to get even more advanced, perhaps even have the ability to intelligently determine which model grid to use automatically.
- Memorization vs. Generalization: The current design of the algorithm constructs manifolds using interpolation. This means that performance is good at points close to PHOENIX subset grid points, but is highly dependent on the type of interpolation used. As interpolators require memorization of the data, advanced interpolation becomes extremely expensive in terms of disk utilization. Future work would involve constructing

- manifolds using more generalizable ML methods such as lasso or ridge regression, which would allow for much better generalization, high speed, and lower disk utilization at the expense of some accuracy.
- Extrinsic Absence: The current design of our algorithm does not account for extrinsic parameters that modify the appearance of spectra such as rotational broadening and Doppler shifting. Future work would need to develop ways to tune these extrinsic parameters alongside stellar parameters, enabling users to optimize these frequently-observed extrinsic parameters on top of the base stellar parameters.
- Framework Overhead: As this algorithm is currently more proof of concept than practical, it uses convenience functions from various libraries, which naturally introduces some level of overhead and leaves performance on the table. Future work would involve writing custom functions expressly designed for blase, most likely a complete rewrite of the library from the ground up. This has the potential to greatly increase the speed of this algorithm, depending on how much overhead is avoided with a bespoke implementation.
- Pseudo-Interpretability: Our algorithm boasts interpretability by considering spectral lines as the objects of interest as opposed to the rather uninterpretable flux values of other approaches. However, this is only a step in the direction of interpretability. True interpretability would decompose a spectrum not into a set of spectral lines, but into a set of species component spectra, which requires a much more advanced understanding of different species and their behavior, as well as direct access to a radiative transfer code as opposed to an off-the-shelf model grid. This approach would also extend the inference from just stellar parameters defined by a grid to any set of parameters accounted for in the radiative transfer model, down to specific species abundances. So while we were able to identify the spectral lines used in our figures, it is not necessarily valuable to try to identify all 128,723 lines that we identify as unique with our algorithm. blase is agnostic to the identity of the line that it is optimizing. We study these lines as blase sees them (i.e. their four shape parameters), because for the purposes of this study, that is the only information that is useful. Having more interpretability would let scientists actually study certain species and their spectral lines.

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- The Continuum Black Box: Continuum normalization is a process that is not yet completely understood, and is currently done as a preprocessing step with a fairly simple algorithm. Future work would dive deeper into the science of continua and develop more advanced methods that can discern continua with greater accuracy and less modeling restrictions. This would increase accuracy for end users.
- One Voigt Fits All: The current assumption of blase is that every spectral line is a Voigt profile. This assumption is largely true, but there are situations where that is simply not enough. Future studies need to account for more advanced spectral line profiles and procedures to deal with phenomena such as ro-vibrational bands. This would increase accuracy for end users.

6. CONCLUSION

In this study, we have presented a proof-of-concept algorithm that deals with a subset of the PHOENIX spectral model grid ([Fe/H]: [-0.5, 0] dex, $T_{\rm eff}$: [2300, 12000] K, $\log(g)$: [2, 6], λ : [8038, 12849] 4). We create state dictionaries for all spectra in the PHOENIX subset using blase, recasting spectra into lists of Voigt profiles, and lossily compress the spectral data by a factor of around 20. They are available on Zenodo at https://zenodo.org/records/11246174 (Shankar 2024). We create the PHOENIX generator and implement a performant spectral reconstruction algorithm, enabling anyone to create reconstructions of PHOENIX spectra with continuously val-

minimization algorithm to infer stellar parameters ters, with average absolute deviations from true values of 185 K in $T_{\rm eff}$, 0.19 in $\log(g)$, and 0.12 dex in [Fe/H]. In its current state, our algorithm operates on spectra within the PHOENIX subset parameter ranges in Table 1, requiring that the spectra not contain noticeable Doppler shifting, rotational broadening, or other confounding factors. The methods discussed here represent a step down a road not traveled in spectral inference, and have the potential to become more advanced in the future by fully utilizing the strengths of physics-informed machine learning.

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679 (Shankar et al. 2024), matplotlib (Hunter 2007), numpy
680 (Harris et al. 2020), pandas (pandas development team
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682 Drake 2009), PyTorch/torch (Paszke et al. 2019), scikit683 optimize/skopt (Head et al. 2018), scipy (Virtanen
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