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# A New Hybrid Machine Learning Method for Stellar Parameter Inference

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ABSTRACT

The advent of machine learning (ML) is revolutionary to numerous scientific disciplines, with a growing number of examples in astronomical spectroscopic inference, as ML is more powerful than traditional techniques. Here we introduce a hybrid ML (HML) method combining automatic differentiation, interpolation, and Bayesian optimization to infer stellar parameters of stellar spectra. We study  $T_{\text{eff}}$ ,  $\log(g)$ , and [Fe/H], but this method could be extended to other parameters such as  $[\alpha/\text{Fe}]$  (alpha element abundance), C/O (carbon-oxygen ratio), and  $f_{sed}$  (sedimentation efficiency). We first use blase to semi-empirically recast spectra into sets of Voigt profiles. blase is run on 1,314 synthetic spectra from a rectilinear subset of the PHOENIX model grid ( $T_{\rm eff}$ : [2300, 12000] K,  $\log(g)$ : [2, 6] dex, [Fe/H]: [-0.5, 0] dex,  $\lambda$ : [8038, 12849] Å). For 128,723 detected features, we map stellar parameters to spectral line parameters using linear interpolation. This creates the PHOENIX generator, enabling parallelized spectral synthesis. Gaussian Process minimization is used to infer stellar parameters by minimizing a root-mean-square loss function. Testing 210 noise-free models ( $T_{\text{eff}}$ : [3000, 11000] K,  $\log(q)$ : [2, 6] dex, [Fe/H]: [-0.5, 0] dex), we find inference errors:  $T_{\text{eff}}$ : 93 K,  $\log(g)$ : 0.24 dex, and [Fe/H]: 0.056 dex for  $T_{\text{eff}}$  < 7000 K, and  $T_{\rm eff}$ : 347 K,  $\log(g)$ : 0.26 dex, and [Fe/H]: 0.16 dex for  $T_{\rm eff} \geq$  7000 K. We also upload online an archive of blase models of the PHOENIX subset. This proof-of-concept study shows that semi-empirical HML is a viable alternative to traditional approaches in spectroscopic inference.

## 1. INTRODUCTION

Stellar spectra are exceedingly rich sources of infor-24 25 mation about the stars that produce them. Spectra en-26 code fundamental properties such as temperature, sur-<sub>27</sub> face gravity, and chemical composition via their numer-28 ous absorption lines. Extrinsic properties such as the 29 stellar radial velocity or the projected equatorial rota-30 tion shift the wavelengths of lines and broaden their 31 widths, respectively. Observing the spectrum alters it 32 again; the resolution, bandwidth, and other properties 33 of the instrument change the fidelity at which we observe 34 the spectrum, and can limit our ability to extract fun-35 damental properties precisely. Observed stellar spectra 36 thus represent extremely complex, data, influenced by 37 multiple parameters, that have gone through multiple 38 transformations before reaching our detectors.

Modern astronomical spectroscopy takes advantage of intuitive, performant spectral models such as

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41 KORG (Wheeler et al. 2023), however it would 42 further benefit from the paradigm of interpretabil-43 ity. The determination of fundamental properties, the 44 creation of Extreme Precision Radial Velocity (EPRV) 45 templates, and the application of composite spectral fit-46 ting could all leverage such an innovation. This am-47 bitious aim may be broadly referred to as a "founda-48 tional spectroscopy model for astrophysics", in reference 49 to the same category of models used for large language 50 models (LLMs) in artificial intelligence (AI). There are 51 many challenges with creating such a foundational spec-52 tral model for astrophysics. Physical inputs into the 53 spectral modeling process are imperfect, and simplify-54 ing assumptions in stellar (and substellar) atmospheres 55 are necessarily inexact due to factors such as asym-56 metries and unknown physics. Computational costs 57 make the training of such models challenging; how-58 ever, advances have been made with attention-59 based (Różański et al. 2023) and transformer-60 based (Leung & Bovy 2024) models, among oth-61 ers. Most prevailing solutions have had to choose ei-62 ther a model driven approach (such as this work), in 63 which precomputed models are taken as gospel, or a data driven/empirical approach (such as Lux (Horta et al. 2025)), in which our knowledge of stellar physics is ignored or treated phenomenologically, depending on the application. Hybrid solutions exist and have been implemented, such as those presented in Leung & Bovy 2019 and Rains et al. 2024. Although a lingering challenge is always how to ideally balance the fusion of model driven and data driven paradigms.

Spectroscopic surveys such as APOGEE (Majewski et al. 2017) use their own in-house pipelines to ex
tract stellar parameters from spectra (ASPCAP (Gar
fecía Pérez et al. 2016) in the case of APOGEE), and

these pipelines appear effective. The core assumption

for the vast majority of pipelines is that the data to be

analyzed is a list of pixels. Analysis pipelines may be

closed-source or limited to the scope of the survey itself,

causing a sort of siloing effect among surveys. This mo
tivates the development of more universal, instrument
agnostic open-source frameworks that can apply broadly

to a range of spectral observations with relatively little

tuning.

Multiple efforts have been made in this direction, treating spectra in different ways. The standard practice is to treat the wavelength and flux as simply two arrays and use bespoke algorithms tailored to a small number of well-calibrated spectral lines to obtain fundamental stellar parameters and chemical compositions (e.g. the IGRINS YSO Survey (López-Valdivia et al. 2023) and the IRTF Spectral Library (Rayner et al. 2009)). Other whole-spectrum fitting abstractions decompose model spectra into an eigenbasis, implementing the data-model comparison stage as a tractable regression, such as starfish (Czekala et al. 2015).

Ideally, we want a system that can self-consistently 100 learn, a genuine AI foundational spectral model. Such a 101 system would enable the assignment of accurate stellar parameters, and could yield re-usable interpretable spec-103 tral models. blase, first presented in Gully-Santiago 104 & Morley 2022, took an important, albeit limited, step 105 in this direction, treating spectra not as a set of pixels 106 or a set of eigenbasis coefficients but as a set of inter-107 pretable and traceable spectral lines, specifically Voigt profiles. Each of these approaches has tradeoffs, but one 109 key scientific advantage of blase comes from its ability 110 to adapt to new information, while preserving some ad-111 herence to physics-based models. This intelligent capability stems from its ability to fit a theoretically unlim-113 ited number of nonlinear spectral line parameters with 114 automatic differentiation (autodiff). Autodiff is a tech-115 nology that tracks transformations made to data using 116 the chain rule, even being able to differentiate control 117 flow transformations involving if-else blocks, for exam-118 ple. With the gradient obtained from autodiff's chain 119 rule, we can optimize model parameters by just going 120 against the direction of the gradient (because we usu-121 ally want to minimize something such as a loss function, 122 we go in the direction of greatest decrease, which is al-123 ways the negative of the gradient). Autodiff has been 124 used successfully in other astrophysical contexts such as 125 exojax (Kawahara et al. 2022) and wobble (Bedell 126 et al. 2019), but the recasting of spectra into sets of 127 inherently nonlinear spectral lines positions blase as a 128 unique and promising semi-empirical tool. The origi-129 nal blase paper demonstrated the ability to tune spec-130 tral lines with autodiff and 'clone' spectra, recasting 131 them as ML models defined by interpretable sets 132 of tuned spectral lines, however it was restricted 133 to a pre-selected static synthetic model.

Here we introduce the next logical step in the sequence of expanding interpretable spectroscopic machine learning ing from operating on a single grid point and towards an entire 3D grid of precomputed spectra. We rebrand this augmentation as blase3D.

Ideally this process would be monolithic, with the 140 end-to-end spectral inference code powered by a single 141 autodiffable machine learning framework, like PvTorch 142 (Paszke et al. 2019) or JAX (Bradbury et al. 2018). 143 However, here we separate the problem into three pieces, only the first of which is currently differentiable. In section 2, we scale out the blase method to 1,314 precom-146 puted synthetic spectral model clones, yielding a down-147 loadable archive of pretrained machine learning mod-148 els with 128,723 unique spectral lines. In section 3, 149 we then fit manifolds mapping stellar parameters to 150 uniformly-derived spectral line parameters using regular 151 grid linear interpolation. Finally, in section 4, we show 152 how reconstructions of the spectra using said manifolds 153 can be used for inferring stellar fundamental properties 154 from spectra. This final step resembles the aims of "at-155 mospheric retrievals", but in principle should be faster, 156 adaptive, and reusable. An overview of this process is 157 shown in Figure 1.

# 2. CLONING THE PHOENIX MODEL GRID

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### 2.1. The PHOENIX Subset

For the purposes of this study, we chose the widely-adopted PHOENIX synthetic spectral model grid (Husser et al. 2013). Our approach can be straightforwardly applied to any other model grid in the future, including substellar atmosphere grids such as Sonora (Marley et al. 2021; Karalidi et al. 2021; Morley et al. 2024; Mukherjee et al. 2024), but for now we limit our

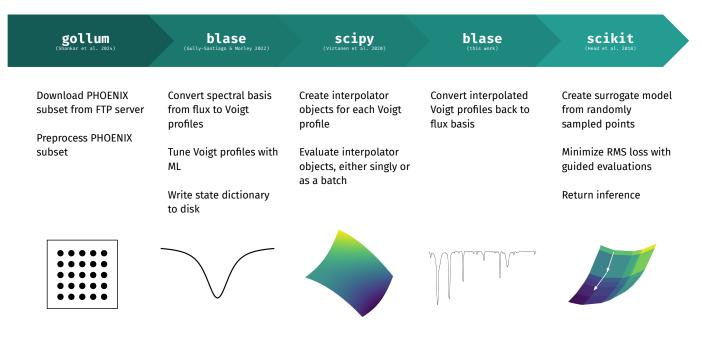


Figure 1. Overview of the process used in this study.

167 scope to a rectilinear subset of the PHOENIX grid, 168 focusing on near solar metallicities and a broad range of 169 effective temperature and surface gravity, with details 170 given in Table 1. This approach is taken due to the 171 computational cost of interpolation algorithms. 172 Future versions with more advanced models will 173 be able to bypass the limitation of a rectilinear 174 subset.

## 2.2. Preprocessing with gollum

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First, the PHOENIX subset was programmatically retrieved with gollum (Shankar et al. 2024), which
downloaded spectra from the PHOENIX FTP server.
The spectra were then put through a short preprocessing pipeline similar to that from Gully-Santiago & Morley 2022.

- 1. Blackbody Division: Since the  $T_{\rm eff}$  of each spectrum is known, the **corresponding** blackbody spectrum was divided out.
- 2. Continuum Normalization: The spectra were further normalized by dividing them by a 5<sup>th</sup> order polynomial continuum fit using a peak-finding filter in order to eliminate curvature that would inhibit line modeling.

190 Mathematically, we can express the preprocessing as fol-191 lows:

$$\bar{S} = \frac{S}{BQ_5} \tag{1}$$

where  $\bar{S}$  is the preprocessed spectrum, S is the original spectrum, B is the blackbody spectrum, and  $Q_n$  is the  $n^{\text{th}}$  order polynomial continuum fit. Arithmetic operations between arrays are assumed to be elementwise in all following notation.

## 2.3. Line Identification with blase

The next step was to convert the PHOENIX subset into a physically interpretable intermediate representation: a table of spectral line properties rather than an array of fluxes. We used blase, which models spectral lines as Voigt profiles and tunes the profiles to mimic the original PHOENIX spectrum with back propagation. Back propagation, put simply, is the process of moving in the autodiff gradient field to update ML model parameters (like mentioned earlier, usually against the gradient ent because we minimize loss functions). Four parameters were optimized: the line center  $\mu$ , the log-amplitude ln(a), the Gaussian width  $\sigma$ , and the Lorentzian width  $\gamma$ . The optimization used the Adam optimizer (Kingma & Ba 2017) with a learning rate of 0.05 over 100 epochs. Gully-Santiago & Morley 2022 recommends this

Parameter	Symbol	Interval	Sampling
Alpha Element Abundance	α	[0] dex	N/A
Iron Abundance	$[\mathrm{Fe/H}]$	[-0.5, 0] dex	$0.5~\mathrm{dex}$
Effective Temperature	$T_{ m eff}$	[2300, 12000]  K	$100~\mathrm{K}$ until $7000~\mathrm{K},$ then $200~\mathrm{K}$
Surface Gravity	$\log(g)$	[2, 6] dex	$0.5  \mathrm{dex}$
Wavelength	$\lambda$	[8038, 12849]  Å	$\mathbf{R}=500,000$

Table 1. The subset of the PHOENIX grid used in this study. These limits were imposed to reduce the computational cost of the algorithms and to ensure a rectilinear parameter space in order to work with scipy's RegularGridInterpolator (Virtanen et al. 2020). The wavelength limits in particular roughly line up with that of the Habitable Zone Planet Finder (HPF) spectrograph (Mahadevan et al. 2012). This subset is comprised of 1,314 individual spectra: 73  $T_{\rm eff}$  values, 9  $\log(g)$  values, and 2 [Fe/H] values.

213 setup as the minimum, and for a proof-of-concept 214 implementation, we found it best to leave it as is. 215 In addition, we limited two custom parameters: wing 216 cut to 6,000 and prominence to 0.005. Wing cut (in 217 **pixels**) is a parameter that determines the extent of 218 the Voigt profile to evaluate, saving computational re-219 sources by not evaluating negligible line wings. Promi-220 nence (in normalized flux counts) sets a lower limit for the amplitude of detected lines, which saves resources 222 by disregarding shallow lines, so in our case we disre-223 gard lines with amplitude less than 0.005. In short, 224 our choices for wing cut and prominence decrease the 225 computational cost of blase's cloning process at the ex-226 pense of decreasing its accuracy slightly. blase uses the 227 pseudo-Voigt approximation, which saves on computa-228 tional cost while remaining accurate to about 1% (Ida 229 et al. 2000). The pseudo-Voigt approximation uses a 230 weighted average of a Gaussian and Lorentzian as op-231 posed to a convolution. blase's pseudo-Voigt profile 232 implementation uses the following:

$$\tilde{\mathbf{V}}_{\mu}(\lambda) = a \left[ \eta \mathbf{L}(\lambda - \mu'; f) + (1 - \eta) \mathbf{G}(\lambda - \mu'; f) \right]$$
(2a)  

$$\eta = \sum_{n=1}^{3} \mathbf{u}_{n} \left( \frac{2\gamma}{f} \right)^{n}$$
(2b)  

$$f = 32 \sum_{n=0}^{5} \mathbf{v}_{n} \left( \sqrt{2 \ln(2)} \sigma \right)^{5-n} (\gamma)^{n}$$
(2c)  

$$\mathbf{u} = \begin{bmatrix} 1.36603 \\ -0.47719 \\ 0.11116 \end{bmatrix} \mathbf{v} = \begin{bmatrix} 1 \\ 2.69269 \\ 2.42843 \\ 4.47163 \\ 0.07842 \\ 1 \end{bmatrix}$$

<sup>233</sup> where **L** and **G** are abbreviations for Lorentzian and <sup>234</sup> Gaussian profiles, respectively. Notice that we use  $\mu'$  <sup>235</sup> instead of  $\mu$  in the formula. This is because blase <sup>236</sup> optionally allows the line center to shift slightly dur- <sup>237</sup> ing optimization, and it is this shifted center which is <sup>238</sup> used in computation. The individual Voigt profiles are

still indexed by  $\mu$  for cross-model line identification, explained in the next section. Once optimization was complete, the list of identified lines was saved to a 'state dictionary': a common representation for pre-trained machine learning models that can be stored to disk for reuse later. These are stored in the .pt file format for each of the 1,314 PHOENIX subset grid points. The total disk space these files take up is 465 MB (382 MB when downloaded as a zip archive). For reference, the storage space the PHOENIX subset takes up on disk is approximately 8.1 GB. This represents a data compression factor of around 20 just by recasting the spectrum with blase. The state dictionaries are available on Zenodo at https://zenodo.org/records/11246174 (Shankar 2024).

### 3. INTERPOLATING MANIFOLDS

# 3.1. Cross-Model Line Identification

As previously mentioned, blase tunes the line centers of detected lines. This means that from one PHOENIX spectrum to the next, the same line could have a slightly different line center. Since the goal of this study is to interpolate the properties of each line, we needed to identify the presence of a particular line across the PHOENIX subset, associating the same line with every occurrence. We decided to do this by using the line centers  $\mu$  of the detected lines pre-optimization.

Pre-optimized line centers were required to be equal in order to group lines together. The values of  $\mu$  pre-optimization are recorded by blase to 0.01 Å(picometer) precision; if they instead used the full available floating point precision, this method would likely detect singular (ungroupable) instances of spectral lines across the grid, completely negating the premise of this study. Of course, this method can be confused by species that produce spectral lines at very close wavelengths and other confounding factors, likely resulting in some false positives and negatives. However, we deem it sufficient to approx-

imate this way, as an in-depth treatment would be time-consuming and computationally expensive.

Now with each spectral line indexed by  $\mu$ , we had four parameters to interpolate:  $\mu'$ ,  $\ln(a)$ ,  $\sigma$ , and  $\gamma$ . Note that since we are dealing with the parameters of Voigt profiles, we can see in Equation 2 that even if the interpolation method is linear, a final spectral reconstruction will vary nonlinearly in flux.

Spectral lines were often only detected in some spectra from the PHOENIX subset. In Figure 2, we show that different grid points **show** differing counts of detected spectral lines.

The number of detected spectral lines changes as a function of stellar parameter for different reasons. Perhaps for astrophysical reasons: stellar atmospheres genuinely do not produce that line at detectable strength at the given temperature and surface gravity. Alternatively, blase's fitting or our line identification assumptions led to artifacts. Whatever the cause, these missing lines have immediate practical consequences. Rectilinear interpolation schemes break in regions where a line does not appear; you can't interposon late a quantity that simply doesn't exist.

To solve this, we artificially populated missing grid points with log-amplitudes of -1000, which retained interpolator stability while nullifying the evaluated line. To prove the feasibility of this computational trick, we can do a simple thought experiment. Moving 1 K in  $T_{\rm eff}$  away from a grid point on the boundary of detectability would reduce a line's amplitude by a factor of over 20,000 (or more precisely,  $e^{10}$ ). This is an extremely large reduction for an extremely small deviation from a grid point, meaning that to any realistic precision, the line immediately vanishes as soon as blase no longer detects it.

Examples of the appearance of missing sections in heatmaps where a line does not appear can be seen in Figure 3 and Figure 4, which show heatmaps of the 11617.66 Å C I and the 10123.66 Å He il lines (identified with NIST (Kramida et al. 20023)) varying over a solar metallicity slice of the PHOENIX subset stellar parameter space. Across the entire PHOENIX subset, blase detected 128,723 spectral lines with unique  $\mu$ . On average, a PHOENIX spectrum has 9,167 detected spectral lines, with the minimum being 252 ( $T_{\rm eff}$  = 12000 K,  $\log(g)$  = 6 dex,  $[{\rm Fe}/{\rm H}]$  = -0.5 dex) and the maximum being 34,551 ( $T_{\rm eff}$  = 2300 K,  $\log(g)$  = 3 dex,  $[{\rm Fe}/{\rm H}]$  = 0 dex). Every one of these lines can be visualized as a manifold mapping a 3D stellar

parameter vector to a 4D spectral line parameter vec-331 tor, and every one was interpolated to map stellar 332 parameters to spectral line properties.

## 3.2. Continuously Evaluable Manifolds

For each line, the inputs to the interpolator were the three input parameters  $T_{\rm eff}$ ,  $\log(g)$ , and [Fe/H], and the output was a list of four parameters,  $\mu'$ ,  $\ln(a)$ ,  $\sigma$ , and  $\gamma$ . For each line, one of these interpolator objects was created using linear interpolation, and these interpolators were aggregated into a single list, which was then written to disk in the .pkl file storage format. These interpolators generate multiple manifolds representing the following mapping:

$$\begin{bmatrix} T_{\text{eff}} \\ \log(g) \\ [\text{Fe/H}] \end{bmatrix} \rightarrow \begin{bmatrix} \mu' \\ \ln(a) \\ \sigma \\ \gamma \end{bmatrix}$$
 (3)

345 These interpolators could now be evaluated at any point 346 lying within the domain of the PHOENIX subset, turn-347 ing a discretely sampled PHOENIX subset into a con-348 tinuously evaluable function, sometimes called a spec-349 tral emulator. With the given size of the PHOENIX 350 subset, the interpolator list takes up 13.2 GB of disk 351 space. This is larger than the original PHOENIX 352 subset by about 63% and than the state dictio-353 nary clone archive by a factor of over 34. This is 354 due to the fact that we are now pickling entire 355 function objects that must memorize the data. 356 Future work with more space-efficient models 357 and clever storage strategies could reduce stor-358 age space requirements in exchange for I/O per-359 formance. This evaluation is able to reconstruct an ex-360 isting PHOENIX spectrum or alternatively interpolate 361 a new spectrum within the domain of the PHOENIX 362 subset, so we call this the PHOENIX generator.

The spectral reconstruction process is done by iterating over the PHOENIX generator, evaluating each interpolator at the given coordinates, then reshaping the
data into the same format that PyTorch uses for state
dictionaries. During the iteration, if the interpolated
log-amplitude of the line is less than -100, the line is
excluded from the state dictionary. We do this to avoid
artifacts in the manifolds due to the artifical population of log-amplitudes of -1000 where grid points were
missing.

Finally, the state dictionary is fed into blase's SparseLinearEmulator, which reconstructs the spectrum by constructing a forward model based on the input state dictionary. Any nan values are set to 1 (which we can do because the spectra are all normalized), and

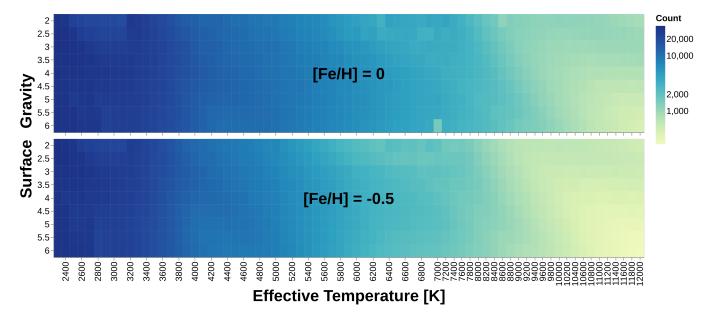


Figure 2. Number of detected spectral lines at each grid point of the PHOENIX subset. We can see that the number of detected lines decreases with increasing  $T_{\rm eff}$ . Remember that from  $T_{\rm eff}=7000$  K onward, PHOENIX's sampling increment changes from 100 K to 200 K. Due to some combination of computational artifacts from our line identification assumptions or innate behavior of PHOENIX grid spectra themselves, outliers such as the obvious one here at  $T_{\rm eff}=7000$  K and  $\log(g)=6$  dex appear. Further exploration into why this happens is not in the scope of this study; for inference we are concerned with the lines themselves, not overall grid point behavior.

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378 the spectral reconstruction is complete. In Figure 5, 379 we see a comparison between a PHOENIX gen-380 erator solar spectrum and two nearby native 381 PHOENIX grid point spectra at the 10123.66 Å 383 He II spectral line.

We can observe in Figure 6 that our He II line from a reconstructed solar spectrum is not simply a pixel interpolation between the nearest PHOENIX grid point spectra. It is interpolating the spectral line properties using hundreds of thousands of manifolds, each representing a nonlinear parameter in the shape of the spectral line.

#### 3.3. Spectral Reconstruction Time

A typical use case for the PHOENIX generator may
be to batch reconstruct spectra from an array of input
stellar parameters. Therefore, there is some motivation
to reduce the computational cost of this procedure to
tractable levels. We evaluate the computational time
needed to use the PHOENIX generator in two distinct
ways. First, for a single input, which would be relevant
in serial applications. Second, for an array of multiple
inputs, which would be relevant in parallel applications.
scipy's RegularGridInterpolator API allows for the
passing in of an entire array of input coordinates to be
evaluated at once. However using blase to reconstruct
the spectrum from our interpolated state dictionary is
always done serially, leading to what is actually more of

 $_{407}$  a pseudo-parallel evaluation, but extremely performant  $_{408}$  nonetheless.

Performance results are shown in Figure 7, and we can 410 see that the PHOENIX generator's parallel mode 411 is much faster than serial mode. While the gen-412 erator takes around 15 seconds per spectrum in 413 serial mode, this drops to 1 second per spectrum 414 in parallel mode as soon as 30 reconstructions. The speedup factor between the two methods in-416 creases as more spectra are generated, reaching a 417 factor of 20 at 60 reconstructions. Assuming lin-418 ear time scaling with wavelength range, accord-419 ing to KORG benchmarks (Wheeler et al. 2023), 420 which generate spectra over a 500 Å wavelength 421 range, the PHOENIX generator in serial mode 422 is approximately as fast as KORG and  $\sim$ 30 times 423 faster than Turbospectrum (Gerber et al. 2023). <sup>424</sup> The speedup factor in parallel mode compared to 425 KORG is then the same variable speedup factor 426 from serial mode (20 times faster at 60 recon-427 structions).

The computer used for this test has specifications shown in Table 2 (note that spectral reconstruction does not currently leverage the GPU):

### 4. BAYESIAN INFERENCE AND TESTING

4.1. Inference Algorithm

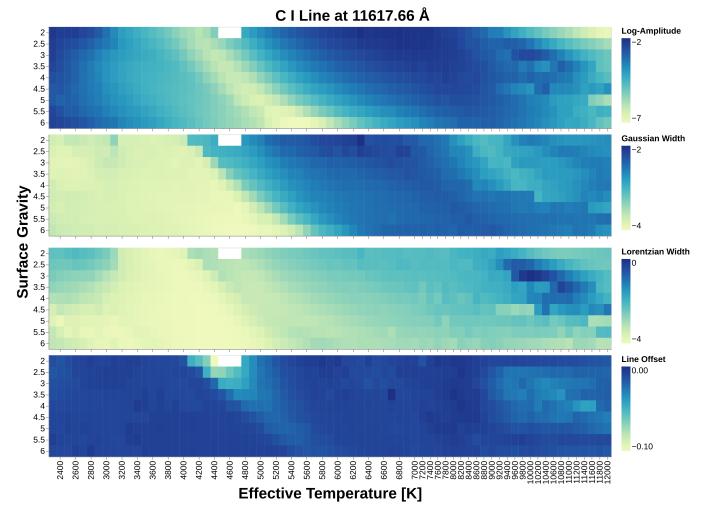


Figure 3. Heatmaps showing how  $\ln(a)$ ,  $\sigma$ ,  $\gamma$ , and  $\mu' - \mu$  vary over the PHOENIX subset slice at solar metallicity of a C I spectral line, notable for being detected at nearly all subset grid points. Notice the missing chunk in the top left; this could perhaps be due to the line center shifting to the point that blase identified the chunk as a different line entirely (notice the line center offset increasing in magnitude approaching the chunk border). Since blase did not detect a spectral line here, we artificially populate those points with lines that have  $\ln(a) = -1000$  during interpolation.

CPU	AMD EPYC 7513 (32c/64t, 3.65 GHz boost)
RAM	256 GB
GPU	Nvidia A100 [40GB] (×2)

Table 2. Specifications of the machine used for cloning and reconstruction testing. This machine is owned by Caroline Morley.

The goals of this study's inference algorithm are to infer the stellar parameters  $T_{\rm eff}$ ,  $\log(g)$ , and [Fe/H] by comparing a spectrum with our reconstructions and solving the optimization problem. We elected to use Bayesian optimization for this component, specifically the gp\_minimize function from the scikit-optimize library (Head et al. 2018). This algorithm uses a Gaussian Process to model the objective function, which in this case was the RMS (Root-Mean-

 $_{444}$  Square) loss between the interpolated spectrum M and  $_{445}$  the true spectrum D, defined as:

$$\mathcal{L} = \left\langle (\mathsf{M} - \mathsf{D})^2 \right\rangle^{1/2} \tag{4}$$

The optimizer was configured to first run 100 random evaluations to seed the surrogate model, then run 20 more evaluations now guided by the surrogate model. A random evaluation is simply a randomly generated tuple of stellar parameters within the parameter space of the PHOENIX generator, which is then evaluated with the generator to get a reconstruction and then compared with the inference target to retrieve its RMS error. The surrogate model is the approximation to the true objective function that the optimizer constructs based on the set of random evaluations (in this case defined by a set of 100 points rather than

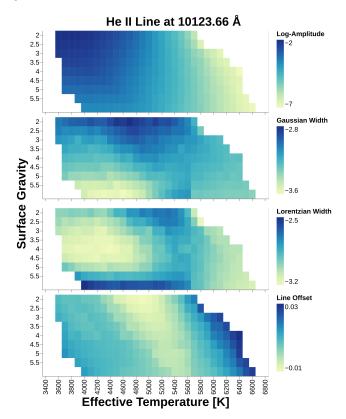


Figure 4. Heatmaps showing how  $\ln(a)$ ,  $\sigma$ ,  $\gamma$ , and  $\mu' - \mu$  vary over the PHOENIX subset slice at solar metallicity of a He II spectral line. blase detects this line at a select chunk of grid points, leading to data only existing between  $T_{\rm eff}$  3600 K and 6600 K.

459 a fully continuous, infinitely resolved function) 460 Guided evaluations are different, they are not randomly generated tuples of stellar parameters. 462 They use the surrogate model in order to select <sup>463</sup> new test points for the minimum of the objective 464 function. This totals to 120 evaluations, 100 to create the surrogate model, then 20 guided evaluations, which was deemed sufficient for this study. Fine-tuning these numbers is possible, but simply not warranted for 468 a proof-of concept method. Tweaking these numbers could lead to a more accurate inference, however 470 it would incur additional computational cost as well. One inference takes on average 200 seconds, us-472 ing the computer with specifications in Table 3. Inference algorithms that output more in-474 formation and produce posterior distributions 475 such as starfish (Czekala et al. 2015) or MINESweeper (Cargile et al. 2020) take on the 477 order of an hour to complete an inference on 478 supercomputers. astroNN (Leung & Bovy 2019) 479 is a more direct comparison, and represents an 480 extremely powerful inference tool that performs

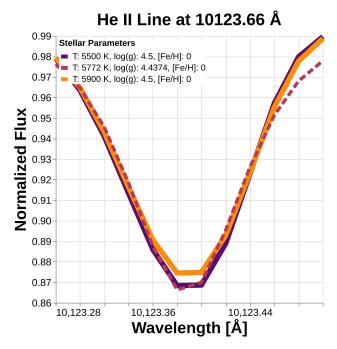


Figure 5. Plot of the 10123.66 Å He II spectral line shown at the closest PHOENIX grid points to the Sun's stellar parameters (solid lines), as well as a solar spectrum reconstructed with the PHOENIX generator (dotted line).

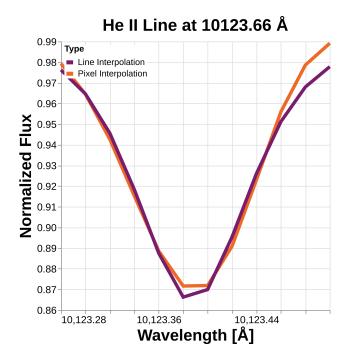


Figure 6. Comparison between the PHOENIX generator's line interpolation and a standard pixel interpolation of the 10123.66 Å He II spectral line. Notice that line interpolation results in more symmetrical line wings due to the use of Voigt profiles.

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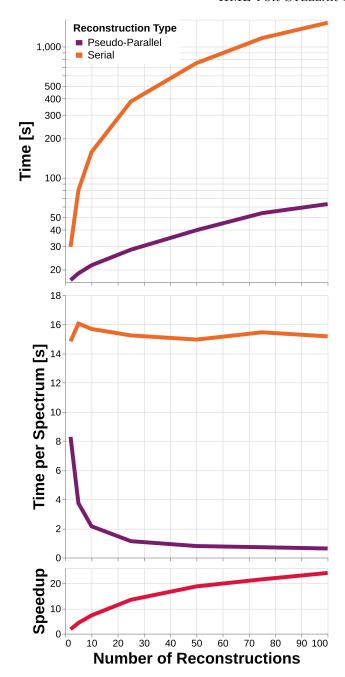


Figure 7. Plots showing the time taken to reconstruct varying numbers of spectra using the PHOENIX generator (lower is better). We can see that the time taken per spectrum for the serial implementation hovers around 15 seconds within run-to-run variance, while the pseudo-parallel implementation continually decreases in time taken per spectrum as the number of inputs increases. The speedup factor (higher is better) increases as more spectra are generated, which is also a desirable outcome.

inference thousands of times faster thanks to its neural network architecture.

CPU AMD Ryzen 9 7950X3D (16c/32t, 5.7 GHz boost)
RAM 32 GB
GPU Nvidia GeForce RTX 4080 SUPER [16GB]

Table 3. Specifications of the machine used for general testing and for generating visualizations. This machine is owned by Sujay Shankar.

#### 4.2. Bayesian Optimizer Performance

To test the performance of the inference algorithm,
we used the PHOENIX subset itself. This is possible
for two reasons: first, the PHOENIX generator
has not truly memorized the PHOENIX subset
due to its Voigt profile basis and the ignoring of
weaker features, and secondly, random samples
within the parameter space are extremely unlikely to be PHOENIX grid points themselves,
avoiding any overlap.

We know that in typical observational settings, a coarse estimate for  $T_{\rm eff}$  tends to be fairly well-constrained from ancillary data such as photometric color index. So when testing the inference algorithm, we limited its search space to only include  $T_{\rm eff}$  which lay within 500 K of the true value on either side.  $\log(g)$  and [Fe/H] were allowed to vary freely. The test sample consisted of 21  $T_{\rm eff}$  values: [3000, 11000] K in steps of 400 K, 5  $\log(g)$  values: [2, 6] dex in steps of 0.5 dex, and 2 [Fe/H] values: [-0.5, 0] dex in steps of 0.5 dex, totaling 210 unique spectra in the test set. Two test passes were run, meaning that 420 inference tests were run in total.

In Figure 8, we show the residuals of the inferred stel-508 lar parameters with respect to the true values. We 510 see that there is a distinction between the algo-<sub>511</sub> rithm's behavior above and below  $T_{\rm eff} = 7000$  K, 512 so we define low and high temperature regimes  $_{513}$  accordingly. For  $T_{
m eff}$  < 7000 K, the inferred  $T_{
m eff}$ 514 differed from the true value by an average of 93 K,  $\log(g)$  0.24 dex, and [Fe/H] 0.056 dex (standard de-516 viations of 139 K, 0.40 dex, and 0.15 dex, respectively). For  $T_{\rm eff} \geq 7000$  K, the inferred  $T_{\rm eff}$ 518 differed from the true value by an average of 347  $_{519}$  K,  $\log(g)$  0.26 dex, and [Fe/H] 0.16 dex (standard 520 deviations of 293 K, 0.32 dex, and 0.23 dex, respectively). From this, we can see that  $T_{\text{eff}}$  was the most accurately inferred parameter, followed by  $\log(g)$ , 523 and then [Fe/H].

### 5. DISCUSSION

# 5.1. Scientific Applications

This study's paradigm of spectral inference can enable scientists to adopt self-consistent model grids and ana-

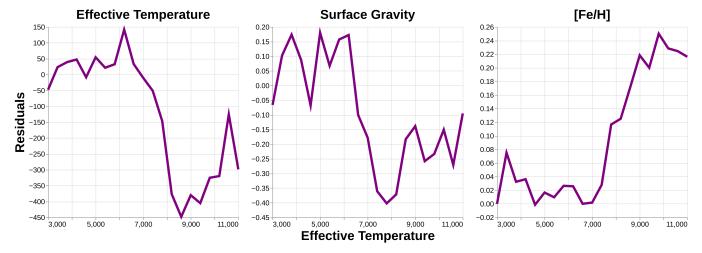


Figure 8. Residual plots for the GP minimization inference algorithm, all plotted with respect to  $T_{\rm eff}$  (values aggregated across  $\log(g)$  and [Fe/H]). Notice the interesting change in behavior of all residuals at around  $T_{\rm eff}=7000$  K.

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1528 lyze their spectral line behavior in an interpretable fash1529 ion, which has been fairly uncommon practice thus far.
1530 Notably, this system tracks the shifting of spectral lines
1531 as a function of stellar parameters, which traditionally
1532 has been uncommon for algorithms to assess systemati1533 cally. We balance rigidity in the Voigt profile basis
1534 and flexibility in line parameter tunability, result1535 ing in an interpretable system.

To summarize, we bring to scientists the ability to understand exactly what spectral properties we consider
mathematically and how we expect those properties to
behave on an incredibly detailed level (the 4 line parameters of all spectral lines and their corresponding interpolating manifolds). We treat the PHOENIX precomputed model grid as the ground truth, constructing
the PHOENIX generator that then interfaces with
our inference algorithm.

# 5.2. Technical Considerations

To reiterate, the manifold fitting steps are not end-546 to-end autodifferentiable. As seen in Figure 1, these 548 steps rely on scipy, which is not equipped with autodiff. Without autodifferentiability, the ability to "machine learn" is significantly reduced compared to a hypothetical monolithic JAX or PyTorch system. We see three reasons for for developing a non-autodifferentiable sys-553 tem. First, the familiar scipy-based system will serve 554 as an easy entry point for most practitioners who are unfamiliar with autodiff, and may still benefit from and 556 modify the code without expert ML knowledge. Second, 557 this non-autodiff version serves as an initial benchmark 558 against which an inevitable autodifferentiable version of 559 blase may be compared. Finally, the inventory of fa-560 miliar interpolation algorithms have not yet been ported 561 to PyTorch or JAX, since machine learning or Gaussian

<sup>562</sup> Process fitting schemes are generally preferred within <sup>563</sup> the ML community.

The interpolation scheme presented here represents a proof of concept, showing that leveraging the mapping between synthetic spectral lines and their inputs can yield a semi-empirical basis for data-model comparisons. There are numerous design considerations that could be improved upon with future work. These include but are not limited to the following:

- Limited PHOENIX Subset: The PHOENIX subset used in this study did not include the full PHOENIX grid, which expands the [Fe/H] range to [-4.0, 1.0] dex and the log(g) range to [0, 6], and also includes the alpha element abundance parameter, which we elected to fix at 0 for this study. In addition to the actual stellar parameters, we also took a subset of the PHOENIX wavelength range, with the full [500, 55000] Å wavelength range also being left to future work. Users would be able to fit a greater variety of stellar spectra in many different wavelength regimes.
- Strict Wavelength Range: Currently, the generator only supports inference on spectra whose wavelength limits are either equal to it, or encompass that of the generator and have been truncated to match. However, when the spectrum in question has a smaller wavelength range than the generator, currently there is no functionality to truncate the generator. This would require externally indexing the generator's individual interpolators by line center position and selectively evaluating those to eliminate wasteful computation. This takes bur-

den off the users to truncate their data to the PHOENIX generators, making use simpler.

- Single Model Grid: The PHOENIX grid is not the only model grid of synthetic spectra available, and it does not apply to all types of stars. Future work would extend the reach of this study's algorithm to encompass other model grids such as the Sonora series of substellar models (Marley et al. 2021; Karalidi et al. 2021; Morley et al. 2024; Mukherjee et al. 2024), ATLAS (Kurucz 2005), and coolTLUSTY (Lacy & Burrows 2023), reaching practitioners studying various types of stars and spectra. Future blase versions will be able to have an option for the user to input which model grid they would like to base the inference on, and to get even more advanced, perhaps even have the ability to intelligently determine which model grid to use automatically.
- Memorization vs. Generalization: The current design of the algorithm constructs manifolds using interpolation. This means that performance is good at points close to PHOENIX subset grid points, but is highly dependent on the type of interpolation used. As interpolators require memorization of the data, advanced interpolation becomes extremely expensive in terms of disk utilization. Future work would involve constructing manifolds using more generalizable ML methods such as lasso or ridge regression, which would allow for much better generalization, high speed, and lower disk utilization at the expense of some accuracy.
- Extrinsic Absence: The current design of our algorithm does not account for extrinsic parameters that modify the appearance of spectra such as rotational broadening and Doppler shifting. Future work would need to develop ways to tune these extrinsic parameters alongside stellar parameters, enabling users to optimize these frequently-observed extrinsic parameters on top of the base stellar parameters.
- Framework Overhead: As this algorithm is currently more proof of concept than practical, it uses convenience functions from various libraries, which naturally introduces some level of overhead and leaves performance on the table. Future work would involve writing custom functions expressly designed for blase, most likely a complete rewrite of the library from the ground up. This has the potential to greatly increase the speed of this

- algorithm, depending on how much overhead is avoided with a bespoke implementation.
- Pseudo-Interpretability: Our algorithm boasts interpretability by considering spectral lines as the objects of interest as opposed to the rather uninterpretable flux values of other approaches. However, this is only a step in the direction of interpretability. True interpretability would decompose a spectrum not into a set of spectral lines, but into a set of species component spectra, which requires a much more advanced understanding of different species and their behavior, as well as direct access to a radiative transfer code as opposed to an off-the-shelf model grid. This approach would also extend the inference from just stellar parameters defined by a grid to any set of parameters accounted for in the radiative transfer model, down to specific species abundances. So while we were able to identify the spectral lines used in our figures, it is not necessarily valuable to try to identify all 128,723 lines that we identify as unique with our algorithm. blase is agnostic to the identity of the line that it is optimizing. We study these lines as blase sees them (i.e. their four shape parameters), because for the purposes of this study, that is the only information that is useful. Having more interpretability would let scientists actually study certain species and their spectral lines.
- The Continuum Black Box: Continuum normalization is a process that is not yet completely understood, and is currently done as a preprocessing step with a fairly simple algorithm. Future work would dive deeper into the science of continua and develop more advanced methods that can discern continua with greater accuracy and less modeling restrictions. This would increase accuracy for end users.
- One Voigt Fits All: The current assumption of blase is that every spectral line is a Voigt profile. This assumption is largely true, but there are situations where that is simply not enough. Future studies need to account for more advanced spectral line profiles and procedures to deal with phenomena such as ro-vibrational bands. This would increase accuracy for end users.

### 6. CONCLUSION

In this study, we have presented a proof-of-concept algorithm that **deals with** a subset of the PHOENIX spectral model grid ( $T_{\rm eff}$ : [2300, 12000] K,  $\log(g)$ :

<sup>693</sup> [2, 6] dex, [Fe/H]: [-0.5, 0] dex, λ: [8038, 12849] <sup>694</sup> Å). We create state dictionaries for all spectra in the <sup>695</sup> PHOENIX subset using blase, recasting spectra <sup>696</sup> into lists of Voigt profiles, and lossily compress the <sup>697</sup> spectral data by a factor of around 20. They are <sup>698</sup> available on Zenodo at https://zenodo.org/records/ <sup>699</sup> 11246174 (Shankar 2024).

We create the PHOENIX generator and implement a performant spectral reconstruction algorithm, enabling anyone to create reconstructions of PHOENIX spectra with continuously valued stellar parameters.

We then introduce and test our GP minimization algorithm to infer stellar parameters. Two test passes on 210 noise-free synthetic models ( $T_{\rm eff}$ : 707 [3000, 11000] K,  $\log(g)$ : [2, 6] dex, [Fe/H]: [-0.5, 0] dex) yield average absolute deviations from true values of 93 K in  $T_{\rm eff}$ , 0.24 dex in  $\log(g)$ , and 0.056 dex in [Fe/H] in low-temperature ( $T_{\rm eff}$  < 7000) regimes. In high-temperature regimes ( $T_{\rm eff}$  > 7000), the errors increase to 347 K in  $T_{\rm eff}$ , 0.26 dex in  $\log(g)$ , and 0.16 dex in [Fe/H].

In its current state, our algorithm requires that the spectra not contain noticeable Doppler shifting, rotational broadening, **noise**, or other confounding factors. The methods discussed here represent a step down a

718 road not traveled in spectral inference, and have the 719 potential to become more advanced in the future by 720 fully utilizing the strengths of physics-informed machine 721 learning.

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Software: altair (VanderPlas et al. 2018; Satya730 narayan et al. 2017), astropy (Astropy Collaboration
731 et al. 2013, 2018, 2022), blasé/blase (Gully-Santiago
732 & Morley 2022), CUDA (NVIDIA et al. 2020), gollum
733 (Shankar et al. 2024), matplotlib (Hunter 2007), numpy
734 (Harris et al. 2020), pandas (pandas development team
735 2020; Wes McKinney 2010), Python (Van Rossum &
736 Drake 2009), PyTorch/torch (Paszke et al. 2019), scikit737 optimize/skopt (Head et al. 2018), scipy (Virtanen
738 et al. 2020), tqdm (da Costa-Luis 2019), vegafusion
739 (Kruchten et al. 2022),

### REFERENCES

782

740 Astropy Collaboration, Robitaille, T. P., Tollerud, E. J., et al. 2013, A&A, 558, A33, 741 doi: 10.1051/0004-6361/201322068 Astropy Collaboration, Price-Whelan, A. M., Sipőcz, B. M., et al. 2018, AJ, 156, 123, doi: 10.3847/1538-3881/aabc4f 745 Astropy Collaboration, Price-Whelan, A. M., Lim, P. L., et al. 2022, ApJ, 935, 167, doi: 10.3847/1538-4357/ac7c74 746 747 Bedell, M., Hogg, D. W., Foreman-Mackey, D., Montet, B. T., & Luger, R. 2019, The Astronomical Journal, 158, 748 164, doi: 10.3847/1538-3881/ab40a7 750 Bradbury, J., Frostig, R., Hawkins, P., et al. 2018, JAX: composable transformations of Python+NumPy 751 programs, 0.3.13. http://github.com/google/jax 752 Cargile, P. A., Conroy, C., Johnson, B. D., et al. 2020, The 753 Astrophysical Journal, 900, 28, 754 doi: 10.3847/1538-4357/aba43b Czekala, I., Andrews, S. M., Mandel, K. S., Hogg, D. W., & Green, G. M. 2015, ApJ, 812, 128, 757 doi: 10.1088/0004-637X/812/2/128 758

da Costa-Luis, C. O. 2019, Journal of Open Source

Software, 4, 1277, doi: 10.21105/joss.01277

759

761 García Pérez, A. E., Allende Prieto, C., Holtzman, J. A., et al. 2016, AJ, 151, 144, doi: 10.3847/0004-6256/151/6/144 763 764 Gerber, J. M., Magg, E., Plez, B., et al. 2023, A&A, 669, A43, doi: 10.1051/0004-6361/202243673 765 766 Gully-Santiago, M., & Morley, C. V. 2022, ApJ, 941, 200, doi: 10.3847/1538-4357/aca0a2 767 768 Harris, C. R., Millman, K. J., van der Walt, S. J., et al. 2020, Nature, 585, 357, doi: 10.1038/s41586-020-2649-2 769 770 Head, T., MechCoder, Louppe, G., et al. 2018, scikit-optimize/scikit-optimize: v0.5.2, v0.5.2, Zenodo, 771 doi: 10.5281/zenodo.1207017 772 773 Horta, D., Price-Whelan, A. M., Hogg, D. W., Ness, M. K., & Casey, A. R. 2025, arXiv e-prints, arXiv:2502.01745. 774 https://arxiv.org/abs/2502.01745 775 776 Hunter, J. D. 2007, Computing in Science & Engineering, 9, 90, doi: 10.1109/MCSE.2007.55 778 Husser, T. O., Wende-von Berg, S., Dreizler, S., et al. 2013, A&A, 553, A6, doi: 10.1051/0004-6361/201219058 780 Ida, T., Ando, M., & Toraya, H. 2000, Journal of Applied Crystallography, 33, 1311, 781

doi: https://doi.org/10.1107/S0021889800010219

```
783 Karalidi, T., Marley, M., Fortney, J. J., et al. 2021, ApJ,
     923, 269, doi: 10.3847/1538-4357/ac3140
785 Kawahara, H., Kawashima, Y., Masuda, K., et al. 2022,
     ExoJAX: Spectrum modeling of exoplanets and brown
786
     dwarfs, Astrophysics Source Code Library, record
787
     ascl:2206.003
    Kingma, D. P., & Ba, J. 2017, Adam: A Method for
     Stochastic Optimization.
790
     https://arxiv.org/abs/1412.6980
791
792 Kramida, A., Yu. Ralchenko, Reader, J., & and NIST ASD
     Team. 2023, NIST Atomic Spectra Database (ver. 5.11),
793
     [Online]. Available: https://physics.nist.gov/asd
794
     [2024, June 12]. National Institute of Standards and
795
     Technology, Gaithersburg, MD.
    Kruchten, N., Mease, J., & Moritz, D. 2022, in 2022 IEEE
797
     Visualization and Visual Analytics (VIS), 11–15,
798
     doi: 10.1109/VIS54862.2022.00011
799
800 Kurucz, R. L. 2005, Memorie della Societa Astronomica
     Italiana Supplementi, 8, 14
801
802 Lacy, B., & Burrows, A. 2023, The Astrophysical Journal,
     950, 8, doi: 10.3847/1538-4357/acc8cb
804 Leung, H. W., & Bovy, J. 2019, MNRAS, 483, 3255,
     doi: 10.1093/mnras/sty3217
805
    -. 2024, MNRAS, 527, 1494, doi: 10.1093/mnras/stad3015
807 López-Valdivia, R., Mace, G. N., Han, E., et al. 2023, ApJ,
     943, 49, doi: 10.3847/1538-4357/acab04
808
  Mahadevan, S., Ramsey, L., Bender, C., et al. 2012, in
809
     Society of Photo-Optical Instrumentation Engineers
810
     (SPIE) Conference Series, Vol. 8446, Ground-based and
811
     Airborne Instrumentation for Astronomy IV, ed. I. S.
812
     McLean, S. K. Ramsay, & H. Takami, 84461S,
813
     doi: 10.1117/12.926102
815 Majewski, S. R., Schiavon, R. P., Frinchaboy, P. M., et al.
     2017, AJ, 154, 94, doi: 10.3847/1538-3881/aa784d
816
```

Marley, M. S., Saumon, D., Visscher, C., et al. 2021, ApJ,

920, 85, doi: 10.3847/1538-4357/ac141d

818

```
arXiv e-prints, arXiv:2402.00758,
     doi: 10.48550/arXiv.2402.00758
821
822 Mukherjee, S., Fortney, J. J., Morley, C. V., et al. 2024,
     arXiv e-prints, arXiv:2402.00756,
823
     doi: 10.48550/arXiv.2402.00756
824
825 NVIDIA, Vingelmann, P., & Fitzek, F. H. 2020, CUDA,
     release: 10.2.89.
     https://developer.nvidia.com/cuda-toolkit
827
  pandas development team, T. 2020, pandas-dev/pandas:
828
     Pandas, latest, Zenodo, doi: 10.5281/zenodo.3509134
820
830 Paszke, A., Gross, S., Massa, F., et al. 2019, PyTorch: An
     Imperative Style, High-Performance Deep Learning
831
     Library. https://arxiv.org/abs/1912.01703
832
833 Rains, A. D., Nordlander, T., Monty, S., et al. 2024,
     MNRAS, 529, 3171, doi: 10.1093/mnras/stae560
834
835 Rayner, J. T., Cushing, M. C., & Vacca, W. D. 2009, ApJS,
     185, 289, doi: 10.1088/0067-0049/185/2/289
836
  Różański, T., Ting, Y.-S., & Jabłońska, M. 2023, arXiv
837
     e-prints, arXiv:2306.15703,
838
     doi: 10.48550/arXiv.2306.15703
839
  Satyanarayan, A., Moritz, D., Wongsuphasawat, K., &
840
     Heer, J. 2017, IEEE transactions on visualization and
841
     computer graphics, 23, 341
843 Shankar, S. 2024, blase II: PHOENIX Subset Clone
     Archive, 0.0.1, Zenodo, doi: 10.5281/zenodo.11246174
845 Shankar, S., Gully-Santiago, M., Morley, C., et al. 2024,
     The Journal of Open Source Software, 9, 6601,
846
     doi: 10.21105/joss.06601
847
  Van Rossum, G., & Drake, F. L. 2009, Python 3 Reference
848
     Manual (Scotts Valley, CA: CreateSpace)
849
   VanderPlas, J., Granger, B., Heer, J., et al. 2018, Journal of
850
     Open Source Software, 3, 1057, doi: 10.21105/joss.01057
851
  Virtanen, P., Gommers, R., Oliphant, T. E., et al. 2020,
     Nature Methods, 17, 261, doi: 10.1038/s41592-019-0686-2
  Wes McKinney. 2010, in Proceedings of the 9th Python in
     Science Conference, ed. Stéfan van der Walt & Jarrod
     Millman, 56 – 61, doi: 10.25080/Majora-92bf1922-00a
856
  Wheeler, A. J., Abruzzo, M. W., Casey, A. R., & Ness,
857
     M. K. 2023, AJ, 165, 68, doi: 10.3847/1538-3881/acaaad
```

819 Morley, C. V., Mukherjee, S., Marley, M. S., et al. 2024,