11

12

13

14

15

16

17

18

19

20

21

22

23

A New Hybrid Machine Learning Method for Stellar Parameter Inference

SUJAY SHANKAR, MICHAEL A. GULLY-SANTIAGO, AND CAROLINE V. MORLEY

¹Department of Astronomy, The University of Texas at Austin, Austin, TX 78712, USA

ABSTRACT

The advent of machine learning (ML) is revolutionary to numerous scientific disciplines, with a growing number of examples in astronomical spectroscopic inference, as ML is expected to be more powerful than traditional techniques. Here we introduce a hybrid ML (HML) method that combines automatic differentiation (autodiff), interpolation, and Bayesian optimization to infer stellar parameters given stellar spectra. The stellar parameters we study are T_{eff} , $\log(g)$, and [Fe/H], but this method has potential for extension to other properties such as $[\alpha/\text{Fe}]$ (alpha element abundance), C/O (carbon-oxygen ratio), and f_{sed} (sedimentation efficiency). We first use blase's nontraditional semi-empirical approach to treating spectra as sets of tunable spectral lines. blase is used on 1,314 spectra from the PHOENIX synthetic spectral model grid, identifying 128,723 spectral lines. For each of these lines, we continuously map stellar parameters to spectral line parameters using regular grid linear interpolation. These manifolds are aggregated to create the PHOENIX generator, enabling parallelized reconstruction of spectra given continuously valued stellar parameters. Gaussian Process minimization is then used to infer stellar parameters by minimizing the root-mean-square (RMS) loss between the input spectrum and PHOENIX generator spectra. From testing, the inference error in $T_{\rm eff}$ was 185 K, $\log(q)$ was 0.19, and [Fe/H] was 0.12 dex. Our products are an archive of the blase models of the PHOENIX subset, as well as the spectral reconstruction and inference algorithms themselves. This study is a proof of concept showing that semi-empirical HML is a viable alternative to traditional approaches.

1. INTRODUCTION

Stellar spectra are exceedingly rich sources of information about the stars that produce them. Spectra encode fundamental properties such as temperature, surface gravity, and chemical composition via their numerous absorption lines. Extrinsic properties such as the stellar radial velocity or the projected equatorial rotation shift the wavelengths of lines and broaden their widths, respectively. Observing the spectrum alters it again; the resolution, bandwidth, and other properties of the instrument change the fidelity at which we observe the spectrum, and can limit our ability to extract fundamental properties precisely. Observed stellar spectra thus represent extremely complex, data, influenced by multiple parameters, that have gone through multiple transformations before reaching our detectors.

Modern astronomical spectroscopy takes advantage of intuitive, performant spectral models such as

Corresponding author: Sujay Shankar sujays2001@gmail.com

41 KORG (Wheeler et al. 2023), however it would 42 further benefit from the paradigm of interpretabil-43 ity. The determination of fundamental properties, the 44 creation of Extreme Precision Radial Velocity (EPRV) 45 templates, and the application of composite spectral fit-46 ting could all leverage such an innovation. This am-47 bitious aim may be broadly referred to as a "founda-48 tional spectroscopy model for astrophysics", in reference 49 to the same category of models used for large language 50 models (LLMs) in artificial intelligence (AI). There are 51 many challenges with creating such a foundational spec-52 tral model for astrophysics. First, we know our physi-53 cal inputs into the spectral modeling process are im-54 perfect. Second, simplifying assumptions in stellar (and 55 substellar) atmospheres are necessarily inexact. Ulti-56 mately computational costs have prevented the training 57 of such models. Most prevailing solutions have therefore 58 had to choose either a model driven approach, in which 59 the precomputed models are taken as gospel, or a data 60 driven/empirical approach, in which our knowledge of 61 stellar physics is ignored or treated phenomenologically, 62 depending on the application.

Spectroscopic surveys such as APOGEE (Majewski et al. 2017) use their own in-house pipelines to extract stellar parameters from spectra (ASPCAP (Gar- cía Pérez et al. 2016) in the case of APOGEE), and these pipelines appear effective. The core assumption for the vast majority of pipelines is that the data to be analyzed is a list of pixels. Analysis pipelines may be closed-source or limited to the scope of the survey itself, causing a sort of siloing effect among surveys. This motivates the development of more universal, instrumentagnostic open-source frameworks that can apply broadly to a range of spectral observations with relatively little tuning.

Multiple efforts have been made in this direction, treating spectra in different ways. The standard practice is to treat the wavelength and flux as simply two arrays and use bespoke algorithms tailored to a small number of well-calibrated spectral lines to obtain fundamental stellar parameters and chemical compositions (López-Valdivia et al. 2023; Rayner et al. 2009). Other wholes spectrum fitting abstractions decompose model spectra into an eigenbasis, implementing the data-model comparison stage as a tractable regression, such as starfish (Czekala et al. 2015).

Ideally, we want a system that can self-consistently 88 learn, a genuine AI foundational spectral model. Such a 89 system would enable the assignment of accurate stellar 90 parameters, and could yield re-usable interpretable spec-91 tral models. blase, first presented in Gully-Santiago 92 & Morley 2022, took an important, albeit limited, step 93 in this direction, treating spectra not as a set of pixels 94 or a set of eigenbasis coefficients but as a set of inter-95 pretable and traceable spectral lines, specifically Voigt 96 profiles. Each of these approaches has tradeoffs, but one 97 key scientific advantage of blase comes from its ability 98 to adapt to new information, while preserving some ad-99 herence to physics-based models. This intelligent capa-100 bility stems from its ability to fit a theoretically unlim-101 ited number of nonlinear spectral line parameters with 102 automatic differentiation (autodiff). Autodiff is a tech-103 nology that tracks transformations made to data using 104 the chain rule, even being able to differentiate control 105 flow transformations involving if-else blocks, for exam-106 ple. With the gradient obtained from autodiff's chain 107 rule, we can optimize model parameters by just going 108 against the direction of the gradient (because we usu-109 ally want to minimize something such as a loss function, 110 we go in the direction of greatest decrease, which is always the negative of the gradient). Autodiff has been 112 used successfully in other astrophysical contexts such as 113 exojax (Kawahara et al. 2022) and wobble (Bedell 114 et al. 2019), but the recasting of spectra into sets of inherently nonlinear spectral lines positions blase as a unique and promising semi-empirical tool. The original blase paper demonstrated the ability to tune spectral lines with autodiff and 'clone' spectra, recasting them as ML models defined by interpretable sets of tuned spectral lines, however it was restricted to a pre-selected static synthetic model.

Here we introduce the next logical step in the sequence of expanding interpretable spectroscopic machine learning from operating on a single grid point and towards an entire 3D grid of precomputed spectra. We rebrand this augmentation as blase3D.

Ideally this process would be monolithic, with the 128 end-to-end spectral inference code powered by a single 129 autodiffable machine learning framework, like PyTorch (Paszke et al. 2019) or JAX (Bradbury et al. 2018). 131 However, here we separate the problem into three pieces, only the first of which is currently differentiable. In sec-133 tion 2, we scale out the blase method to 1,314 precom-134 puted synthetic spectral model clones, yielding a down-135 loadable archive of pretrained machine learning mod-136 els with 128,723 unique spectral lines. In section 3, 137 we then fit manifolds mapping stellar parameters to 138 uniformly-derived spectral line parameters using regular 139 grid linear interpolation. Finally, in section 4, we show 140 how reconstructions of the spectra using said manifolds 141 can be used for inferring stellar fundamental properties 142 from spectra. This final step resembles the aims of "at-143 mospheric retrievals", but in principle should be faster, 144 adaptive, and reusable. An overview of this process is 145 shown in Figure 1.

2. CLONING THE PHOENIX MODEL GRID

2.1. The PHOENIX Subset

For the purposes of this study, we chose the widely-adopted PHOENIX synthetic spectral model grid (Husser et al. 2013). Our approach can be straightforwardly applied to any other model grid in the future, including substellar atmosphere grids such as Sonora (Marley et al. 2021; Karalidi et al. 2021; Morley et al. 2024; Mukherjee et al. 2024), but for now we limit our scope to a rectilinear subset of the PHOENIX grid, focusing on near solar metallicities and a broad range of effective temperature and surface gravity, with details given in Table 1. This approach is taken due to the computational cost of interpolation algorithms. Future versions with more advanced models will be able to bypass the limitation of a rectilinear subset.

146

147

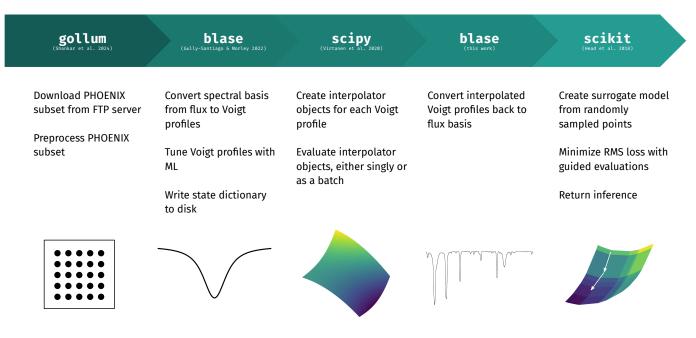


Figure 1. Overview of the process used in this study.

Parameter	Symbol	Interval	Sampling
Alpha Element Abundance	α	[0] dex	N/A
Iron Abundance	$[\mathrm{Fe/H}]$	[-0.5, 0] dex	$0.5 \mathrm{dex}$
Effective Temperature	$T_{ m eff}$	[2300, 12000] K	$100~\mathrm{K}$ until $7000~\mathrm{K},$ then $200~\mathrm{K}$
Surface Gravity	$\log(g)$	[2, 6]	0.5
Wavelength	λ	[8038, 12849] Å	$\mathbf{R}=500,000$

Table 1. The subset of the PHOENIX grid used in this study. These limits were imposed to reduce the computational cost of the algorithms and to ensure a rectilinear parameter space in order to work with scipy's RegularGridInterpolator (Virtanen et al. 2020). The wavelength limits in particular roughly line up with that of the Habitable Zone Planet Finder (HPF) spectrograph (Mahadevan et al. 2012). This subset is comprised of 1,314 individual spectra: 73 $T_{\rm eff}$ values, 9 $\log(g)$ values, and 2 [Fe/H] replaces

178

179

180

181

First, the PHOENIX subset was programmatically retrieved with gollum (Shankar et al. 2024), which
downloaded spectra from the PHOENIX FTP server.
The spectra were then put through a three-step preprocessing pipeline similar to that from Gully-Santiago &
Morley 2022.

170

171

172

173

174

175

176

- 1. Blackbody Division: Since the T_{eff} of each spectrum is known, the **corresponding** blackbody spectrum was divided out.
- 2. Percentile Normalization: The spectra were normalized by dividing them by their 99th percentile in order to collapse the dynamic range of flux and only look at relative features.

3. Continuum Normalization: The spectra were further normalized by dividing them by a 5th order polynomial continuum fit using a peak-finding filter in order to eliminate curvature that would inhibit line modeling.

 $_{\rm 182}$ Mathematically, we can express the preprocessing as follows:

$$\bar{\mathsf{S}} = \frac{\mathsf{S}}{\mathsf{BQ}_5 P_{99}} \tag{1}$$

where $\bar{\mathsf{S}}$ is the preprocessed spectrum, S is the original spectrum, B is the blackbody spectrum, Q_n is the n^{th} order polynomial continuum fit, and P_n is the n^{th} percentile function. Arithmetic operations between arrays are assumed to be elementwise in all following notation.

2.3. Line Identification with blase

The next step was to convert the PHOENIX subset 191 into a physically interpretable intermediate representa-192 tion: a table of spectral line properties rather than an 193 array of fluxes. We used blase, which models spectral 194 lines as Voigt profiles and tunes the profiles to mimic the 195 original PHOENIX spectrum with back propagation. 196 Back propagation, put simply, is the process of moving 197 in the autodiff gradient field to update ML model param-198 eters (like mentioned earlier, usually against the gradi-199 ent because we minimize loss functions). Four parameters were optimized: the line center μ , the log-amplitude $201 \ln(a)$, the Gaussian width σ , and the Lorentzian width γ . The optimization used the Adam optimizer (Kingma & 203 Ba 2017) with a learning rate of 0.05 over 100 epochs. 204 In addition, we limited two custom parameters: wing cut 205 to 6000 and prominence to 0.005. Wing cut (in pixels) 206 is a parameter that determines the extent of the Voigt 207 profile to evaluate, saving computational resources by 208 not evaluating negligible line wings. Prominence (in 209 normalized flux counts) sets a lower limit for the 210 amplitude of detected lines, which saves resources by 211 disregarding shallow lines, so in our case we disregard 212 lines that affect the spectrum by < 0.5%. In short, our 213 choices for wing cut and prominence decrease the com-214 putational cost of blase's cloning process at the expense 215 of decreasing its accuracy slightly. We note that blase 216 uses the pseudo-Voigt approximation, which saves on 217 computational cost while remaining accurate to about 218 1% (Ida et al. 2000). The pseudo-Voigt approximation 219 uses a weighted average of a Gaussian and Lorentzian as 220 opposed to a convolution. blase's pseudo-Voigt profile 221 implementation uses the following:

$$\tilde{\mathbf{V}}_{\mu}(\lambda) = a \left[\eta \mathbf{L}(\lambda - \mu'; f) + (1 - \eta) \mathbf{G}(\lambda - \mu'; f) \right]$$
(2a)
$$\eta = \sum_{n=1}^{3} \mathbf{u}_{n} \left(\frac{2\gamma}{f} \right)^{n}$$
(2b)
$$f = 32 \sum_{n=0}^{5} \mathbf{v}_{n} \left(\sqrt{2 \ln(2)} \sigma \right)^{5-n} (\gamma)^{n}$$
(2c)

$$\mathbf{u} = \begin{bmatrix} 1.36603 \\ -0.47719 \\ 0.11116 \end{bmatrix} \quad \mathbf{v} = \begin{bmatrix} 1 \\ 2.69269 \\ 2.42843 \\ 4.47163 \\ 0.07842 \\ 1 \end{bmatrix}$$

where **L** and **G** are abbreviations for Lorentzian and Gaussian profiles, respectively. Notice that we use μ' instead of μ in the formula. This is because blase optionally allows the line center to shift slightly during op-

timization, and it is this shifted center which is used in computation. The individual Voigt profiles are still indexed by μ for cross-model line identification, explained in the next section. Once optimization was complete, the list of identified lines, was saved to a 'state dictionary': a common representation for pre-trained machine learning models that can be stored to disk for reuse later. These are stored in the .pt file format for each of the 1,314 PHOENIX subset grid points. The total disk space these files take up is 465 MB (382 MB when downloaded as a zip archive). For reference, the storage space the PHOENIX subset takes up on disk is approximately 8.1 GB. This represents a data compression factor of around 20 just by recasting the spectrum with blase.

3. INTERPOLATING MANIFOLDS

240

241

3.1. Cross-Model Line Identification

As previously mentioned, blase tunes the line centers of detected lines. This means that from one PHOENIX spectrum to the next, the same line could have a slightly different line center. Since the goal of this study is to interpolate the properties of each line, we needed to identify the presence of a particular line across the PHOENIX subset, associating the same line with every occurrence. We decided to do this by using the line centers μ of the detected lines pre-optimization. Now with each spectral line indexed by μ , we had four parameters to interpolate: μ' , $\ln(a)$, σ , and γ . Note that since we are dealing with the parameters of Voigt profiles, we can see in Equation 2 that even if the interpolation method is linear, a final spectral reconstruction will vary nonlinearly in flux.

Spectral lines were often only detected in some spectra 258 from the PHOENIX subset. In Figure 2, we show that 259 different grid points sport differing counts of detected 260 spectral lines.

This missing-lines phenomenon can arise for different reasons. Perhaps for astrophysical reasons: stellar atmospheres genuinely do not produce that line at detectable strength at the given temperature and surface gravity. Or alternatively, our line-finding and line-association algorithms missed it. Whatever the cause, these missing lines have immediate practical consequences. Rectilines ear interpolation schemes break in regions where a line does not appear; you can't interpolate a quantity that simply doesn't exist.

To solve this, we artificially populated missing grid points with log-amplitudes of -1000, which retained interpolator stability while nullifying the evaluated line. Examples of the appearance of missing sections in heatmaps where a line does not appear are shown in Figure 3 and Figure 4. In total, across the entire PHOENIX

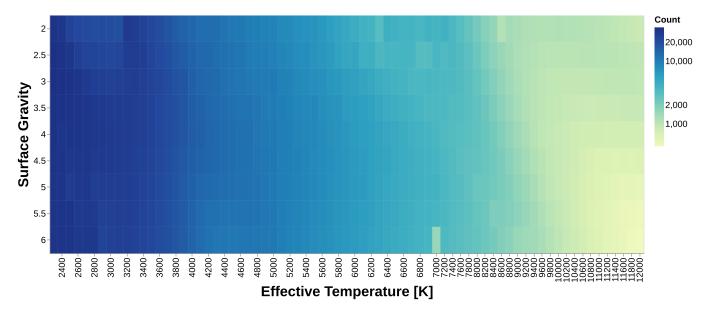


Figure 2. Number of detected spectral lines at each grid point of a slice of the PHOENIX subset at solar metallicity. We can see that the number of detected lines decreases with increasing $T_{\rm eff}$. Also note that from $T_{\rm eff}=7000$ K onward, PHOENIX's sampling increment changes from 100 K to 200 K.

325

subset, blase detected 128,723 individual spectral lines. Every one of these lines can be visualized as a manifold mapping a 3D stellar parameter vector to a 4D spectral line parameter vector, and every one must be interpolated.

3.2. Continuously Evaluable Manifolds

285

For each line, the inputs to the interpolator were the three input parameters $T_{\rm eff}$, $\log(g)$, and [Fe/H], and the output was a list of four parameters, μ' , $\ln(a)$, σ , and γ . For each line, one of these interpolator objects was created using linear interpolation, and these interpolators were aggregated into a single list, which was then written to disk in the .pkl file storage format. These interpolators generate multiple manifolds representing the following mapping:

$$\begin{bmatrix} T_{\text{eff}} \\ \log(g) \\ [\text{Fe/H}] \end{bmatrix} \rightarrow \begin{bmatrix} \mu' \\ \ln(a) \\ \sigma \\ \gamma \end{bmatrix}$$
 (3)

These interpolators could now be evaluated at any point lying within the domain of the PHOENIX subset, turning a discretely sampled PHOENIX subset into a continuously evaluable function, sometimes called a spectral emulator. With the given size of the PHOENIX
subset, the interpolator list takes up 13.2 GB of disk
space. This evaluation is able to reconstruct an existing PHOENIX spectrum or alternatively interpolate a new
spectrum within the domain of the PHOENIX subset,
so we call this the PHOENIX generator. In Figure 5

²⁹⁶ and Figure 6, we show the same spectral lines as in Fig-²⁹⁷ ure 3 and Figure 4, but now supersampled using the ²⁹⁸ PHOENIX generator evaluated over the same slice.

The spectral reconstruction process is done by iterating over the PHOENIX generator, evaluating each interpolator at the given coordinates, then reshaping the data into the same format that PyTorch uses for state dictionaries. During the iteration, if the interpolated log-amplitude of the line is less than -100, the line is excluded from the state dictionary. We do this to avoid artifacts in the manifolds due to the artifical population of log-amplitudes of -1000 where grid points were missing.

Finally, the state dictionary is fed into blase's SparseLinearEmulator, which reconstructs the spec313 trum by constructing a forward model based on the in314 put state dictionary. Any nan values are set to 1 (which
315 we can do because the spectra are all normalized), and
316 the spectral reconstruction is complete. We can observe
318 in Figure 7 that the reconstructed solar spectrum is not
319 simply a pixel interpolation between the nearest grid
320 points. It is interpolating the spectral line properties
321 using hundreds of thousands of manifolds, each repre322 senting a nonlinear parameter in the shape of the spec323 tral line.

4. BAYESIAN INFERENCE AND TESTING

4.1. Spectral Reconstruction Time

A typical use case for the PHOENIX generator may be to batch reconstruct spectra from an array of input stellar parameters. Therefore, there is some motivation

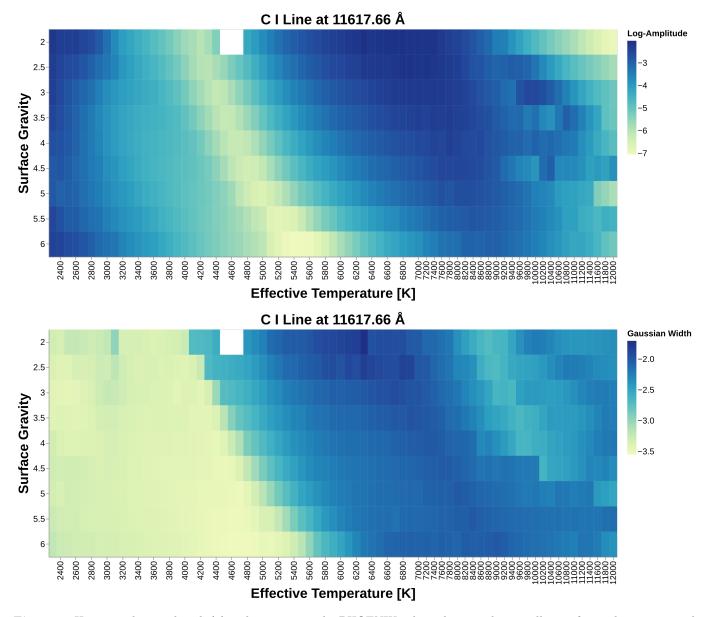


Figure 3. Heatmap showing how $\ln(a)$ and σ vary over the PHOENIX subset slice at solar metallicity of an unknown spectral line. Notice the missing chunk in the top left of the figure; blase did not detect a spectral line here, but we have to artificially populate those points with lines that have $\ln(a) = -1000$. This and all spectral lines shown in this paper were identified using the NIST spectral line database (Kramida et al. 2023).

to reduce the computational cost of this procedure to tractable levels. We evaluate the computational time needed to use the PHOENIX generator in two distinct ways. First, for a single input, which would be relevant in serial applications. Second, for an array of multiple inputs, which would be relevant in parallel applications. The RegularGridInterpolator API allows for the passing in of an entire array of input coordinates to be evaluated at once. However using blase to reconstruct the spectrum from our interpolated state dictionary is always done serially, leading to what is actually more of a pseudo-parallel evaluation, but extremely per-

³⁴¹ formant nonetheless. Performance results are shown in Figure 8, and we can see that the multi-reconstruction ³⁴² is much faster than a series of single reconstructions.

4.2. Inference Algorithm

We elected to use Bayesian optimization as the inference algorithm, specifically the gp_minimize function from the scikit-optimize library (Head et al. 2018). This algorithm uses a Gaussian Process to model the objective function, which in this case was the RMS (Root-Mean-Square) loss between the interpolated spectrum

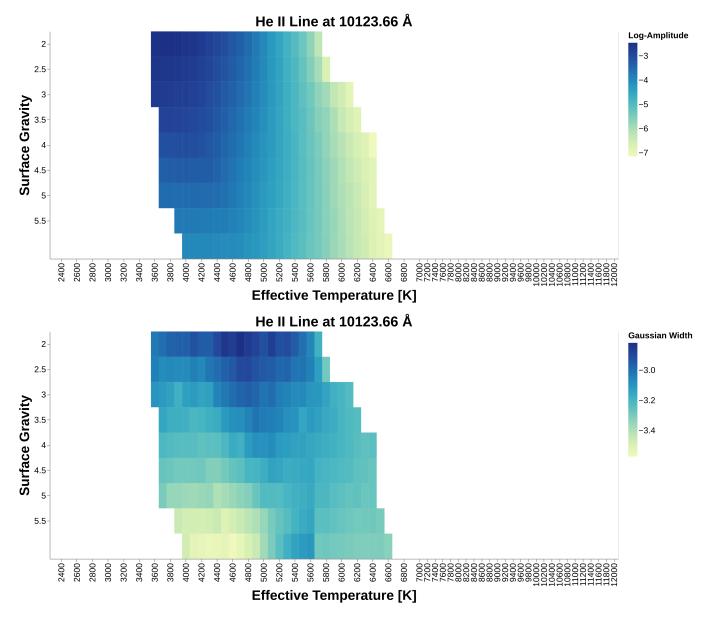


Figure 4. Heatmap showing how $\ln(a)$ and σ vary over the PHOENIX subset slice at solar metallicity of a Helium II spectral line. We can see that blase detects this line at only a select chunk of grid points in PHOENIX, leading to the large amount of missing data for the line.

M and the true spectrum D, defined as:

$$\mathcal{L} = \left\langle (\mathsf{M} - \mathsf{D})^{\circ 2} \right\rangle^{1/2} \tag{4}$$

The optimizer was configured to first run 100 random evaluations to seed the surrogate model, then run 20 more evaluations now guided by the surrogate model. This totals to 120 evaluations, a large sample to create a fairly detailed surrogate model, then a moderately precise guided evaluation phase, which was deemed sufficient for this study. Fine-tuning these numbers is possible, but simply not warranted for a proof-of concept method. One inference run takes on average just under 7.5 minutes to complete.

4.3. Bayesian Optimizer Performance

To test the performance of the inference algorithm,
we used the PHOENIX subset itself. At first glance,
this may seem circular, as the PHOENIX generator
has memorized the PHOENIX subset, being able to
reconstruct a PHOENIX spectrum when evaluated at
that grid point. However, that strategy allows us to
use the PHOENIX subset as test data in the context
has of Bayesian optimization. The gp_minimize surrogate
model is seeded by random continuously sampled generator evaluations within the search space, not grid points
of the PHOENIX subset, meaning the surrogate model

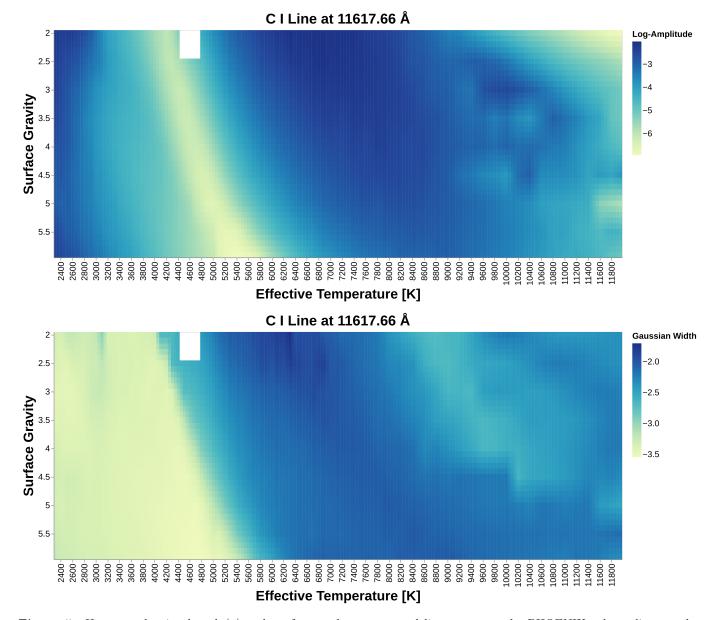


Figure 5. Heatmap showing how $\ln(a)$ and σ of our unknown spectral line vary over the PHOENIX subset slice at solar metallicity, now supersampled with the PHOENIX generator. Notice that the missing chunk in the top left still exists and does not display any artifacts, as the artificially populated points are removed after interpolation to retain the model's integrity. Also see that the x-axis spacing is now uniform, as the PHOENIX generator was evaluated at constant step.

³⁶⁷ has no memorization to speak of. If the optimizer had ³⁶⁸ been a grid-based strategy, this would not have been ³⁶⁹ possible, because then the surrogate model would be af-³⁷⁰ fected by memorization.

We know that in typical observational settings, are a coarse estimate for $T_{\rm eff}$ tends to be fairly well-some account and from ancillary data prior to even looking at the spectra. So when testing the inference algorithm, we limited its search space to only include $T_{\rm eff}$ which lay within 500 K of the true value on either side. $\log(g)$ and [Fe/H] were allowed to vary freely. The test sample consisted of 9 unique $T_{\rm eff}$ values, 3 unique $\log(g)$ values,

 $_{379}$ and 2 unique [Fe/H] values, totaling 54 unique spectra $_{380}$ in the test set. $T_{\rm eff}$ ranged from 3000 K to 11000 K $_{381}$ in increments of 1000 K, $\log(g)$ ranged from 2 to 6 in $_{382}$ increments of 2, and [Fe/H] ranged from -0.5 to 0 in $_{383}$ increments of 0.5.

The results of the inference algorithm are as follows: $T_{\rm eff}$ differed from the true result by an average of 185 K or 2.6%. $\log(g)$ differed by an average of 0.19 or 6.8%. $_{387}$ [Fe/H] differed by an average of 0.12 dex, which is 24% of our search range. From this, we can see that $T_{\rm eff}$ was the most accurately inferred parameter, followed by $\log(g)$, and then [Fe/H].

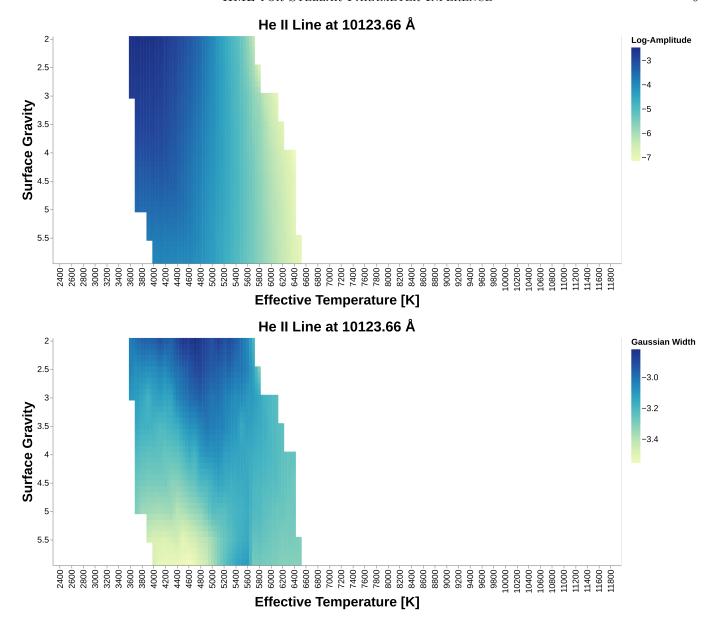


Figure 6. Heatmap showing how $\ln(a)$ and σ of our Helium II spectral line vary over the PHOENIX subset slice at solar metallicity, now supersampled with the PHOENIX generator.

5. DISCUSSION

391

393

5.1. Scientific Applications

This study's paradigm of spectral inference can enable scientists to adopt self-consistent model grids and analyze their spectral line behavior in an interpretable fash-395 396 ion, which has been fairly uncommon practice thus far. Notably, this system tracks the shifting of spectral lines 398 as a function of stellar parameters, which traditionally 399 has been uncommon for algorithms to assess systemati-400 cally. We balance rigidity and flexibility where we want 401 them while maintaining interpretability.

To summarize, we bring to scientists the ability to un-403 derstand exactly what spectral properties we consider 404 mathematically and how we expect those properties to 405 behave on an incredibly detailed level (the 4 line pa-406 rameters of all spectral lines and their corresponding 407 interpolating manifolds), and introduce the concept of 408 postulating one precomputed model grid as the ground 409 truth to base all further analysis on, converting the grid 410 into a generator that can then interface with our infer-411 ence algorithm.

5.2. Technical Considerations

To reiterate, the manifold fitting steps are not end-414 to-end autodifferentiable. As seen in Figure 1, these steps rely on scipy, which is not equipped with autodiff. 416 Without autodifferentiability, the ability to "machine

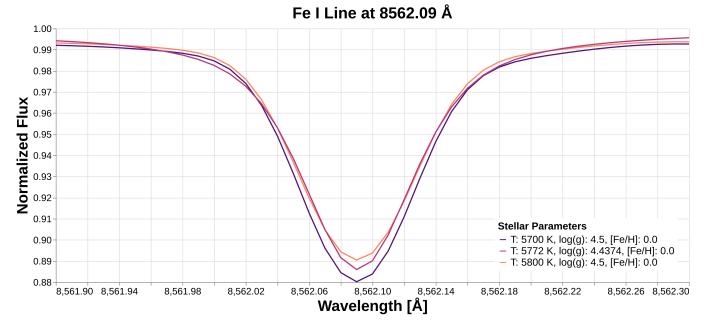


Figure 7. Plot of an Fe I spectral line shown at the closest PHOENIX grid points to the Sun's stellar parameters, as well as a solar spectrum reconstructed with the PHOENIX generator. We can see the spectral line shape be reconstructed mostly between the two native PHOENIX spectra, being closer to the 5800 K spectrum as the Sun's $T_{\rm eff}$ used here is 5772 K.

learn" is significantly reduced compared to a hypothetatical monolithic JAX or PyTorch system. We see three reasons for for developing a non-autodifferentiable system. First, the familiar scipy-based system will serve as an easy entry point for most practitioners who are unfamiliar with autodiff, and may still benefit from and modify the code without expert ML knowledge. Second, this non-autodiff version serves as a pathfinder and benchmark against which an inevitable autodifferentiable version may be compared. Finally, the inventory of familation in interpolation algorithms have not yet been ported to PyTorch or JAX, since machine learning or Gaussian Process fitting schemes are generally preferred within the ML community.

The interpolation scheme presented here represents a proof of concept, showing that leveraging the mapping between synthetic spectral lines and their inputs can yield a semi-empirical basis for data-model comparisons. There are numerous design considerations that could be improved upon with future work. These include but are not limited to the following:

- Limited PHOENIX Subset: The PHOENIX subset used in this study did not include the full PHOENIX grid, which expands the [Fe/H] range to [-4.0, 1.0] dex and the $\log(g)$ range to [0, 6], and also includes the alpha element abundance parameter, which we elected to fix at 0 for this study. In addition to the actual stellar parameters, we also took a subset of the PHOENIX wavelength range,

with the full [500, 55000] Å wavelength range also being left to future work. Users would be able to fit a greater variety of stellar spectra in many different wavelength regimes.

- Strict Wavelength Range: Currently, the generator only supports inference on spectra whose wavelength limits are either equal to it, or encompass that of the generator and have been truncated to match. However, when the spectrum in question has a smaller wavelength range than the generator, currently there is no functionality to truncate the generator. This would require externally indexing the generator's individual interpolators by line center position and selectively evaluating those to eliminate wasteful computation. This takes burden off the users to truncate their data to the PHOENIX generators, making use simpler.
- Single Model Grid: The PHOENIX grid is not the only model grid of synthetic spectra available, and it does not apply to all types of stars. Future work would extend the reach of this study's algorithm to encompass other model grids such as the Sonora series of substellar models, ATLAS (Kurucz 2005), and coolTLUSTY (Lacy & Burrows 2023), reaching practitioners studying various types of stars and spectra. blase should be able to have an option for the user to input which model grid they would like to base the inference on, and to get even more advanced, perhaps even have the abil-

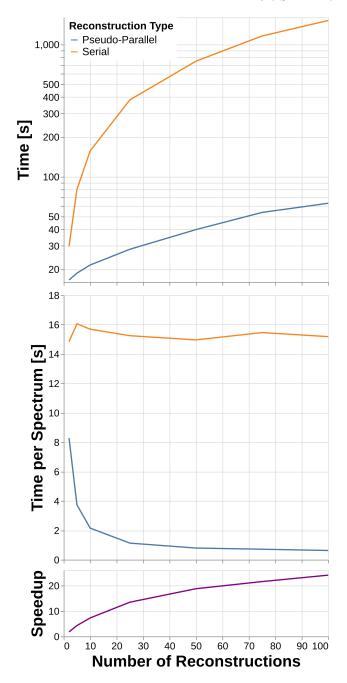


Figure 8. Line chart showing the time taken to reconstruct varying numbers of spectra using the PHOENIX generator (lower is better). We can see that the time taken per spectra for the serial implementation hovers around 15 seconds within run-to-run variance, while the pseudo-parallel implementation continually decreases in time taken per spectrum as the number of inputs increases. The speedup factor (higher is better) increases as more spectra are generated, which is also a desirable outcome.

ity to intelligently determine which model grid to use automatically.

- Memorization vs. Generalization: The current design of the algorithm constructs manifolds using interpolation. This means that performance is good at points close to PHOENIX subset grid points, but is highly dependent on the type of interpolation used. As interpolators require memorization of the data, advanced interpolation becomes extremely expensive in terms of disk utilization. Future work would involve constructing manifolds using more advanced methods, which would allow for much better generalization, high speed, and lower disk utilization at the expense of some accuracy.
- Extrinsic Absence: The current design of our algorithm does not account for extrinsic parameters that modify the appearance of spectra such as rotational broadening and Doppler shifting. Future work would need to develop ways to tune these extrinsic parameters alongside stellar parameters, enabling users to optimize these frequently-observed extrinsic parameters on top of the base stellar parameters.
- Framework Overhead: As this algorithm is currently more proof of concept than practical, it uses convenience functions from various libraries, which naturally introduces some level of overhead and leaves performance on the table. Future work would involve writing custom functions expressly designed for blase, most likely a complete rewrite of the library from the ground up. This has the potential to greatly increase the speed of this algorithm, depending on how much overhead is avoided with a bespoke implementation.
- Pseudo-Interpretability: Our algorithm boasts interpretability by considering spectral lines as the objects of interest as opposed to the rather uninterpretable flux values of other approaches. However, this is only a step in the direction of interpretability. True interpretability would decompose a spectrum not into a set of spectral lines, but into a set of species component spectra, which requires a much more advanced understanding of different species and their behavior, as well as direct access to a radiative transfer code as opposed to an off-the-shelf model grid. This approach would also extend the inference from just stellar parameters defined by a grid to any set of parameters accounted for in the radiative transfer model, down to specific species abundances. So while we were able to identify the spectral lines used in our figures, it is not necessarily valuable to try to identify

529

530

531

532

533

535

536

537

538

539

540

541

542

543

544

545

547

548

549

551

552

555

557

all 128,723 lines that we identify as unique with our algorithm. blase is agnostic to the identity of the line that it is optimizing. We study these lines as blase sees them (i.e. their four shape parameters), because for the purposes of this study, that is the only information that is useful. Having more interpretability would let scientists actually study certain species and their spectral lines.

- The Continuum Black Box: Continuum normalization is a process that is not yet completely understood, and is currently done as a preprocessing step with a fairly simple algorithm. Future work would dive deeper into the science of continuums and develop more advanced methods that can discern continuums with greater accuracy and less modeling restrictions. This would increase accuracy for end users.
- One Voigt Fits All: The current assumption of blase is that every spectral line is a Voigt profile. This assumption is largely true, but there are situations where that is simply not enough. Future studies need to account for more advanced spectral line profiles and procedures to deal with phenomena such as ro-vibrational bands. This would increase accuracy for end users.

The computer used for this study, Triton, has the following specifications:

CPU AMD EPYC 7513 RAM 256 GB GPU Nvidia A100 40GB (\times 2)

Table 2. This machine was used for all computations, but not for generating visualizations. The EPYC 7513 is a 32c/64t CPU with a boost clock of 3.65 GHz. The A100 has 6912 CUDA cores.

6. CONCLUSION

In this study, we have presented a proof-of-concept algorithm that interpolates a subset of the PHOENIX

560 spectral model grid and then uses GP minimization for ⁵⁶¹ an inference algorithm. We create state dictionaries for 562 all spectra in the PHOENIX subset, lossily distilling 563 the spectra with a data compression factor of around 564 20. These state dictionaries have been uploaded to Zenodo at https://zenodo.org/records/11246174 (Shankar 566 2024). We create the PHOENIX generator and imple-567 ment a performant spectral reconstruction algorithm, 568 enabling anyone to create reconstructions of PHOENIX 569 spectra with continuously valued stellar parameters. We 570 introduce and test our inference algorithm, with aver-₅₇₁ age absolute deviations from true values of 185 K in $T_{\rm eff}$, 0.19 in $\log(g)$, and 0.12 dex in [Fe/H]. In its cur-573 rent state, our algorithm operates on spectra within 574 the PHOENIX subset parameter ranges in Table 1, re-575 quiring that the spectra not contain noticeable Doppler 576 shifting, rotational broadening, or other confounding 577 factors. The methods discussed here represent a step 578 down a road not traveled in spectral inference, and have 579 the potential to become more advanced in the future by 580 fully utilizing the strengths of physics-informed machine 581 learning.

This material is based on work supported by the National Aeronautics and Space Administration under grant No. 80NSSC21K0650 for the NNH20ZDA001N-585 ADAP:D.2 program. C.V.M. acknowledges support from the Alfred P. Sloan Foundation under grant number FG-2021-16592 and support from the National Science Foundation under grant number 1910969.

Software: altair (VanderPlas et al. 2018; Satyanarayan et al. 2017), astropy (Astropy Collaboration
et al. 2013, 2018, 2022), blasé/blase (Gully-Santiago
& Morley 2022), CUDA (NVIDIA et al. 2020), gollum
(Shankar et al. 2024), matplotlib (Hunter 2007), numpy
(Harris et al. 2020), pandas (pandas development team
but 2020; Wes McKinney 2010), Python (Van Rossum &
Drake 2009), PyTorch/torch (Paszke et al. 2019), scikitoptimize/skopt (Head et al. 2018), scipy (Virtanen
et al. 2020), tqdm (da Costa-Luis 2019), vegafusion
(Kruchten et al. 2022),

REFERENCES

Astropy Collaboration, Robitaille, T. P., Tollerud, E. J.,
et al. 2013, A&A, 558, A33,
doi: 10.1051/0004-6361/201322068
Astropy Collaboration, Price-Whelan, A. M., Sipőcz, B. M.,
et al. 2018, AJ, 156, 123, doi: 10.3847/1538-3881/aabc4f

Astropy Collaboration, Price-Whelan, A. M., Lim, P. L.,
et al. 2022, ApJ, 935, 167, doi: 10.3847/1538-4357/ac7c74
Bedell, M., Hogg, D. W., Foreman-Mackey, D., Montet,
B. T., & Luger, R. 2019, The Astronomical Journal, 158,
164, doi: 10.3847/1538-3881/ab40a7

610 Bradbury, J., Frostig, R., Hawkins, P., et al. 2018, JAX: composable transformations of Python+NumPy 611 programs, 0.3.13. http://github.com/google/jax 612 613 Czekala, I., Andrews, S. M., Mandel, K. S., Hogg, D. W., & Green, G. M. 2015, ApJ, 812, 128, 614 doi: 10.1088/0004-637X/812/2/128 615 616 da Costa-Luis, C. O. 2019, Journal of Open Source Software, 4, 1277, doi: 10.21105/joss.01277 617 618 García Pérez, A. E., Allende Prieto, C., Holtzman, J. A., et al. 2016, AJ, 151, 144, 619 doi: 10.3847/0004-6256/151/6/144 620 Gully-Santiago, M., & Morley, C. V. 2022, ApJ, 941, 200, 621 doi: 10.3847/1538-4357/aca0a2 622 623 Harris, C. R., Millman, K. J., van der Walt, S. J., et al. 2020, Nature, 585, 357, doi: 10.1038/s41586-020-2649-2 624 625 Head, T., MechCoder, Louppe, G., et al. 2018, scikit-optimize/scikit-optimize: v0.5.2, v0.5.2, Zenodo, 626 doi: 10.5281/zenodo.1207017 627 628 Hunter, J. D. 2007, Computing in Science & Engineering, 9, 90, doi: 10.1109/MCSE.2007.55 629 630 Husser, T. O., Wende-von Berg, S., Dreizler, S., et al. 2013, A&A, 553, A6, doi: 10.1051/0004-6361/201219058 631 632 Ida, T., Ando, M., & Toraya, H. 2000, Journal of Applied Crystallography, 33, 1311, 633 doi: https://doi.org/10.1107/S0021889800010219 634 635 Karalidi, T., Marley, M., Fortney, J. J., et al. 2021, ApJ, 923, 269, doi: 10.3847/1538-4357/ac3140 636 Kawahara, H., Kawashima, Y., Masuda, K., et al. 2022, 637 ExoJAX: Spectrum modeling of exoplanets and brown 638 dwarfs, Astrophysics Source Code Library, record 639 ascl:2206.003 640 641 Kingma, D. P., & Ba, J. 2017, Adam: A Method for Stochastic Optimization. 642 https://arxiv.org/abs/1412.6980 643 Kramida, A., Yu. Ralchenko, Reader, J., & and NIST ASD 644 l

Team. 2023, NIST Atomic Spectra Database (ver. 5.11),

[Online]. Available: https://physics.nist.gov/asd

[2024, June 12]. National Institute of Standards and

Visualization and Visual Analytics (VIS), 11–15,

652 Kurucz, R. L. 2005, Memorie della Societa Astronomica

654 Lacy, B., & Burrows, A. 2023, The Astrophysical Journal,

656 López-Valdivia, R., Mace, G. N., Han, E., et al. 2023, ApJ,

Kruchten, N., Mease, J., & Moritz, D. 2022, in 2022 IEEE

Technology, Gaithersburg, MD.

doi: 10.1109/VIS54862.2022.00011

950, 8, doi: 10.3847/1538-4357/acc8cb

943, 49, doi: 10.3847/1538-4357/acab04

Italiana Supplementi, 8, 14

645

646

647

648

650

651

653

655

658 Mahadevan, S., Ramsey, L., Bender, C., et al. 2012, in Society of Photo-Optical Instrumentation Engineers 659 (SPIE) Conference Series, Vol. 8446, Ground-based and 660 Airborne Instrumentation for Astronomy IV, ed. I. S. McLean, S. K. Ramsay, & H. Takami, 84461S, 662 doi: 10.1117/12.926102 664 Majewski, S. R., Schiavon, R. P., Frinchaboy, P. M., et al. 2017, AJ, 154, 94, doi: 10.3847/1538-3881/aa784d 666 Marley, M. S., Saumon, D., Visscher, C., et al. 2021, ApJ, 920, 85, doi: 10.3847/1538-4357/ac141d 668 Morley, C. V., Mukherjee, S., Marley, M. S., et al. 2024, arXiv e-prints, arXiv:2402.00758, 669 doi: 10.48550/arXiv.2402.00758 670 671 Mukherjee, S., Fortney, J. J., Morley, C. V., et al. 2024, arXiv e-prints, arXiv:2402.00756, 672 doi: 10.48550/arXiv.2402.00756 674 NVIDIA, Vingelmann, P., & Fitzek, F. H. 2020, CUDA, release: 10.2.89. 675 https://developer.nvidia.com/cuda-toolkit 676 677 pandas development team, T. 2020, pandas-dev/pandas: Pandas, latest, Zenodo, doi: 10.5281/zenodo.3509134 678 Paszke, A., Gross, S., Massa, F., et al. 2019, PyTorch: An 679 Imperative Style, High-Performance Deep Learning 680 Library. https://arxiv.org/abs/1912.01703 681 682 Rayner, J. T., Cushing, M. C., & Vacca, W. D. 2009, ApJS, 185, 289, doi: 10.1088/0067-0049/185/2/289 683 684 Satyanarayan, A., Moritz, D., Wongsuphasawat, K., & Heer, J. 2017, IEEE transactions on visualization and 685 computer graphics, 23, 341 686 687 Shankar, S. 2024, blase II: PHOENIX Subset Clone Archive, 0.0.1, Zenodo, doi: 10.5281/zenodo.11246174 Shankar, S., Gully-Santiago, M., Morley, C., et al. 2024, The Journal of Open Source Software, 9, 6601, doi: 10.21105/joss.06601 691 Van Rossum, G., & Drake, F. L. 2009, Python 3 Reference 692 Manual (Scotts Valley, CA: CreateSpace) 693 694 VanderPlas, J., Granger, B., Heer, J., et al. 2018, Journal of Open Source Software, 3, 1057, doi: 10.21105/joss.01057 696 Virtanen, P., Gommers, R., Oliphant, T. E., et al. 2020, Nature Methods, 17, 261, doi: 10.1038/s41592-019-0686-2 697 Wes McKinney. 2010, in Proceedings of the 9th Python in 698 Science Conference, ed. Stéfan van der Walt & Jarrod Millman, 56 – 61, doi: 10.25080/Majora-92bf1922-00a Wheeler, A. J., Abruzzo, M. W., Casey, A. R., & Ness, M. K. 2023, AJ, 165, 68, doi: 10.3847/1538-3881/acaaad