

Question 1

Examine the relationship between daily study hours and exam scores using the following data:

- Study Hours: \{1, 2, 3, 4, 5\}
- Exam Scores: \{50, 60, 70, 80, 90\}

Predict the exam score for a student who studies 3.5 hours using linear regression.

Sample data

```
study_hours <- c(1, 2, 3, 4, 5)
exam_scores <- c(50, 60, 70, 80, 90)
```

Perform linear regression

```
model <- lm(exam_scores ~ study_hours)
```

Summary of the model

```
summary(model)
```

Predict a value

```
study_time <- 3.5
predicted_score <- predict(model, newdata = data.frame(study_hours =
study_time))
cat("Predicted exam score for studying", study_time, "hours:", predicted_score,
"\n")
```

Plotting

```
plot(study_hours, exam_scores, main = "Linear Regression: Study Hours vs
Exam Scores", xlab = "Study Hours", ylab = "Exam Scores", pch = 19, col =
"blue")
abline(model, col = "red")
```

Question 2

Analyze the association between vehicle type (Sedan, SUV, Truck) and fuel efficiency (Low, Medium, High) using the following contingency table with a chi-square test for independence:

	Low	Medium	High
Sedan	15	25	10
SUV	10	30	20
Truck	20	10	5

Contingency table

```
data <- matrix(c(15, 25, 10, 10, 30, 20, 20, 10, 5), nrow = 3, byrow = TRUE)
colnames(data) <- c("Low", "Medium", "High")
rownames(data) <- c("Sedan", "SUV", "Truck")
```

Perform Chi-Square test

```
chi_square_test <- chisq.test(data)
```

Results

```
cat("Chi-Square Statistic:", chi_square_test$statistic, "\n")
cat("P-value:", chi_square_test$p.value, "\n")
```

Interpretation of the p-value

```
alpha <- 0.05
if (chi_square_test$p.value < alpha) {
  cat("Reject the null hypothesis: There is a significant association.\n")
} else {
  cat("Fail to reject the null hypothesis: No significant association.\n")
}
```

Question 3

Assess the differences in customer satisfaction ratings across three different service types:

- Service Type A: $\{4, 5, 4, 5\}$
- Service Type B: $\{3, 3, 4, 2\}$
- Service Type C: $\{5, 5, 4, 5\}$. Use one-way ANOVA to determine if there are significant differences in mean ratings at a significance level of 0.05.

Sample data from three different groups

```
service_a <- c(4, 5, 4, 5)
service_b <- c(3, 3, 4, 2)
service_c <- c(5, 5, 4, 5)
```

Combine groups into a data frame

```
data <- data.frame(
  ratings = c(service_a, service_b, service_c),
  service = factor(rep(c("Service_A", "Service_B", "Service_C"), each = 4))
)
```

Perform One-Way ANOVA

```
anova_result <- aov(ratings ~ service, data = data)
summary(anova_result)
```

Interpretation

```
anova_p_value <- summary(anova_result)[[1]][["Pr(>F)"]][1]
alpha <- 0.05
if (anova_p_value < alpha) {
  cat("Reject the null hypothesis: At least one group mean is significantly
different.\n")
} else {
  cat("Fail to reject the null hypothesis: No significant differences between
group means.\n")
}
```

Question 4

Compare the average waiting times for two different restaurants:

- Restaurant A: $\{15, 20, 18, 16, 14\}$
- Restaurant B: $\{30, 25, 28, 32, 29\}$. Use a two-sample t-test to determine if the means are significantly different at a significance level of 0.05.

Sample data from two independent groups

```
restaurant_a <- c(15, 20, 18, 16, 14)
```

```
restaurant_b <- c(30, 25, 28, 32, 29)
```

Perform Two-Sample T-Test

```
t_test_result <- t.test(restaurant_a, restaurant_b)
```

Results

```
cat("T-Statistic:", t_test_result$statistic, "\n")
```

```
cat("P-Value:", t_test_result$p.value, "\n")
```

Interpretation of the p-value

```
alpha <- 0.05
```

```
if (t_test_result$p.value < alpha) {
```

```
  cat("Reject the null hypothesis: The means are significantly different.\n")
```

```
} else {
```

```
  cat("Fail to reject the null hypothesis: No significant difference between the means.\n")
```

```
}
```