# RAMANUJAN COLLEGE

# UNIVERSITY OF DELHI



Core: Design and Analysis of Algorithms

Practical File

**SUBMITTED TO:** Mrs. Sheetal Singh

SUBMITTED BY: Sukaina Inam Naqvi

**ROLL NO - 20201426** 

**Examination Roll Number-20020570033** 

B.Sc (H) Computer Science | IV Semester

# For Basic Sorting Algorithms: Algo.hpp

```
#ifndef _algo_hpp_
#define _algo_hpp_
#pragma once
#include <iostream> #include <cstdlib>
using namespace std;
namespace algo
  template <class T>
  void printArray(T *array, const uint &len)
  { cout << "\n { "; for (uint i = 0; i < len - 1; i++)
    cout << array[i] << ", ";
    cout << array[len - 1] << " }\n";</pre>
  }
  template <class T>
  void swap(T *a, T *b)
  {
    T tmp = *a;
    *a = *b;
    *b = tmp;
  }
```

# **Insertion Sort**

```
template <class Tp, class _Comp = less<Tp>>
uint insertionSort(Tp *array, const uint &len,
                                  const _Comp &cmp = _Comp())
{
  uint count = 0; Tp key; if (len >
  1)
     for (int i = 1, j = 0; i < len; i++)
     {j = i - 1; key = array[i];}
        while (j \ge 0 \&\& cmp (key, array[j]))
        \{ array[j+1] = array[j]; \}
          j--;
          count++;
        array[j + 1] = key;
        count++;
  return count;
}
```

## **Merge Sort**

```
template <typename T, class _comp>
uint merge(T *arr, const uint &I, const uint &m,
                         const uint &r, const _comp &cmp)
{ uint n1 = m - l + 1, n2 = r - m, i, j, k; T L[n1], R[n2];
  for (i = 0; i < n1; i++)
     L[i] = arr[l + i]; for (j = 0; j < n2; j++)
     R[j] = arr[m + 1 + j];
  i = j = 0; k = I;
  while (i < n1 && j < n2)
  { if (cmp(L[i], R[j])) arr[k] = L[i++];
     else arr[k] = R[j++];
     k++;
  while (i < n1) arr[k++] = L[i++];
  while (j < n2) arr[k++] = R[j++];
  return k - I - 1;
}
template <typename T, class comp = less<T>>
uint mergeSort(T *arr, const uint &begin, const uint &end,
                                          const _comp &cmp = _comp())
{ if (begin < end)
  \{ uint mid = (begin + end) / 2; \}
  return mergeSort(arr, begin, mid, cmp) +
              mergeSort(arr, mid + 1, end, cmp) +
                 merge(arr, begin, mid, end, cmp);
  }
  return 1;
}
```

# **Heap Sort**

```
template < class T, class Comp>
void heapify(T array[], const int &i, const uint &len,const Comp &cmp, uint &count)
{ uint left, right, top = i; left = 2 * i + 1;
   right = 2 * i + 2;
  if (left < len && cmp(array[top], array[left]))</pre>
     count++, top = left;
  if (right < len && cmp(array[top], array[right]))</pre>
     count++, top = right;
  if (top != i)
  { swap(array + i, array + top);
     count++;
     heapify(array, top, len, cmp, count); }
}
template <class Tp, class _Comp = less<Tp>>
uint heapSort(Tp *array, const uint &len,const _Comp &cmp = _Comp())
{
  uint count = 0; // Counter
  // Build a Heap
  for (int i = len / 2 - 1; i >= 0; i--)
     heapify(array, i, len, cmp, count);
  // One by one extract an element from heap
  for (uint i = len - 1; i > 0; i--)
  {
     // Move current root to end swap(array, array + i);
     // call heapify on the reduced heap heapify(array, 0, i, cmp, count);
   }
   return count;
}
```

### **Quick Sort**

```
template < class T, class Comp>
int partition(T *array, const int &start, const int &end, const Comp &cmp)
{
  T x = array[end]; int i = start;
  for (int j = start; j < end; j++)
     if (cmp(array[j], x))
        swap(array + j, array + i); i++;
     } swap(&array[i], array + end); return i;
template <class T, class _Comp> int random_partition(T *array, const int &start, const
int &end, const _Comp &cmp)
{
  srand(time(NULL));
  swap(&array[start + rand() % (end - start + 1)], &array[end]); return partition(array,
  start, end, cmp);
}
template <class T, class _Comp = less<T>> uint random_quickSort(T *array, const int
&start, const int &end, const _Comp &cmp = _Comp())
{ if (start < end)
  { int piv = random partition(array, start, end, cmp); return (piv - start) +
     random quickSort(array, start, piv - 1, cmp) +
          random quickSort(array, piv + 1, end, cmp);
   }
   return 1;
}
```

# **Randomized Select**

```
template <typename tp, class _Comp = less<tp>>
tp randomizedSelect(tp *array, const int &start, const int &end, const int &i,
                               const _Comp &cmp = _Comp())
  {
 if (i \le 0)
       throw invalid argument("Index Error: Index starts with 1 not from 0 or
negative !!!");
       if (start == end)
       return array[start];
    int piv = random_partition(array, start, end, cmp); int k = piv - start + 1;
    if (i == k)
       return array[piv];
    else if (i < k)
                  return randomizedSelect(array, start, piv - 1, i, cmp);
    else
                  return randomizedSelect(array, piv + 1, end, i - k, cmp);
#endif
```

# **Practical Questions**

#### Question 1.

 i. Implement Insertion Sort. (The program should report the number of comparisons)

Code:-

#### **Output:-**

```
Practical 1
A. Insertion Sort

Unsorted Array:
{ 1, 0, 2, 3, 6, 4, 9, -2, 5 }

Comparisons in Insertion Sort : 19

Sorted array in ascending order:
{ -2, 0, 1, 2, 3, 4, 5, 6, 9 }
```

#### ii. Implement Merge Sort (The program should report the number of comparisons)

#### Ans.

```
Code
```

```
#include "algo.hpp" using namespace algo;
int main()
{
    int a[] = {5, 10, 2, 0, 3, 4, 8, 9, 6}; int n = sizeof(a) / sizeof(a[0]); cout <<
        "\n\t\t Practical 1\n\t\tB. Merge Sort\n"; cout << "\n Unsorted Array:
    \n"; printArray(a, n);

cout << "\n Comparisons in Merge Sort : " << mergeSort(a, 0, n - 1)
        << endl;

cout << "\n Sorted array in ascending order: \n"; printArray(a, n);
}</pre>
```

```
Practical 1
B. Merge Sort

Unsorted Array:
{ 5, 10, 2, 0, 3, 4, 8, 9, 6 }

Comparisons in Merge Sort : 30

Sorted array in ascending order:
{ 0, 2, 3, 4, 5, 6, 8, 9, 10 }
```

# Q.2. Implement Heap Sort (The program should report the number of comparisons)

#### Ans.

```
Code
```

```
Practical 2
Heap Sort

Unsorted Array:

{ 5, 13, 2, 25, 7, 17, 20, 8, 4 }

Comparisons in Heap Sort : 31

Sorted array in descending order:

{ 25, 20, 17, 13, 8, 7, 5, 4, 2 }
```

# Q.3. Implement Randomized Quick sort (The program should report the number of comparisons)

Ans.

```
Code
```

```
Practical 3
Randomized Quick Sort

Unsorted Array:
{ 8, 70, 16, 1, 10, 9, 12, 1, 10, 3, 2 }

Comparisons in Randomized Quick Sort : 19

Sorted array in ascending order:
{ 1, 1, 2, 3, 8, 9, 10, 10, 12, 16, 70 }
```

# Q.4. Implement Radix Sort.

#### Ans.

```
Code
#include "algo.hpp" using namespace algo;
int getMax(int *array, const uint &len)
  int max = array[0]; for (uint i = 1; i < len; i++)
     if (max < array[i])</pre>
       max = array[i];
  return max;
void countSort(int *array, const uint &len, const uint &exp)
  int i, *count = new int[10]{0}, *out = new int[len];
  for (i = 0; i < len; i++) count[(array[i] / exp) % 10]++;</pre>
  for (i = 1; i < 10; i++)
     count[i] += count[i - 1];
  for (i = len - 1; i >= 0; i--)
  { out[count[(array[i] / exp) % 10] - 1] = array[i]; count[(array[i] / exp) %
     10]--;
  }
  for (i = 0; i < len; i++)
     array[i] = out[i];
  delete out;
  delete count;
```

```
void radixSort(int *array, const uint &len)
  uint max = getMax(array, len); for (uint i = 1; (max / i) >
  0; i *= 10)
     countSort(array, len, i);
int main()
  int a[] = {10, 1, 20, 300, 5, 7, 4, 1024, 995, 87}; int n = sizeof(a) /
  sizeof(a[0]); cout << "\n\t\t Practical 4\n\t\t Radix Sort\n";</pre>
  cout << "\n Unsorted Array: \n"; printArray(a, n);</pre>
  radixSort(a, n);
  cout << "\n After applying Radix Sort on the Array :\n"; cout << "\n Sorted array in
  ascending order: \n"; printArray(a, n);
```

```
Practical 4
Radix Sort

Unsorted Array:
{ 10, 1, 20, 300, 5, 7, 4, 1024, 995, 87 }

After applying Radix Sort on the Array:

Sorted array in ascending order:
{ 1, 4, 5, 7, 10, 20, 87, 300, 995, 1024 }
```

#### Q.5. Implement Bucket Sort.

#### Ans.

```
#include <iostream>
#include <vector> #include <algorithm>
using namespace std;
void printArray(float *array, const uint &len)
{ cout << "\n { ";
  for (uint i = 0; i < len - 1; i++) cout << array[i] << ", ";
  cout << array[len - 1] << " }\n";
int main()
{ vector<float> hash[10];
  float a[] = \{0.01, 0.23, 0.13, 0.11, 0.25, 0.35, 0.42, 0.02, 0.9, 0.45, 0.05\}; int n = sizeof(a) /
  sizeof(a[0]), j = 0; cout << "\n\t\t\t Practical 5\n\t\t\t Bucket Sort\n";</pre>
  cout << "\n Unsorted Array: \n"; printArray(a, n);</pre>
  // Bucket Sort for (float &i : a)
     hash[int(i * 10)].push_back(i);
  for (vector<float> &v : hash) sort(v.begin(), v.end());
  for (vector<float> &v : hash) for (float &f : v)
     a[j++] = f;
  cout << "\n After applying bucket-sort on the array\n"</pre>
        << "\n Sorted array in ascending order: \n"; printArray(a, n);
```

```
Practical 5
Bucket Sort

Unsorted Array:

{ 0.01, 0.23, 0.13, 0.11, 0.25, 0.35, 0.42, 0.02, 0.9, 0.45, 0.05 }

After applying bucket-sort on the array

Sorted array in ascending order:

{ 0.01, 0.02, 0.05, 0.11, 0.13, 0.23, 0.25, 0.35, 0.42, 0.45, 0.9 }
```

#### Q.6. Implement Randomized Select.

#### Ans.

```
Practical 6
Randomized Select Algorithm

Unsorted Array:
{ 5, 3, 2, 7, 1, 0, 8, 4 }

Finding minimum element at position 1 : 0

Now Array is :
{ 0, 1, 2, 7, 5, 3, 8, 4 }

Finding minimum element at position 7 : 7

Now Array is :
{ 0, 1, 2, 3, 4, 5, 7, 8 }
```

### Q.7. Implement Breadth-First Search in a graph.

#### Ans.

```
return;
  int begin;
  q.push(start); visited[start] = true; while
  (!q.empty())
  { begin = q.front(); q.pop(); cout << '\t' <<
     begin;
     for (int i = 0; i < v; i++) if (Graph[begin][i] && !visited[i])</pre>
        { visited[i] = true; q.push(i);
        }
  }
int main()
{ cout << "\n\t\t Practical 7\n\tBreadth First Traversal for Graphs\n";
  cout << "\n\n Given Graph is :\n\n\t Nodes : Edges\n"; for (int i = 0; i < v; i++)
  for (int j = 0; j < v; j++) if (Graph[i][j] && !(visited[j]))</pre>
        { visited[i] = true;
           cout << "\t " << i << " -- " << j << " :\t" << Graph[i][j] << endl; }
  fill(visited, visited + v, false);
  cout << "\n Breadth First Traversal for Graph at node 1 :\n"; BFS(1);</pre>
```

```
Practical 7
Breadth First Traversal for Graphs

Given Graph is:

Nodes: Edges
0 -- 0 : 1
0 -- 4 : 1
1 -- 1 : 1
1 -- 2 : 1
1 -- 4 : 1
2 -- 3 : 1
4 -- 4 : 1

Breadth First Traversal for Graph at node 1:
1 2 4 3 0
```

# Q.8. Implement Depth-First Search in a graph.

#### Ans.

```
Practical 8
       Depth First Traversal for Graphs
Given Graph is :
                      Edges
         Nodes
        0 -- 3
                        1
                        1
        1 -- 4
                        1
        2 -- 3
                  ٠
                        1
Depth First Traversal for Graph at node 0 :
       0
                3
```

# Q.9. Write a program to determine the minimum spanning tree of a graph using both Prims and Kruskal's algorithm.

#### Ans.

```
#include <iostream> #include <climits>
using namespace std; #define v 5 int
parent[v]; bool visited[v] = {0};
              Kruskal's Algorithm
/****
                                        ******/
int find(int i)
{ while (parent[i] != i) i = parent[i];
  return i;
void union1(int i, int j)
{            int a = find(i), b = find(j);
  parent[a] = b;
} int kruskal_mst(int cost[][v])
  int mincost = 0;
  int edge_count = 0; for (int i = 0; i < v;</pre>
  i++)
     parent[i] = i;
  while (edge_count < v - 1)
  { int min = INT_MAX, a = -1, b = -1; for (int i = 0; i < v;
     i++)
        for (int j = 0; j < v; j++) if (find(i) != find(j)
           &&
              cost[i][j] < min)
           \{ \min = \text{cost}[i][j]; a = i; b = j;
```

```
} union1(a, b); mincost +=
     min;
                            cout << "\n\t Edge " << edge count++ << " ("
           << a << ", " << b << ") : " << min;
  }
  return mincost;
             Prim's Algorithm ******/ bool validEdge(int a, int b)
{ if (a == b | | visited[a] == visited[b]) return false;
  return true;
} int prim_mst(int cost[][v])
  int mincost = 0, edge_count = 0; fill(visited, visited + v,
  false); visited[0] = true;
  while (edge_count < v - 1)
  { int min = INT_MAX, a = -1, b = -1; for (int i = 0; i < v;
     i++)
       for (int j = 0; j < v; j++)
          if (cost[i][ j] < min &&
             validEdge(i, j))
          \{ min = cost[i][j]; a = i; b = j; 
          } visited[a] = visited[b] = true; mincost +=
     min;
                cout << "\n\t Edge " << edge count++ << " ("
                     << a << ", " << b << ") : " << min;
  return mincost;
```

```
int main()
{ int Graph[][v] = {
    {INT_MAX, 2, INT_MAX, 6, INT_MAX},
    {2, INT_MAX, 3, 8, 5},
    {INT_MAX, 3, INT_MAX, INT_MAX, 7},
    {6, 8, INT_MAX, INT_MAX, 9},
    {INT_MAX, 5, 7, 9, INT_MAX},
  };
  cout << "\n\t\t Practical 9\n\tMinimum Spanning Tree</pre>
             Algorithms\n\t\t Kruskal & Prim\n";
  cout << "\n\n Given Graph is :\n\n\t Edges : Weights\n"; for (int i = 0; i < v; i++)
  for (int j = 0; j < v; j++)
       if (Graph[i][j] != INT MAX && !(visited[j]))
       { visited[i] = true;
         cout << "\t " << i << " - " << j << " :\t" << Graph[i][j] << endl; } cout << "\n 1. Minimum
  Spanning Tree using Kruskal's Algorithm: \n"; int k = kruskal mst(Graph);
  cout << "\n\n\t Minimum Cost\t: " << k << endl; cout << "\n 2. Minimum Spanning Tree using
  Prim's Algorithm : \n"; k = prim_mst(Graph); cout << "\n\n\t Minimum Cost\t: " << k << endl;
```

# Practical 9 Minimum Spanning Tree Algorithms Kruskal & Prim

Given Graph is :

Edges : Weights 0 - 1 2 0 - 3 6 1 - 2 3 1 - 3 : 8 1 - 4 5 2 - 4 : 7 3 - 4 9

J - 4 . 9

1. Minimum Spanning Tree using Kruskal's Algorithm :

Edge 0 (0 , 1) : 2 Edge 1 (1 , 2) : 3 Edge 2 (1 , 4) : 5 Edge 3 (0 , 3) : 6

Minimum Cost : 16

2. Minimum Spanning Tree using Prim's Algorithm :

Edge 0 (0 , 1) : 2 Edge 1 (1 , 2) : 3 Edge 2 (1 , 4) : 5 Edge 3 (0 , 3) : 6

Minimum Cost : 16

7 101 111 1 10 1 10 1 11 10

#### Q.10. Write a program to solve the weighted interval scheduling problem.

#### Ans.

```
Code
```

```
// Weighted Interval Scheduling
#include <iostream> #include <algorithm>
using namespace std;
struct job
{ uint start, finish, profit;
  // Constructor
  job(const\ uint\ \&s = 0,\ const\ uint\ \&f = 0,\ const\ uint\ \&p = 0)
  { start = s; finish = f; profit = p;
};
bool cmp(const job &a, const job &b)
{ return a.finish < b.finish;
int check_Overloop(const job *j, const uint &n)
{ for (int i = n - 2; i > -1; i--)
     if (j[n - 1].start >= j[i].finish)
        return i;
  return -1;
uint wi_sch(const job *j, const uint &n)
  if (n == 0)
     return j[0].profit;
  else
```

```
{ int i = check_Overloop(j, n); int incl = j[n -
     1].profit;
     if (i != -1)
        incl += wi sch(j, i + 1);
     int excl = wi sch(j, n - 1); return (incl > excl ? incl :
     excl);
uint max_profit(job *j, const uint &n)
{ sort(j, j + n, cmp);
  cout << "\n\nSorted jobs according to respective finish time are :\n\n"</pre>
         << "S.N.\t Start-time\t Finish-time\t\tProfit\n"; for (int i = 0; i < n; i++)
     cout << "\n " << i + 1 << "\t\t" << i[i].start << "\t\t"
            << i[i].finish << "\t\t" << i[i].profit; return wi sch(i, n);
int main()
\{ \text{ job i} [] = \{\{3, 10, 20\}, \{1, 24, 50\}, \{6, 19, 100\}, \{2, 100, 20\}\}; \text{ int } n = \text{sizeof(j) / sizeof(j[0]); cout} \}
  << "\n\t\t Practical 10 \n\t Weighted Interval Scheduling \n";</pre>
  cout << "\nGiven jobs are :\n\nS.N.\t Start-time\t</pre>
               Finish-time\t\tProfit\n";
  for (int i = 0; i < n; i++)
     cout << "\n " << i + 1 << "\t\t" << j[i].start << "\t\t" << i[i].finish << "\t\t" <<
            j[i].profit;
  int mx = max_profit(j, n); cout << "\n\nThe Maximum Optimal Profit is : " << mx << endl;</pre>
```

```
Practical 10
         Weighted Interval Schedueling
Given jobs are :
S.N.
           Start-time Finish-time
                                                 Profit
 1
                                 10
                                                 20
 2
                1
                                 24
                                                 50
 3
                6
                                 19
                                                 100
 4
                2
                                 100
                                                 20
Sorted jobs according to respective finish time are :
S.N.
           Start-time
                           Finish-time
                                                 Profit
                                                 20
 1
                3
                                 10
 2
                6
                                 19
                                                 100
 3
                1
                                 24
                                                 50
                2
                                 100
                                                 20
The Maximum Optimal Profit is: 100
```

#### Q.11. Write a program to solve the 0-1 knapsack problem.

#### Ans.

```
#include <iostream> #include <algorithm>
using namespace std; #define max(a, b) a >
b ? a : b;

struct Item
{ int val, wt;

// Constructor
```

```
Item(int value, int weight)
  { this->val = value;
     this->wt = weight;
  }
};
int knapsack_dynamic(const uint &n, const uint &W, const Item arr[])
  int dp[W + 1] = \{0\};
  for (int i = 1; i \le n; i++) for (int w = W; w >= 0;
     w--) if (arr[i-1].wt <= w)
        {
          dp[w] = max(dp[w], dp[w - arr[i - 1].wt] + arr[i - 1].val); }
  return dp[W];
double knapsack greedy(const uint &n, uint W, Item arr[])
  sort(arr, arr + n, [](const Item &a, const Item &b){ return (a.val * 1.0 / a.wt) >
           (b.val * 1.0 / b.wt);
       });
  double finalVal = 0;
  for (int i = 0; i < n; i++)
  { if (arr[i].wt <= W)
     {
        W -= arr[i].wt; finalVal += arr[i].val;
     } else
     { finalVal += arr[i].val * W * 1.0 / arr[i].wt;
        break;
     }
  }
```

```
Practical 11
               KnapSack Algorithm
Given Items are :
S.N.
       Values
              Weight
 1
       60
               10
 2
               20
       100
       120
               30
Dynamic Approach
Obtained maximum value: 220
Greedy Approach
Obtained maximum value: 240
```