

Prelab5

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```
##This is the Prelab5 of STATS 413
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```

(a.) Using the which function. Generate a vector Z of 100 iid standard normal variables. Use which to find the indices for which $Z_i > 1.8$. Print the values of Z_i for these indices. Use which to find the index of $\max_i Z_i$ and $\max_i |Z_i|$.

```
set.seed(1)
Z=rnorm(100,0,1)
Z_I<-which(Z>1.8)#Zi > 1.8
Z_I;Z[Z_I]# Print the values of Zi for these indices
```

```
## [1] 4 11 15 31 39 55 56 61 68 70 83 87 92 93 95
```

```
## [1] 1.595281 1.511781 1.124931 1.358680 1.100025 1.433024 1.980400 2.401618
```

```
## [9] 1.465555 2.172612 1.178087 1.063100 1.207868 1.160403 1.586833
```

```
which(Z==max(Z)) #maxi Zi
```

```
## [1] 61
```

```
which(abs(Z)==max(abs(Z)))#maxi |Zi|
```

```
## [1] 61
```

(b.) Converting data frames to matrices. Import the Carseats dataset from the ISLR package. Convert the variable Sales to a vector of length 400. Remove the three categorical variables, then convert the remaining continuous variables in the dataset to a matrix of size 400×7 . Directly compute the estimate β for the regression of Sales on these seven continuous variables. (There is no need to add a column for the intercept.) (Hint: the functions data.matrix and crossprod may be helpful here.)

```
library(ISLR)
data(Carseats)
summary(Carseats)
```

```
##      Sales      CompPrice      Income      Advertising
## Min.   : 0.000   Min.   : 77   Min.   : 21.00   Min.   : 0.000
## 1st Qu.: 5.390   1st Qu.:115   1st Qu.: 42.75   1st Qu.: 0.000
## Median : 7.490   Median :125   Median : 69.00   Median : 5.000
## Mean   : 7.496   Mean   :125   Mean   : 68.66   Mean   : 6.635
## 3rd Qu.: 9.320   3rd Qu.:135   3rd Qu.: 91.00   3rd Qu.:12.000
## Max.   :16.270   Max.   :175   Max.   :120.00   Max.   :29.000
##      Population      Price      ShelfLoc      Age      Education
## Min.   : 10.0   Min.   : 24.0   Bad   : 96   Min.   :25.00   Min.   :10.0
## 1st Qu.:139.0   1st Qu.:100.0   Good  : 85   1st Qu.:39.75   1st Qu.:12.0
## Median :272.0   Median :117.0   Medium:219   Median :54.50   Median :14.0
```

```
## Mean :264.8 Mean :115.8 Mean :53.32 Mean :13.9
## 3rd Qu.:398.5 3rd Qu.:131.0 3rd Qu.:66.00 3rd Qu.:16.0
## Max. :509.0 Max. :191.0 Max. :80.00 Max. :18.0
## Urban US
## No :118 No :142
## Yes:282 Yes:258
##
##
##
##
```

```
y=Carseats$Sales
x=as.matrix(Carseats[,c(-1,-7,-10,-11)])
model_1<-lm(y~x)
solve(t(x) %*% x) %*% t(x) %*% y #directly calculate the estimate hat(beta)
```

```
## [1,]
## CompPrice 0.127226700
## Income 0.020139922
## Advertising 0.133488157
## Population 0.001192478
## Price -0.091783793
## Age -0.029567078
## Education 0.083395449
```

```
summary(model_1) #Same as directly calculate the estimate hat(beta)
```

```
##
## Call:
## lm(formula = y ~ x)
##
## Residuals:
## Min 1Q Median 3Q Max
## -5.0598 -1.3515 -0.1739 1.1331 4.8304
##
## Coefficients:
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 7.7076934 1.1176260 6.896 2.15e-11 ***
## xCompPrice 0.0939149 0.0078395 11.980 < 2e-16 ***
## xIncome 0.0128717 0.0034757 3.703 0.000243 ***
## xAdvertising 0.1308637 0.0151219 8.654 < 2e-16 ***
## xPopulation -0.0001239 0.0006877 -0.180 0.857092
## xPrice -0.0925226 0.0050521 -18.314 < 2e-16 ***
## xAge -0.0449743 0.0060083 -7.485 4.75e-13 ***
## xEducation -0.0399844 0.0371257 -1.077 0.282142
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.929 on 392 degrees of freedom
## Multiple R-squared: 0.5417, Adjusted R-squared: 0.5335
## F-statistic: 66.18 on 7 and 392 DF, p-value: < 2.2e-16
```