

## Homework 3

due date: 11:59pm (Eastern time), Friday Oct 23, 2020

Questions 12 and 14 in Chapter 3.7 Exercises in An Introduction to Statistical Learning

(<http://faculty.marshall.usc.edu/gareth-james/ISL/ISLR%20Seventh%20Printing.pdf>).

Questions 9.1 and 9.4 in Applied Linear Regression book (4<sup>th</sup> Edition); see below for descriptions of these questions.

**9.1** (Data file: `Rpdata`) The data in this file has a response  $y$  and six regressors  $x_1, \dots, x_6$ . The data are artificial, to make a few points.

Data link: <http://users.stat.umn.edu/~sandy/alr4ed/data/>

**9.1.1** First draw a scatterplot matrix of all data and comment. Is there anything strange?

**9.1.2** Fit the OLS regression  $y \sim x_1 + x_2 + x_3 + x_4 + x_5 + x_6$ . Is there anything strange?

**9.1.3** Draw a plot of residuals versus fitted values. Is there anything strange? See Stefanski (2007) if you want to find out how this data set came about.

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**9.4 Simple regression** Consider the simple regression model,  $E(Y|X = x) = \beta_0 + \beta_1 x$ ,  $\text{Var}(Y|X = x) = \sigma^2$ .

**9.4.1** Find a formula for the  $h_{ij}$  and for the leverages  $h_{ii}$ .

**9.4.2** In a 2D plot of the response versus the predictor in a simple regression problem, explain how high-leverage points can be identified.

**9.4.3** Make up a predictor  $X$  so that the value of the leverage in simple regression for one of the cases is equal to 1.

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