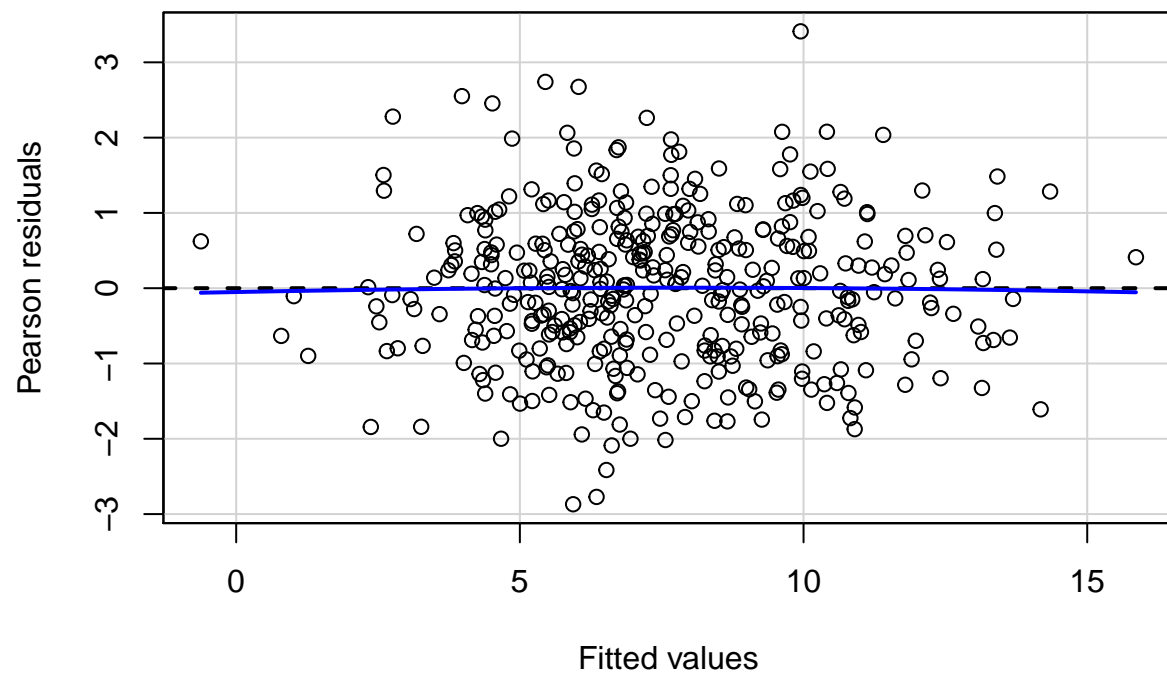


2 Q2.

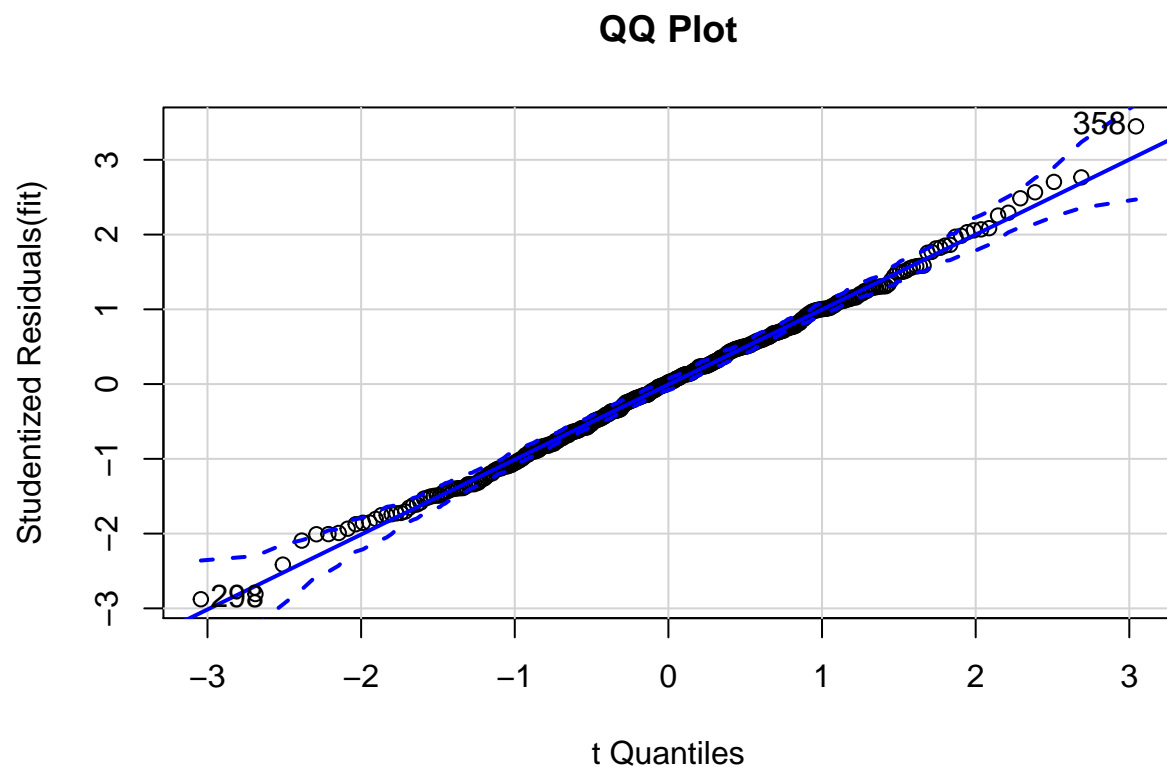
(a)

```
library(ISLR)
data("Carseats")
fit <- lm(Sales ~ CompPrice+Income+Advertising+Population+Price+ShelveLoc+Age+Education+Urban+US, data = Carseats)
summary(fit)

##
## Call:
## lm(formula = Sales ~ CompPrice + Income + Advertising + Population +
##     Price + ShelveLoc + Age + Education + Urban + US, data = Carseats)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.8692 -0.6908  0.0211  0.6636  3.4115
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   5.6606231   0.6034487   9.380 < 2e-16 ***
## CompPrice     0.0928153   0.0041477  22.378 < 2e-16 ***
## Income        0.0158028   0.0018451   8.565 2.58e-16 ***
## Advertising    0.1230951   0.0111237  11.066 < 2e-16 ***
## Population     0.0002079   0.0003705   0.561  0.575
## Price        -0.0953579   0.0026711 -35.700 < 2e-16 ***
## ShelveLocGood  4.8501827   0.1531100  31.678 < 2e-16 ***
## ShelveLocMedium 1.9567148   0.1261056  15.516 < 2e-16 ***
## Age          -0.0460452   0.0031817 -14.472 < 2e-16 ***
## Education     -0.0211018   0.0197205  -1.070  0.285
## UrbanYes       0.1228864   0.1129761   1.088  0.277
## USYes        -0.1840928   0.1498423  -1.229  0.220
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.019 on 388 degrees of freedom
## Multiple R-squared:  0.8734, Adjusted R-squared:  0.8698
## F-statistic: 243.4 on 11 and 388 DF, p-value: < 2.2e-16
##The multiple R-squared value is 0.8698, which shows that this regression
##can interpret 87% of the changes of the dependent variable.
residualPlot(fit)      #Diagnostic residual plots
```



```
qqPlot(fit, main="QQ Plot") #qq plot for studentized residuals
```



```
## [1] 298 358
```

```
##There is no clear interaction between the predicted value and residuals
```

(b)

```
##We can see that CompPrice, Income, Advertising, Price,  
##and ShelfLoc have significant p-values.
```

```
##For the variable "Urban", we have the P-value = 0.277 > 0.05, hence, we  
##rejected the hypothesis that the variable Urban is significant.
```

(c)

```
fit1 <- lm(Sales ~ CompPrice+Income+Advertising+Price+ShelveLoc, data = Carseats)  
summary(fit1)
```

```
##
```

```
## Call:
```

```
## lm(formula = Sales ~ CompPrice + Income + Advertising + Price +  
##     ShelfLoc, data = Carseats)
```

```
##
```

```
## Residuals:
```

```
##      Min       1Q   Median       3Q      Max  
## -3.7962 -0.9251  0.0043  0.8457  4.4179
```

```
##
```

```
## Coefficients:
```

```
##              Estimate Std. Error t value Pr(>|t|)
```

```
## (Intercept)      2.431262    0.569032    4.273 2.43e-05 ***
## CompPrice        0.095676    0.005100   18.760 < 2e-16 ***
## Income           0.016042    0.002276    7.049 8.16e-12 ***
## Advertising      0.116205    0.009566   12.148 < 2e-16 ***
## Price           -0.093241    0.003302  -28.236 < 2e-16 ***
## ShelveLocGood    4.797696    0.188847   25.405 < 2e-16 ***
## ShelveLocMedium  1.849895    0.155037   11.932 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.263 on 393 degrees of freedom
## Multiple R-squared:  0.8031, Adjusted R-squared:  0.8001
## F-statistic: 267.2 on 6 and 393 DF, p-value: < 2.2e-16
```

##The multiple R-squared value is 0.8001, which shows that this regression can interpret 80% of the changes of the dependent variable

##The R-squared value of the reduced model slightly decreased from the previous value with the full model.

(d)

```
anova(fit,fit1)
```

```
## Analysis of Variance Table
##
## Model 1: Sales ~ CompPrice + Income + Advertising + Population + Price +
##      ShelveLoc + Age + Education + Urban + US
## Model 2: Sales ~ CompPrice + Income + Advertising + Price + ShelveLoc
##   Res.Df    RSS Df Sum of Sq    F    Pr(>F)
## 1      388 402.83
## 2      393 626.51 -5    -223.68 43.088 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

#The P-value is significant, i.e. we can not reject the hypothesis that the two models have different variance.

#Hence, the different between the R-squared value is not significant, and the second model is better.

(e)

$y = 2.431 + 0.096 \times \text{CompPrice} + 0.016 \times \text{Income} + 0.116 \times \text{Advertising} - 0.093 \times \text{Price} + 4.798$ (If shelveLoc = Good) + 1.850 (If ShelveLoc = Medium)

(f)

```
fit2 <- lm(Sales ~ CompPrice+Income+Advertising+Price+ShelveLoc + Price:ShelveLoc, data = Carseats)
summary(fit2)
```

```
##
## Call:
## lm(formula = Sales ~ CompPrice + Income + Advertising + Price +
##      ShelveLoc + Price:ShelveLoc, data = Carseats)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
```

```
## -3.7547 -0.9336 0.0078 0.8386 4.3561
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    1.964179   0.795606   2.469  0.01398 *
## CompPrice      0.095881   0.005144  18.638 < 2e-16 ***
## Income         0.015969   0.002290   6.974 1.32e-11 ***
## Advertising    0.116309   0.009596  12.121 < 2e-16 ***
## Price        -0.089335   0.005739 -15.567 < 2e-16 ***
## ShelveLocGood  5.353757   0.920389   5.817 1.25e-08 ***
## ShelveLocMedium 2.473173   0.774915   3.192 0.00153 **
## Price:ShelveLocGood -0.004843 0.007752  -0.625 0.53249
## Price:ShelveLocMedium -0.005441 0.006626  -0.821 0.41205
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.265 on 391 degrees of freedom
## Multiple R-squared:  0.8035, Adjusted R-squared:  0.7995
## F-statistic: 199.8 on 8 and 391 DF, p-value: < 2.2e-16
```

*##We can see that the interaction between Price and ShelveLoc have
##non-significant p-values, hence the interaction term is not necessary.*

(d)

```
anova(fit1,fit2)
```

```
## Analysis of Variance Table
##
## Model 1: Sales ~ CompPrice + Income + Advertising + Price + ShelveLoc
## Model 2: Sales ~ CompPrice + Income + Advertising + Price + ShelveLoc +
##      Price:ShelveLoc
##   Res.Df    RSS Df Sum of Sq    F Pr(>F)
## 1      393 626.51
## 2      391 625.38  2    1.1343 0.3546 0.7017
```

*##The P-value is not significant, i.e. we can reject the hypothesis that the two
models have different variance.*

*##Hence, the different between the R-squared value is significant, and the
#interaction term is not necessary.*