

University of Michigan Data Mining Stats415

ASSIGNMENT 5

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a.

According to logistic regression function, we have

$$\log(\frac{p}{1-p}) = \beta_0 + \beta_1 X_1 + \beta_2 X_2 = -4 + 0.05 X_1 + X_2 \tag{1}$$

Given that $X_1 = 5$ and $X_2 = 3.5$ we have

$$\log \frac{p}{1-p} = -4 + 0.25 + 3.5 = -0.25 \tag{2}$$

Hence *P*= 0.438

b.

$$odds = \frac{p}{1 - p} = \frac{0.438}{1 - 0.438} = 0.779 \tag{3}$$

C.

We have P = 0.5 and $X_2 = 3.5$

$$\log \frac{0.5}{1 - 0.5} = -4 + 0.25X_1 + 3.5 \tag{4}$$

Hence $X_1 = 10$, which means that 10 hours study is required

Q2.

```
(a)
```

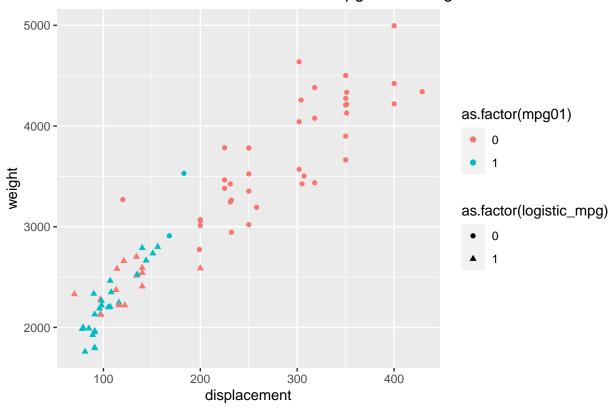
```
library(ISLR)
data("Auto")
mpg01 <- ifelse(Auto$mpg > 25, 1, 0)
Auto <- data.frame(Auto, mpg01)
set.seed(123)
num_train <- nrow(Auto) * 0.8</pre>
inTrain <- sample(nrow(Auto), size = num_train)</pre>
training <- Auto[inTrain,]</pre>
testing <- Auto[-inTrain,]</pre>
logistic_model <- glm(mpg01 ~ displacement + horsepower + weight + cylinders, data = training)</pre>
summary(logistic_model)
##
## Call:
## glm(formula = mpg01 ~ displacement + horsepower + weight + cylinders,
##
       data = training)
##
## Deviance Residuals:
##
       Min
                      Median
                                    3Q
                 1Q
                                            Max
## -0.7775 -0.3107
                      0.1283
                               0.2552
                                         0.8809
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
                 1.748e+00 1.383e-01 12.644 < 2e-16 ***
## (Intercept)
## displacement 9.839e-04 8.153e-04
                                        1.207
                                                 0.2284
              -1.213e-03 1.208e-03 -1.003
## horsepower
## weight
                -3.276e-04 6.586e-05 -4.974 1.09e-06 ***
## cylinders
                -7.823e-02 3.710e-02 -2.108 0.0358 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for gaussian family taken to be 0.1243352)
##
##
       Null deviance: 75.834 on 312 degrees of freedom
## Residual deviance: 38.295 on 308 degrees of freedom
## AIC: 242.68
##
## Number of Fisher Scoring iterations: 2
Hence, only "weight" and "cylinders" are significant in the logistic regression. (b) For testing error
pred_test <- predict(logistic_model, testing)</pre>
testPrediction = rep("0", nrow(testing))
testPrediction[pred_test > .5] = "1"
testing$logistic_mpg = testPrediction
table(testPrediction, testing$mpg01, dnn = c("Predicted", "Actual"))
##
            Actual
## Predicted 0 1
##
           0 38 2
           1 14 25
##
```

```
round(mean(testPrediction != testing$mpg01), 2)

## [1] 0.2

##Hence, the testing error is 0.2
ggplot(testing, aes(x=displacement, y=weight, color = as.factor(mpg01),shape = as.factor(logistic_mpg))
```

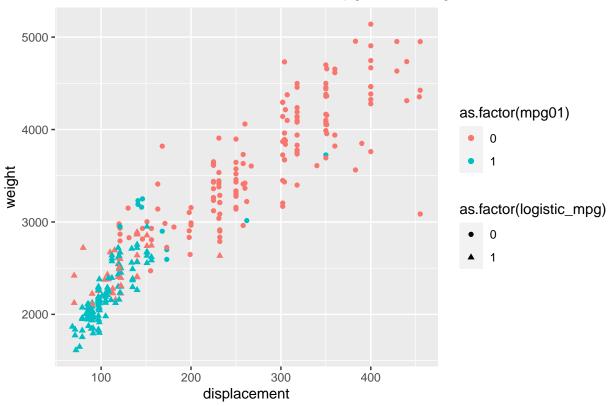
True values vs. Predicted Values of Mpg01 with Logistic



For training error

```
pred_train <- predict(logistic_model, training)</pre>
trainPrediction = rep("0", nrow(training))
trainPrediction[pred_train > .5] = "1"
training$logistic_mpg = trainPrediction
table(trainPrediction, training$mpg01, dnn = c("Predicted", "Actual"))
##
            Actual
               0
## Predicted
                   1
##
           0 149 10
           1 35 119
round(mean(trainPrediction != training$mpg01), 2)
## [1] 0.14
##Hence, the training error is 0.14
ggplot(training, aes(x=displacement, y=weight, color = as.factor(mpg01), shape = as.factor(logistic_mpg)
```





(c)

 $\log \frac{p}{1-p} = 1.748 + 9.839 \times 10^{-4} displacement - 1.213 \times 10^{-3} horsepower - 3.276 \times 10^{-4} weight - 7.823 \times 10^{-2} cylinders \tag{1}$

median(training\$displacement)

[1] 146

median(training\$horsepower)

[1] 95

median(training\$weight)

[1] 2807

median(training\$cylinders)

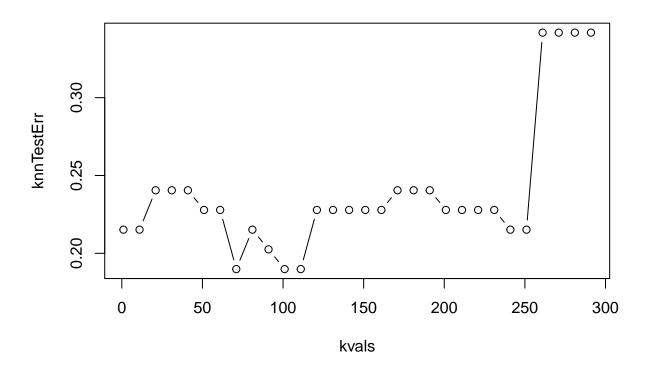
[1] 4

Hence odds = 0.408, p = 0.6 (d)

```
trainX = as.matrix(training[c("displacement", "horsepower", "weight", "cylinders")])
testX = as.matrix(testing[c("displacement", "horsepower", "weight", "cylinders")])
set.seed(1)
kvals = seq(1, 300, 10)
```

testing error

```
knnTestErr = vector(length = length(kvals))
for (i in 1:length(kvals)) {
knn.pred = knn(train = trainX, test = testX, cl = training$mpg01, k=kvals[i])
knnTestErr[i] = mean(knn.pred != testing$mpg01)
}
plot(knnTestErr ~ kvals, type = "b")
```



```
knnTestErr ##The minimum value is obtained when k = 71

## [1] 0.2151899 0.2151899 0.2405063 0.2405063 0.2405063 0.2278481 0.2278481

## [8] 0.1898734 0.2151899 0.2025316 0.1898734 0.1898734 0.2278481 0.2278481

## [15] 0.2278481 0.2278481 0.2278481 0.2405063 0.2405063 0.2405063 0.2278481

## [22] 0.2278481 0.2278481 0.2278481 0.2151899 0.2151899 0.3417722 0.3417722

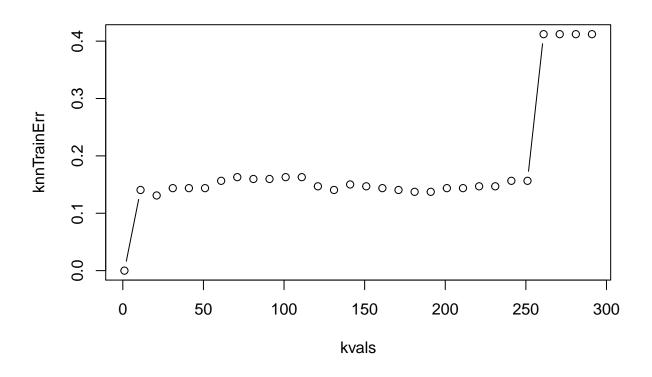
## [29] 0.3417722 0.3417722

training error

kvals = seq(1, 300, 10)

knnTrainErr = vector(length = length(kvals))

for (i in 1:length(kvals)) {
 knn.pred1 = knn(train = trainX, test = trainX, cl = training$mpg01, k=kvals[i])
 knnTrainErr[i] = mean(knn.pred1 != training$mpg01)
}
plot(knnTrainErr ~ kvals, type = "b")
```



```
knnTrainErr ##The minimum value is obtained when k = 1

## [1] 0.0000000 0.1405751 0.1309904 0.1437700 0.1437700 0.1437700 0.1565495

## [8] 0.1629393 0.1597444 0.1597444 0.1629393 0.1629393 0.1469649 0.1405751

## [15] 0.1501597 0.1469649 0.1437700 0.1405751 0.1373802 0.1373802 0.1437700

## [22] 0.1437700 0.1469649 0.1469649 0.1565495 0.1565495 0.4121406 0.4121406

## [29] 0.4121406 0.4121406

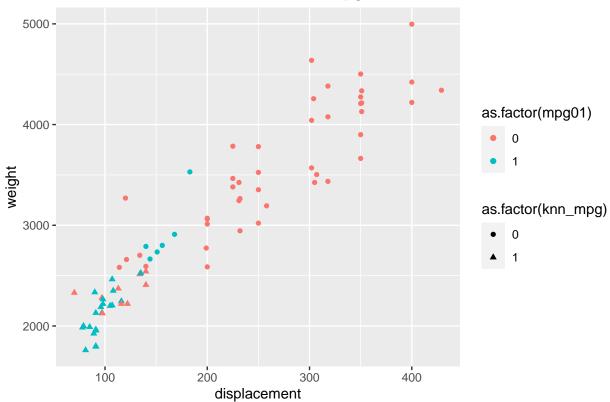
##except for k = 1m the minimum value is obtained when k = 21

(e)

knn.pred = knn(train = trainX, test = testX, cl = training$mpg01, k=71)

testing$knn_mpg = knn.pred
ggplot(testing, aes(x=displacement, y=weight, color = as.factor(mpg01),shape = as.factor(knn_mpg)))+georetical color = as.factor(mpg01),shape = as.factor(mpg01),sha
```





```
knn.pred1 = knn(train = trainX, test = trainX, cl = training$mpg01, k=21)
training$knn_mpg = knn.pred1
ggplot(training, aes(x=displacement, y=weight, color = as.factor(mpg01),shape = as.factor(knn_mpg)))+ge
```

True values vs. Predicted Values of Mpg01 with Knn 5000 as.factor(mpg01) 4000 -0 weight as.factor(knn_mpg) 3000 -0 2000 -200 100 300 400 displacement (f) table(knn.pred, testing\$mpg01, dnn = c("Predicted", "Actual")) ## Actual ## Predicted 0 1 0 43 6 ## 1 9 21 round(mean(knn.pred != testing\$mpg01), 2) ## [1] 0.19 ##Hence, the testing error is 0.19 table(knn.pred1, training\$mpg01, dnn = c("Predicted", "Actual")) ## Actual ## Predicted 0 ## 0 160 17 24 112 ## round(mean(knn.pred1 != training\$mpg01), 2)

```
##Hence, the training error is 0.13

In this experiment, we choose k-value with a non-efficient for loop, which is similar to bubbling selection.
```

[1] 0.13

In this experiment, we choose k-value with a non-efficient for loop, which is similar to bubbling selection, the efficiency of this algorithm is O(n), which is super slow and might cause extremely long estimation time.

However, if we have determined the range of k-value, we can use a more efficient algorithm to cut off the time into Olog(n).

Also, normalization is also very important in Knn classification, if we ignored the normalization part it might jeopardize the estimation.

(g) Regarding the test error, QDA performs the best, and about the training error both QDA and Knn classification performs the best. Hence the distribution of the data is non-linear, and the boundary between classes is quadratic.