

1) Find the global minimum point for 2 iterations

$$f(x) = x^4 + 3x^2 + 10$$

Step 0: Initialization

$$x = 1.2, \eta = 0.01, \text{epoch} = 2, \text{iteration} = 1$$

Step 1: Derivation at $x = 1.2$

$$\begin{aligned} \left(\frac{df}{dx} \right)_{x=1.2} &= (4x^3 + 6x) = 4(1.2)^3 + 6(1.2) \\ &= 6.912 + 7.2 \\ &= 14.112 \end{aligned}$$

Step 2:

$$\begin{aligned} \Delta x &= -\eta \frac{df}{dx} = (-0.01)(14.112) \\ &= -0.14112 \end{aligned}$$

Step 3: $x = x + \Delta x$

$$\begin{aligned} x &= 1.2 - 0.14112 \\ &= 1.05888 \end{aligned}$$

Step 4: iteration = iteration + 1

$$\begin{aligned} &> 1+1 \\ &> 2 \end{aligned}$$

Step 6: if (step 7 reaches)

272 go to step 7

else

go to step 2

if

done 272

then go to step 2

Step 2:

$$\left(\frac{df}{dx}\right)_{at x=1.05}$$

$$4x^3 + 6x = 4(1.05)^3 + 6(1.05)$$

if

$$= 10.9305$$

$$\text{Step 3: } \Delta x = -\eta \frac{df}{dx}$$

$$-(0.01) (10.9305)$$

$$= 0.109305$$

$$\text{Step 4: } x = x + \Delta x$$

$$1.05 + 0.109305$$

$$= 1.159305$$

step 5: iteration = iteration + 1

> 200

> 3

step 6: if (iteration > epochs)

go to step 1

else

go to step 2

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~~true~~ True

step 7: $m = 1.155$

$$m^4 + 3m^2 + 10$$

$$(1.15)^4 + 3(1.15)^2 + 10$$

$$> 15.7165$$