

Formatting Instructions for CoRL 2020

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Abstract: ABSTRACT PLACEHOLDER

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1 Introduction

Path planning is a search problem where the goal is to find a sequence of actions that will lead to an obstacle-free optimal path from a start state to a target state [1]. Grid-based search algorithms have been proposed in the past [2] [3] that guarantee finding optimal paths that exists. However, these techniques do not scale well to higher dimensional problems as they require discretization of the state space. On the other hand, sampling-based path planning algorithms [4] [5] can solve high-dimensional path planning problems more efficiently, but often compute sub-optimal paths. Many attempts have been made to make improvements to sampling-based methods, using techniques such as heuristic guided searches [6], or the reduction of the sampling space [7]. The goal of this project is to implement three probabilistic sampling-based path planning algorithms, and compare their performances through simulations.

2 Problem

Path planning in continuous space is a difficult problem. On one hand, there are graph based approaches such as Dijkstra's algorithm, A*, etc. These approaches find the optimal solution, if one exists. In the case of A*, it uses a heuristic to find the optimal solution in fewer iterations. However, graph based approaches require discretization of continuous space. This is a problem for two reasons: First, a increasing the number of dimensions causes an explosion in the number of nodes. Second, increasing the resolution with finer discretization also causes a growth in the number of nodes. Having a high number of nodes creates a problem because the computational time of graph based approaches increases rapidly with the number of nodes.

On the other hand, there are sampling based approaches. They sample states from the continuous space, and create a tree, known as a Random Tree (RT). In Rapidly-exploring RT (RRT) algorithms, each new sampled state is added to the closest point on current tree. A more detailed description of the various sampling based approaches is presented in 3. However, while sampling rather than discretizing makes them more scalable, they do not have the ordered nature of graph based approaches for a more efficient search process.

PLACEHOLDER FOR PROBLEM - DISCUSS MOTIVATION FOR USING ASYMPTOTICALLY OPTIMAL SAMPLING BASED PATH PLANNING (asymptotic optimality, probabilistic completeness)

3 Related Work

FOR EACH ALGORITHM, LIST TECHNIQUES/ALGORITHMS ITS BUILDING ON OR IMPROVING UPON AND GIVE BRIEF A EXPLANATION

35 RRT - Create a tree of connected nodes by sampling a state from the continuous space and extending
36 closest state on the existing tree towards the newly sampled state RRT* - Before each iteration of
37 RRT, optimize the existing tree - More optimal path - Longer iterations Informed RRT* - Once a
38 sub-optimal solution is found, reduces the continuous space from which states are being sampled
39 to a space (an ellipse) that can improve the current solution, allowing for faster convergence to
40 the optimal FMT* - Marching method to process single set of samples Randomized A* (RA*)
41 and Sampling based A* (SBA*) - Sample near heuristically selected vertices of the graph - Biases
42 growth of the tree but requires methods avoid local minima - Good for spaces with no obstacles,
43 but not good for spaces with a lot of obstacles - They address these problems but with trade-offs -
44 SBA* trade-off doesn't seem bad, may be worth comparing? NRRT* - RRT*, A*, Informed RRT*,
45 A*-RRT*, Threer*-RRT* (mention limitations due to scalability)

46 **4 Proposed Method**

47 - BRIEF DESCRIPTION OF EACH OF THE ALGORITHMS BEING IMPLEMENTED (IN-
48 CLUDE ANY TECHNICAL/THEORETICAL DETAILS TO HIGHLIGHT CORE IDEAS, DO
49 NOT GO INTO DETAILS)

50 In this project, we propose a comparison study of three asymptotically-optimal sampling-based path
51 planning algorithms: Fast-marching trees (FMT*), batch informed trees (BIT*), and neural rapidly
52 random-exploring trees (NRRT*) [8]. The following section will briefly describe each of these
53 algorithms.

54 **4.1 Fast-Marching Trees**

55 Sampling based algorithms can be divided into two categories: Single query (RRT* []) and Multiple
56 query. FMT* combines the

57 **4.2 Bath Informed Trees**

58 Uses batches of samples to perform an ordered search Sample randomly but use heuristic to deter-
59 mine which sample from the batch to process next Allows converging asymptotically towards the
60 global optimum with anytime resolution (quickly find sub-optimal solution, then optimize it) In-
61 corporate the new samples into the existing search Focus on the subproblem that contain a better
62 solution

63 **4.3 Neural RRT***

64 Neural RRT* is a non-uniform sampling-based path planning algorithm that aims to take advantage
65 of the optimal path costs of the A* algorithm as well as the asymptotic optimality of the RRT*
66 algorithm. Instead of sampling from the state space using just a uniform distribution, a non-uniform
67 distribution learned by a convolutional neural network (CNN) trained on optimal paths generated
68 from the A* algorithm is used to achieve non-uniform sampling. Unlike many of the RRT variant
69 algorithms [CITATIONS PLACEHOLDER], the NRRT* algorithm does not depend on any human-
70 designed heuristics to improve its performance. It also maintains the probabilistic completeness
71 and the asymptotic optimality of the RRT* algorithm. Through simulations, it has been shown to
72 perform superior compared to traditional algorithms such as RRT* and informed RRT* (IRRT*)
73 [CITAION PLACEHOLDER].

74 **5 Proposed Evaluation**

75 We will implement the individual algorithms in python as per the discussions and directives men-
76 tioned in the individual papers ([9] FMT, [8] NRRT*, \cite{BIT* paper cite} BIT*). In order to make
77 direct comparisons between optimal paths returned by the different algorithms, we will run them on

78 a common set of cluttered environments (these would include bug traps and a set of 2D maze). We
79 will measure 2 metrics as part of running the simulation: Optimal Path Cost (\mathcal{J}) and Execution
80 Time (\mathcal{T}). ET is calculated based on the convergence criteria for each algorithm. We evaluate the
81 cost (\mathcal{J}) as follows: For a grid having N nodes in the free space \mathcal{X}_{free} , let $\mathcal{P} \subset \mathcal{X}_{free}$ be the set
82 of nodes along the optimal path as computed by the path planning algorithm $\{\mathcal{X}_{free}, x_{init}, \mathcal{X}_{goal}\}$;
83 Then the cost \mathcal{J} is defined as,

$$\mathcal{J} = \sum_{i=1}^N \mathbb{I}[x_i \in \mathcal{P}], \text{ where } x_i \text{ are the nodes in the free space.} \quad (1)$$

84 Since, NRRT* does not involve setting the sample size / iteration count, we will do an additional
85 comparison of the variation of cost (\mathcal{J}) and ET (\mathcal{T}) with sample count for FMT* and BIT*. Com-
86 parison will be done for 10 different sample counts in the range $[1000, 10000]$. Finally, we will also
87 provide a qualitative comparison of the optimal paths resulting from each algorithm for the same set
88 of environments highlighting their behaviour around corners and near obstacles.

89 6 Citations

90 Citations can be made using either `\citep{}` or `\citet{}`, depending from the appropriateness. To
91 avoid the citation moving to the next line, it is often a good practice to replace the space before with
92 a tilde (~) character. Example 1: “CoRL is the best conference ever [?].” Example 2: “?] proved,
93 both theoretically and numerically, that CoRL is the best conference ever.”

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