

Single Value Decomposition

	Indiana Jones	Star Wars	X Y Z	B31	B32
Bob	4	5	5	4	4
Ted	3	3	3	5	4
Ann	4	5	5	5	2

Matrix $\rightarrow R$



	Action	SciFi	Classic
Bob	0.3	0.5	0.2
Ted	0.1	0.1	0.8
Ann	0.3	0.6	0.1

Matrix $\rightarrow U$

Here Bob is described

{ Here
each row is divided
into user

action + sci fi + classic

Matrix $\rightarrow RT$

	Bob	ann	Ted
Indiana Jones	4	3	4
Star Wars	5	3	5
X Y Z	5	3	5
B31	4	5	5
B32	4	4	2

Matrix R^T

	Action	scif	classic
Indian Jones	0.6	0.3	1
Star Wars	0.4	0.6	0
X Y Z	0.4	0.6	0
B B 1	0.8	0.2	0
B B 2	0.2	0	0.8

Matrix M

~~Here~~ Each movie is divided into
"Action & classic"

Matrix factorization \Rightarrow

$$R = U \Sigma M^T$$

user movie

↪ If we have missing values in R (matrix R) we

can reconstruct using matrix U & matrix M

↪ That's why it is known as

Matrix Factorization.

$\{$ we describe our training data in terms of smaller matrices ; and missing values in that, we want to predict that. $\}$

$$R = U \Sigma M^T$$

↓
User
matrix

Movie matrix

→ The way of Computing all 3 together

$\left\{ \begin{array}{c} U \\ \downarrow \\ \text{User} \\ \text{matrix} \end{array}, \sum, M^T \right. \} \text{ is known}$

\downarrow Sigma ↓
Transposed
Movie matrix

as Single Value Decomposition.

Note:-

When the original matrices "R" is having missing values then we can't

run PCA on that. {some of them} . It must be missing

be a complete matrix

Suppose:-

	Indian Jones	Star Wars	X Y Z	B B 1	B B 2
Bob	4	5	?	?	?
Ann	?	?	?	?	1
Ted	9	6	5	5	?

$$R_{Bob, XYZ} = U_{Bob} \cdot M_{XYZ}^T$$

↳ Using SVD we calculate $R_{Bob, XYZ}$.

↳ We can treat this problem as Minimization

Problem:

↳ There is not only SVD; there are some other ML techniques i.e. ~~Stochastic~~
Stochastic Gradient

Descent Method

{ It will iterate until it reaches minimum value }