

Dept. of Electrical Engineering, IIT Madras
CADLAB July 2015 session

- ▷ Time duration of exam is two hours
- ▷ vector operations are a must or lose lots of marks!!
- ▷ Label all plots. Add legends. Make the plots professional looking.
- ▷ Comments are not optional. They are required.
- ▷ pseudocode should be readable and neatly formatted.
- ▷ code should be written as part of a LyX file.
- ▷ Please download the blank LyX file with noweb enabled.
- ▷ LyX file should be named *your-roll-number.lyx*
- ▷ I should be able to extract the python code using the view menu.
- ▷ Include the plots in the lyx file and generate a pdf.
- ▷ Internet will be turned off at the beginning of the exam.
- ▷ Zip the LyX file and the pdf file together and name it as *your-roll-number.zip*. Leave it in the home directory of your machine and show the same to the TA before leaving.
- ▷ Late submission will result in reduced marks.

A long wire carries a current $I = 4\pi/\mu_0$ Amp. The wire is along the z -axis except that it has a semi-circular bend of radius 10 cm centered about the origin. The semi-circle lies in the $x - z$ plane. The problem is to compute and plot the magnetic field \vec{B} on the $x - y$ plane at $z = 0$. Plot both a contour plot of the strength of the field $|\vec{B}|$ and a vector plot of the field in the plane.

The computation involves the calculation of the Biot-Savart integral:

$$\vec{B}(x, y, 0) = \frac{\mu_0}{4\pi} \int \frac{I d\vec{l} \times \vec{R}}{R^3} \approx \frac{\mu_0 I}{4\pi} \sum_{k=0}^{N-1} \frac{d\vec{l}_k \times \vec{R}}{R^3}$$

where $\vec{R} = \vec{r} - \vec{r}'$. Here $\vec{r} = x\hat{x} + y\hat{y}$ is the point where we want the field, and \vec{r}' is the point on the wire and $d\vec{l}$ is the differential length along the wire.

Assume that the wire goes from -30 to 30 cm, and assume that the region to plot is a square $-20 < x, y < 20$. The expression to be computed is

$$\vec{B}_{ij} = \sum_{k=0}^{N-1} \frac{d\vec{l}_k \times \vec{R}_{ijk}}{R_{ijk}^3}$$

where $\vec{R}_{ijk} = \vec{r}_{ij} - \vec{r}'_k$.

- ▷ Write pseudocode for how you will solve this problem.
- ▷ Break the square region into a 101 by 101 mesh and the wire into 200 sections. Use 30% of the points in the wires for each of the straight sections and 40% for the loop. Define the data structures required for the problem. Plot the wire in the $x - z$ plane with bounds $(-20, 20)$ along x and $(-30, 30)$ along z . Properly label the graph.
- ▷ Obtain the vectors \vec{r}'_k , $d\vec{l}_k$ and \vec{r}_{ij} , where k indexes the segments of the wire and i, j index the x and y positions of the square region.
- ▷ Define a function `calc(k)` that calculates \vec{R}_{ijk} for all i, j , for the value of k passed to the function (k is the index into the \vec{r}' array, which you have defined earlier.) Note: vectorize this function!
- ▷ Extend `calc` to generate the terms in the sum, i.e., write out the cross product and divide by R_{ij}^3 , and return the term to add to \vec{B} . Note: vectorize the function
- ▷ Use the function to compute \vec{B}_{ij} (you can use a for loop here. Justify in a comment)
- ▷ Plot the magnetic field (contour and arrow plots). To show more detail, plot the contour of $\log_{10} |\vec{B}|$ and plot the vector plot of $\vec{B}/|\vec{B}|$ (arrows of constant length). Locate the (x, y) position of the straight segments. Why is field not going round that

Useful Python Commands (use “?” to get help on these from ipython)

```
from pylab import *
import system-function as name
Note: lstsq is found as scipy.linalg.lstsq
ones(List)
zeros(List)
range(N0,N1,Nstep)
arange(N0,N1,Nstep)
linspace(a,b,N)
logspace(log10(a),log10(b),N)
X,Y=meshgrid(x,y)
where(condition)
where(condition & condition)
where(condition | condition)
a=b.copy()
lstsq(A,b) to fit  $A \cdot x = b$ 
A.max() to find max value of numpy array (similarly min)
A.astype(type) to convert a numpy array to another type (eg int)
def func(args):
    ...
    return List
matrix=c_[vector,vector,...] to create a matrix from vectors
figure(n) to switch to, or start a new figure labelled n
plot(x,y,style,...,lw=...)
semilogx(x,y,style,...,lw=...)
semilogy(x,y,style,...,lw=...)
contour(x,y,matrix,levels...)
quiver(X,Y,U,V) # X,Y,U,V all matrices
xlabel(label,size=)
ylabel(label,size=)
title(label,size=)
xticks(size=) # to change size of xaxis numbers
yticks(size=)
legend(List) to create a list of strings in plot
annotate(str,pos,blpos,...) to create annotation in plot
grid(Boolean)
```