

# Task 5

Let  $x_1, x_2, x_3, x_4$  be state variable

$$x_1 = \theta$$

$$x_2 = \dot{\theta} = \dot{x}_1$$

$$\dot{x}_2 = \ddot{\theta}$$

$$x_3 = x$$

$$\dot{x}_3 = \dot{x}_4$$

$$\dot{x}_4 = \ddot{x}$$

$$M\dot{x}_4 = F - mgx_1$$

$$\dot{x}_4 = -\frac{mg}{M}x_1 + \frac{F}{M}$$

$$ML\dot{x}_2 = (M+m)gx_1 - F$$

$$\dot{x}_2 = \frac{(M+m)g}{ML}x_1 - \frac{F}{ML}$$

$$\dot{x}_1 = x_2$$

$$\dot{x}_3 = x_4$$

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \\ \dot{x}_4 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ \frac{(M+m)g}{ML} & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ -\frac{mg}{M} & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} + \begin{bmatrix} 0 \\ -\frac{1}{ML} \\ 0 \\ \frac{1}{M} \end{bmatrix} [F]$$

$$\begin{bmatrix} y_1 \\ y_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix}$$

Let  $M = 5$

$m = 1$

$L = 1$