

# Unit: 4 : Mission Vision.

Date \_\_\_\_\_

Saathi

\* performance Index: NPV-dec.

determine performance index

translation (3,1)

(Q.8) a)

⇒ Template       $\begin{matrix} & & & y \\ & & & \downarrow \\ 6 & 2 & 7 & 0 & 7 & 3 & 7 & 3 & 8 \\ 7 & 2 & 4 & 1 & 7 & 4 & 3 & 4 & 4 \\ 1 & 5 & 6 & 2 & 5 & 2 & 9 & 3 & 5 \\ 8 & 4 & 8 & 3 & 4 & 7 & 1 & 4 & 6 \\ 5 & 9 & 5 & 4 & 8 & 8 & 1 & 7 & 6 \\ 1 & 6 & 6 & 1 & 6 & 6 & 6 & 6 & 8 \end{matrix}$  Image.

Template	Image
6 2 7	0 7 3 7 3 8
7 2 4	1 7 4 3 4 4
1 5 6	2 5 2 9 3 5
8 4 8	3 4 7 1 4 6
5 9 5	4 8 8 1 7 6
1 6 6	1 6 6 6 6 8

Template:

Image. (3,1)

6 2 7	7 1 7
7 2 7	8 1 7
1 5 6	1 6 6

performance Matrix.

$$P(\text{faulty}) = d \cdot T_{\text{faulty}}$$

1	1	0
1	1	0
0	1	0

performance Index

$$P(3,1) = \underline{\underline{5}}.$$

Date \_\_\_\_\_

## \* cross-correlation

- May-Jun:
- correlation factor = ?  
translation (111).

Template,

			Img.				
			0	1	2	3	4
8	1	8	0	2	2	6	5
1	1	32	1	4	5	9	9
4	8	23	2	7	8	1	9
			3	9	1	1	3
			4	5	4	9	6
			5	1	6	4	8



Template.

Avg. Intensity (T).

8	1	8
1	1	2
4	8	3

84      1      64

1      1      4

16      64      9

= 224= 14.966

Img.

Avg. intensity Img.

5	9	9
8	1	9
1	1	3

25      81      81

64      1      81

1      1      9

= 344= 18.54

$$11711, 11311 = 14.966 \times 18.5472 \\ = \underline{277.5779}.$$

- product of Img & Template

$$\begin{array}{r} 40. \\ \begin{array}{r} 24 \quad 9 \quad 35 \quad 9 \quad 72 \\ 6 \quad 4 \quad 8 \quad 1 \quad 18 \\ \hline 169 \quad 608 \quad 4 \quad 8 \quad 9 \end{array} \\ = \underline{169.} \end{array}$$

$$\text{for normalization} = \frac{169}{277.5779}$$

$$\boxed{\sigma = 0.5908 \cdot 0.6088}$$

matching about: 59.08%, 60.88%.

Date \_\_\_\_\_ / \_\_\_\_\_ / \_\_\_\_\_

 $\Rightarrow$  Template:

Jmg.

$$\begin{array}{ccccccccc}
 9 & 2 & 8 & 5 & & 2 & 7 & 5 & 3 \\
 3 & 6 & 7 & 3 & - & 2 & 8 & 7 & 1 \\
 0 & 9 & 9 & 8 & & 4 & 4 & 3 & 8 \\
 7 & 9 & 1 & 5 & & 2 & 9 & 2 & 5
 \end{array}$$

$$\begin{array}{ccccc}
 & 7 & 5 & 3 & 2 \\
 \text{performance} = & 1 & 1 & 0 & 2 \\
 \text{matrix} & 4 & 5 & 6 & 2 \\
 & 5 & 0 & 1 & 0
 \end{array}$$

$$\begin{array}{c}
 \text{performance} = \underline{\underline{44}} \\
 \text{index}
 \end{array}$$

Q.19

use prewitt operator.

$$\begin{array}{ccc}
 4 & 6 & 8 \\
 3 & 7 & 8 \\
 2 & 9 & 1
 \end{array}$$

$$\text{Avg. I} = \frac{45}{7} = \underline{\underline{6.4285}}$$

To determine gradient of function

using gradient operator

$$m_2 = \begin{bmatrix} 1 & 0 & 1 \\ 1 & 0 & 1 \\ 1 & 0 & 1 \end{bmatrix}, m_3 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 1 & 0 & 1 \end{bmatrix}$$

$$m_1 = \begin{bmatrix} -4 & 0 & 5 \\ -3 & 0 & 8 \\ -2 & 0 & 1 \end{bmatrix}, m_2 = \begin{bmatrix} -4 & 6 & 5 \\ 0 & 0 & 0 \\ 2 & 3 & 1 \end{bmatrix}$$

$$\nabla = \sqrt{(f(x))^2 + (f(y))^2}$$

$$\therefore f(x) = \frac{|x - (-4)| + |x - (-3)| + |x - (-2)|}{3}$$

$$f(x) = \frac{1 + 2 + 1}{3} = \frac{4}{3} = 2.33$$

$$f(y) = \frac{|y - (-4)| + |y - (-3)| + |y - (-2)|}{3}$$

$$= \frac{2 + 3 + 4}{3} = \frac{9}{3} = 3$$

$$\therefore \nabla = \sqrt{(2.33)^2 + (3)^2}$$

$$\boxed{\nabla = 3.7925}$$

gradient of intensity of light

Date \_\_\_\_\_

May - Jun:

$$\text{Q. 4) a) } \begin{array}{ccc} 5 & 8 & 4 \\ 6 & 2 & 3 \\ 4 & 8 & 1 \end{array} \quad \begin{array}{l} \text{Img} \\ \Rightarrow \text{Avg I} = \frac{39}{2} \\ = \underline{19.5} \end{array}$$

$$m_{ae} = \begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix} \quad m_y = \begin{bmatrix} -1 & -1 & -1 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

$$m_1 = \begin{bmatrix} -5 & 0 & 4 \\ -6 & 0 & 3 \\ -4 & 0 & 1 \end{bmatrix}, \quad m_2 = \begin{bmatrix} -5 & -8 & -4 \\ 0 & 0 & 0 \\ 4 & 6 & 1 \end{bmatrix}$$

$$\nabla = \sqrt{(f(x))^2 + (f(y))^2}$$

$$f(x) = \frac{|4 - (-5)| + |3 - (-6)| + |1 - (-4)|}{3}$$

$$f(x) = \frac{1 + 3 + 3}{3} = \frac{7}{3} = \underline{2.33}$$

$$f(y) = \frac{|4 - (-5)| + |6 - (-8)| + |2 - (-4)|}{3}$$

$$= \frac{1 + 2 + 3}{3} = \frac{6}{3} = \underline{\underline{2}}$$

$$\therefore \nabla f = \sqrt{(2.33)^2 + (2)^2} = \underline{\underline{3.0765}}$$

~~=~~

Nov-Dec! Q.4) a)

$$\begin{array}{ccc} 2 & 6 & 8 \\ 4 & 3 & 2 \\ 1 & 7 & 6 \end{array} \quad \text{Avg.} = \frac{2+3+6}{3} = \boxed{3}.$$

$$m_x = \begin{bmatrix} -1 & 0 & -1 \\ -1 & 0 & -1 \\ -1 & 0 & 1 \end{bmatrix} \quad m_y = \begin{bmatrix} -1 & -1 & -1 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

$$m_1 = \begin{bmatrix} -2 & 0 & 8 \\ -4 & 0 & 2 \\ -1 & 0 & 6 \end{bmatrix} \quad m_2 = \begin{bmatrix} -2 & -6 & -8 \\ 0 & 0 & 0 \\ 1 & 4 & 6 \end{bmatrix}$$

$$\nabla = \sqrt{(f(2))^2 + (f(4))^2}$$

$$f(x) = \frac{|8 - (-2)| + |2 - (-4)| + |6 - (-1)|}{3} = \frac{6 + 2 + 5}{3} = \boxed{4.33}.$$

$$f(y) = \frac{|3 - (-2)| + |7 - (-6)| + |6 - (-8)|}{3}$$

$$= \frac{1+1+2}{3} = \frac{4}{3} = \boxed{1.33}$$

$$\nabla f = \sqrt{(4.33)^2 + (1.33)^2}$$

$$\nabla f = \boxed{4.5296}.$$

Date \_\_\_\_\_

Nov-dec! Q.4) a)

$$\begin{array}{ccc} 2 & 6 & 8 \\ 4 & 3 & 2 \\ 1 & 7 & 6 \end{array} \quad \text{Avg - I} = \underline{\underline{39}} \quad \text{I Avg.I} = \underline{\underline{13}}$$

$$m_x = \begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix}, \quad m_y = \begin{bmatrix} -1 & -1 & -1 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

$$m_1 = \begin{bmatrix} -2 & 0 & 8 \\ -4 & 0 & 2 \\ -1 & 0 & 6 \end{bmatrix}, \quad m_2 = \begin{bmatrix} -2 & -6 & -8 \\ 0 & 0 & 0 \\ 1 & 7 & 6 \end{bmatrix}$$

$$\nabla = \sqrt{(f(x))^2 + (f(y))^2}$$

$$f(x) = \frac{|8 - (-2)| + |2 - (-4)| + |6 - (-1)|}{3} = \frac{6 + 2 + 5}{3} = \underline{\underline{4.33}}$$

$$f(y) = \frac{|9 - (-2)| + |7 - (-6)| + |6 - (-8)|}{3}$$

$$= \frac{1 + 1 + 2}{3} = \frac{4}{3} = \underline{\underline{1.33}}$$

$$\nabla f = \sqrt{(4.33)^2 + (1.33)^2}$$

$$\boxed{\nabla f = \underline{\underline{4.5296}}}.$$

Date \_\_\_\_\_

## \* example: sobel operator

$$\begin{bmatrix} 2 & 6 & 8 \\ 4 & \boxed{3} & 2 \\ 1 & 7 & 6 \end{bmatrix}$$

$$A_{49}: I = \frac{39}{3} = \underline{\underline{13}}$$

$$\Rightarrow m_x = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}, m_y = \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}$$

$$m_1 = \begin{bmatrix} -2 & 0 & 8 \\ -8 & 0 & 4 \\ -1 & 0 & 6 \end{bmatrix} \quad ; \quad m_2 = \begin{bmatrix} -2 & -12 & 8 \\ 0 & 0 & 0 \\ 1 & 14 & 8 \end{bmatrix}$$

$$\nabla F = \sqrt{(f(x))^2 + (f(y))^2}$$

$$f(x) = \frac{|8 - (-2)| + |4 - (-8)| + |6 - (-1)|}{3} \\ = \frac{6 + 4 + 5}{3} = \underline{\underline{5}}$$

$$f(y) = \frac{|1 - (-2)| + |14 - (-12)| + |8 - (-8)|}{3} \\ = \frac{1 + 2 + 2}{3} = \frac{5}{3} = \underline{\underline{1.666}}$$

$$\nabla F = \sqrt{(5)^2 + (1.666)^2} \\ = \underline{\underline{5.2683}}$$

Date \_\_\_\_\_ / \_\_\_\_\_ / \_\_\_\_\_

$$\nabla F < \text{Avg J.}$$

\* If  $\nabla F$  is Less than Avg J. then it is not on edge.

\* If  $\nabla F$  is greater than Avg J. then it is on edge.

$$\nabla F > \text{Avg J.}$$

\* Centroids :-

Moment = Intensity of light  $\times$  distance from origin.

$\rightarrow$  mom

$$M_{KJ} = \sum M_{xe}^K \cdot M_y^J$$

Area., A = m<sub>00</sub>

$$x_c = \frac{m_{01}}{m_{00}}$$

$$y_c = \frac{m_{10}}{m_{00}}$$

$I_{02}$  = moment of inertia corresponding x-axis.

$I_{20}$  = moment of inertia to y-axis.

Date \_\_\_\_\_

May-Jun: Q. 3) (b)

determine centroids.

(0,0)	1	2	3
1	2	0	3
2	1	1	4
3	2	1	3

$$\Rightarrow M_x = \begin{bmatrix} 2 & 0 & 3 \\ 2 & 2 & 8 \\ 6 & 3 & 9 \end{bmatrix}, M_y = \begin{bmatrix} 2 & 0 & 9 \\ 1 & 2 & 12 \\ 2 & 2 & 9 \end{bmatrix}$$

$$M_x = 35, M_y = 39$$

$$M_{KJ} = M_x^{\circ K} \cdot M_y^{\circ J}$$

$$M_{00} = M_x^{\circ} \cdot M_y^{\circ}$$

$$M_{00} = \begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} = 8$$

$$M_{10} = M_x^1 \cdot M_y^0$$

$$= \begin{bmatrix} 2 & 0 & 3 \\ 2 & 2 & 8 \\ 6 & 3 & 9 \end{bmatrix} = 35$$

$$M_{01} = \begin{bmatrix} 2 & 0 & 3 \\ 1 & 2 & 12 \\ 2 & 2 & 9 \end{bmatrix} = 39.$$

$$\therefore M_{00} = 8$$

$$M_{10} = 35$$

$$M_{01} = 39$$

$$\alpha_c = \frac{M_{10}}{M_{00}} = \frac{35}{8} = 4.375$$

$$\gamma_c = \frac{M_{01}}{M_{00}} = \frac{39}{8} = 4.875$$

X — Central moments.

$$M_{20} - \alpha_c = m_{2c}$$

$$M_{2c} = \begin{bmatrix} -2.375 & 0 & -1.375 \\ -2.375 & -2.375 & 3.625 \\ 1.625 & -1.375 & 4.625 \end{bmatrix}$$

$$m_{4c} = m_4 - \gamma_c$$

$$M_{4c} = \begin{bmatrix} -2.875 & 0 & 4.125 \\ -3.875 & -2.875 & 7.125 \\ -2.875 & -2.875 & 4.125 \end{bmatrix}$$

$$M_{kj} = \sum M_{2c}^k \cdot m_{4c}^j$$

## \* Region Growing \*

Sauthi

Date \_\_\_\_\_

Q.13) for the img. make two segment using region growing method.

3	4	0	0	2	4	4	2
3	1	0	2	1	3	4	1
2	0	4	4	1	2	1	5
4	3	2	0	3	2	4	8
2	4	3	2	1	1	1	6
7	6	8	8	8	8	0	5
6	8	6	7	7	6	4	5
8	7	6	7	6	8	2	8

⇒ ① finding seed point and threshold.

seed point = 8 (max point in img.)

∴ max. point in img.

threshold point =  $\frac{\text{max-min}}{2}$

$$\text{threshold} = \frac{8-0}{2} = \underline{\underline{4}}$$

②. Diff. matrix = seed point + each intensity

5	4	8	8	5	4	4	6	
5	7	8	8	7	5	4	7	
6	8	4	4	7	6	7	3	
4	8	6	8	5	6	4	0	
<u>8</u>	<u>4</u>	<u>5</u>	<u>6</u>	<u>7</u>	<u>7</u>	<u>7</u>	<u>2</u>	
1	2	0	0	0	0	8	3	
2	0	2	1	1	2	4	3	
0	1	2	1	2	0	6	0	

(3) make two segment of img.

$\text{DIFF} \geq \text{threshold}$ . value: = Segment A.

Diff < threshold value = segment B.

for seg : A' . = 4,5,6,7,8.

$$B = \underline{0, 1, 2, 3}.$$

A	A	A	A	A	A	A	A.	segment A
A	A	A	A	A	A	A	A	
A	A	A	A	A	A	A	B	
A	A	A	A	A	A	A	B	
A	A	A	A	A	A	A	B	
B	B	B	B	B	B	A	B	seg. B
B	B	B	B	B	B	A	B	
B	B	B	B	B	B	A	B	

# \* Run length encoding \*.

Saathi

Date \_\_\_\_\_

- used for the img. or data compression.

- img compression is done by reducing bit value
- includes calculation of 0's and 1's
- following terminologies used in run length encoding.

1) length = no. of 0's and 1's occurs in matrix.

2) Run = counting of subsequent bit until the bit changes.

3) string length = decoded value of binary string is known for string value length

or minimum no. of bits required to represent no. of length.

Date \_\_\_\_\_

Q.20) for a certain binary img, following data operates.. Determine the compression ratio using Run length encoding.

```

1 1 1 1 1 1
1 1 1 1 0 0
0 0 0 0 0 0
0 0 0 0 0 0
1 1 1 1 0 0

```

⇒ (Before compression).

Run	Bit	length	string length
1	1	10	$2^0 + 2^1 + 2^2 + 2^3 = 15$
2	0	14	$2^0 + 2^1 + 2^2 + 2^3 = 15$
3	1	5	$2^0 + 2^1 + 2^2 = 7$
4	0	1	$2^0 = 1$
= <u>30</u>			

$$2^0 + 2^1 + 2^2 + 2^3$$

Date / /

Now applying run length encoding to compress.

Run	length	Bit	total.
1	1010 0000	1	5
2	1110	0	5
3	0101	1	5
4	0001	0	5
			20

$$\text{Total length} = \text{length} + \text{Bit}$$

$$\text{compression Ratio} = \frac{\sum \text{length} - \sum \text{total}}{\sum \text{length}}$$

$$= \frac{30 - 20}{30} = \frac{10}{30}$$

$$\text{compression} = \underline{0.333}$$

$$\text{and compression Ratio} = \frac{20}{30}$$

$$1 : 0.66$$

$$\text{compression Ratio} = \frac{\sum \text{total}}{\sum \text{length}}$$

Date \_\_\_\_\_ / \_\_\_\_\_ / \_\_\_\_\_

Q. 4) b) Nov - dec

Run	Bitvalue	Length
1	1	12
2	0	18
3	1	7
4	0	17
5	1	10
		64

⇒ Run length Bit total.

1	01100	1	6
2	10010	0	6
3	00111	1	6
4	10001	0	6
5	01010	1	6
			<u>30</u>

$$\therefore \text{Compression Ratio} = \frac{64}{30}$$

$$= 0.5312$$

$$= 53.12\%$$

$$\text{Compression Ratio} = 1 : 0.13$$

$$\frac{64}{30} = 2.13$$

# Mission Endsem:

AJR.

Date \_\_\_\_\_ / \_\_\_\_\_ / \_\_\_\_\_  
17/05/2024



\* simulated annealing:

Q.5) function value: = 35

updated new temp = 50

at temp =  $100^{\circ}\text{C}$

To find: probability of accepting new solution

$\Rightarrow$

$$\therefore \boxed{e^{-\frac{\Delta C}{T}}}$$

$$\therefore \Delta C = 50 - 35$$

$$= 15$$

$$\therefore \frac{-15}{100} = -0.15$$

$$\therefore e^{-\frac{15}{100}}$$

$$= \underline{0.86070} = \underline{86.07\%}$$

Q.6) SA:

$$\Delta = 20.$$

$$x_{\max}, UB = 50,$$

$$x_{\min}, LB = 10.$$

$\delta N = 5$  (Randomly generated)  
 $R_i^*, \varepsilon = 1.87.$

updated value: ?

$\Rightarrow$  updated value of  $x$

$$= x' = \bar{x} + \sigma \times \left( \frac{\sum R_i - \frac{N}{2}}{2} \right)$$

$$\therefore 6\sigma = X_{\max} - X_{\min}$$

$$= 50 - 10$$

$$6\sigma = 40$$

$$\sigma = \frac{40}{6} = \underline{6.66}$$

$$\bar{x}' = \bar{x} + \sigma \times \left( \frac{\sum R_i - \frac{N}{2}}{2} \right)$$

$$= 20 + 6.66 \times \left[ 8 + 1.87 - \frac{5}{2} \right]$$

$$= 20 + 6.66 \times [1.87 - 2.5]$$

$$\therefore \underline{15.8042}$$

Date \_\_\_\_\_ / \_\_\_\_\_ / \_\_\_\_\_

May - Jun:

Q.1) b) SAG:

function value: 20.

updated New value: 30.

temp = 55°C

prob. of accepting New solu<sup>n</sup> = ?

→

$$= e^{\frac{-\Delta C}{T}}$$

$$\Delta C = 30 - 20$$

$$= 10$$

$$\therefore e^{\frac{-10}{55}} = e^{-0.1818}$$

$$= 0.83346 \quad = \underline{83.37\%}$$

Nov - déc:

Q.1) b)

$$x = 20$$

$$N = 5$$

$$x_{\min}, LB = 10,$$

$$\sum R_i = 1.87$$

$$x_{\max}, UB = 50,$$

$$= x' = x + \sigma \times \left( \sum R_i - \frac{N}{2} \right).$$

$$\therefore \sigma = x_{\max} - x_{\min}$$

$$= 50 - 10$$

$$\sigma = 40$$

$$\sigma = \frac{40}{6} = 6.666.$$

$$x' = x + \sigma \times \left( \sum R_i - \frac{N}{2} \right).$$

Date \_\_\_\_\_

$$= 20 + 6.66 \times \left( 51.87 - \frac{5}{2} \right)$$

$$= \underline{15.8042}$$

SA. Two type of problems :-

① - for finding probability of new solu<sup>n</sup> :-

$$\Rightarrow \text{if } e^{-\frac{\Delta C}{T}}$$

$$\therefore \Delta C = \text{New temp} - \text{fun}^n \text{ value.}$$

② for finding updated value !

$$\Rightarrow \text{if } x' = x + \sigma \times \left( E_{Ri} - \frac{N}{2} \right).$$

$$\text{if } \sigma = x_{\max} - x_{\min}.$$

Date \_\_\_\_\_ / \_\_\_\_\_ / \_\_\_\_\_

## \* Learnco:

$$\textcircled{1} \quad \text{fun}^n \text{ value: } 120$$

$$\text{new value: } 142$$

$$\text{temp: } 200^\circ\text{C}$$

$$\Delta C = 142 - 120$$

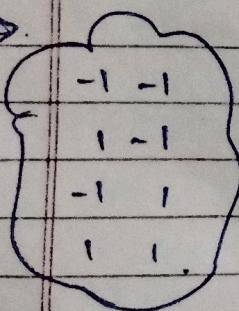
$$= 22$$

$$\therefore e^{-\frac{\Delta C}{T}} = e^{-\frac{22}{200}} = e^{-0.11}$$

$$= 0.8958$$

$$= 89.58\%$$

- \textcircled{2} A fun<sup>n</sup>:  $2x_1^2 + x_2 - 3x_2$ , is to be minimized using SA. If  $5 \leq x_1 \leq 8$  and  $3 \leq x_2 \leq 10$ .  
The value of initial temp. could be.



	$x_1$	$x_2$	$Z$
8	10	5	141
8	3	375	
5	10	3470	
8	10	1250	

put 4 these 4 combination in fun<sup>n</sup>

$$2x_1^2 + x_2 - 3x_2 =$$

$$25^2 \cdot 3 - 3 \cdot 3 = 141$$

Date \_\_\_ / \_\_\_ / \_\_\_

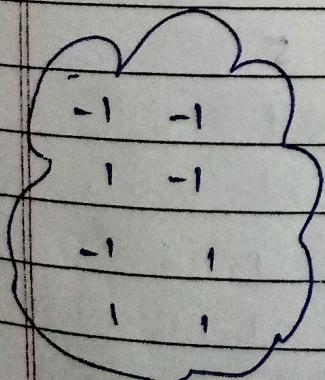
$$\therefore \text{initial temp} = \frac{141 + 375 + 470 + 1280}{4}$$

$$= \frac{2236}{4} = \underline{\underline{559}}$$

(2)

$$z = 3x_1 - x_2^2$$

$$1 \leq x_1, x_2 \leq 3$$



$x_1$	$x_2$	$=$	$z$
-1	-1	=	2
1	-1	=	8
-1	1	=	-6
1	1	=	0

$$\therefore \frac{2 + 8 + (-6) + 0}{4} = \frac{4}{4} = \underline{\underline{1}}$$

Initial Temp is 1

Date \_\_\_ / \_\_\_ / \_\_\_

\* - ACO - May-Jun & Nov-Dec

A = starting station:

what is probab. that ant can choose 1 to 3<sup>rd</sup>  
initial pheromone.

	1	2	3	4	5
distance	1	0	04	16	19
Matrix. =	2	14	0	15	13
	3	16	15	0	11
	4	19	13	11	0
	5	12	10	17	21
					0.

	1	2	3	4	5
pheromon	1	1	1	1	1
men	2	1	1	1	1
deposition	3	1	1	1	1
	4	1	1	1	1
	5	1	1	1	1

efficiency = 1

(d) distance matrix,

	1	2	3	4	5
1	0.00	0.0714	0.0628	0.0526	0.0833 0.8333
2	0.0714	0.00	0.0666	0.0769	0.1
3	0.0628	0.0866	0.00	0.0909	0.0476 0.476
4	0.0526	0.0769	0.0909	0	0.0476 0.476
5	0.0833 0.8333	0.1	0.0769 0.769	0.0476 0.476	0.
			0.0588		

∴ from station 1 to station 3 column will be eliminated. in efficiency matrix.

(Saathi)

Date \_\_\_\_\_ / \_\_\_\_\_ / \_\_\_\_\_

prob. of ant 1's fomation 1:

B	C	D	E	Total -
0.00509	0.00390	0.00276	0.00694 0.00694	= 0.01869
0.2723	(0.2086 : 0.1476)			0.3713

i) 1st Row: Individual =  $(\text{efficiency})^2 * \text{phero}^n \text{ depo}$   
=  $(0.0714)^2 * 1$

ii) 2nd Row: Relative =  $\frac{0.00509}{0.01869}$

% probability of Ant 1 will choose path 1 to 3  
is ~~20~~ 0.2086  
i.e. 20.866%.

→ x → ∵  
Mor dec: same que :

∴ prob of Ant 1 will choose path A to D.  
is 0.1476.  
i.e. 14.76%.

ACO :-

Q.7)

starting station 'A'

Y. prob. of A 1 to 3=?

pheremone level as 1:

⇒.

distance matrix: (d) ..

	1	2	3	4
1	0	32	51	28
2	32	0	43	38
3	51	43	0	49
4	28	38	49	0

pheromone deposition

	1	2	3	4
1	1	1	1	1
2	1	1	1	1
3	1	1	1	1
4	1	1	1	1

efficiency matrix ( $\eta$ ) .

	1	2	3	4
1	0	0.0312	0.0196	0.0357
2	0.0312	0	0.0232	0.0263
3	0.0196	0.0232	0	0.0204
4	0.0357	0.0263	0.0204	0

	2	3	4	Total
(ii)	0.000973	0.000384	0.00127	= <del>0.0026</del>
	0.37137	<u>0.1465</u>	<u>0.4847</u>	

∴ The probability is 0.1465

i.e. 14.65%

Q.8) probability of A to D = ?  
⇒

∴ The probability is. 0.4847..

i.e. 48.47%

Q. 9).

Distance Matrix:

	A	B	C	D
A	0	32	51	28
B	<u>32</u>	0	43	38
C	51	43	0	<u>49</u>
D	28	<u>38</u>	49	0

A - C - D - B - A.

$$A \text{ to } C = 51$$

$$\therefore D = 49,$$

$$D - B = 38$$

$$B - A = 32$$

Total distance travel by ant -

$$51 + 49 + 38 + 32$$

$$= 170.$$

Pheromone deposition by ant 1:-

$$(ΔC) = \frac{1}{170} = 0.00588.$$

Updated pheromone deposition by ant 1.

$$= (1 - r) * t + Δt$$

$$= (1 - 0.5) * 1 + 0.00588.$$

$$= \underline{\underline{0.50588}}.$$

## ACO formulae:-

① Distance Matrix: (known to us).

② pheromone deposition: ( $\tau$ )

(for 1st Itera<sup>n</sup> consider same amount  
of pheromone on all path i.e.  $\frac{1}{n}$ )

③ efficiency matrix =  $\frac{1}{\text{distance}(d)}$  matrix.

④ probability:

i) 1st Row = efficiency<sup>2</sup> \* pheromone depo<sup>n</sup>.

ii) 2nd Row =  $\frac{\text{Individual } (\text{1st Row})}{\text{Individual sum } (\text{1st row sum})}$ .

iii) Total distance: sum

iv) pheromone deposition by ant<sub>i</sub> =  $\frac{1}{(\Delta t) \text{ or } (Dt)} \text{ Total distance}$

v) updated pheromone deposition

$$= (1-r) * t + Dt$$

$\therefore r$  = rate of evaporation (consider 0.5)  
i.e. 50%

$t$  = current pheromone deposition (i.e. 1).

$Dt$  = pheromone deposited by Ant<sub>i</sub>