

**PH3103 Mathematical Methods of Physics**  
**Autumn Semester - 2025**  
Indian Institute of Science Education and Research, Kolkata  
Instructor: Koushik Dutta

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Homework: 5

Submission Date: 8/09/2025

The hand written solutions must be submitted at the start of the class

1. Evaluate the following integral

$$\int_0^\infty \frac{\sin x}{x(x^2 + a^2)}, \quad a > 0. \quad (1)$$

2. Evaluate the following integral

$$I = P \int_{-\infty}^\infty \frac{dw'}{(w' - w)[(w' - w_0)^2 + a^2]} \quad (2)$$

3. Evaluate the following integral

$$\int_0^{2\pi} \frac{d\theta}{a + b \cos 2\theta} \quad (3)$$

4. Evaluate the following integral

$$\int_0^{2\pi} \frac{\cos n\theta \, d\theta}{5 - 4 \cos 2\theta} \quad (4)$$

5. Find the residues at the poles of

$$f(z) = \frac{z^2 + 2}{z^2(z^2 + 1)} \quad (5)$$

$$g(z) = \frac{\cos z}{\sin^2 z} \quad (6)$$