

# Scalar Products

Integer sequence  $a_i$  having length  $2n+2$  is defined as follows:

- $a_0 = 0$
- $a_1 = C$
- $a_{i+2} = (a_{i+1} + a_i) \% M$ , where  $0 \leq i < 2n$

Write a function generator, `gen`, to generate the remaining values for  $a_2$  through  $a_{2n+1}$ . The values returned by `gen` describe two-dimensional vectors  $v_1 \dots v_n$ , where each sequential pair of values describes the respective  $x$  and  $y$  coordinates for some vector  $v$  in the form  $x_1, y_1, x_2, y_2, \dots, x_n, y_n$ . In other words,  $v_1 = (a_2, a_3)$ ,  $v_2 = (a_4, a_5)$ ,  $\dots$ ,  $v_n = (a_{2n}, a_{2n+1})$ .

Let  $S$  be the set of scalar products of  $v_i$  and  $v_j$  for each  $1 \leq i, j \leq n$ , where  $i \neq j$ . Determine the number of different **residues** in  $S$  and print the resulting value modulo  $M$ .

## Input Format

A single line of three space-separated positive integers:  $C$  (the value of  $a_1$ ),  $M$  (the modulus), and  $n$  (the number of two-dimensional vectors), respectively.

## Constraints

- $1 \leq C \leq 10^9$
- $1 \leq M \leq 10^9$
- $1 \leq n \leq 3 \times 10^5$

## Output Format

Print a single integer denoting the number of different residues  $\% M$  in  $S$ .

## Sample Input

4 5 3

## Sample Output

2

## Explanation

Sequence  $a = a_0, a_1, (a_1+a_0)\%M, (a_2+a_1)\%M, \dots, (a_{2n}+a_{2n-1})\%M$   $= \{0, 4, (4+0)\%5, (4+4)\%5, (3+4)\%5, (2+3)\%5, (0+2)\%5, (2+0)\%5\}$   $= \{0, 4, 4, 3, 2, 0, 2, 2\}$ .

This gives us our vectors:  $v_1 = (4, 3)$ ,  $v_2 = (2, 0)$ , and  $v_3 = (2, 2)$ .

- Scalar product  $S_0(v_1,v_2) = 8$ .
- Scalar product  $S_2(v_2,v_3) = 4$ .
- Scalar product  $S_0(v_1,v_3) = 14$ .

There are 2 residues  $\% \ 5$  in  $S$  (i.e.: 3 and 4), so we print the result of  $2 \% 5$  (which is 2).