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**Seminar GIT**

## **Topic 2: Story Maps**

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**Geodesy and Geoinformatics**

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June 23, 2022

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## Contents

<b>1 Hypothese</b>	<b>1</b>
<b>2 Introduction</b>	<b>1</b>
2.1 Simple Choropleth maps . . . . .	1
<b>3 Basic color information</b>	<b>2</b>
3.1 Human' color perception . . . . .	2
3.2 Color models . . . . .	3
<b>4 Criteria</b>	<b>3</b>
4.1 Color distance . . . . .	4
4.1.1 Equation . . . . .	4
4.2 Further aspects . . . . .	6
4.2.1 Number of classes . . . . .	6
4.2.2 Spatial distance . . . . .	7
4.2.3 Brightness of colors . . . . .	7
<b>5 Examples</b>	<b>7</b>
5.1 ColorBrewer2.0 . . . . .	7
5.2 Sequential color scheme generator . . . . .	8
<b>6 Conclusion</b>	<b>9</b>
<b>A Further equation</b>	<b>11</b>

# 1 Hypothese

Die Differenzierbarkeit von Farben beim Betrachten von Choroplethenkarten hängt vorallem von der Farbdistanz zwischen den Farben und der Anzahl der Farbklassen ab.

## 2 Introduction

From a designer's perspective, colors play an essential role in cartography. Nevertheless, according to Brychtová and Çöltekin (2017), there is little research to empirically determine the minimum effective color distance to safely and correctly distinguish cartographic symbols.

The ability to distinguish colors and shades of the same color plays an important role in cartography (Brychtová & Çöltekin, 2017).

Even subtle manipulation of color spacing shows significant effects on the impact on overall readability of a map (Brychtova & Coltekin, 2015; Brychtová & Vondráková, 2014).

Lack of proper visual distance in variables colour hue and colour value is a known contributor to legibility problems in map use tasks (Chesneau, 2007; Steinrücken & Plümer, 2013; Stigmar, 2010).

### 2.1 Simple Choropleth maps

Unlike chorochromatic maps, which visualize nominal (qualitative) data, simple choropleth maps have made it their business to display quantitative data in terms of area. In doing so, hue, saturation and brightness are used to show corresponding changes in the data. Although in theory choropleth maps are only useful for data related to areas (Bollmann et al. 2001), in practice they are also used for non-area related data. E.G. ??? (Hruby, 2016; Schiewe, 2015).

Some advantages of choropleth maps are e.g. the simplified visibility. For this, the data are classified. For example, one can distinguish between an equal interval and a quantile class division. With equal interval each class possesses the same size independently of its occupation, whereas with a quantile class division each class contains the same number of elements.

Depending on the use case and data frequency, one or the other class division is more suitable, because they have a significant influence on the appearance of a map (Rahlf, 2020; Schiewe, 2015).

Due to the public availability of static data, the production of these maps is easy and can be linked, analyzed, classified and visualized with any suitable GIS software (Hruby, 2016).

### **3 Basic color information**

To understand the following chapters it is important to know some basics about human' color perception and color models.

#### **3.1 Human' color perception**

Although our current understanding is that color vision results from the response of three photoreceptor cells in the retina to incident light, their perception cannot be fully understood. This may be due to both individual and environmental factors that influence color perception (Lafer-Sousa et al., 2015; Xiao et al., 2016).

Some of these factors can be, for example, the amount of light in the environment, shadows, surrounding materials, and reflectivity. In addition, the viewer's prior knowledge and cognitive biases play a significant role in color perception (Derefeldt et al., 2004; Foster, 2011).

In addition, there is evidence that the number and distribution of photoreceptors in the eye influences what we see (Roy et al., 1991), and that our brain assumes a particular direction or light source e.g., (Gegenfurtner et al., 2015; Lafer-Sousa et al., 2015).

Thus, it can be said that the color perception of an individual is not stable over space and time. The same is true not only for individuals but also for groups.

Nevertheless, there are many efforts to model and quantify color perception such as mathematical models that attempt to determine thresholds by which two colors or shades of the same color become distinguishable.

This color distance describes a metric that quantifies the human ability to visually distinguish differences between two colors see chapter 4.1 (Brychtová & Çötekin, 2017).

### 3.2 Color models

There are a lot of color models that have set themselves the task of representing the logic of generating colors (Kuehni, 2001). These color models can be divided into four main groups: instrumental, pseudo-perceptual, colorimetric, and perceptual unitary color models.

In the majority of times we define colors by three RGB values which define the amount of red, green and blue color which combined forms a unique color. Such a color models are called Instrumental color models another example would be the CYMK Model which is used by printers. Pseudoperceptual color models are e.g. HVS or HSB, whereas colorimetric color models are represented e.g. by CIE 1931 XYZ. To the latter model (perceptually uniform) belong for example the Munsell system, CIELAB or CIELUV. Such color models tries to make a color model on how human eyes percept the colors. This will be important when calculating a distance between colors how humans see the colors. When calculating the color distance all color models will play its role except the pseudoreceptual color models.

A color space is understood to be all existing colors that can be represented e.g. by a screen, printer or the human eye, which are generated from a combination of the components of a model (Munsell, Nickerson, et al., 1915). Color spaces are also important cause it is important to know that mediums are limited in the colors they can visualize. When creating a map it should be the goal that the colors used can be visualized by the medium where the map will be shown.

## 4 Criteria

In the following chapter critirias will be introduced which affects how humans differentiate colors on a choropletic map. This is mainly affected by the color distance but there are also other aspects which can create difficulties when reading the colors of a map.

## 4.1 Color distance

Visual distance in cartography is understood as a measurement of differences between visual variables such as size, shape and orientation (Brychtová, 2015). Here we focus on the variable of color hue and color value. The human perceived difference between two colors or color shades can be described as the color distance. In other words, certain change of colour in the perceptually uniform space produces equal change in human perception of that colour (Brychtová & Çöltekin, 2017).

To describe the distance of two colors scientists have developed a method to describe the color distance. To express color quantitatively a colour space corresponding to the human perception is needed. Such color spaces are called perceptually uniform or linear. The use of such color spaces try to ensure results of color distance which are proportional to the human perception (Brychtová, 2015). Presently the CIEDE2000 model ( $\Delta E_{00}$ , equation defined in Brychtová (2015)) is regarded as the best coinciding color distance model with visual perception.

The colors of digital maps are usually represented in the RGB color space, since the colors on most, if not all, digital screens are generated with these three colors (red, green, blue). However RGB values do not lead to specific color if they are not related to an absolute color space such as sRGB, Adobe RGB or ProPhoto RGB. To use the most realistic color space, colors should be specified and selected in the sRGB color space in the initial situation. Why most realistic? As mentioned before sRGB is the smallest color space of the three. The vast majority of digital screens cannot create all Adobe RGB or even ProPhoto RGB colors. Even sRGB isn't fully supported by cheap laptop screens. However sRGB is known as the default color space (KenRockwell.com, 2006). Therefore sRGB should be chosen to increase the chance that the users screen actually is able to display the color which was chosen by the creator of a map.

### 4.1.1 Equation

The first step to calculate the color distance  $\Delta E_{00}$  is the transformation from the original color space (as mentioned above this would be sRGB in most cases) to the CIE 1931 XYZ color space (see equations 4.1 and 4.2). For that the RGB values have to be normalized so the values lie in the interval [0; 1].

$$R_{lin} = G_{lin} = B_{lin} = \begin{cases} \frac{V_{R,G,B}}{12.92}, & \text{if } V_{R,G,B} \leq 0.04045 \\ \sqrt[5]{\left(\frac{R+0.055}{1+0.055}\right)^{12}}, & \text{otherwise} \end{cases} \quad (4.1)$$

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 0.4124 & 0.3576 & 0.1805 \\ 0.2126 & 0.7152 & 0.0722 \\ 0.0193 & 0.1192 & 0.9505 \end{bmatrix} \begin{bmatrix} R_{lin} \\ G_{lin} \\ B_{lin} \end{bmatrix} \quad (4.2)$$

The second step is the transformation of the colors into CIE Lab (see equations 4.3 - 4.6). The CIELAB Colorspace, also known as CIE 1976 ( $L^*$ ,  $a^*$ ,  $b^*$ ) describes all colors perceptible by human eyes (Levkowitz, 1997). It consists of three components:  $L$  describes the brightness [0 - 100],  $a$  describes the axis between red and green and  $b$  describes the axis of the blue and yellow colors. While negative values stand for green/blue colors and positive values for magenta and yellow). Theoretically the  $a$  and  $b$  values are not limited but in praxis human eyes can only see colors upin a specific value.

$$L = 116f\left(\frac{Y}{Y_n}\right) - 16 \quad (4.3)$$

$$a = 500 \left[ f\left(\frac{X}{X_n}\right) - f\left(\frac{Y}{Y_n}\right) \right] \quad (4.4)$$

$$b = 200 \left[ f\left(\frac{Y}{Y_n}\right) - f\left(\frac{Z}{Z_n}\right) \right] \quad (4.5)$$

where

$$f(t) = \begin{cases} \sqrt[3]{t}, & \text{if } t > \left(\frac{6}{29}\right)^3 \\ \frac{1}{3}\left(\frac{29}{6}\right)^3 t + \frac{4}{29}, & \text{otherwise} \end{cases} \quad (4.6)$$

Finally the last step is to calculate the color distance  $\Delta E_{00}$  between two colors with the CIEDE2000 model (see equation 4.7).

$$\Delta E_{00} = \sqrt{\left(\frac{\Delta L'}{k_L S_L}\right)^2 + \left(\frac{\Delta C'}{k_C S_C}\right)^2 + \left(\frac{\Delta H'}{k_H S_H}\right)^2 + R_T \frac{\Delta C'}{k_C S_C} \frac{\Delta H'}{k_H S_H}} \quad (4.7)$$

where  $\Delta L'$ ,  $\Delta C'$  and  $\Delta H'$  are the CIELAB metric lightness, chroma, and hue differences, calculated between the standard and sample in a pair and  $S_L$ ,  $S_C$  and  $S_H$  are the weighting functions for the lightness, chroma, and hue components. However, since the formulas are quite extensive, the equations can be read in the appendix A. The  $k_L$ ,  $k_C$  and  $k_H$  values are the



parametric factors to be adjusted according to different viewing parameters such as textures, backgrounds, separations etc. (Luo et al., 2001).

## 4.2 Further aspects

While the color distance of course has the biggest impact on human ability to differentiate colors there are some other aspects which play a role.

### 4.2.1 Number of classes

Obviously the number of classes also has an impact on the differentiability of colors. For example if we reduce the number of classes to 1 (which makes no sense in practice) the color will be determined in hopefully all cases. The more classes we create, the harder it becomes to tell the colors apart as the probability decreases. In addition to that it is clear that the color distance decreases with more classes as the number of color shades are limited by the color space.

Brychtová and Çöltekin (2017) makes the finding that with ColorBrewer 2.0 the color distance becomes smaller the more classes are used, which is to be expected. For the selected 18 sequential schemes, the color distance was analyzed and calculated between 3, 6 and 9 classes. These numbers of classes were selected according to Brychtová and Çöltekin (2017), since they represent the minimum, maximum and middle of the class selection. Thus, the results (see table 4.1) show that the number of classes have an influence on how the distance of the colors is chosen and thus becomes distinguishable to the human eye.

**Table 4.1** Color distance depending on number of classes  
(According to Brychtová and Çöltekin (2017))

Number of classes	$\Delta E_{00min}$	$\Delta E_{00max}$	$\Delta E_{00mean}$
3	11.26	33.92	20.61
6	6.24	26.44	12.41
9	3.04	20.46	10.28

### 4.2.2 Spatial distance

The greater the spatial distance between two color cells, the more the ability to distinguish the colors decreases. This is true for both sequential and qualitative schemes. However, at a color distance of  $\Delta E_{00} = 10$ , the accuracy of color discrimination increases, even at relatively large spatial distances (Brychtová & Çöltekin, 2017).

### 4.2.3 Brightness of colors

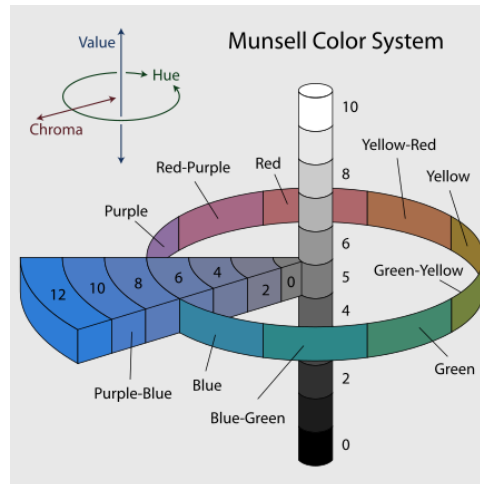
An evaluating case study of color distances in ColorBrewer 2.0 from Brychtová and Çöltekin (2017) has investigated the color distances in 18 color schemes made by colorBrewer 2.0. All color schemes were investigated with 9, 6 and 3 classes. As a result Brychtová and Çöltekin (2017) figured out that mostly the darker the color becomes, the larger the color distance becomes. Therefore it can be assumed that the developers of ColorBrewer 2.0 came to the result that darker colors need a larger color distance to correctly determine a difference between colors. Color schemes with 9 classes show their largest color distances in the darker middle colors.

Bild einfügen.

## 5 Examples

### 5.1 ColorBrewer2.0

Brewer and her colleagues (Brewer, 1994, 1996, 1997; Brewer et al., 1999; Brewer et al., 2003) did research on color, developing color schemes to visualize both quantitative and qualitative data. In the process, the online software ColorBrewer 2.0 was developed, which can be very helpful for many applications. ColorBrewer 2.0 offers the user a choice between 18 sequential, 9 divergent and 8 qualitative color schemes. Depending on the selection, a distinction can be made between 3 and 12 classes. They used Munsell diagrams to design color schemes that would maintain consistency in perceived color distances between classes (Brychtová & Çöltekin, 2017).



**Figure 5.1** Munsell Color System

(Source: Rus (2007))

The Munsell Color System is a color system that is the first complete, most widely used, and still in use today. It is based on three essential criteria: Hue, Chroma and Value, with Hue being the most important criterion (5.1). Munsell chose five main hues: red (R), yellow (Y), green (G), blue (B) and purple (P). Now he subdivides the perceptible color nuances into further color tones, which are to represent the intermediate color tones: YR (yellow-red), GY (green-yellow), BG (blue-green), PB (purple-blue) and RP (red-purple). These ten hues are further subdivided a few times into ten gradations. Numbers from 0 to 10 are also added to the hues. Towards the outside, the saturation of the color (chroma) increases. The vertical center axis, which ranges from white (value 10) to black (value 0), which can be represented with colorants, is represented by the value. This results in a 10-row gray scale (Munsell, Nickerson, et al., 1915).

## 5.2 Sequential color scheme generator

To develop a suitable sequential color scheme, the analytical geometry is calculated. The intersection of two subspaces is searched for. This is the intersection of the CIELAB color space and a straight line on which the color scheme lies.

For this we look which color tones lie on the straight line. This follows at given distances defined with CIEDE2000.

It must be kept in mind that this method is only suitable for the creation of schemata that are to

be used for digital maps. Therefore its construction is limited by the sRGB color space.

This method shows a reverse approach to design color schemes based on the color distance as described in chapter 4.1.1 (Brychtová & Çöltekin, 2017). The online tool Color Scheme Generator 1.0 has implemented this software (freely available at: <http://eyetracking.upol.cz/color>).

The user of this online tool can display a color scheme by selecting a base color of the whole scheme, the color classes and the CIEDE2000 color distances between the classes (Brychtová & Doležalová, 2015)

## 6 Conclusion

Colors which can not be differentiated correctly and quickly are a main problem when reading choroplethic maps. It can lead to errors when it comes to understanding and interpreting the map. Therefore the selection of colors should be done wisely.

The perception of colors by human eyes is not stable, it is affected by environment light, shadows and surrounding materials. In addition the color perception differs from human to human and also changes with time. Extrem examples of course are colorblind people.

Irgendwas über color spaces.

It can be concluded, that the ability to differentiate colors on a choroplethic map is mainly affected by the color distance. The color distance is a measure to quantify the difference of two colors or shades of a color from the perspective of an human eye. Another aspect which is closely connected to the color distance is the number of classes. Since the colors are limited by the color space sRGB the color distances are likely to become smaller when choosing more classes. In addition to that the spatial distance between two colors also has an impact how precisely humans can differentiate the colors. Brychtová and Çöltekin (2017) has figured out that the color schemes at the well known software ColorBrewer 2.0 tend to have wider color distances at dark colors, which is an indicator that darker colors are more difficult to differentiate. A thesis which could be evaluated further also with the ulterior motive that the calculation of the color distance does consider the brightness of the color.

Examples for useful software when selection color schemes and specific colors for choropletic

maps are ColorBrewer 2.0 and Sequential Color Scheme Generator. Last one is definatly a tool for map creators with previous knowledge about color distance.

Der Farbabstand (eine von der International Commission on Illumination zur Quantifizierung der menschlichen Fähigkeit, zwischen Farben zu unterscheiden) wurde empirisch nachgewiesen, dass er ein wichtiger Faktor für die Lesbarkeit von Karten insgesamt ist (z. B. Brychtova und Coltekin 2015, Brychtova 2015, Brychtova und Coltekin 2014, Brychtova und Vondrakova 2014). Unzureichender Farbabstand zwischen kartografischen Symbolen beeinträchtigt die Fähigkeit der Kartennutzer, die und Interpretation der visualisierten räumlichen Informationen. (Brychtova & Doležalová, 2015)

## A Further equation

$$C_{1,ab} = \sqrt{(a_1)^2 + (b_1)^2} \quad C_{2,ab} = \sqrt{(a_2)^2 + (b_2)^2} \quad (\text{A.1})$$

$$\bar{C}_{ab} = \frac{C_{1,ab} + C_{2,ab}}{2} \quad (\text{A.2})$$

$$G = 0.5 \left( 1 - \sqrt{\frac{\bar{C}_{ab}^7}{\bar{C}_{ab}^7 + 25^7}} \right) \quad (\text{A.3})$$

$$a'_1 = (1 + G)a_1 \quad a'_2 = (1 + G)a_2 \quad (\text{A.4})$$

$$C'_1 = \sqrt{(a'_1)^2 + (b_1)^2} \quad C'_2 = \sqrt{(a'_2)^2 + (b_2)^2} \quad (\text{A.5})$$

$$h'_1 = \arctan 2(b_1, a'_1) = \begin{cases} \tan^{-1}\left(\frac{b_1}{a'_1}\right), & b_1 > 0, a'_1 \geq 0 \\ \tan^{-1}\left(\frac{b_1}{a'_1}\right) + 180^\circ, & b_1 < 0 \\ \tan^{-1}\left(\frac{b_1}{a'_1}\right) + 360^\circ, & b_1 > 0, a'_1 < 0 \\ 90^\circ, & b_1 = 0, a'_1 > 0 \\ 270^\circ, & b_1 = 0, a'_1 < 0 \\ 0^\circ, & b_1 = 0, a'_1 = 0 \end{cases} \quad (\text{A.6})$$

$$h'_2 = \arctan 2(b_2, a'_2) = \begin{cases} \tan^{-1}\left(\frac{b_2}{a'_2}\right), & b_2 > 0, a'_2 \geq 0 \\ \tan^{-1}\left(\frac{b_2}{a'_2}\right) + 180^\circ, & b_2 < 0 \\ \tan^{-1}\left(\frac{b_2}{a'_2}\right) + 360^\circ, & b_2 > 0, a'_2 < 0 \\ 90^\circ, & b_2 = 0, a'_2 > 0 \\ 270^\circ, & b_2 = 0, a'_2 < 0 \\ 0^\circ, & b_2 = 0, a'_2 = 0 \end{cases} \quad (\text{A.7})$$

$$\Delta L' = L_2 - L_1 \quad (\text{A.8})$$

$$\Delta C' = C'_2 - C'_1 \quad (\text{A.9})$$

$$\Delta h' = \begin{cases} 0, & C'_1 C'_2 = 0 \\ h'_2 - h'_1, & C'_1 C'_2 \neq 0, |h'_2 - h'_1| \leq -180^\circ \\ (h'_2 - h'_1) - 360^\circ, & C'_1 C'_2 \neq 0, (h'_2 - h'_1) > -180^\circ \\ (h'_2 - h'_1) + 360^\circ, & C'_1 C'_2 \neq 0, (h'_2 - h'_1) < -180^\circ \end{cases} \quad (\text{A.10})$$

$$\Delta H' = 2\sqrt{C'_1 C'_2} \sin\left(\frac{\Delta h'}{2}\right) \quad (\text{A.11})$$

$$\bar{L}' = \frac{L_1 + L_2}{2} \quad (\text{A.12})$$

$$\bar{C}' = \frac{C'_1 + C'_2}{2} \quad (\text{A.13})$$

$$\bar{h}' = \begin{cases} \frac{h'_1 + h'_2}{2}, & C'_1 C'_2 \neq 0 \wedge |h'_2 - h'_1| \leq 180^\circ \\ \frac{h'_1 + h'_2 + 360^\circ}{2}, & |h'_2 - h'_1| > 180^\circ \wedge (h'_2 - h'_1) < 180^\circ \\ \frac{h'_1 + h'_2 - 360^\circ}{2}, & |h'_2 - h'_1| > 180^\circ \wedge (h'_2 - h'_1) \geq 360^\circ \\ h'_1 + h'_2, & C'_1 C'_2 = 0 \end{cases} \quad (\text{A.14})$$

$$T = 1 - 0.17 \cos(\bar{h}' - 30^\circ) + 0.24 \cos(2\bar{h}') + 0.32 \cos(3\bar{h}' + 6^\circ) - 0.2 \cos(4\bar{h}' - 63^\circ) \quad (\text{A.15})$$

$$\Delta 0 = 30e^{-(\frac{h' - 275^\circ}{25})^2} \quad (\text{A.16})$$

$$R_c = 2\sqrt{\frac{\bar{C}'_{ab}{}^7}{\bar{C}'_{ab}{}^7 + 25^7}} \quad (\text{A.17})$$

$$S_L = 1 + \frac{0.015(\bar{L}' - 50)^2}{\sqrt{20 + (\bar{L}' - 50)^2}} \quad (\text{A.18})$$

$$S_C = 1 + 0.0045\bar{C}' \quad (\text{A.19})$$

$$S_H = 1 + 0.0045\bar{C}'T \quad (\text{A.20})$$

$$R_T = -\sin(2\Delta\theta)R_c \quad (\text{A.21})$$