

NumPy Universal Functions

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NumPy Universal Functions Introduction

What are Universal Functions in NumPy?

Universal Functions, commonly called **ufuncs**, are **special NumPy functions** that work **element-by-element** on NumPy arrays.

They allow you to perform **fast mathematical and logical operations** without using loops.

Why are ufuncs important?

Universal functions are important because they:

- Work **much faster** than normal Python loops
 - Support **array operations directly**
 - Automatically handle **broadcasting**
 - Use **less memory**
 - Are perfect for **data analysis and scientific computing**
-

Key Features of NumPy ufuncs

1. **Element-wise operation**
Each element is processed independently.
2. **High performance**
Implemented in C, so execution is very fast.
3. **Broadcasting support**
Can operate on arrays of different shapes.
4. **Vectorized code**
No need for for loops.

NumPy Universal Functions – Creating a Custom ufunc

In NumPy, apart from using built-in universal functions, we can also **create our own Universal Function (ufunc)**. A **custom ufunc** allows a user-defined Python function to behave like a NumPy ufunc, meaning it will work **element-by-element on arrays** and support vectorized operations.

To create a universal function in NumPy, we use the **np.frompyfunc()** method. This method converts a normal Python function into a NumPy ufunc.

Why Create a Custom ufunc?

Creating a custom ufunc is useful when:

- A required operation is **not available** in built-in ufuncs
 - The same logic must be applied to **every array element**
 - You want **clean and reusable** array-based code
-

Syntax to Create a ufunc

```
np.frompyfunc(function, input_count, output_count)
```

Parameters:

- **function** → Normal Python function
 - **input_count** → Number of input arguments
 - **output_count** → Number of values returned
-

Example: Creating a Custom Universal Function

Step 1: Define a normal Python function

```
def square(x):  
  
    return x * x
```

Step 2: Convert it into a NumPy ufunc

```
import numpy as np

square_ufunc = np.frompyfunc(square, 1, 1)
```

Step 3: Apply it to a NumPy array

```
arr = np.array([1, 2, 3, 4, 5])

result = square_ufunc(arr)

print(result)
```

Output:

```
[1 4 9 16 25]
```

The function is automatically applied to **each element** of the array.

Example 2: Custom ufunc with Two Inputs

```
def add_numbers(a, b):

    return a + b

add_ufunc = np.frompyfunc(add_numbers, 2, 1)

x = np.array([1, 2, 3])

y = np.array([10, 20, 30])

print(add_ufunc(x, y))
```

Output:

```
[11 22 33]
```

NumPy Universal Functions – Simple Arithmetic

In NumPy, **Universal Functions (ufuncs)** are used to perform **simple arithmetic operations** directly on arrays. These functions apply the operation **element by element**, which means the same calculation is automatically performed on every value in the array.

Simple arithmetic ufuncs remove the need for loops and make calculations **faster, cleaner, and more efficient**. They are commonly used in data analysis and numerical computing.

Common Simple Arithmetic Universal Functions

1. Addition (`np.add`)

Adds elements of two arrays.

```
import numpy as np
```

```
a = np.array([2, 4, 6])
```

```
b = np.array([1, 3, 5])
```

```
result = np.add(a, b)
```

```
print(result)
```

Output:

```
[3 7 11]
```

2. Subtraction (`np.subtract`)

Subtracts elements of one array from another.

```
x = np.array([10, 20, 30])
```

```
y = np.array([2, 5, 10])  
  
result = np.subtract(x, y)  
  
print(result)
```

Output:

```
[ 8 15 20]
```

3. Multiplication (np.multiply)

Multiplies corresponding elements of arrays.

```
m = np.array([2, 3, 4])  
  
n = np.array([5, 6, 7])  
  
result = np.multiply(m, n)  
  
print(result)
```

Output:

```
[10 18 28]
```

4. Division (np.divide)

Divides elements of one array by another.

```
p = np.array([20, 40, 60])  
  
q = np.array([2, 4, 5])  
  
result = np.divide(p, q)  
  
print(result)
```

Output:

```
[10. 10. 12.]
```

5. Power (np.power)

Raises elements of one array to the power of another.

```
base = np.array([2, 3, 4])
```

```
exp = np.array([3, 2, 2])
```

```
result = np.power(base, exp)
```

```
print(result)
```

Output:

```
[ 8  9 16]
```

NumPy Universal Functions (Ufuncs) – Rounding Decimals

What are Universal Functions (Ufuncs)?

NumPy **Universal Functions (ufuncs)** are built-in functions that work **element-wise** on NumPy arrays.

They are:

- Very fast
- Easy to use
- Applied to each value in an array automatically

Rounding functions are a special type of ufunc used to **round decimal numbers**.

Why Rounding Decimals is Important?

In data analysis:

- We round prices, percentages, and averages
- We clean noisy decimal values
- We make data more readable in reports

Example:

Original value: 23.678945

Rounded value : 23.68

NumPy Rounding Decimal Functions

np.around() / np.round()

Rounds numbers to a specified number of decimal places.

Syntax:

```
np.around(array, decimals)
```

Example:

```
import numpy as np

data = np.array([12.345, 67.891, 45.567, 89.999])

rounded = np.around(data, 2)

print(rounded)
```

Output:

```
[12.35 67.89 45.57 90. ]
```

✓ Rounds each value to **2 decimal places**

np.round() (same as np.around)

`np.round(data, 1)`

✓ Works exactly like `around()`

Rounding Without Decimals (Whole Numbers)

np.floor()

Rounds **down** to the nearest integer.

Example:

```
values = np.array([4.7, 2.3, 9.9, 5.1])
```

```
print(np.floor(values))
```

Output:

```
[4. 2. 9. 5.]
```

✓ Always rounds **down**

np.ceil()

Rounds **up** to the nearest integer.

```
print(np.ceil(values))
```

Output:

```
[5. 3. 10. 6.]
```

✓ Always rounds **up**

np.trunc()

Removes decimal part (no rounding).

```
print(np.trunc(values))
```

Output:

```
[4. 2. 9. 5.]
```

✓ Just **cuts** the decimal part

Difference Between Rounding Functions

Function	Behavior	Example (4.7)
round	Normal rounding	5
floor	Always down	4
ceil	Always up	5
trunc	Remove decimal	4

Real-Life Example (Marks Data)

```
marks = np.array([78.456, 89.123, 67.999, 92.555])
```

```
final_marks = np.round(marks, 1)
```

```
print(final_marks)
```

Output:

```
[78.5 89.1 68. 92.6]
```

NumPy Universal Functions (Ufuncs) – Logarithmic Functions

What are Logarithmic Functions?

A **logarithm** answers the question:

“Power kitni hai?”

If

[

$$a^x = b$$

]

then

[

$$\log_a(b) = x$$

]

In data science, logarithms are used to:

- Reduce very large values
- Handle exponential growth
- Normalize skewed data
- Improve model performance

NumPy provides **logarithmic ufuncs** that work **element-wise** on arrays.

Why NumPy Log Ufuncs?

- ✓ Very fast
 - ✓ No loops required
 - ✓ Apply automatically to each element
 - ✓ Widely used in data analysis & ML
-

Types of Logarithmic Functions in NumPy

np.log() – Natural Log (Base e)

Definition:

Natural logarithm where base **e** ≈ 2.718

Syntax:

```
np.log(array)
```

Example:

```
import numpy as np
```

```
data = np.array([1, 2, 4, 10])
```

```
result = np.log(data)
```

```
print(result)
```

Output:

```
[0.         0.69314718 1.38629436 2.30258509]
```

✓ Used in **machine learning, statistics, growth rate analysis**

np.log10() – Log Base 10

Syntax:

```
np.log10(array)
```

Example:

```
values = np.array([1, 10, 100, 1000])
```

```
print(np.log10(values))
```

Output:

```
[0. 1. 2. 3.]
```

✓ Common in:

- Scientific calculations
 - Earthquake scale
 - Sound intensity (decibel)
-

np.log2() – Log Base 2**Syntax:**

```
np.log2(array)
```

Example:

```
nums = np.array([1, 2, 4, 8, 16])
```

```
print(np.log2(nums))
```

Output:

```
[0. 1. 2. 3. 4.]
```

✓ Used in:

- Computer science
 - Binary systems
 - Data compression
-

Comparison of Log Functions

Function	Base	Example Input	Output
----------	------	---------------	--------

np.log()	e	10	2.302
----------	---	----	-------

np.log10()	10	100	2
------------	----	-----	---

np.log2()	2	8	3
-----------	---	---	---

Log of Zero & Negative Numbers

```
arr = np.array([1, 0, -5])
```

```
print(np.log(arr))
```

Output:

```
[0. -inf nan]
```

Explanation:

- $\log(0) \rightarrow -\text{inf}$
- $\log(\text{negative}) \rightarrow \text{nan}$ (Not a Number)

✓ Always clean data before applying logs

Real-Life Example – Sales Data Normalization

```
sales = np.array([100, 500, 2000, 10000])
```

```
log_sales = np.log10(sales)
```

```
print(log_sales)
```

Output:

```
[2. 2.69897 3.30103 4. ]
```

✓ Helps reduce **data skewness**

Log with Custom Base (Formula Method)

NumPy does not directly provide custom base log, but we use:

```
[  
\log_b(x) = \frac{\log(x)}{\log(b)}  
]
```

Example:

```
x = np.array([8, 16, 32])
```

```
base = 2
```

```
custom_log = np.log(x) / np.log(base)
```

```
print(custom_log)
```

Output:

```
[3. 4. 5.]
```

NumPy Universal Functions (Ufuncs) – Products

What is Product in NumPy?

Product means multiplying numbers together.

In NumPy, product-related operations are handled using **universal functions (ufuncs)** and fast aggregation functions that:

- Work **element-wise**
 - Are **high-performance**
 - Easily handle **1D, 2D, and multi-dimensional arrays**
-

Why Use NumPy for Product Operations?

- ✓ Faster than Python loops
 - ✓ Cleaner and shorter code
 - ✓ Works directly on arrays
 - ✓ Very useful in statistics & data analysis
-

Important NumPy Product Functions

np.prod() – Product of All Elements

Syntax:

```
np.prod(array)
```

Example (1D Array):

```
import numpy as np
```

```
data = np.array([2, 3, 4])
```

```
result = np.prod(data)
```

```
print(result)
```


Output:

24

✓ Calculation: $2 \times 3 \times 4 = 24$

Product in 2D Array

```
matrix = np.array([[1, 2],  
                  [3, 4]])
```

```
print(np.prod(matrix))
```

Output:

24

✓ Multiplies **all values**

axis Parameter in Product ★**a) Column-wise Product (axis=0)**

```
print(np.prod(matrix, axis=0))
```

Output:

[3 8]

✓ Calculation:

Column 1 $\rightarrow 1 \times 3 = 3$

Column 2 $\rightarrow 2 \times 4 = 8$

b) Row-wise Product (axis=1)

```
print(np.prod(matrix, axis=1))
```

Output:

```
[2 12]
```

✓ Row 1 $\rightarrow 1 \times 2 = 2$

✓ Row 2 $\rightarrow 3 \times 4 = 12$

Visual Meaning of Axis

Axis Operation

axis = 0 Column-wise

axis = 1 Row-wise

np.multiply() – Element-wise Multiplication (Ufunc)

Syntax:

```
np.multiply(array1, array2)
```

Example:

```
a = np.array([2, 4, 6])
```

```
b = np.array([3, 5, 7])
```

```
print(np.multiply(a, b))
```

Output:

```
[ 6 20 42 ]
```

✓ Multiplies corresponding elements

Broadcasting Example

```
arr = np.array([1, 2, 3])  
print(np.multiply(arr, 2))
```

Output:

```
[2 4 6]
```

✓ Multiplies each element by 2

Cumulative Product – np.cumprod()

Definition:

Each element is the product of previous elements.

```
values = np.array([2, 3, 4])  
print(np.cumprod(values))
```

Output:

```
[ 2  6 24]
```

✓ Useful for:

- Growth calculation
 - Compound interest
 - Probability chains
-

np.nanprod() – Ignore NaN Values

```
arr = np.array([2, 3, np.nan, 4])
```

```
print(np.nanprod(arr))
```

Output:

24.0

✓ Ignores missing values (NaN)

Real-Life Example – Stock Growth Factor

```
growth = np.array([1.05, 1.10, 0.95])
```

```
total_growth = np.prod(growth)
```

```
print(total_growth)
```

Output:

1.09725

✓ Shows total growth after multiple periods

Difference Between prod() and multiply()

Function	Purpose
np.prod()	Multiplies all elements
np.multiply()	Element-wise multiplication

NumPy Universal Functions (Ufuncs) – Differences

What is “Difference” in NumPy?

Difference means finding how much a value has **changed** compared to another value.

In NumPy, “differences” are commonly used to:

- Measure **change** between consecutive values
- Analyze **trends** in time-series data
- Calculate **increments / decrements**
- Detect sudden jumps or drops in data

NumPy provides fast functions (built on ufuncs) to compute differences **without loops**.

Why Use NumPy Difference Functions?

- ✓ Very fast
 - ✓ Simple syntax
 - ✓ Works on arrays directly
 - ✓ Perfect for data analysis & statistics
-

Main NumPy Function for Differences

`np.diff()` – Difference Between Consecutive Elements

Definition:

`np.diff()` calculates the difference between **adjacent elements**.

Formula:

```
[  
 \text{diff}[i] = a[i+1] - a[i]  
]
```

Syntax:

```
np.diff(array)
```

Example (1D Array):

```
import numpy as np
```

```
data = np.array([10, 15, 25, 40])
```

```
result = np.diff(data)
```

```
print(result)
```

Output:

```
[ 5 10 15]
```

✓ Calculations:

- $15 - 10 = 5$
 - $25 - 15 = 10$
 - $40 - 25 = 15$
-

Length Change Rule ⚠

If array length is **n**, the result length is **n - 1**

Difference in 2D Arrays

```
matrix = np.array([[1, 4, 9],  
                  [2, 6, 12]])
```

```
print(np.diff(matrix))
```

Output:

```
[[3 5]
```

```
[4 6]]
```

✓ Difference is calculated **row-wise** by default

Using axis in np.diff()

a) Row-wise Difference (axis=1) – Default

```
np.diff(matrix, axis=1)
```

✓ Difference across columns

b) Column-wise Difference (axis=0)

```
np.diff(matrix, axis=0)
```

Output:

```
[[1 2 3]]
```

✓ Calculates difference between rows

Visual Understanding of Axis

Axis Meaning

axis = 0 Vertical (between rows)

axis = 1 Horizontal (between columns)

Higher Order Differences (Second Difference)

Definition:

Difference of differences

```
values = np.array([2, 5, 10, 17])
```

```
print(np.diff(values, n=2))
```

Output:

```
[2 2]
```

✓ Used in:

- Polynomial trend analysis
 - Acceleration calculation
-

Difference vs Subtraction (np.subtract())

Element-wise Subtraction:

```
a = np.array([20, 30, 40])
```

```
b = np.array([5, 10, 15])
```



```
print(np.subtract(a, b))
```

Output:

```
[15 20 25]
```

✓ np.subtract() subtracts **corresponding elements**

Key Difference Table

Function	Purpose
np.diff()	Difference between consecutive values
np.subtract()	Element-wise subtraction

Real-Life Example – Daily Sales Change

```
sales = np.array([100, 120, 115, 140, 160])
```

```
daily_change = np.diff(sales)
```

```
print(daily_change)
```

Output:

```
[ 20 -5 25 20]
```

✓ Shows daily increase or decrease in sales

Handling Negative Differences

Negative values mean:

- Decrease

- Drop in data

✓ Very useful for trend analysis

NumPy Universal Functions – Finding LCM (Least Common Multiple)

What is LCM?

LCM (Least Common Multiple) of two or more numbers is the **smallest positive number** that is **divisible by all the given numbers**.

Example (Math Concept)

- LCM of **4 and 6**
 - Multiples of 4 → 4, 8, 12, 16, ...
 - Multiples of 6 → 6, 12, 18, ...
 - Common smallest multiple → **12**
- So, **LCM = 12**

What is NumPy LCM ufunc?

NumPy provides a **universal function** called:

`np.lcm()`

It calculates the **LCM element-wise** for arrays or between numbers.

Being a **ufunc**, it is:

- Fast

- Vectorized
 - Works on arrays without loops
-

Syntax

`numpy.lcm(x, y)`

Parameters:

- `x` → first number or array
- `y` → second number or array

Returns:

- LCM of `x` and `y`
-

Example 1: LCM of Two Numbers

```
import numpy as np
```

```
result = np.lcm(6, 8)
```

```
print(result)
```

Output:

```
24
```

Explanation:

- Multiples of 6 → 6, 12, 18, 24
 - Multiples of 8 → 8, 16, 24
 - Smallest common multiple → **24**
-

Example 2: LCM of Two Arrays

```
import numpy as np
```

```
a = np.array([2, 4, 6])
```

```
b = np.array([3, 5, 9])
```

```
result = np.lcm(a, b)
```

```
print(result)
```

Output:

```
[ 6 20 18 ]
```

Explanation:

a b LCM

```
2 3 6
```

```
4 5 20
```

```
6 9 18
```

Each element is calculated **pair-wise**.

Example 3: LCM of Array and Single Number

```
import numpy as np
```

```
arr = np.array([4, 5, 6])
```

```
result = np.lcm(arr, 10)
```

```
print(result)
```

Output:

```
[20 10 30]
```

Explanation:

- $\text{LCM}(4,10) = 20$
 - $\text{LCM}(5,10) = 10$
 - $\text{LCM}(6,10) = 30$
-

Example 4: LCM Using Multiple Values (Step by Step)

To find LCM of more than two numbers:

```
import numpy as np
```

```
from functools import reduce
```

```
numbers = np.array([4, 6, 8])
```

```
lcm_result = reduce(np.lcm, numbers)
```

```
print(lcm_result)
```

Output:

```
24
```

✓ Explanation:

- $\text{LCM}(4,6) = 12$
 - $\text{LCM}(12,8) = 24$
-

Example 5: LCM in 2D Array

```
import numpy as np

a = np.array([[2, 3], [4, 5]])
b = np.array([[6, 9], [10, 15]])
```

```
result = np.lcm(a, b)

print(result)
```

Output:

```
[[ 6  9]
 [20 15]]
```

NumPy Universal Functions – Finding GCD

Full form :- (Greatest Common Divisor)

What is GCD?

GCD (Greatest Common Divisor) is the **largest positive number** that divides **two or more numbers exactly**, without leaving any remainder.

Simple Math Example

- Numbers: **18 and 24**

- Factors of 18 → 1, 2, 3, 6, 9, 18
- Factors of 24 → 1, 2, 3, 4, 6, 8, 12, 24
- Largest common factor → **6**

GCD = 6

What is NumPy GCD ufunc?

NumPy provides a **Universal Function (ufunc)** called:

`np.gcd()`

It calculates the **GCD element-by-element** for numbers or arrays.

Why is it a ufunc?

- Works on arrays automatically
 - No need for loops
 - Fast and optimized
 - Handles large datasets easily
-

Syntax

`numpy.gcd(x, y)`

Parameters:

- `x` → first number or array
- `y` → second number or array

Returns:

- GCD of `x` and `y`
-

Example 1: GCD of Two Numbers

```
import numpy as np
```

```
result = np.gcd(20, 30)
```

```
print(result)
```

Output:

10

Explanation:

- Common divisors → 1, 2, 5, 10
 - Greatest one → **10**
-

Example 2: GCD of Two Arrays

```
import numpy as np
```

```
a = np.array([12, 18, 24])
```

```
b = np.array([6, 12, 36])
```

```
result = np.gcd(a, b)
```

```
print(result)
```

Output:

[6 6 12]

Explanation:

a b GCD

12 6 6

18 12 6

24 36 12

Each element is processed **pair-wise**.

Example 3: GCD of Array and Single Number

```
import numpy as np
```

```
arr = np.array([15, 25, 35])
```

```
result = np.gcd(arr, 5)
```

```
print(result)
```

Output:

```
[5 5 5]
```

Explanation:

- 5 divides all values completely
-

Example 4: GCD of Multiple Numbers

To find GCD of more than two numbers:

```
import numpy as np
```

```
from functools import reduce
```

```
numbers = np.array([16, 24, 32])

gcd_result = reduce(np.gcd, numbers)

print(gcd_result)
```

Output:

8

Explanation:

- $\text{GCD}(16, 24) = 8$
 - $\text{GCD}(8, 32) = 8$
-

Example 5: GCD in a 2D Array

```
import numpy as np

a = np.array([[8, 16], [18, 24]])

b = np.array([[4, 8], [6, 12]])
```

```
result = np.gcd(a, b)

print(result)
```

Output:

```
[[ 4  8]

 [ 6 12]]
```

GCD vs LCM (Quick Comparison)

Feature	GCD	LCM
Meaning	Largest common divisor	Smallest common multiple
NumPy function	<code>np.gcd()</code>	<code>np.lcm()</code>
Use	Simplification	Scheduling

NumPy Universal Functions – Trigonometric Functions

What are Trigonometric Functions?

Trigonometric functions are **mathematical functions** used to find relationships between **angles and sides of a triangle**.

The most common trigonometric functions are:

- **sin (sine)**
- **cos (cosine)**
- **tan (tangent)**

NumPy provides these as **Universal Functions (ufuncs)**, which means they work **fast and element-wise on arrays**.

Important Point (Very Important for Students)

NumPy trigonometric functions work in RADIANS, not degrees

Degrees Radians

0°	0
30°	$\pi/6$
45°	$\pi/4$
60°	$\pi/3$
90°	$\pi/2$

To convert degrees to radians, NumPy provides:

```
np.deg2rad()
```

Common Trigonometric ufuncs in NumPy

Function	Description
<code>np.sin()</code>	Sine of angle
<code>np.cos()</code>	Cosine of angle
<code>np.tan()</code>	Tangent of angle
<code>np.arcsin()</code>	Inverse sine
<code>np.arccos()</code>	Inverse cosine
<code>np.arctan()</code>	Inverse tangent
<code>np.deg2rad()</code>	Degree → Radian
<code>np.rad2deg()</code>	Radian → Degree

Example 1: Sine Function

```
import numpy as np
```

```
angle = np.pi / 2 # 90 degrees
```

```
result = np.sin(angle)
```

```
print(result)
```

Output:

1.0

Explanation:

- $\sin(90^\circ) = 1$
 - $\pi/2$ radians = 90 degrees
-

Example 2: Cosine Function

```
import numpy as np
```

```
angle = 0
```

```
result = np.cos(angle)
```

```
print(result)
```

Output:

1.0

Explanation:

- $\cos(0^\circ) = 1$
-

Example 3: Tangent Function

```
import numpy as np
```

```
angle = np.pi / 4 # 45 degrees
```

```
result = np.tan(angle)
```

```
print(result)
```

Output:

```
0.9999999999999999
```

✓ This is approximately **1** (small floating-point error).

Example 4: Trigonometric Functions on Array

```
import numpy as np
```

```
angles = np.array([0, np.pi/2, np.pi])
```

```
result = np.sin(angles)
```

```
print(result)
```

Output:

```
[0. 1. 0.]
```

Explanation:

- $\sin(0^\circ) = 0$
 - $\sin(90^\circ) = 1$
 - $\sin(180^\circ) = 0$
-

Example 5: Degrees to Radians

```
import numpy as np
```

```
degrees = np.array([0, 30, 45, 60, 90])
```

```
radians = np.deg2rad(degrees)
```

```
print(radians)
```

Output:

```
[0.    0.52359878 0.78539816 1.04719755 1.57079633]
```

Example 6: Sin of Angles in Degrees

```
import numpy as np
```

```
degrees = np.array([0, 30, 60, 90])
```

```
radians = np.deg2rad(degrees)
```

```
result = np.sin(radians)
```

```
print(result)
```

Output:

```
[0.    0.5   0.8660254 1.    ]
```

Example 7: Inverse Trigonometric Functions

```
import numpy as np
```

```
value = 1
```

```
angle_rad = np.arcsin(value)
```

```
angle_deg = np.rad2deg(angle_rad)
```

```
print(angle_deg)
```

Output:

90.0

Explanation:

- $\arcsin(1) = 90^\circ$

Example 8: Trigonometric Functions in 2D Array

```
import numpy as np

angles = np.array([[0, np.pi/2], [np.pi/4, np.pi]])

result = np.cos(angles)

print(result)
```

Output:

```
[[ 1.  0.]

 [ 0.70710678 -1.]]
```

NumPy Universal Functions – Hyperbolic Functions

What are Hyperbolic Functions?

Hyperbolic functions are **mathematical functions** similar to trigonometric functions, but they are based on **hyperbolas** instead of circles.

They are widely used in:

- Engineering

- Physics
- Machine learning
- Signal processing
- Mathematical modeling

In NumPy, hyperbolic functions are provided as **Universal Functions (ufuncs)**, which means they:

- Work element-wise on arrays
- Are fast and optimized
- Do not require loops

Common Hyperbolic Functions in NumPy

Function	Meaning
<code>np.sinh()</code>	Hyperbolic sine
<code>np.cosh()</code>	Hyperbolic cosine
<code>np.tanh()</code>	Hyperbolic tangent
<code>np.arcsinh()</code>	Inverse hyperbolic sine
<code>np.arccosh()</code>	Inverse hyperbolic cosine
<code>np.arctanh()</code>	Inverse hyperbolic tangent

Important:

Hyperbolic functions **do NOT use degrees or radians**. They work directly with **real numbers**.

Mathematical Idea (Simple Understanding)

Hyperbolic functions are defined using **exponential functions**:

- $\sinh(x) = (e^x - e^{-x}) / 2$
- $\cosh(x) = (e^x + e^{-x}) / 2$
- $\tanh(x) = \sinh(x) / \cosh(x)$

(You do **not** need to memorize this for coding, but it helps conceptually.)

Example 1: Hyperbolic Sine – np.sinh()

```
import numpy as np
```

```
x = 1
```

```
result = np.sinh(x)
```

```
print(result)
```

Output:

```
1.1752011936438014
```

Explanation:

- Calculates hyperbolic sine of 1
- Result grows faster than normal sine

Example 2: Hyperbolic Cosine – np.cosh()

```
import numpy as np
```

```
x = 1
```

```
result = np.cosh(x)
```

```
print(result)
```

Output:

```
1.5430806348152437
```

Explanation:

- $\cosh(x)$ is always **positive**
 - $\cosh(0) = 1$
-

Example 3: Hyperbolic Tangent – `np.tanh()`

```
import numpy as np
```

```
x = 1
```

```
result = np.tanh(x)
```

```
print(result)
```

Output:

```
0.7615941559557649
```

Explanation:

- $\tanh(x)$ value is always between **-1 and 1**
 - Very popular in **neural networks**
-

Example 4: Hyperbolic Functions on an Array

```
import numpy as np
```

```
values = np.array([0, 1, 2])
```

```
print(np.sinh(values))
```

```
print(np.cosh(values))
```

```
print(np.tanh(values))
```

Output:

```
[0.    1.17520119 3.62686041]
```

```
[1.    1.54308063 3.76219569]
```

```
[0.    0.76159416 0.96402758]
```

Example 5: Inverse Hyperbolic Sine – `np.arcsinh()`

```
import numpy as np
```

```
x = 1.5
```

```
result = np.arcsinh(x)
```

```
print(result)
```

Explanation:

- Finds the value whose sinh is x

Example 6: Inverse Hyperbolic Cosine – `np.arccosh()`

```
import numpy as np
```

```
x = 2
```

```
result = np.arccosh(x)
```

```
print(result)
```

Note:

- Input must be ≥ 1

Example 7: Inverse Hyperbolic Tangent – np.arctanh()

```
import numpy as np
```

```
x = 0.5
```

```
result = np.arctanh(x)
```

```
print(result)
```

Note:

- Input must be between **-1 and 1**

Example 8: Hyperbolic Functions on 2D Array

```
import numpy as np
```

```
matrix = np.array([[0, 1], [2, 3]])
```

```
result = np.tanh(matrix)
```

```
print(result)
```

Output:

```
[[0.    0.76159416]
```

```
 [0.96402758 0.99505475]]
```

NumPy Universal Functions – Set Operations

What are Set Operations?

Set operations are used to **compare two or more arrays** and find:

- Common elements
- Unique elements
- Differences between arrays

In NumPy, **set operations treat arrays like mathematical sets**.

Important:

- Output contains **unique values**
 - Result is usually **sorted**
 - Mostly used with **1-D arrays**
-

Common NumPy Set Operation Functions

Function	Description
<code>np.unique()</code>	Finds unique elements
<code>np.union1d()</code>	Union of two arrays
<code>np.intersect1d()</code>	Common elements
<code>np.setdiff1d()</code>	Difference of arrays
<code>np.setxor1d()</code>	Symmetric difference
<code>np.in1d()</code>	Membership test

Example 1: Unique Elements – `np.unique()`

```
import numpy as np
```

```
arr = np.array([1, 2, 2, 3, 4, 4, 5])
```

```
result = np.unique(arr)
```

```
print(result)
```

Output:

```
[1 2 3 4 5]
```

Explanation:

- Removes duplicate values
 - Returns sorted unique elements
-

Example 2: Union of Two Arrays – np.union1d()

```
import numpy as np
```

```
a = np.array([1, 2, 3])
```

```
b = np.array([3, 4, 5])
```

```
result = np.union1d(a, b)
```

```
print(result)
```

Output:

```
[1 2 3 4 5]
```

Explanation:

- Combines both arrays
 - Removes duplicates
-

Example 3: Intersection – np.intersect1d()

```
import numpy as np
```

```
a = np.array([1, 2, 3, 4])  
  
b = np.array([3, 4, 5, 6])  
  
result = np.intersect1d(a, b)  
  
print(result)
```

Output:

```
[3 4]
```

Explanation:

- Finds common elements between arrays
-

Example 4: Difference – np.setdiff1d()

```
import numpy as np  
  
a = np.array([1, 2, 3, 4])  
  
b = np.array([2, 4])  
  
result = np.setdiff1d(a, b)  
  
print(result)
```

Output:

```
[1 3]
```

Explanation:

- Elements present in a but not in b
-

Example 5: Symmetric Difference – np.setxor1d()


```
import numpy as np

a = np.array([1, 2, 3])

b = np.array([3, 4, 5])

result = np.setxor1d(a, b)

print(result)
```

Output:

```
[1 2 4 5]
```

Explanation:

- Elements that are in **either array**
 - But **not in both**
-

Example 6: Membership Test – np.in1d()

```
import numpy as np

a = np.array([1, 2, 3, 4])

b = np.array([2, 4])

result = np.in1d(a, b)

print(result)
```

Output:

```
[False True False True]
```

Explanation:

- Checks which elements of a exist in b
- Returns Boolean values

Example 7: Set Operations with Characters

```
import numpy as np

a = np.array(['a', 'b', 'c'])

b = np.array(['b', 'c', 'd'])

print(np.union1d(a, b))

print(np.intersect1d(a, b))
```

Output:

```
['a' 'b' 'c' 'd']

['b' 'c']
```

Example 8: Set Operations in Real-Life Scenario

Student Roll Numbers

```
import numpy as np

class_A = np.array([101, 102, 103, 104])

class_B = np.array([103, 104, 105, 106])

print("All students:", np.union1d(class_A, class_B))

print("Common students:", np.intersect1d(class_A, class_B))

print("Only in Class A:", np.setdiff1d(class_A, class_B))
```

Why Use NumPy Set Operations?

Removes duplicates automatically

Faster than Python loops

Clean and readable code

Useful in data analysis