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LING 185A
Assignment #1

A. $((\lambda x \rightarrow (\lambda y \rightarrow y + (3 * x))) 4) 1$

$\Rightarrow ((\lambda y \rightarrow y + (3 * 4))) 1$

lambda reduction

$\Rightarrow (\lambda y \rightarrow y + 12) 1$

arithmetic

$\Rightarrow 1 + 12$

lambda reduction

$\Rightarrow 13$

arithmetic

B. $((\lambda x \rightarrow (\lambda y \rightarrow x + (3 * x))) 4) 1$

$\Rightarrow ((\lambda y \rightarrow 4 + (3 * 4))) 1$

lambda reduction

$\Rightarrow (\lambda y \rightarrow 4 + 12) 1$

arithmetic

$\Rightarrow (\lambda y \rightarrow 16) 1$

arithmetic

$\Rightarrow 16$

lambda reduction

C. $((\lambda x \rightarrow (\lambda y \rightarrow y + (3 * y))) 4) 1$

$\Rightarrow ((\lambda y \rightarrow y + (3 * y))) 1$

lambda reduction

$\Rightarrow (1 + (3 * 1))$

lambda reduction

$\Rightarrow (1 + 3)$

arithmetic

$\Rightarrow 4$

arithmetic

D. $(\lambda y \rightarrow y + ((\lambda y \rightarrow 3 * y) 4)) 5$

$\Rightarrow (\lambda y \rightarrow y + (3 * 4)) 5$

lambda reduction

$\Rightarrow 5 + (3 * 4)$

lambda reduction

$\Rightarrow 5 + 12$

arithmetic

$\Rightarrow 17$

arithmetic

E. $(\lambda y \rightarrow ((\lambda y \rightarrow 3 * y) 4) + y) 5$

$\Rightarrow (\lambda y \rightarrow (3 * 4) + y) 5$

lambda reduction

$\Rightarrow (3 * 4) + 5$

lambda reduction

$\Rightarrow 12 + 5$

arithmetic

$\Rightarrow 17$

arithmetic

F. $f((\lambda n \rightarrow fn \text{ Rock}) (\lambda x \rightarrow \text{whatItBeats } x))$

$\Rightarrow f((\lambda x \rightarrow \text{whatItBeats } x) \text{ Rock})$

lambda reduction

$\Rightarrow f(\text{whatItBeats Rock})$

lambda reduction

$\Rightarrow f((\lambda s \rightarrow \text{case } s \text{ of } \{\text{Rock} \rightarrow \text{Scissors}; \text{Paper} \rightarrow \text{Rock}; \text{Scissors} \rightarrow \text{Paper}\}) \text{ Rock})$

substitution

$\Rightarrow f(\text{case Rock of } \{\text{Rock} \rightarrow \text{Scissors}; \text{Paper} \rightarrow \text{Rock}; \text{Scissors} \rightarrow \text{Paper}\})$

lambda reduction

⇒ f Scissors **case reduction**

⇒ (λs -> case s of {Rock -> 334; Paper -> 138; Scissors -> 99}) Scissors

substitution

⇒ case Scissors of {Rock -> 334; Paper -> 138; Scissors -> 99}

lambda reduction

⇒ 99 **case reduction**

G. whatItBeats (case Paper of {Rock -> Paper; Paper -> Rock; Scissors -> Scissors})

⇒ whatItBeats Rock **case reduction**

⇒ (λs -> case s of {Rock -> Scissors; Paper -> Rock; Scissors -> Paper}) Rock

substitution

⇒ case Rock of {Rock -> Scissors; Paper -> Rock; Scissors -> Paper}

lambda reduction

⇒ Scissors **case reduction**

H. (case (n+1) of {3 -> whatItBeats; 2 -> (λs -> Scissors)}) Paper

⇒ (case (1+1) of {3 -> whatItBeats; 2 -> (λs -> Scissors)}) Paper **substitution**

⇒ (case 2 of {3 -> whatItBeats; 2 -> (λs -> Scissors)}) Paper **arithmetic**

⇒ (λs -> Scissors) Paper **case reduction**

⇒ Scissors **lambda reduction**

I. case (Win (whatItBeats Rock)) of {Draw -> n; Win x -> (n + f x)}

⇒ case (Win ((λs -> case s of {Rock -> Scissors; Paper -> Rock; Scissors -> Paper})

Rock)) of {Draw -> n; Win x -> (n + f x)} **substitution**

⇒ case (Win (case Rock of {Rock -> Scissors; Paper -> Rock; Scissors -> Paper}) of

{Draw -> n; Win x -> (n + f x)}) **lambda reduction**

⇒ case (Win Scissors) of {Draw -> n; Win x -> (n + f x)} **case reduction**

⇒ n + f Scissors **case reduction**

⇒ 1 + (λs -> case s of {Rock -> 334; Paper -> 138; Scissors -> 99}) Scissors

substitution

⇒ 1 + case Scissors of {Rock -> 334; Paper -> 138; Scissors -> 99}

lambda reduction

⇒ 1 + 99 **case reduction**

⇒ 100 **arithmetic**