

```
In [15]: # import needed libries
import numpy as np
import matplotlib.pyplot as plt
```

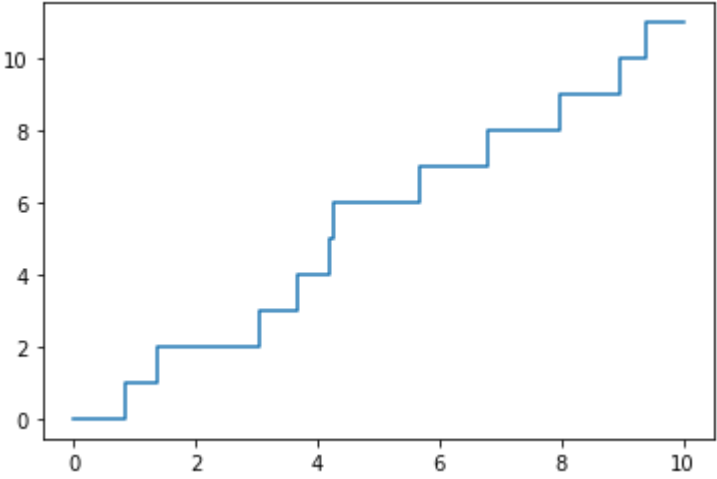
```
In [16]: # generating possion process with lambda > 0, up untile time T
def PoissonProcess(lam,T):
    timeCount = 0 # the total time that has elapsed after each arrival
    val = 0 # value of each poisson process
    Nt = [0] # a list of values of poisson process
    times = [0] # a list that contains the arrival times
    while(timeCount <= T):
        x = np.random.exponential(1/lam)
        timeCount = timeCount + x
        if(timeCount <= T):
            val = val + 1
            Nt.append(val)
            times.append(timeCount)
        if(timeCount > T):
            Nt.append(val)
            times.append(T)
    return Nt, times
```

```
In [17]: PoissonSim = PoissonProcess(1,10) # simulate poisson process with lambda = 1 on the time interval [0,1]
PoissonSim
```

```
Out[17]: ([0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 11],
[0,
0.8611534391968315,
1.3850448998129707,
3.060240896910573,
3.6694067238569126,
4.21439175428265,
4.2612132227532555,
5.670972611118373,
6.7882022193440426,
7.96468456783027,
8.95933928700481,
9.40043905030836,
10])
```

```
In [18]: # draw the poisson process
Nt = PoissonSim[0]
times = PoissonSim[1]
plt.plot(times, Nt, drawstyle='steps-post')
```

```
Out[18]: [<matplotlib.lines.Line2D at 0x7fa8ba2ae3a0>]
```



```
In [19]: # generating a compound possion process with lambda > 0, up untile time T
def CompoundPoissonProcess(lam,T,mu,sigma):
    timeCount = 0
    val = 0
    Nt = [0]
    times = [0]
    while(timeCount <= T):
        x = np.random.exponential(1/lam)
        timeCount = timeCount + x
        if(timeCount <= T):
            Z = np.random.normal(mu, sigma)
            val = val + np.exp(Z)
            Nt.append(val)
            times.append(timeCount)
        if(timeCount > T):
            Nt.append(val)
            times.append(T)
    return Nt, times
```

```
In [20]: # plot the compound poisson process with lamda = 1, mu = 0, sigma = 1 on the time interval [0,10]
CompoundPoissonSim = CompoundPoissonProcess(1,10,0,1)
CNT = CompoundPoissonSim[0]
Ctimes = CompoundPoissonSim[1]
plt.plot(Ctimes, CNT, drawstyle='steps-post')
```

```
Out[20]: [<matplotlib.lines.Line2D at 0x7fa8ba32bc40>]
```

