



ASSIGNMENT NO # 4

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Subject: APPLIED PHYSICS

Applicant ID: BSCSGHR-22-0021

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Title: Applications of Gauss law.

Dated:

Question no 1:

Write the application of GAUSS' LAW.
Explain?

GAUSS' LAW

Statement:-

"Electric flux through any surface is equal to the ratio of total charge enclosed in it to the absolute permittivity."

Mathematically.

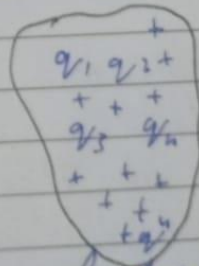
$$\Phi_e = \frac{q}{\epsilon_0}$$

(Undefined)

Proof:-

Consider an arbitrary shape with the total charge "q" enclosed in it.

i.e: $q_1 + q_2 + q_3 + \dots + q_n$



If we want to determine electric flux then

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take q_1 as a centre and draw a sharp sphere around it which is called Gaussian surface. Now the electric flux due to the charge q_1 can be obtain as:

$$\begin{aligned}\phi_e &= \phi_{e1} + \phi_{e2} + \phi_{e3} \dots + \phi_{en} \\ \phi_e &= \frac{q_1}{\epsilon_0} + \frac{q_2}{\epsilon_0} + \frac{q_3}{\epsilon_0} \dots + \frac{q_n}{\epsilon_0}\end{aligned}$$

$$\phi_e = \frac{1}{\epsilon_0} (q_1 + q_2 + q_3 \dots + q_n)$$

$$\phi_e = \frac{1}{\epsilon_0} (q)$$

$$\left[\phi_e = \frac{q}{\epsilon_0} \right] \text{ Proved!}$$

APPLICATION OF GAUSS' LAW First:

Electric intensity due to the charge sphere at a point "P" outside the sphere.

Consideration:-

Consider an insulating sphere with radius "R" such that charge "q" is uniformly distributed at the surface of the sphere. To determine the electric intensity at point "P" consider an Gaussian sphere with passes

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from "P".

As we know.

$$\phi_e = \vec{E} \cdot \vec{\Delta A}$$

$$\phi_e = E \Delta A \cos \theta$$

For Sphere $\theta = 0^\circ$

$$\phi_e = E \Delta A \cos 0$$

$$\phi_e = E \Delta A \quad \text{--- (i)}$$

A/c to Gauss Law.

$$\phi_e = \frac{q}{\epsilon_0}$$

Sub in eq (i)

$$\frac{q}{\epsilon_0} = E \Delta A$$

$$\frac{q}{\epsilon_0} = E 4\pi R^2$$

$$\frac{q}{4\pi R^2 \epsilon_0} = E$$

$$\frac{1}{4\pi \epsilon_0} \times \frac{q}{R^2} = E$$

$$\left[E = K \frac{q}{R^2} \right]$$

$$\therefore K = \frac{1}{4\pi \epsilon_0}$$

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Part (B).

Application of Gauss Law.

Electric intensity due to when the point at the centre of the sphere then replace 'R' from 'r'.

$$[E = K \frac{q}{r^2}]$$

Part (C).

When the point inside the sphere then electric charge becomes zero.

$$[E = 0]$$

Second APPLICATION OF GAUSS LAW

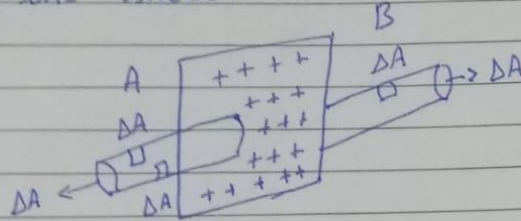
Electric intensity due to infinite sheet of charge.

Consideration:-

Consider a plane infinite sheet on which charge is distributed uniformly. To determine electric intensity. Consider a Gaussian surface as a cylinder which passes from the centre

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of the sheet.



The angle b/w curve surface area and infinite sheet of either side is 90° on side and the angle b/w cross sectional area and infinite sheet is zero.

\therefore The angle b/w curve surface and infinite sheet is 90° on either side.

$$\begin{aligned}\therefore \phi_{e_1} &= E \Delta A \cos \theta \\ &= E \Delta A \cos 90^\circ \\ &= E \Delta A (0) \\ \Rightarrow \phi_{e_1} &= 0\end{aligned}$$

Side A:

ϕ_e on cross sectional area

$$\phi_{e_2} = E \Delta A \cos 0^\circ$$

$$\phi_{e_2} = E \Delta A$$

Side B:

$$\phi_e = \phi_{e_1} + \phi_{e_2} + \phi_{e_3}$$

$$= 0 + E \Delta A + E \Delta A$$

$$\phi_e = 2 E \Delta A \quad \text{--- (i)}$$

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A/c to Gauss Law:

$$\phi_e = \frac{q}{\epsilon_0}$$

$$\frac{q}{\epsilon_0} = 2E\Delta A$$

$$E = \frac{q}{2\epsilon_0\Delta A}$$

$$E = \frac{1}{2\epsilon_0} \times \frac{q}{\Delta A}$$

$$\therefore \alpha = \frac{\text{Charge}}{\text{Area}}$$

$$\therefore \alpha = \frac{q}{\Delta A}$$

$$\left[E = \frac{\alpha}{2\epsilon_0} \right]$$

Third Application Of Gauss Law.

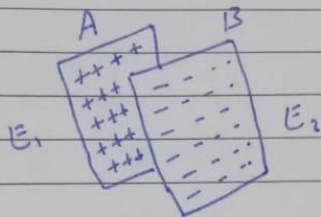
Electric intensity b/w two charge plates/sheet.

Consideration:-

Consider a point P b/w two oppositely

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but equal charge sheet. The electric intensity at point P can be obtained as.



Electric intensity due to sheet A.

$$E_1 = \frac{\sigma}{2\epsilon_0}$$

E due to sheet B

E_2 due to sheet B

$$E_2 = \frac{\sigma}{2\epsilon_0}$$

Total intensity at P

$$E = E_1 + E_2$$

$$E = \frac{\sigma}{2\epsilon_0} + \frac{\sigma}{2\epsilon_0}$$

$$E = \frac{\sigma}{\epsilon_0}$$

$$\boxed{E = \frac{\sigma}{\epsilon_0}}$$

