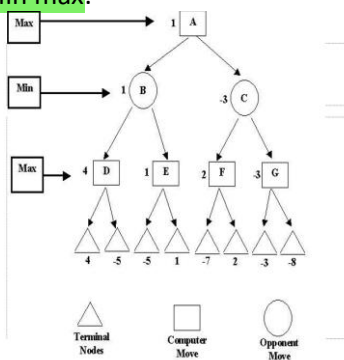


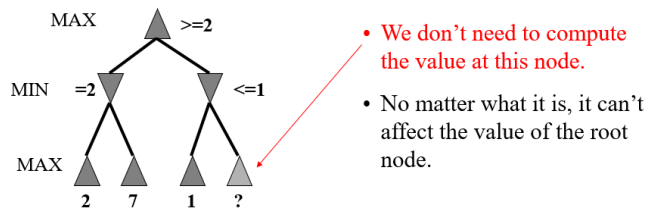
<p>Pros: When very <b>large spaces</b>, BFS is not used</p> <p>Solve hard problems with <b>minimal initial structure</b></p> <p><b>Min max:</b></p>  <p>Backtracking algo – DFS Optimal Complete Time complexity: <math>O(b^m)</math> Space complexity: <math>O(bm)</math> <math>b</math>-legal moves <math>m</math>-depth</p>	<p>Example:</p> <ul style="list-style-type: none"> <li>- Chess</li> <li>- Checkers</li> <li>- Go</li> <li>- Bridge</li> <li>- Nim</li> <li>- Tic-tac-toe</li> <li>- Othello</li> </ul> <p>Agents <b>2 types</b>:</p> <p><b>Competitive</b> <b>Cooperative</b></p>	<p>Characteristics:</p> <ul style="list-style-type: none"> <li>- 2 person game (multiagent environments)</li> <li>- Alternate moves (one after another)</li> <li>- <b>Zero sum</b></li> <li>- Perfect information</li> <li>- No chance involved</li> </ul> <p><b>Game tree</b>: a tree where the nodes are game states and the edges are moves</p>	<p><b>How to play:</b> Consider all the legal moves you can make.</p> <p>Compute the new position resulting from each move.</p> <p>Evaluate each resulting position and determine which is best.</p> <p>Make that move.</p> <p>Wait for your opponent to move and repeat.</p>	<p><b>Evaluation function:</b></p> <p><b><math>f(n) \gg 0</math>:</b> position <math>n</math> good for me and bad for you</p> <p><b><math>f(n) \ll 0</math>:</b> position <math>n</math> bad for me and good for you</p> <p><b><math>f(n)</math> near 0:</b> neutral position</p> <p><b><math>f(n) = +\infty</math>:</b> win for me</p> <p><b><math>f(n) = -\infty</math>:</b> win for you</p>
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**Alpha beta pruning**: improve performance of minmax.

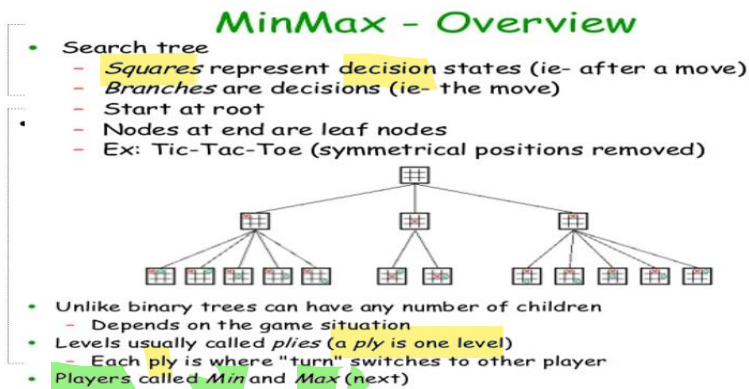
Gives **same value** of the **root** node **as minmax** algo, but needs **less or equal computation**.

**DFS algo follow**, time complexity:  $O(b^{m/2})$

- **Worst case**: no pruning, examining  $b^d$  leaf nodes, where each node has  $b$  children and a  $d$ -ply search is performed
- **Best case**: examine only  $(2b)^{d/2}$  leaf nodes.
- **Best case** is when each player's best move is the first alternative generated



- At each **MAX** node  $n$ ,  **$\alpha(n)$**  = maximum value found so far, start at **-infinity** and only **increase**
- At each **MIN** node  $n$ ,  **$\beta(n)$**  = minimum value found so far, start at **+infinity** and only **decrease**.



Extra:

- 1) **Zero sum**: one's loss is other's gain.
- 2) **Perfect Information**: both players have access to complete information about the state of the game.
- 3) **No chance**: players have full control over their moves and the outcome of the game is solely determined by their strategic decisions and actions.
- 4) **Evaluation function / static evaluator**: evaluate the "goodness" of a game position.
- 5) **Heuristic evaluation function**: approximate the true utility of a state without doing a complete search. Ex: pruning
- 6) **Alpha cutoff**: stop searching below MIN node  $n$  if  **$\beta(n) \leq \alpha(i)$**  for some MAX node ancestor  $i$  of  $n$ .
- 7) **Beta cutoff**: stop searching below MAX node  $n$  if  **$\beta(i) \leq \alpha(n)$**  for some MIN node ancestor  $i$  of  $n$ .
- 8) **Pruning**: ignore portions of the search tree that **make no difference to the final choice**
- 9) **Metareasoning**: It involves the ability to monitor, evaluate, and control one's own cognitive activities to improve problem-solving, decision-making, and learning.