

Part A

1. Answer the following Questions (Any Five).

5 × 2 = 10

- (a) What is the resolution of an image?
- (b) If we use direct coding with 8 bits per primary color, how many possible colors do we have for each pixel?
- (c) What do you require for 3D viewing an object? Mathematically how do you specify the view plane?
- (d) Ideally view volume is infinite but in reality we prefer to use a finite volume, why?
- (e) How do you specify the finite view volume?
- (f) If $d_i = -3$, $x_i = 3$, $y_i = 2$ what will be the x_{i+1} and y_{i+1} for Bresenham's line drawing algorithm?
- (g) The direct coding method is flexible in that it allows the allocation of a different number of bits to each primary color. If we use 5 bits each for red and blue and 6 bits for green for a total of 16 bits per pixel, how many possible simultaneous colors do we have?

2. Answer the following Questions (Any Four).

4 × 5 = 20

- (a) Under the standard perspective transformation P_{erk} , what is the projected image of a point in the plane $z = -d$? What does this anomaly called?
- (b) Given points $P_1(1, 2, 0)$, $P_2(3, 6, 20)$ and $P_3(2, 4, 6)$ and a viewpoint $C(0, 0, -10)$, determine which points obscure the others when viewed from C.
- (c) When eight-way symmetry is used to obtain a full circle from pixel coordinates generated for the first octant, certain pixels are set or plotted twice. This phenomenon is sometimes referred to as over-stroke. How to remove this over-stroke phenomenon?
- (d) Compare between 'Bresenham's', and 'Direct' line drawing approach.
- (e) What steps are required to plot a dashed circle? Modify Bresenham's circle drawing algorithm to achieve this.
- (f) Apply Bresenham's line algorithm to draw a line from (2,3) to (8,12). Show the steps and the resulting pixel coordinates.

3. Answer the following Questions (Any TWO).

2 × 10 = 20

- (a) Let R be a rectangular window whose lower left-hand corner is at L(-3,1) and upper right-hand corner is at R(2,6).
 - [i] Find the region codes for the endpoints $A(-2, 3) \rightarrow B(1, 2)$, $C(-4, 7) \rightarrow D(-2, 10)$ and $E(-4, 2) \rightarrow F(-1, 7)$.
 - [ii] Find the clipping categories for the line segment in part-i.
 - [iii] Use the Cohen-Sutherland algorithm to clip the line segments in part-i.
- (b) Triangle ABC where the vertices of $\triangle ABC$ are A(-1,-3), B(-4,-1), and C(-6,-4) undergoes a composition of transformations described as: a translation 10 units to the right, then a reflection in the x-axis. After all the transformations are applied what will be the triangle coordinates?
- (c) Reflect the diamond-shaped polygon whose vertices are A(-1, 0), B(0, -2), C(1, 0), and D(0, 2) about the horizontal line $y = 3$.

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Part B

4. Answer the following Questions (Any Five).

$5 \times 2 = 10$

- (a) What is "Histogram Equalization" in image processing?
- (b) What is region code? What does each bit represent?
- (c) What is "Analog Image"?
- (d) Find the transformation that scales (with respect to the origin) by 'a' units in the X direction for point P(x,y).
- (e) What are the conditions for the clipping candidate in the Cohen-Sutherland algorithm?
- (f) How do you model an object in computer graphics?
- (g) What are the geometric forms used for modeling of objects?

5. Answer the following Questions (Any Four).

$5 \times 4 = 20$

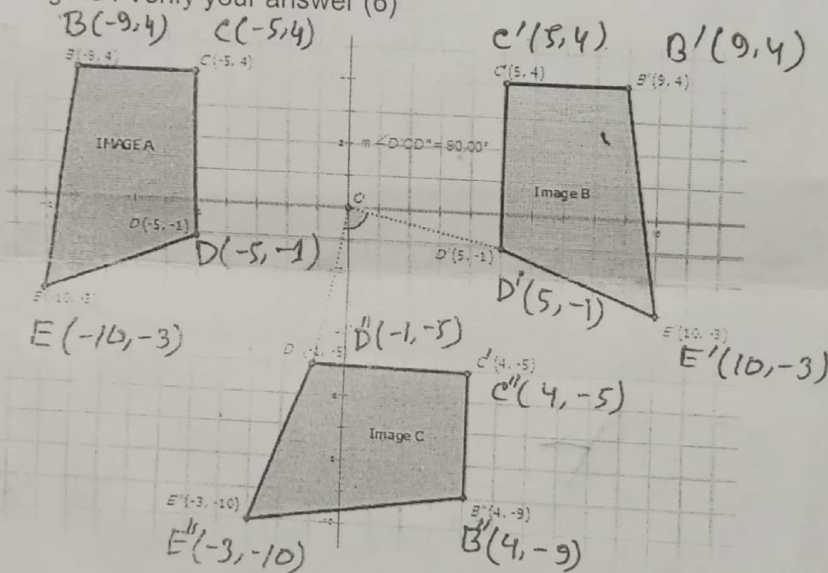
- (a) Find the normalization transformation that maps a window whose lower left corner is at (1,1) and upper right corner is at (3,5) onto a viewport that is the entire normalized device screen.
- (b) What are the types of Image Compression Techniques? Differentiate between them.
- (c) Apply Cohen-Sutherland line clipping to clip a line segment with endpoints (-5, 4) and (7, 10) against a window with corners (-3, 8) and (5, 6).
- (d) The matrix $\begin{pmatrix} 1 & a \\ b & 1 \end{pmatrix}$ defines a transformation called a simultaneous shearing or shearing for short. The special case when $b = 0$ is called shearing in the x direction. When $a = 0$ we have shearing in the y direction. Illustrate the effect of these shearing transformations on the square A(0,0), B(1,0), C(1,1), and D(0,1) when $a=2$ and $b=3$. Draw suitable diagrams.
- (e) Tilting is defined as a rotation about the x-axis followed by a rotation about the y-axis: (i) find the tilting matrix; (ii) does the order of performing rotation matter? Show mathematically.
- (f) Show that $S_{a,b} \cdot S_{c,d} = S_{c,d} \cdot S_{a,b} = S_{ac} \cdot S_{bd}$.

6. Answer the following Questions (Any Two).

$2 \times 10 = 20$

- (a) Use the Cohen-Sutherland algorithm to clip two lines P1(35,10)- P2(65,40) and P3(65,20)-P4(95,10) against a window A(50,10), B(80,10), C(80,40) and D(50,40). Also, find the clipping position.
- (b) Find a transformation A_V which aligns a given vector V with the vector K along the positive z axis.
- (c) Under the standard perspective transformation P_{erk} , what is the projected image of the line segment joining $P_1(-1, 1, -2d)$ to $P_2(2, 2, 0)$. Use suitable figures.

1. What is 8-way symmetry for a Circle? Explain. (2+2)
2. In Bransenham's Circle drawing algorithm, we defined the decision variable $d_i = D(T) + D(S)$ where T is the top pixel and S is the lower. Is there any chance that $d_i = 0$ but pixels S and T are not equally far from the true circle? Justify your answer. (5)
3. Modify the "Midpoint circle drawing" algorithm pseudocode to draw a dashed circle. A "dashed circle" generally refers to a circular shape or outline where the perimeter is represented by a dashed or dotted line rather than a solid line. (5)
4. Define the possible steps & find the composite matrix to transform 'Image A' to 'Image C'. Verify your answer (6)



$$M_{xy} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

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initial variable, $x=0, y=n$
decision variable, $(1-n)$

$$A \times B \times C$$

$$= A \times (B \times C)$$

$$= (A \times B) \times C$$

$$M_{xy} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

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Shahjalal University of Science and Technology
Software Engineering

Institute of Information and Communication Technology
4th Year 2nd Semester Final Examination' (Session: 2016-17)

Course Code: SWE 423 Credits: 3 Course Title: Computer Graphics and Image Processing
Time: 2 hrs Total Marks: 50

Group A

[Answer all the questions]

1. Answer any TWO

2x2.5=5

- Write the basic differences between Sutherland-Hodgeman and Weiler-Atherton Algorithm.
- Compute the size of a 640 X 480 image at 240 pixels per inch.
- Give real life examples of co-ordinate transformation.

2. Answer any TWO

2x10=20

- Write the differences between DDA line drawing and Bresenham's Line Drawing algorithm. 2+3+5=10
 - What do you understand by composite transformation? Explain with example.
 - The endpoints of a given line are (0,0) and (6,18). Compute each value of y as x steps from 0 to 6 and plot the results.
- Perform a 45° rotation of triangle A(0,0), B(1,1), C(5,2) about a point P(-1,-1) 5+5=10
 - Let $S_x = \frac{vx_{max} - vx_{min}}{wx_{max} - wx_{min}}$ and $S_y = \frac{vy_{max} - vy_{min}}{wy_{max} - wy_{min}}$. Express window-to-viewport mapping in the form of a composite transformation matrix.
- What do you understand by polygon and polylines? Explain their differences. 2+3+5=10
 - What are 4 connected and 8 connected pixels. Explain with possible diagrams and examples.
 - Clipping against rectangular windows whose sides are aligned with the x and y axes involves computing intersections with vertical and horizontal lines. Find the intersections of a line segment P_1P_2 [joining $P_1(x_1, y_1)$ to $P_2(x_2, y_2)$] with
 - the vertical line $x = a$ and
 - the horizontal line $y = b$.

Group B
[Answer all the questions]

3. Answer any TWO

2x2.5=5

- a) Name two algorithms that can be used to find out the visible portion of given lines in a certain viewport.
- b) What is the resolution of an image?
- c) What do you understand by window to viewport mapping?

4. Answer any TWO

2x10=20

- a)
 - I. Give two real life examples of scaling transformation.
 - II. What do you understand by Circle Symmetry property?
 - III. Find the normalization transformation that maps a window whose lower left corner is at (1,1) and upper right corner is at (3,5) onto -
 - (a) a viewport that is the entire normalized device screen and
 - (b) a viewport that has lower left corner at (0,0) and upper right corner at $(\frac{1}{2}, \frac{1}{2})$.

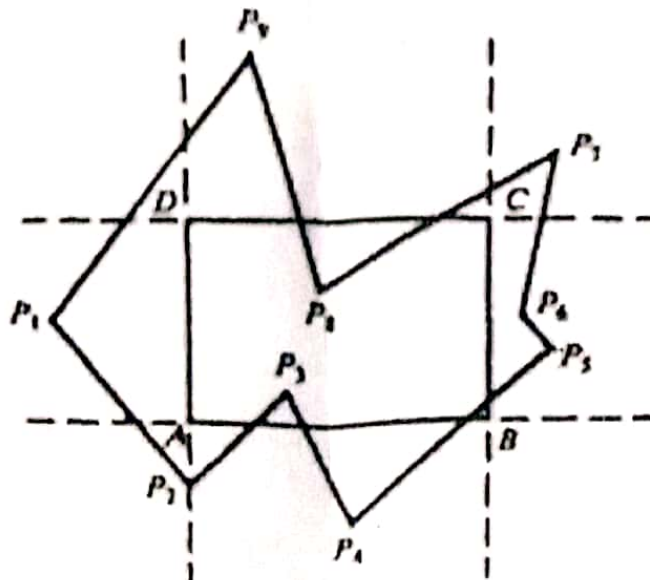
2+3+5
=10

- b)
 - I. Define translation.
 - II. How can we determine whether a point $P(x,y)$ lies to the left or to the right of a line segment joining the points $A(x_1, y_1)$ and $B(x_2, y_2)$. Explain with necessary diagrams.
 - III. Magnify the triangle with vertices $A(0,0)$, $B(1,1)$, and $C(5,2)$ to twice its size while keeping $C(5,2)$ fixed.

2+3+5
=10

c)

5+5=10



- I. Clip the above polygon using Sutherland-Hodgeman algorithm. Show the figures at each step.
- II. Describe the transformation M_r which reflects an Object about a line
 1. Draw necessary diagrams.

TT#02	Computer Graphics and Image Processing (SWE 335)	
Marks: 10		Time: 25 mins

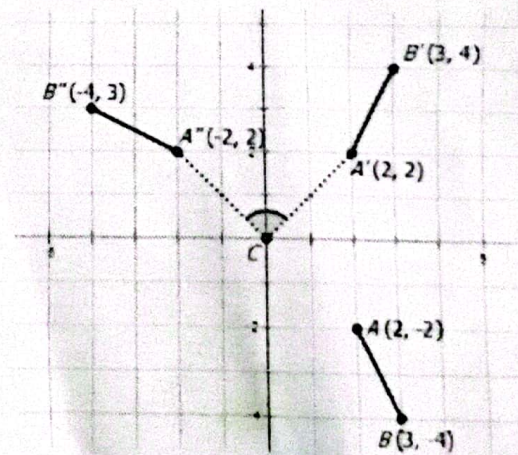
1. Find the matrix to reflect any 2D vector across $y = (-x)$. What are the new coordinates of the point $P(2,3)$ after reflection? 2

2. Show that rotation of a vector by Π has the same result as multiplication of the vector by the inversion matrix, 2

$$M = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}$$

3. Describe the transformations in the diagram below. The transformation flow is defined as:
 $AB \rightarrow A'B' \rightarrow A''B''$

matrix



6

TT#01	Computer Graphics and Image Processing (SWE 335)	
Marks: 10		Time: 25 mins

- ✓ 1. What does Rasterization mean? 1
 - ✓ 2. We have a 1024 x 768 inch image at a resolution of 300 PPI, what would be the pixel count of that image? 1
 - ✓ 3. Briefly explain the concept of octant symmetry used in the Midpoint Circle Algorithm. 2
 4. Indicate which raster locations would be chosen by the Midpoint Circle Algorithm when scan-converting a circle for the given equation of: 6
- $$(x - 15)^2 + (y - 10)^2 = 60$$