

Encryption: A means to allow two parties to establish confidential communication over an insecure channel that is subject to eavesdropping.

plaintext  $(M)$   $\xrightarrow[\text{algo}]{\text{encryption}}$  ciphertext  $(C)$

$$C = E(M), M = D(C)$$

$D \rightarrow$  Decryption

set of 7 components of cryptosystem:

- 1) plaintexts
- 2) ciphertexts
- 3) encryption keys
- 4) decryption "
- 5) correspondence between encryption and decryption keys
- 6) encryption algo
- 7) decryption "

Caesar cipher: one of the cryptosystem  
 $\rightarrow$  shifting letters

$(K > 0)$  encryption key,  $\{K = 3\}$   $AB \rightarrow EF \rightarrow$  forward shift  
 $(K < 0)$  decryption key,  $\{K = -3\}$   $EF \rightarrow AB \rightarrow$  backward

$S(C, K)$  : Ex:  $S(A, -3) = D$   
 $S(D, -3) = A$

$\downarrow$  letter    $\downarrow$  key  
 $\downarrow$     $\downarrow$

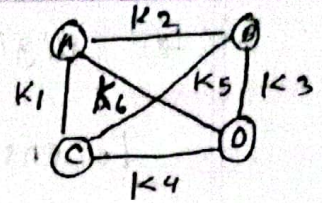


→ sender and receiver has same key

## ▣ Symmetric key distribution:

Pros: fast and efficient

Cons: each pair needs a separate secret key



\*  $n$  parties need  $n(n-1)/2$  keys

## ▣ Public key cryptography:

B has 2 keys: public  $P_B$   
private  $S_B$

A  $\xrightarrow[\text{message}]{\text{send encrypted}}$  B

, needs  $P_B$ ,  $C = E_{P_B}(m)$

B  $\xrightarrow[\text{message}]{\text{decrypt}}$

, needs  $S_B$ ,  $M = D_{S_B}(C)$

\*  $n$  person has  $2n$  keys

Pros: provides strong security guarantees

Cons: slower than symmetric  
unsuitable for interactive sessions  
larger key length

## ▣ Combining symmetric and public key system:

Pros:

- 1) Efficient and fast
- 2) shared secret key  $\rightarrow$  ensures secured data transmission

Cons: complex, additional computational overhead



Q. Digital signature: It's needed <sup>a specific</sup> to ensure that the text has come from sender

$$\cancel{D_{SB}(E_{PB}(M)) = M}$$

$$\checkmark E_{PB}(D_{SB}(M)) = M$$

- reversal of encryption and decryption order.
- A signs the contract using secret key
- B verifies the sign using A's public key

Pros:

- ensure messages are authentic and unchanged during transmission
- reliable and secured
- easy validation using sender's public key

Cons

- complex key mgmt.
- signature size can be large as message
- slow performance
- transmission and storage cost is high.

Q. Crypto-system 2 attacks:

- 1) MITM (man in the middle): It occurs when an unauthorized 3rd party interrupts communication between 2 parties.



3<sup>rd</sup> party can — add, delete, modify, view traffic.  
 — potentially compromise confidentiality  
 authenticity  
 integrity of message

s → signature  
 3<sup>rd</sup> person can't decrypt and see the real message

\* Bob send  $(m, s) : (c, s)$   
 \* 3<sup>rd</sup> person change  $(c, s')$   
 \* A thinks it's from B →  $(c', s') : (m', s')$

2) **Brute-force attack**: trying different probable (possible) keys over a ciphertext to decrypt it into meaningful text. (try every possible keys)

If the real message (m) is  
 → binary string, hard to find the valid message  
 → if natural language, find meaningful results after a few try.

\* **Unicity distance**: It's the point at which the ciphertext becomes long enough for an attacker to successfully decrypt it, recover the original message, even without knowing the key.

$$n = \frac{k}{1 - \alpha}$$

k - key length  
 α - constant



- \* Cons:** 1) ineffective for long, random, complex passwords  
2) more time, resource, power needed

**\* English text:** 1 character = 8 bits

Suppose,  $n = 8t$        $t$  "       $= 8t$  "

$$\rightarrow t = \frac{n}{8} \therefore \text{total possible array} = 2^{8t} = 2^n$$

1 char  $\rightarrow$  1.25 bits info

$\therefore t$  "  $\rightarrow$  1.25t bits

no. of t-byte array =  $2^{1.25t}$

$$= 2^{1.25n/8} = 2^{0.16n}$$

$$\text{valid text} = 2^{\alpha n} \quad [\alpha - \text{constant}]$$

$\therefore$  probability of getting valid text

$$= \frac{2^{\alpha n}}{2^n} = 2^{(\alpha-1)n} = \frac{1}{2^{(1-\alpha)n}}$$

Now,  $k \rightarrow$  length of decryption key

for a ciphertext  $\xrightarrow{k \text{ keys}}$   $\cancel{2^k}$  plaintext

$\therefore$  probability of getting plain text

$$= \frac{2^k}{2^{(1-\alpha)n}}$$



Final  
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1) ASCII  $\rightarrow 1.25$  bits info  $\rightarrow 32$  bit sequence

calculate the probability of getting meaningful text message

$$\rightarrow \text{probability}_{\text{valid text}} = \frac{1}{2^{(1-\alpha)^n}} = \frac{1}{2^{(1-1.25)32}} = 256$$

$$\therefore \text{probability (among all combo)} = \boxed{\frac{256}{2^{32}}} \quad (\text{Ans})$$

Final

2) 1.25 bits info per character.  
8 bit ASCII

6.75 bits per character are redundant.

$$\rightarrow \text{probability} = \frac{\text{total valid msg}}{\text{no. of total t byte msg}} = \frac{2^{1.25t}}{2^{8t}} = 2^{-6.75t}$$