

1. 请给出下列语言的一个上下文无关文法

$$L = \{a^n b^m c^m d^n \mid m \geq 1, n \geq 1\}$$

解：记 $CFG = (V, T, P, S)$, 则

$$V = \{S, A\} \quad T = \{a, b, c, d\}$$

$$\begin{aligned} P: \quad S &\longrightarrow a S d \mid a A d \\ A &\longrightarrow b A c \mid bc \end{aligned}$$

2. 请给出下列语言的一个上下文无关文法

$$L = \{a^m b^n \mid m \geq 0 \wedge n \geq 0 \wedge m \neq n\}$$

解：记 $CFG = (V, T, P, S)$

$$V = \{S, A, B, C\}, T = \{a, b\}$$

$$P: \quad S \longrightarrow A C \mid C B$$

$$A \longrightarrow a A \mid a$$

$$B \longrightarrow B b \mid b$$

$$C \longrightarrow a C b \mid \epsilon$$

3. 假设给定文法: $S \rightarrow 0S1|A$, $A \rightarrow 1A0|S|\epsilon$, 请构造一个以空栈方式接受同样语言的 PDA.

解: 构造的PDA 状态图如下:

$\epsilon, S/0S1 \quad \epsilon, S/A$

$\epsilon, A/1A0 \quad \epsilon, A/S \quad \epsilon, A/\epsilon$

$0, 0/\epsilon \quad 1, 1/\epsilon$

