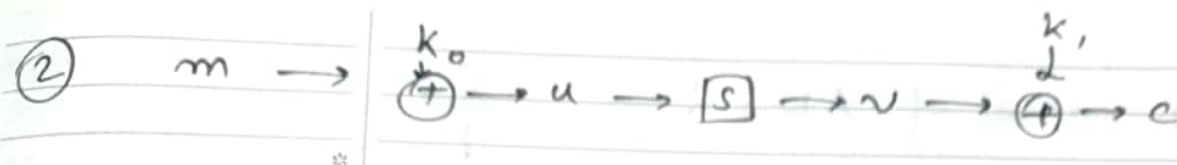


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21CS91R14



$$(i) \dots c_1 \oplus c_2 = v_1 \oplus v_2 = S[u_1] \oplus S[u_2]$$

$$= S[m_1 \oplus k_0] \oplus S[m_2 \oplus k_0]$$

$$= 1 \oplus 8 = 9$$

$$(ii) \dots m_1 \oplus m_2 = u_1 \oplus u_2 = S^{-1}[v_1] \oplus S^{-1}[v_2]$$

$$= S^{-1}[c_1 \oplus k_1] \oplus S^{-1}[c_2 \oplus k_1]$$

$$= S^{-1}[1 \oplus k_1] \oplus S^{-1}[8 \oplus k_1]$$

steps:

→ we can guess  $k_0$  and derive eqn (i) and

→ we can guess  $k_1$  and derive eqn (ii) because

→ if we know  $k_0$  then we can get a relation between  $k_1$

and  $k_0$  i.e. guess  $m_1$  and  $m_2$  with further

guesses and derive end value of (ii) [i.e.  $m_1 \oplus m_2$ ]

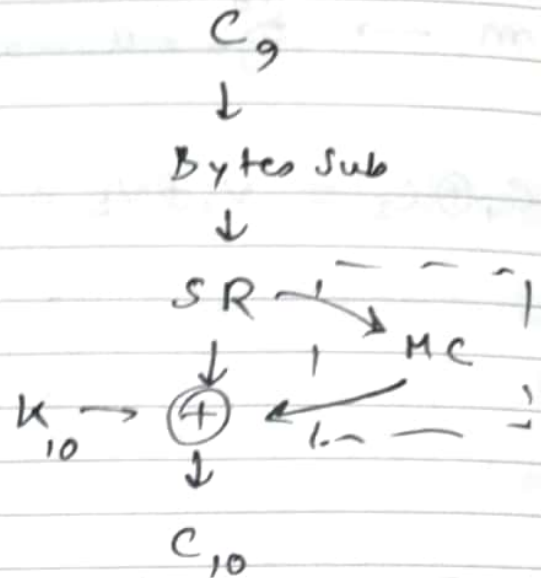
(Proved)

③ Last round of AES:

$$C_{10} = SR[BSB[C_9]] \oplus K_{10}$$

with MC

i)  $C'_{10} = MC[SR[BSB[C_9]]] \oplus K_{10}$



$$MC^{-1}[C'_{10}] = SR[BSB[C_9]] \oplus MC^{-1}[K_{10}]$$

$$\tilde{C}_{10} = SR[BSB[C_9]] \oplus \tilde{K}_{10} \quad \text{i.e. a new cipher with a new key without MC like eq (i)}$$

∴ it adds no extra security and

hence skipped for at the last round to make the decryption also symmetric to encryption.

④

Steps:

(i) We can log the time at start and end of the execution and measure time for every  $A[i], A[j]$  pairs i.e.  $N \times N$  iterations

(ii) the lowest time consumption will signify no swap i.e.  $A[i] < A[j] \forall j \leq N$   
 $\Rightarrow B[i] = 1$

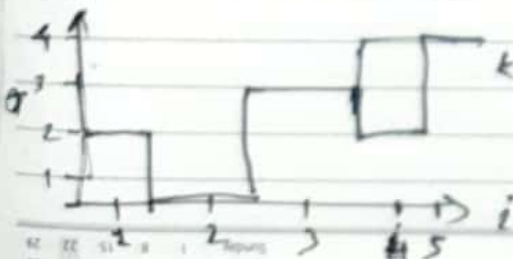
(iii) As the time signature increases we can be sure there are more swaps f.e.  
 if  $T(A[i_1], A[j_1]) > T(A[i_2], A[j_2])$   
 $\forall j_1 \leq N, \forall j_2 \leq N$

$\Rightarrow$  ~~if~~  $A[i_1] > A[i_2]$  and

sorting these  $T(i)$  values [Time sig]

we can figure out ~~that~~  $B[i_1] > B[i_2]$

Time



← is the expected time consumption for  
 given  $A = [2, 0, 3, 1, 4, 3]$   
 $\Rightarrow B = [3, 1, 2, 5, 4]$  (Proved)

~~if~~

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$$(1) \quad P(x) = x^m + x^n + 1 \Rightarrow x^m = x^n + 1$$

$$A(x) = \sum_{i=0}^{m-1} a_i x^i$$

$$x^{m+1} = x^{n+1} + x$$

$$x^{2m-2} = x^{n-2} + x^{m-2} + 1$$

$$(A(x))^n = \sum_{i=0}^m a_i^n x^{2i}$$

~~$\therefore$  there will be only even coefficients even after~~

$$\therefore C(x) = \sum_{i=0}^{m-1} c_i x^i$$

$$\therefore \text{if } i \text{ is even and } i < n \text{ or } i \geq 2n \Rightarrow c_i = a_i^n$$

$$\text{if } i \text{ is } n < i < 2n \Rightarrow c_i = a_i^n \oplus a_i^n$$

$$2n < j < 2m-2$$

$$\text{where } j \in [2n-2, 2m-2]$$

$$\text{if } i \text{ is odd and } i < n \Rightarrow c_i = a_i^n$$

$$m \leq j < 2m-2$$

$$\text{if } i \text{ is odd and } i \geq n \Rightarrow c_i = a_i^n \oplus a_i^n$$

$$m \leq j < 2m-2$$