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import numpy as np
class Softmax(object):
 def __init__(self, dims=[10, 3073]):
  self.init_weights(dims=dims)
 def init_weights(self, dims):
   Initializes the weight matrix of the Softmax classifier.
   Note that it has shape (C, D) where C is the number of
   classes and D is the feature size.
  self.W = np.random.normal(size=dims) * 0.0001
 def loss(self, X, y):
   Calculates the softmax loss.
   Inputs have dimension D, there are C classes, and we operate on minibatches
   of N examples.
   Inputs:

    X: A numpy array of shape (N, D) containing a minibatch of data.

   - y: A numpy array of shape (N,) containing training labels; y[i] = c means
    that X[i] has label c, where 0 <= c < C.
   Returns a tuple of:
   - loss as single float
   # Initialize the loss to zero.
   loss = 0.0
   # YOUR CODE HERE:
   # Calculate the normalized softmax loss. Store it as the variable loss.
   # (That is, calculate the sum of the losses of all the training
     set margins, and then normalize the loss by the number of
   # training examples.)
   # =============================== #
   # sum[1:m]{log sum[1:c]{e^{(w' * x)} - w' * x}/m
   for i in range(X.shape[0]):
    loss += (np.log(np.sum(np.exp(self.W @ X[i]))) - self.W[y[i]] @ X[i]) / X.shape[0]
   # END YOUR CODE HERE
   return loss
 def loss_and_grad(self, X, y):
   Same as self.loss(X, y), except that it also returns the gradient.
   Output: grad —— a matrix of the same dimensions as W containing
    the gradient of the loss with respect to W.
   # Initialize the loss and gradient to zero.
   loss = 0.0
   grad = np.zeros_like(self.W)
   # YOUR CODE HERE:
     Calculate the softmax loss and the gradient. Store the gradient
      as the variable grad.
   loss = self.loss(X,y)
   # sum[1:m]\{x * (softmax(x))-Indicato(y=j)\}
   for i in range(X.shape[0]):
    for j in range(self.W.shape[0]):
      grad[j] += (np.exp(self.W[j] @ X[i]) * X[i]) / np.sum(np.exp(self.W @ X[i])) - ((j == y[i]) * X[i])
   grad /= X.shape[0]
   # END YOUR CODE HERE
   return loss, grad
 def grad_check_sparse(self, X, y, your_grad, num_checks=10, h=1e-5):
   sample a few random elements and only return numerical
   in these dimensions.
   for i in np.arange(num_checks):
    ix = tuple([np.random.randint(m) for m in self.W.shape])
    oldval = self.W[ix]
    self.W[ix] = oldval + h # increment by h
    fxph = self_loss(X, y)
    self.W[ix] = oldval - h # decrement by h
    fxmh = self_loss(X,y) # evaluate f(x - h)
    self.W[ix] = oldval # reset
    grad_numerical = (fxph - fxmh) / (2 * h)
    grad_analytic = your_grad[ix]
    rel_error = abs(grad_numerical - grad_analytic) / (abs(grad_numerical) + abs(grad_analytic))
    print('numerical: %f analytic: %f, relative error: %e' % (grad_numerical, grad_analytic, rel_error))
 def fast_loss_and_grad(self, X, y):
   A vectorized implementation of loss_and_grad. It shares the same
   inputs and ouptuts as loss_and_grad.
   loss = 0.0
   grad = np.zeros(self.W.shape) # initialize the gradient as zero
   # ============================= #
   # YOUR CODE HERE:
   # Calculate the softmax loss and gradient WITHOUT any for loops.
   # =================== #
   loss = np.sum(np.log(np.sum(np.exp(self.W @ X.T),axis=0)) - np.sum(self.W[y] * X, axis=1)) / X.shape[0]
   softmax = np.exp(self.W @ X.T) / np.sum(np.exp(X @ self.W.T), axis=1)
   softmax[y,np.arange(X.shape[0])] -= 1
   grad = softmax @ X / X.shape[0]
   # END YOUR CODE HERE
   return loss, grad
 def train(self, X, y, learning_rate=1e-3, num_iters=100,
         batch_size=200, verbose=False):
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   Train this linear classifier using stochastic gradient descent.

    X: A numpy array of shape (N, D) containing training data; there are N

    training samples each of dimension D.
   - y: A numpy array of shape (N,) containing training labels; y[i] = c
    means that X[i] has label 0 <= c < C for C classes.</pre>
   - learning_rate: (float) learning rate for optimization.
   - num_iters: (integer) number of steps to take when optimizing
   - batch_size: (integer) number of training examples to use at each step.

    verbose: (boolean) If true, print progress during optimization.

   Outputs:
   A list containing the value of the loss function at each training iteration.
   num_train, dim = X.shape
   num_classes = np_max(y) + 1 \# assume y takes values 0...K-1 where K is number of classes
   self.init_weights(dims=[np.max(y) + 1, X.shape[1]]) # initializes the weights of self.W
   # Run stochastic gradient descent to optimize W
   loss_history = []
   for it in np.arange(num_iters):
    X_batch = None
    y_batch = None
    # YOUR CODE HERE:
       Sample batch_size elements from the training data for use in
         gradient descent. After sampling,
        - X_batch should have shape: (dim, batch_size)
        - y_batch should have shape: (batch_size,)
       The indices should be randomly generated to reduce correlations
       in the dataset. Use np.random.choice. It's okay to sample with
       replacement.
    batch_samples = np.random.choice(np.arange(num_train), batch_size)
    X_batch = X[batch_samples]
    y_batch = y[batch_samples]
    # END YOUR CODE HERE
     # evaluate loss and gradient
    loss, grad = self.fast_loss_and_grad(X_batch, y_batch)
    loss_history_append(loss)
    # YOUR CODE HERE:
    # Update the parameters, self.W, with a gradient step
    self.W -= learning_rate*grad
    # END YOUR CODE HERE
    if verbose and it % 100 == 0:
      print('iteration {} / {}: loss {}'.format(it, num_iters, loss))
   return loss_history
 def predict(self, X):
   Inputs:

    X: N x D array of training data. Each row is a D-dimensional point.

   Returns:
   - y_pred: Predicted labels for the data in X. y_pred is a 1-dimensional
    array of length N, and each element is an integer giving the predicted
    class.
   y_pred = np.zeros(X.shape[1])
   # YOUR CODE HERE:
   # Predict the labels given the training data.
       ______#
   y_pred = np.argmax((self.W @ X.T),axis=0)
   # END YOUR CODE HERE
   return y_pred
```