

```
import numpy as np
import pdb
```

```
class KNN(object):
```

```
    def __init__(self):
        pass
```

```
    def train(self, X, y):
        """
        Inputs:
        - X is a numpy array of size (num_examples, D)
        - y is a numpy array of size (num_examples, )
        """
        self.X_train = X
        self.y_train = y
```

```
    def compute_distances(self, X, norm=None):
        """
        Compute the distance between each test point in X and each training point
        in self.X_train.

        Inputs:
        - X: A numpy array of shape (num_test, D) containing test data.
        - norm: the function with which the norm is taken.

        Returns:
        - dists: A numpy array of shape (num_test, num_train) where dists[i, j]
          is the Euclidean distance between the ith test point and the jth training
          point.
        """
        if norm is None:
            norm = lambda x: np.sqrt(np.sum(x**2))
            #norm = 2
```

```
        num_test = X.shape[0]
        num_train = self.X_train.shape[0]
        dists = np.zeros((num_test, num_train))
        for i in np.arange(num_test):

            for j in np.arange(num_train):
                # ===== #
                # YOUR CODE HERE:
                #   Compute the distance between the ith test point and the jth
                #   training point using norm(), and store the result in dists[i, j].
                # ===== #

                dists[i,j] = norm(self.X_train[j,:] - X[i,:])

                # ===== #
                # END YOUR CODE HERE
                # ===== #

            return dists
```

```
    def compute_L2_distances_vectorized(self, X):
        """
        Compute the distance between each test point in X and each training point
        in self.X_train WITHOUT using any for loops.

        Inputs:
        - X: A numpy array of shape (num_test, D) containing test data.

        Returns:
        - dists: A numpy array of shape (num_test, num_train) where dists[i, j]
          is the Euclidean distance between the ith test point and the jth training
          point.
        """
        num_test = X.shape[0]
        num_train = self.X_train.shape[0]
        dists = np.zeros((num_test, num_train))

        # ===== #
        # YOUR CODE HERE:
        #   Compute the L2 distance between the ith test point and the jth
        #   training point and store the result in dists[i, j]. You may
        #   NOT use a for loop (or list comprehension). You may only use
        #   numpy operations.
        #
        #   HINT: use broadcasting. If you have a shape (N,1) array and
        #   a shape (M,) array, adding them together produces a shape (N, M)
        #   array.
        # ===== #

        # Compute (A-B)^2
        # For memory efficiency: Compute sqrt( X^2 + X_train^2 - 2*X*X_train')
        # Need to use broadcasting to get all columns element
        # Source: https://stackoverflow.com/a/35814006

        X_sq_sum = np.sum(np.square(X),axis=1).reshape(X.shape[0],1)    # X^2 + add axis for broadcasting
        X_train_sq_sum = np.sum(np.square(self.X_train),axis=1)          # X_train^2
        X_dot_X_train = np.dot(X,self.X_train.T)                         # X*X_train'

        dists = np.sqrt(X_sq_sum + X_train_sq_sum - 2 * X_dot_X_train)    # Compute sqrt( X^2 + X_train^2 - 2*X*X_train')

        # ===== #
        # END YOUR CODE HERE
        # ===== #

        return dists
```

```
    def predict_labels(self, dists, k=1):
        """
        Given a matrix of distances between test points and training points,
        predict a label for each test point.

        Inputs:
        - dists: A numpy array of shape (num_test, num_train) where dists[i, j]
          gives the distance between the ith test point and the jth training point.

        Returns:
        - y: A numpy array of shape (num_test,) containing predicted labels for the
          test data, where y[i] is the predicted label for the test point X[i].
        """
        num_test = dists.shape[0]
        y_pred = np.zeros(num_test)
        for i in np.arange(num_test):
            # A list of length k storing the labels of the k nearest neighbors to
            # the ith test point.
            # closest_y = []
            # ===== #
            # YOUR CODE HERE:
            #   Use the distances to calculate and then store the labels of
            #   the k-nearest neighbors to the ith test point. The function
            #   numpy.argsort may be useful.
            #
            #   After doing this, find the most common label of the k-nearest
            #   neighbors. Store the predicted label of the ith training example
            #   as y_pred[i]. Break ties by choosing the smaller label.
            # ===== #

            # Sources: https://stackoverflow.com/a/23734295 , https://www.delftstack.com/howto/python/mode-of-list-in-python/

            closest_y_s = self.y_train[dists[i,:].argsort()[:k]].tolist()
            y_pred[i] = (max(set(closest_y_s), key = closest_y_s.count))

            # ===== #
            # END YOUR CODE HERE
            # ===== #

        return y_pred
```