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import numpy as np
"""
This file implements various first-order update rules that are commonly used for
training neural networks. Each update rule accepts current weights and the
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training neural networks. Each update rule accepts current weights and the
gradient of the loss with respect to those weights and produces the next set of
weights. Each update rule has the same interface:
def update(w, dw, config=None):
Inputs:

    w: A numpy array giving the current weights.

    dw: A numpy array of the same shape as w giving the gradient of the

   loss with respect to w.
 - config: A dictionary containing hyperparameter values such as learning rate,
   momentum, etc. If the update rule requires caching values over many
   iterations, then config will also hold these cached values.
Returns:
 next_w: The next point after the update.

    config: The config dictionary to be passed to the next iteration of the

   update rule.
NOTE: For most update rules, the default learning rate will probably not perform
well; however the default values of the other hyperparameters should work well
for a variety of different problems.
For efficiency, update rules may perform in-place updates, mutating w and
setting next_w equal to w.
def sgd(w, dw, config=None):
 Performs vanilla stochastic gradient descent.
 config format:
 - learning_rate: Scalar learning rate.
 if config is None: config = {}
  config.setdefault('learning_rate', 1e-2)
 w -= config['learning_rate'] * dw
 return w, config
def sgd_momentum(w, dw, config=None):
 Performs stochastic gradient descent with momentum.
 config format:
 - learning_rate: Scalar learning rate.

    momentum: Scalar between 0 and 1 giving the momentum value.

   Setting momentum = 0 reduces to sgd.
 - velocity: A numpy array of the same shape as w and dw used to store a moving
   average of the gradients.
  if config is None: config = {}
  config.setdefault('learning_rate', 1e-2)
  config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
 v = config.get('velocity', np.zeros_like(w)) # gets velocity, else sets it to zero.
 # YOUR CODE HERE:
    Implement the momentum update formula. Return the updated weights
    as next_w, and the updated velocity as v.
 v = config['momentum'] * v - config['learning_rate'] * dw
 next_w = w + v
  # END YOUR CODE HERE
  config['velocity'] = v
 return next_w, config
def sgd_nesterov_momentum(w, dw, config=None):
 Performs stochastic gradient descent with Nesterov momentum.
  config format:
 - learning_rate: Scalar learning rate.
 - momentum: Scalar between 0 and 1 giving the momentum value.
   Setting momentum = 0 reduces to sqd.

    velocity: A numpy array of the same shape as w and dw used to store a moving

   average of the gradients.
 if config is None: config = {}
 config.setdefault('learning_rate', 1e-2)
 config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
  v = config.get('velocity', np.zeros_like(w)) # gets velocity, else sets it to zero.
 # YOUR CODE HERE:
   Implement the momentum update formula. Return the updated weights
    as next_w, and the updated velocity as v.
  # =================== #
 # Use change of vars implementation
 v \text{ old} = v
 v = config['momentum'] * v - config['learning_rate'] * dw
 next_w = w + v + config['momentum'] * (v - v_old)
  # END YOUR CODE HERE
 config['velocity'] = v
 return next_w, config
def rmsprop(w, dw, config=None):
 Uses the RMSProp update rule, which uses a moving average of squared gradient
 values to set adaptive per-parameter learning rates.
  config format:
 - learning_rate: Scalar learning rate.
 - decay_rate: Scalar between 0 and 1 giving the decay rate for the squared
   gradient cache.

    epsilon: Small scalar used for smoothing to avoid dividing by zero.

    beta: Moving average of second moments of gradients.

 if config is None: config = {}
  config.setdefault('learning_rate', 1e-2)
  config.setdefault('decay_rate', 0.99)
  config.setdefault('epsilon', 1e-8)
  config.setdefault('a', np.zeros_like(w))
 next_w = None
  # =============================== #
 # YOUR CODE HERE:
     Implement RMSProp. Store the next value of w as next_w. You need
    to also store in config['a'] the moving average of the second
     moment gradients, so they can be used for future gradients. Concretely,
     config['a'] corresponds to "a" in the lecture notes.
   config['a'] = config['a'] * config['decay_rate'] + (1-config['decay_rate']) * dw**2
 next_w = w - config['learning_rate']/(np.sqrt(config['a']) + config['epsilon']) * dw
  # END YOUR CODE HERE
 return next_w, config
def adam(w, dw, config=None):
 Uses the Adam update rule, which incorporates moving averages of both the
 gradient and its square and a bias correction term.
 config format:
 - learning_rate: Scalar learning rate.

    beta1: Decay rate for moving average of first moment of gradient.

    beta2: Decay rate for moving average of second moment of gradient.

 - epsilon: Small scalar used for smoothing to avoid dividing by zero.
 m: Moving average of gradient.
 v: Moving average of squared gradient.
 - t: Iteration number.
 if config is None: config = {}
  config.setdefault('learning_rate', 1e-3)
  config.setdefault('beta1', 0.9)
  config.setdefault('beta2', 0.999)
  config.setdefault('epsilon', 1e-8)
  config.setdefault('v', np.zeros_like(w))
  config.setdefault('a', np.zeros_like(w))
 config.setdefault('t', 0)
 next_w = None
  # YOUR CODE HERE:
    Implement Adam. Store the next value of w as next_w. You need
    to also store in config['a'] the moving average of the second
     moment gradients, and in config['v'] the moving average of the
     first moments. Finally, store in config['t'] the increasing time.
 config['t'] += 1
 # Moment Updates
 config['v'] = config['beta1'] * config['v'] + (1-config['beta1']) * dw
  config['a'] = config['beta2'] * config['a'] + (1-config['beta2']) * dw**2
 # Bias Corection
 v_corr = config['v'] / (1-config['beta1']**config['t'])
 a_corr = config['a'] / (1-config['beta2']**config['t'])
 # Param Update
 next_w = w - config['learning_rate']/(np.sqrt(a_corr) + config['epsilon']) * v_corr
  # END YOUR CODE HERE
  return next_w, config
```