

# RUCStatBeamer—Typst Template Make your slides with Typst

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**Section A** 

**Section B** 



**Section A** 

**Section B** 



#### How to choose a threshold?

- Control Per-Comparison Type I Error (PCER)
  - 1. a.k.a. "uncorrected testing", many type I errors
  - 2. Gives  $\mathbb{P}\{\mathrm{FD}_i > 0\} \leqslant \alpha$  marginally for all  $1 \leqslant i \leqslant m$
- Control Familywise Type I Error (FWER)
  - 1. e.g. Bonferroni method, or using per-comparison significance level  $\frac{\alpha}{m}$
  - 2. Guarantees  $\mathbb{P}\{FD > 0\} \leqslant \alpha$
- Control False Discovery Rate (FDR)
  - 1. First defined by Benjamini & Hochberg [1]
  - 2. Guarantees  $FDR \equiv \mathbb{E}(\frac{FD}{D}) \leqslant \alpha$



#### **BH Procedure**

#### Theorem 1

The Benjamini–Hochberg procedure (BH step-up procedure) controls the FDR at level  $\alpha$  for independent multiple tests.



## Visualization and Algorithm

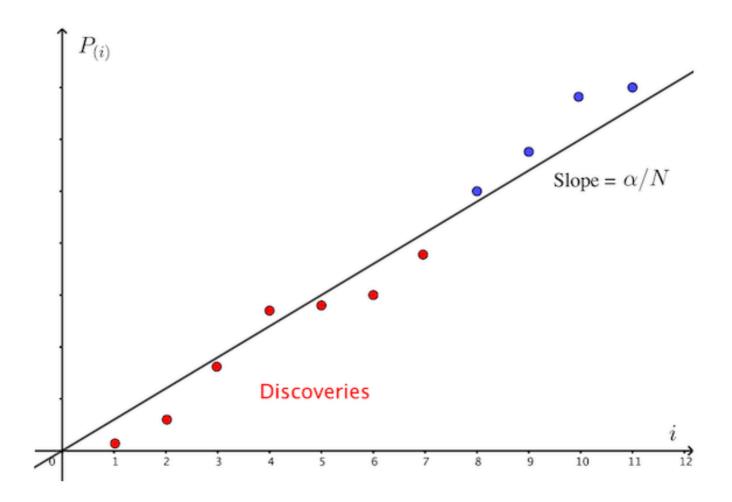


Figure 1: BH Procedure



### Visualization and Algorithm

- 1. For a given  $\alpha$ , find the largest k such that  $P_{(k)} \leq \frac{k}{m}\alpha$ .
- 2. Reject the null hypothesis (i.e., declare discoveries) for all  $H_{(i)}$  for i=1,...,k.



**Section** A

**Section B** 



9 / 10

#### R Code

```
bh <- function() {</pre>
    UseMethod("bh")
}
bh.func <- function(pv,</pre>
                                alpha
0.05) {
    m <- length(pv)</pre>
    i < -1:m
    sorted pv <- sort(pv)</pre>
    if (sorted_pv[1] > alpha / m) {
         return(rep(0, m))
     k <- max(i[sorted_pv <= i / m</pre>
* alpha])
    criterion <- sorted pv[k]</pre>
    return(1 * (pv <= criterion))</pre>
}
```

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### **Subsection B.2**

You can use #pause to pause display some proof. 😲





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**Proof:** Let  $\alpha_r = \alpha r/K$  for  $r \in \mathcal{K}$ . We can write

$$\mathbb{E}\left[\frac{F_{\mathcal{D}}}{R_{\mathcal{D}}}\right] = \mathbb{E}\left[\frac{\sum_{k \in \mathcal{N}} \mathbb{1}_{\{P_k \leqslant \alpha_{R_{\mathcal{D}}}\}}}{R_{\mathcal{D}}}\right] = \sum_{k \in \mathcal{N}} \sum_{r=1}^{K} \frac{1}{r} \mathbb{E}\left[\mathbb{1}_{\{P_k \leqslant \alpha_r\}} \mathbb{1}_{\{R_{\mathcal{D}} = r\}}\right]. \tag{1}$$

For  $k \in \mathcal{N}$ , let  $R_k$  be the number of rejection from the BH procedure if it is applied to  $\mathbf{P}$  with  $P_k$  replaced by 0. Note that  $\{P_k \leqslant \alpha_r, R_{\mathcal{D}} = r\} = \{P_k \leqslant \alpha_r, R_k = r\}$  for each k, r. Hence, we have

$$\mathbb{E}\left[\mathbb{1}_{\{P_k \leqslant \alpha_r\}} \mathbb{1}_{\{R_{\mathcal{D}} = r\}}\right] = \mathbb{E}\left[\mathbb{1}_{\{P_k \leqslant \alpha_r\}} \mathbb{1}_{\{R_k = r\}}\right]. \tag{2}$$

Putting this into Equation 1, we get

$$\mathbb{E}\Big[\frac{F_{\mathcal{D}}}{R_{\mathcal{D}}}\Big] = \frac{\alpha}{K} \sum_{k \in \mathcal{N}} \sum_{r=1}^{K} \mathbb{P}(R_k = r) = \frac{K_0 \alpha}{K},$$

and this completes the proof.





**Section** A

**Section B** 



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