

CosFace

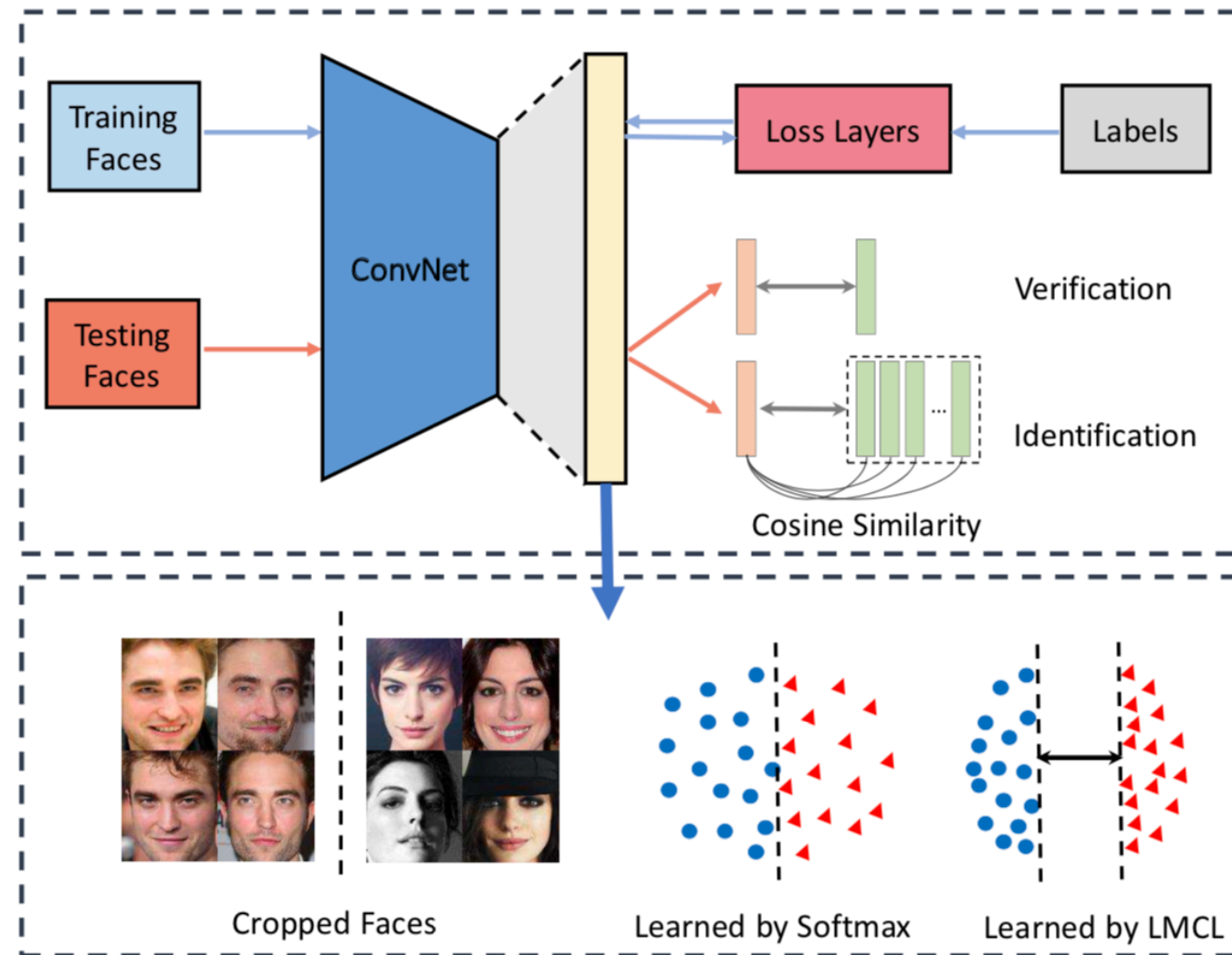
Cho Sung Man

Index

- Introduction
- LMCL(Large Margin Cosine Loss)
- Experiments

Introduction

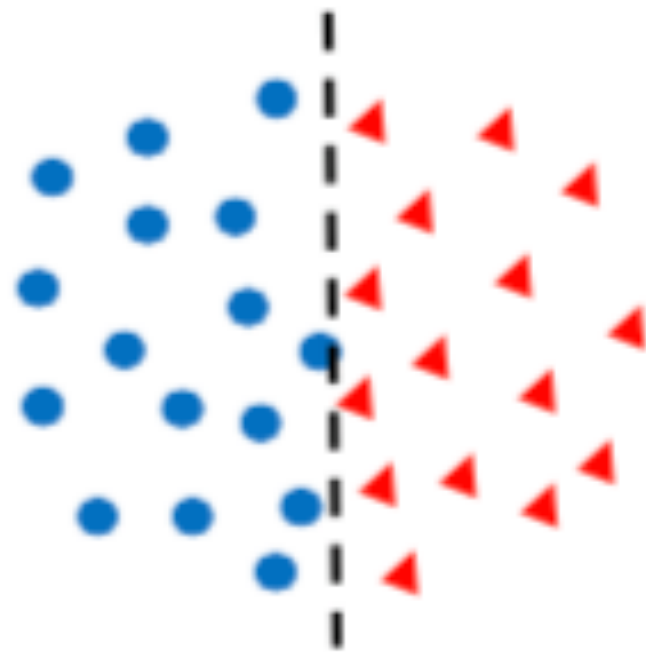
In this presentation,



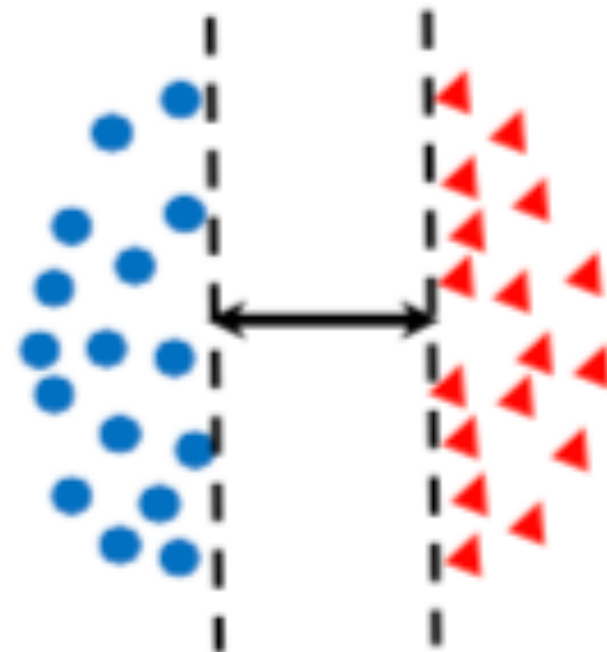
- **Traditional soft-max in the face recognition task**
- **Several loss functions**
- **LMCL (Large Margin Cosine Loss)**

Traditional Problem

In face recognition task,



Learned by Softmax

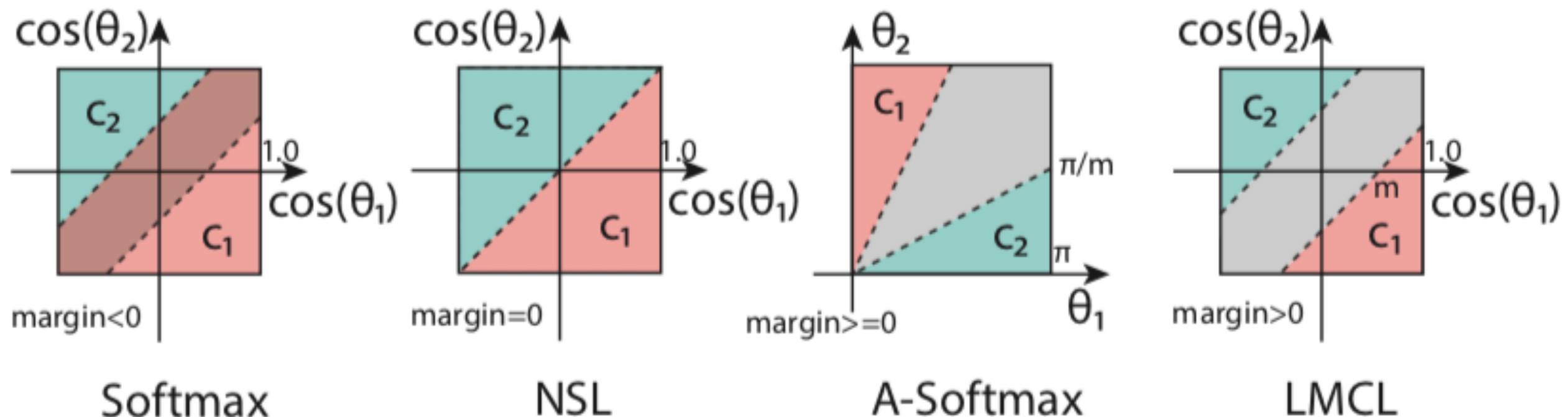


Learned by LMCL

Maximizing inter-class variance
Minimizing intra-class variance

Other Loss Functions

Softmax, NSL, A-Softmax



Compared to the Euclidean margin, **the angular margin is preferred** because the cosine of the angle has intrinsic consistency with softmax.

LMCL

LMCL

The softmax loss separates features from different classes by **maximizing the posterior probability of the ground-truth class.**

$$L_s = \frac{1}{N} \sum_{i=1}^N -\log p_i = \frac{1}{N} \sum_{i=1}^N -\log \frac{e^{f_{y_i}}}{\sum_{j=1}^C e^{f_j}},$$

Posterior probability ↓
↑ *Training Sample*

$$f_j = W_j^T x = \|W_j\| \|x\| \cos \theta_j,$$

Both norm and angle of vectors contribute to the posterior prob.

LMCL

$$L_s = \frac{1}{N} \sum_{i=1}^N -\log p_i = \frac{1}{N} \sum_{i=1}^N -\log \frac{e^{f_{y_i}}}{\sum_{j=1}^C e^{f_j}},$$

To develop effective feature learning, L2 normalization.

$$\|W_j\| = 1$$

norm of feature vector x is not contributing to the scoring function.

$$\|x\| = s$$

$$L_{ns} = \frac{1}{N} \sum_i -\log \frac{e^{s \cos(\theta_{y_i, i})}}{\sum_j e^{s \cos(\theta_{j, i})}}.$$

LMCL

$$L_s = \frac{1}{N} \sum_{i=1}^N -\log p_i = \frac{1}{N} \sum_{i=1}^N -\log \frac{e^{f_{y_i}}}{\sum_{j=1}^C e^{f_j}},$$

Normalized version of Softmax Loss (NSL)

To develop effective feature learning, L2 normalization.

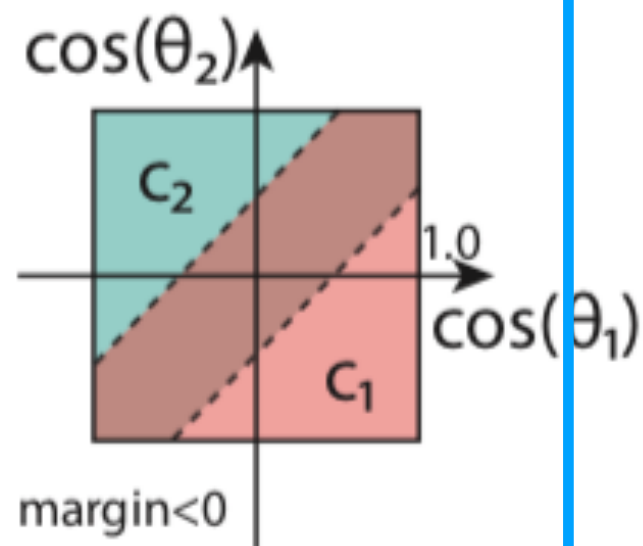
$$\|W_j\| = 1$$

norm of feature vector x is not contributing to the scoring function.

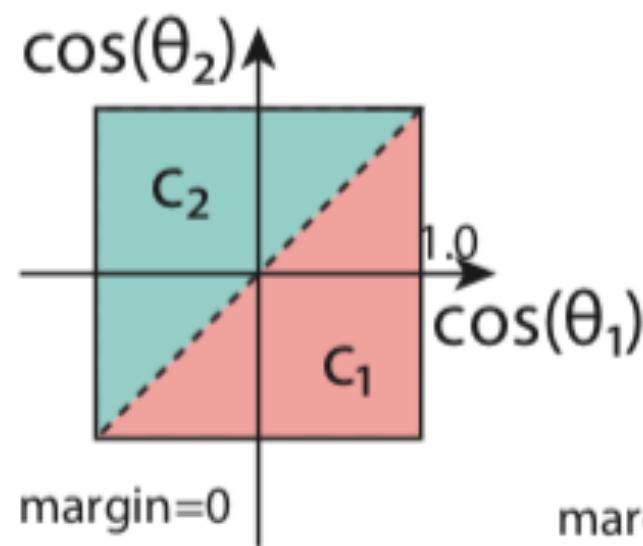
$$\|x\| = s$$

$$L_{ns} = \frac{1}{N} \sum_i -\log \frac{e^{s \cos(\theta_{y_i, i})}}{\sum_j e^{s \cos(\theta_{j, i})}}.$$

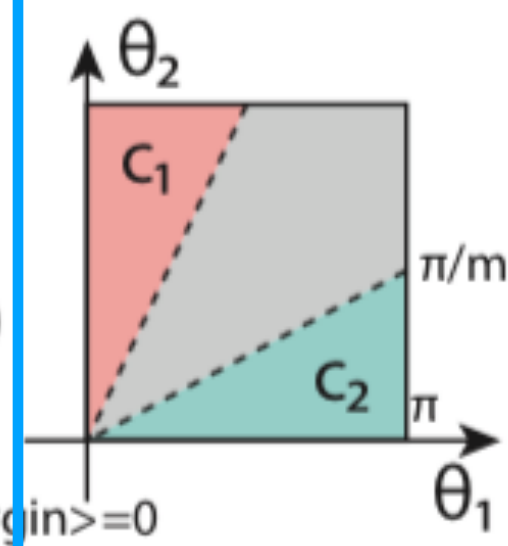
NSL



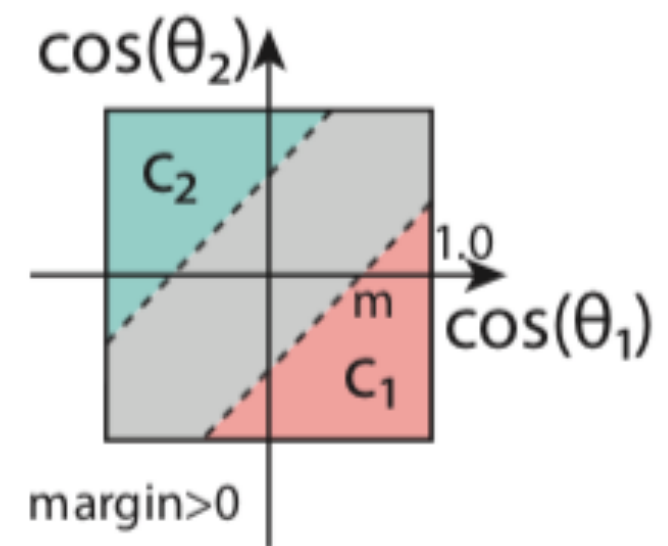
Softmax



NSL



A-Softmax



LMCL

NSL only emphasizes correct classification

LMCL

Considering a scenario of binary-classes, NSL forces (for C1)

$$\cos(\theta_1) > \cos(\theta_2)$$

To develop a large margin classifier, we further require

$$\cos(\theta_1) - m > \cos(\theta_2)$$

Formally, we define the Large Margin Cosine Loss,

$$L_{lmc} = \frac{1}{N} \sum_i -\log \frac{e^{s(\cos(\theta_{y_i,i})-m)}}{e^{s(\cos(\theta_{y_i,i})-m)} + \sum_{j \neq y_i} e^{s \cos(\theta_{j,i})}},$$

subject to,

$$W = \frac{W^*}{\|W^*\|}, \quad x = \frac{x^*}{\|x^*\|}, \quad \cos(\theta_{j,i}) = W_j^T x_i,$$

Comparisons

Softmax : $\|W_1\| \cos(\theta_1) = \|W_2\| \cos(\theta_2).$ **overlap !**

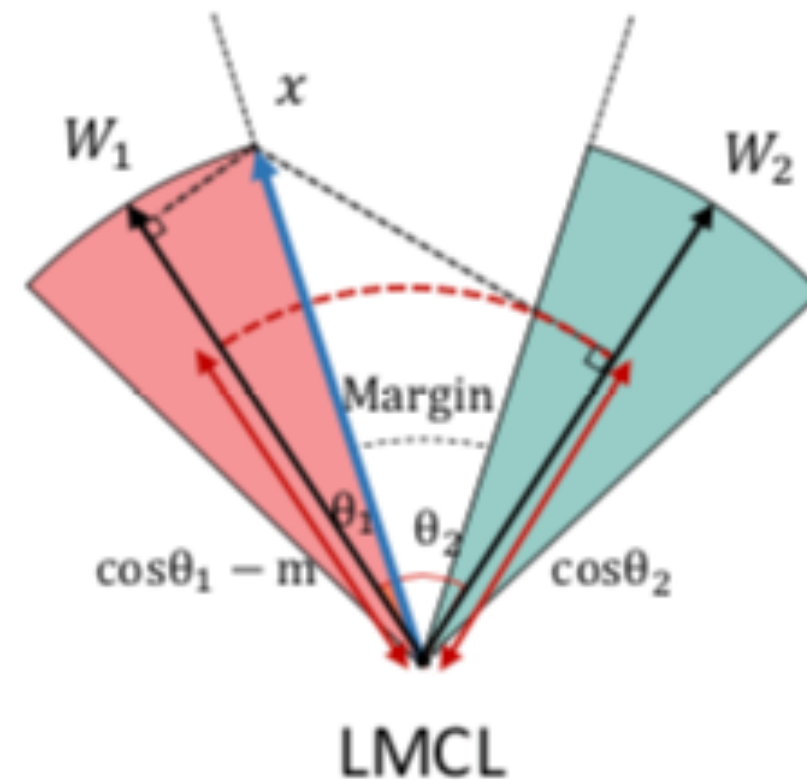
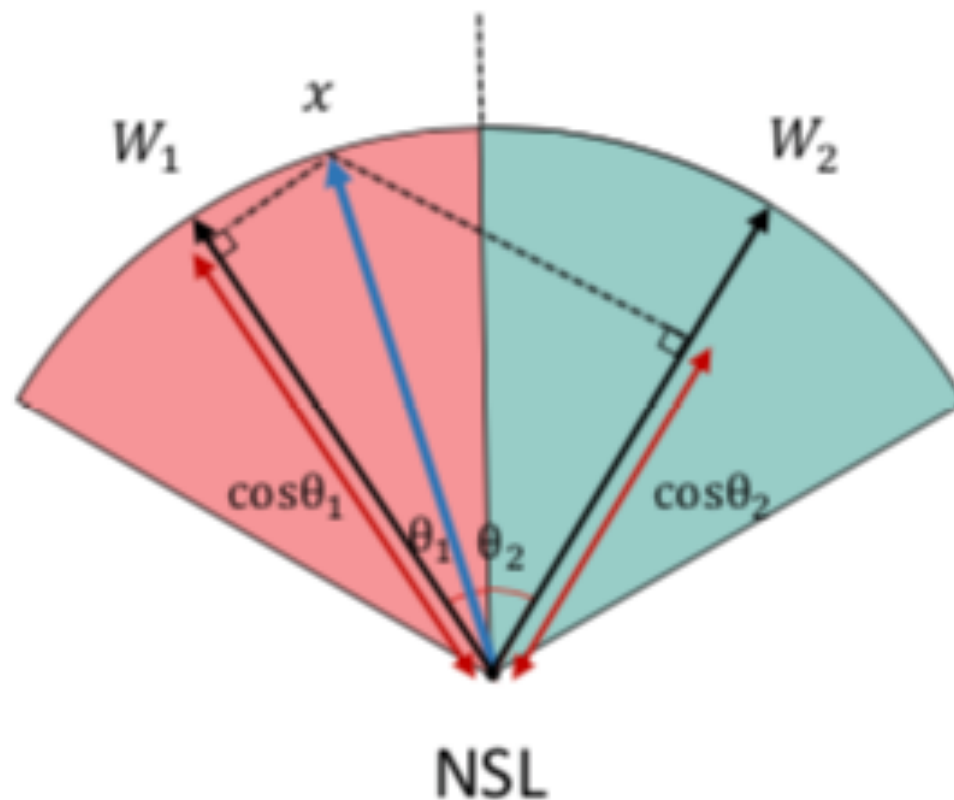
NSL : $\cos(\theta_1) = \cos(\theta_2).$ **Weight Normalization**

A-Softmax : $C_1 : \cos(m\theta_1) \geq \cos(\theta_2),$
 $C_2 : \cos(m\theta_2) \geq \cos(\theta_1).$ **if theta = 0 ?**

LMCL : $C_1 : \cos(\theta_1) \geq \cos(\theta_2) + m,$
 $C_2 : \cos(\theta_2) \geq \cos(\theta_1) + m.$

Normalization on Features

LMCL simultaneously **normalizes both weight vectors and feature vectors**.



learning only depends on cosine values to develop the discriminative power.

Why Normalization?

$$L_{lmc} = \frac{1}{N} \sum_i -\log \frac{e^{s(\cos(\theta_{y_i,i}) - m)}}{e^{s(\cos(\theta_{y_i,i}) - m)} + \sum_{j \neq y_i} e^{s \cos(\theta_{j,i})}},$$

Do NOT change ! for optimization

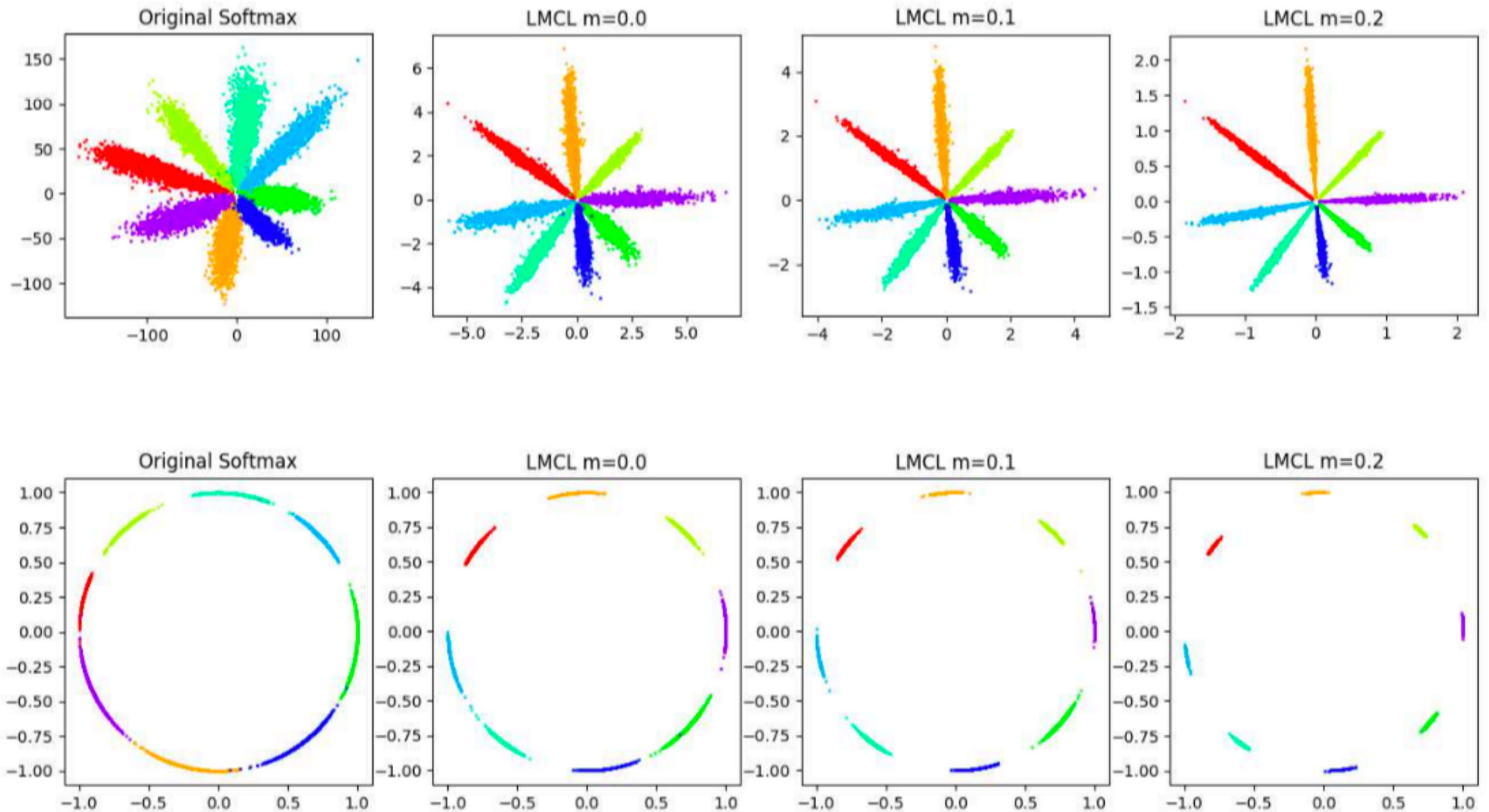
$$\boxed{\|x\|}(\cos(\theta_i) - m) > \boxed{\|x\|}\cos(\theta_j).$$

scaling parameter lower bound

$$s \geq \frac{C-1}{C} \log \frac{(C-1)P_W}{1-P_W}.$$

↑
expected minimum posterior probability

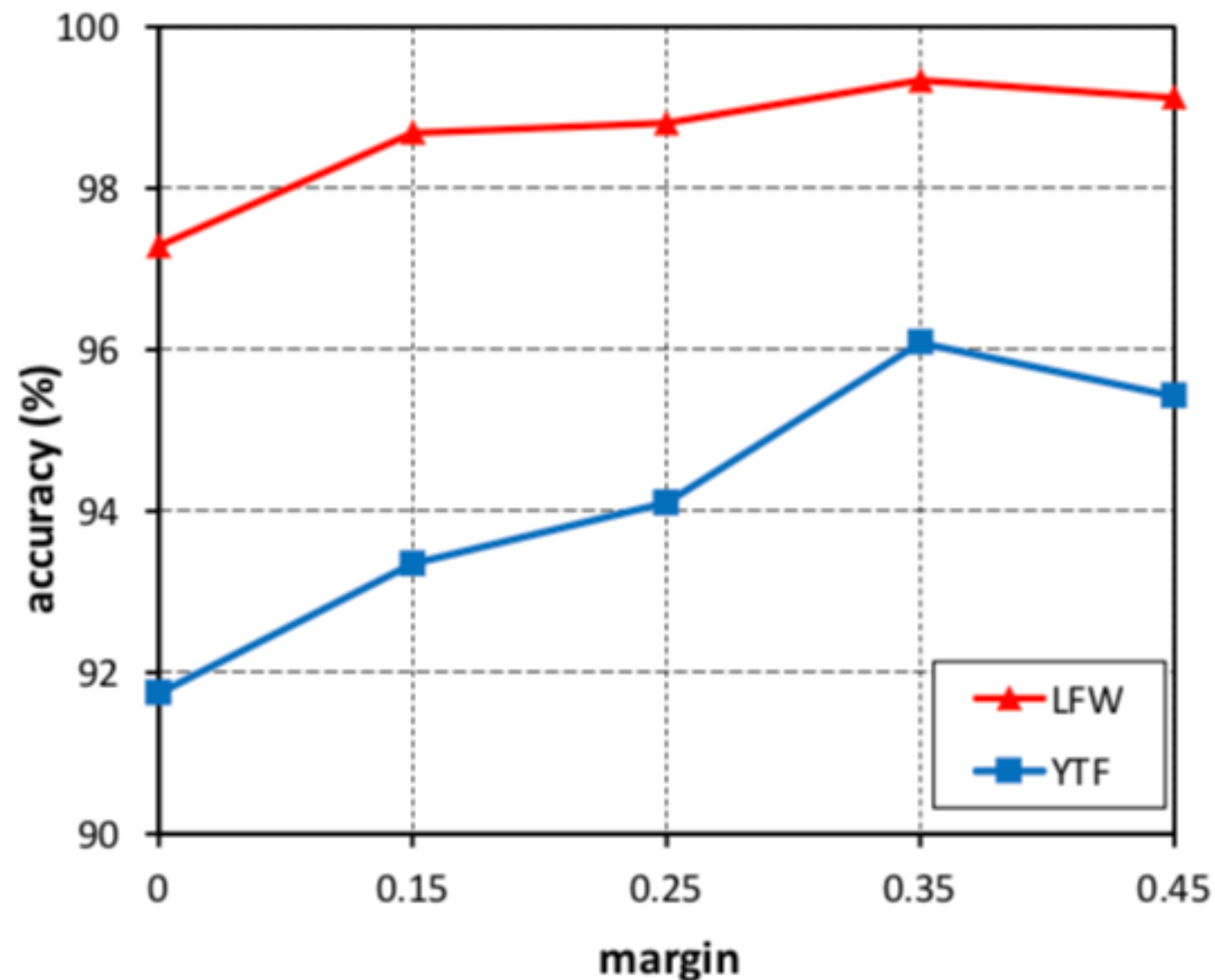
2D features



Experiments

Experiments

Accuracy of CosFace with different margin parameters on LFW and YTF



Experiments

Effect of feature normalization

Normalization	LFW	YTF	MF1 Rank 1	MF1 Veri.
No	99.10	93.1	75.10	88.65
Yes	99.33	96.1	77.11	89.88

with and without feature normalization

Benchmarks

Method	Protocol	MF1 Rank1	MF1 Veri.
SIAT_MMLAB[42]	Small	65.23	76.72
DeepSense - Small	Small	70.98	82.85
SphereFace - Small[23]	Small	75.76	90.04
Beijing FaceAll V2	Small	76.66	77.60
GRCCV	Small	77.67	74.88
FUDAN-CS_SDS[41]	Small	77.98	79.19
CosFace(Single-patch)	Small	77.11	89.88
CosFace(3-patch ensemble)	Small	79.54	92.22
Beijing FaceAll_Norm_1600	Large	64.80	67.11
Google - FaceNet v8[29]	Large	70.49	86.47
NTechLAB - facenx_large	Large	73.30	85.08
SIATMMLAB TencentVision	Large	74.20	87.27
DeepSense V2	Large	81.29	95.99
YouTu Lab	Large	83.29	91.34
Vocord - deepVo V3	Large	91.76	94.96
CosFace(Single-patch)	Large	82.72	96.65
CosFace(3-patch ensemble)	Large	84.26	97.96

Benchmarks

Method	Training Data	#Models	LFW	YTF
Deep Face[35]	4M	3	97.35	91.4
FaceNet[29]	200M	1	99.63	95.1
DeepFR [27]	2.6M	1	98.95	97.3
DeepID2+[33]	300K	25	99.47	93.2
Center Face[42]	0.7M	1	99.28	94.9
Baidu[21]	1.3M	1	99.13	-
SphereFace[23]	0.49M	1	99.42	95.0
CosFace	5M	1	99.73	97.6