

## Siddaganga Institute of Technology, Tumakuru – 572 103

(An Autonomous Institute affiliated to Visvesvaraya Technological University, Belagavi, Approved by AICTE, New Delhi)

Course : B.E  
Branch : CSE and ISETEST - 2  
December 2020ODD : 2020-21  
Sem : Third

## Mathematical Concepts for Information Technology

Time: 1 ½ Hours

Max. Marks: 50

	Answer all the questions	Marks	BL	COs	POs														
1	a) The pressure and volume of a gas are related by the equation $pv^{\gamma} = k$ where $\gamma$ and $k$ are constants. Fit this equation to the following set of observations: <table><tr><td>p</td><td>0.5</td><td>1</td><td>1.5</td><td>2</td><td>2.5</td></tr><tr><td>v</td><td>1.62</td><td>1</td><td>0.75</td><td>0.62</td><td>0.52</td></tr></table>	p	0.5	1	1.5	2	2.5	v	1.62	1	0.75	0.62	0.52	5	3	4	1		
	p	0.5	1	1.5	2	2.5													
v	1.62	1	0.75	0.62	0.52														
b)	Derive $r = \frac{\sigma_x^2 + \sigma_y^2 - \sigma_{x-y}^2}{2\sigma_x\sigma_y}$ with usual notations.	5	2	4	1														
c)	In the following table are recorded data showing the test scores made by salesmen on an intelligence test and their weekly sales: <table><tr><td>Test scores</td><td>40</td><td>70</td><td>60</td><td>80</td><td>50</td><td>90</td></tr><tr><td>Sales</td><td>2.5</td><td>6.0</td><td>5.0</td><td>4.5</td><td>2.0</td><td>5.5</td></tr></table> Obtain the regression line of sales on test scores. Also, estimate the most probable weekly sales volume if a salesman makes a score of 57.	Test scores	40	70	60	80	50	90	Sales	2.5	6.0	5.0	4.5	2.0	5.5	6	3	4	1
	Test scores	40	70	60	80	50	90												
Sales	2.5	6.0	5.0	4.5	2.0	5.5													
2	a) A simply supported beam carries a concentrated load P at its midpoint. Corresponding to various values of P, the maximum deflection y is measured. The data is as follows. <table><tr><td>P</td><td>100</td><td>120</td><td>140</td><td>180</td><td>200</td></tr><tr><td>y</td><td>0.45</td><td>0.55</td><td>0.6</td><td>0.8</td><td>0.85</td></tr></table> Find the law of the form $y = a + bP$ using the method of least squares.	P	100	120	140	180	200	y	0.45	0.55	0.6	0.8	0.85	5	3	4	1		
	P	100	120	140	180	200													
y	0.45	0.55	0.6	0.8	0.85														
b)	Solve the Lagrange's partial differential equation $(z^2 - 2yz - y^2)p + (xy + zx)q = xy - zx$	6	3	3	1														
c)	Classify the p.d.e. $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$ . Using the method of separation of variables find the solution of $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$ for all possible values of the parameter.	6	2	3	1														
3	a) Eliminate a, b and c from $z = a(x + y) + b(x - y) + abt + ct$ to form a first order partial differential equation.	5	4	3	1														
	b) Evaluate $\int_C \frac{z}{(z-1)(z-2)^2} dz$ where $C:  z - 2  = \frac{1}{2}$ using Cauchy's Residue theorem.	6	3	2	1														
c)	Form the partial differential equation by eliminating arbitrary functions from $z = xf_1(x + y) + f_2(x + y)$ .	6	4	3	1														