

Q.1) A database has four transactions. Let $\text{min_sup} = 60\%$, $\text{min_conf} = 80\%$. Apply Apriori algorithm to find the frequent itemsets and the strong association rules.

Transaction	Date	List of items
T100	10/15/99	{K, A, D, B}
T200	10/15/99	{D, A, C, E, B}
T300	10/19/99	{C, A, B, E}
T400	10/22/99	{B, A, D}

Q.1st: Support threshold = 60%
 $\therefore \text{min_sup} = 0.6 \times \text{no. of transaction}$
 $= 0.6 \times 4 = 2.4$
 $\therefore \text{min_sup} = 2.4$

① Count of each Itemset (C_1) by scanning the database

Itemset	Count
{A}	4
{B}	4
{C}	2
{D}	3
{E}	2
{K}	1

② ~~Prune step (1): Remove min_sup < below value~~

② Prune step (L_1):- C_1 show ~~that~~ that Itemset $\{C\}$, $\{E\}$ and $\{K\}$ does not meet the min sup.

Itemset	Count
$\{A, B\}$	4
$\{A, D\}$	4
$\{B, D\}$	3

③ Join step (C_2):- Form C_2 from $L_1 \times L_1$ and find out their occurrences.

Itemset	Count
$\{A, B\}$	4
$\{A, D\}$	3
$\{B, D\}$	3

④ Prune step (L_2):- C_2 show that all Itemset does meet the min sup.

Itemset	Count
$\{A, B\}$	4
$\{A, D\}$	3
$\{B, D\}$	3

⑤ Join step (C_3):- Form C_3 from $L_2 \times L_2$ and find out their occurrences.

Item set	Count
$\{A, B, D\}$	3

Thus, $\{A, B, D\}$ it is frequent.

⑥ Generate Association Rule:-

From frequent itemset discovered above, the association could be:-

$$\bullet \{A, B\} \rightarrow \{D\}$$

$$\begin{aligned}\text{confidence} &= \text{support} \{A, B, D\} / \text{support} \{A, B\} \\ &= (3/4) \times 100 \\ &= 75\%.\end{aligned}$$

$$\bullet \{A, D\} \rightarrow \{B\}$$

$$\begin{aligned}\text{confidence} &= \text{support} \{A, B, D\} / \text{support} \{A, D\} \\ &= (3/3) \times 100 \\ &= 100\%.\end{aligned}$$

$$\bullet \{B, D\} \rightarrow \{A\}$$

$$\begin{aligned}\text{confidence} &= \text{support} \{A, B, D\} / \text{support} \{B, D\} \\ &= (3/3) \times 100 \\ &= 100\%.\end{aligned}$$

$$\bullet \{A\} \rightarrow \{B, D\}$$

$$\begin{aligned}\text{confidence} &= \text{support} \{A, B, D\} / \text{support} \{A\} \\ &= \frac{3}{4} (3/4) \times 100 \\ &= 75\%.\end{aligned}$$

$$\{B\} \rightarrow \{A, D\}$$

$$\begin{aligned}\text{Confidence} &= \frac{\text{support } \{A, B, D\}}{\text{support } \{B\}} \\ &= \frac{(3/4)}{(4/4)} \times 100 \\ &= 75\%\end{aligned}$$

$$\{D\} \rightarrow \{A, B\}$$

$$\begin{aligned}\text{Confidence} &= \frac{\text{support } \{A, B, D\}}{\text{support } \{D\}} \\ &= \frac{(3/3)}{(3/3)} \times 100 \\ &= 100\%\end{aligned}$$

So if minimum confidence is 80%, then $\{A, D\} \rightarrow \{B\}$, $\{B, D\} \rightarrow \{A\}$, and $\{D\} \rightarrow \{A, B\}$ can be considered as strong association rules.

Q.2) Generate frequent pattern free for the following transaction with 30% minimum support.

Transaction ID	Items
T1	E, A, D, B
T2	D, A, C, E, B
T3	C, A, B, E
T4	B, A, D
T5	D
T6	D, B
T7	A, D, E
T8	B, C

Soln: $\text{Sup_count} = 8 \times 30\% = 8 \times 0.3 = 2.4$
 $\text{Sup_count} = 2.4$

Step 1 :- Scan the database for count the each dataset.

Item set	Sup count
A	5
B	6
C	3
D	6
E	4

Step 2:- Sort the set of frequent Itemset in the order of descending support order.

Itemset	Sup count
B	6
D	6
A	5
E	4
C	3

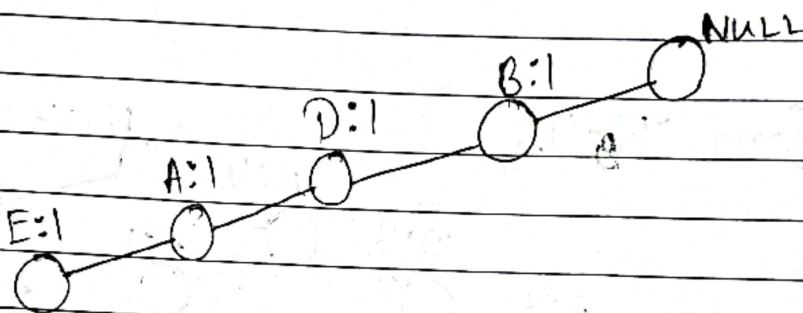
Step 3:- Scan the database for 2nd time sort item in each transaction according to descending support count

Transaction ID	Item bought
T 1	{ B, D, A, E }
T 2	{ B, D, A, E, C }
T 3	{ B, A, E, C }
T 4	{ B, D, A }
T 5	{ D }
T 6	{ B, D }
T 7	{ D, A, E }
T 8	{ B, C }

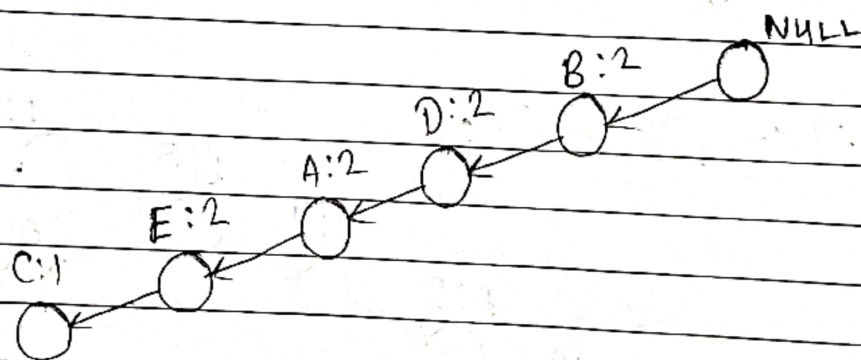
Step 4:- Construct of Frequent Pattern Tree.

4.1:- Create a root node with label null (O^{NULL})

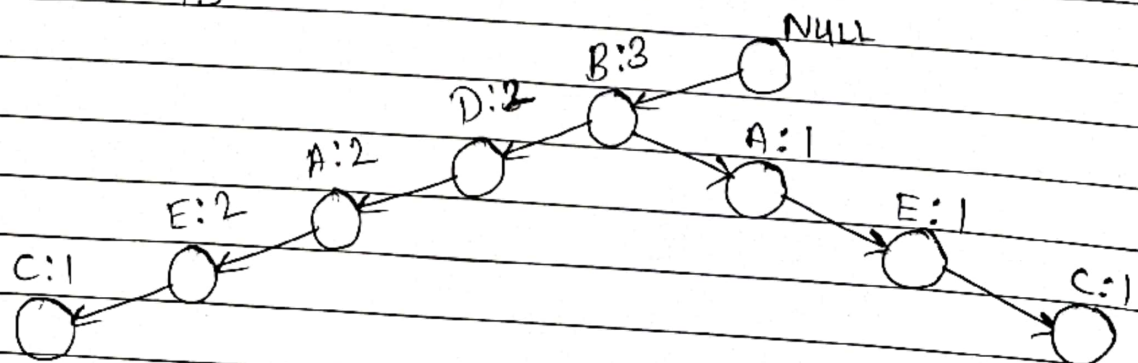
4.2:- Scan T_1



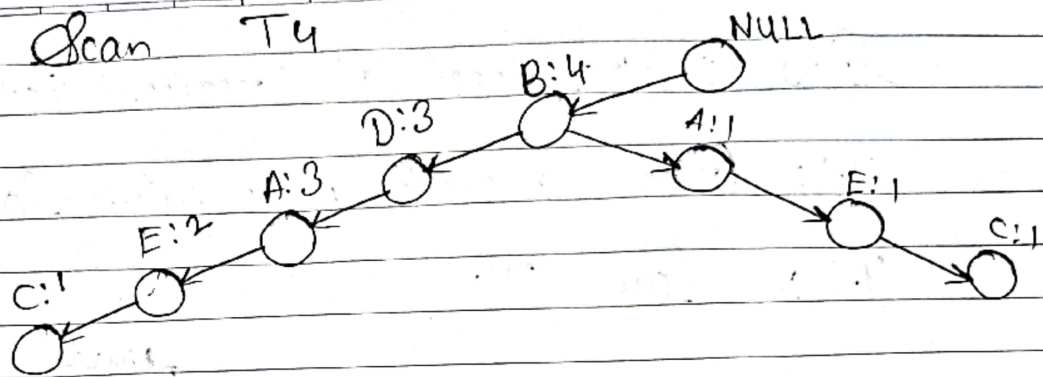
4.3:- Scan T_2



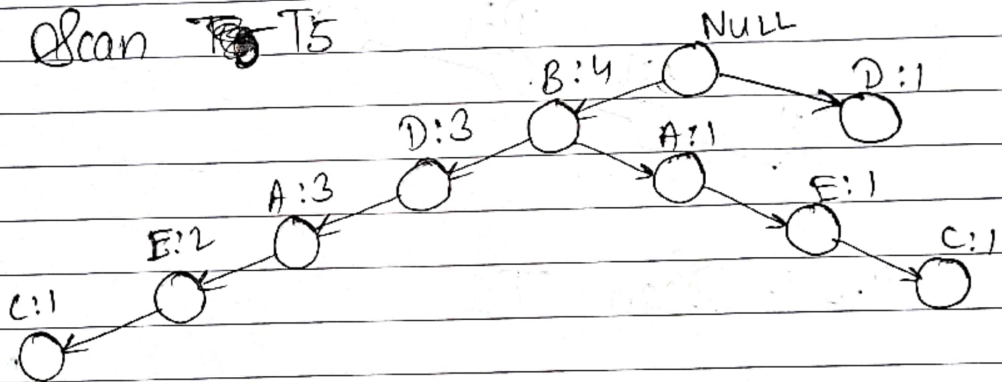
4.4:- Scan T_3



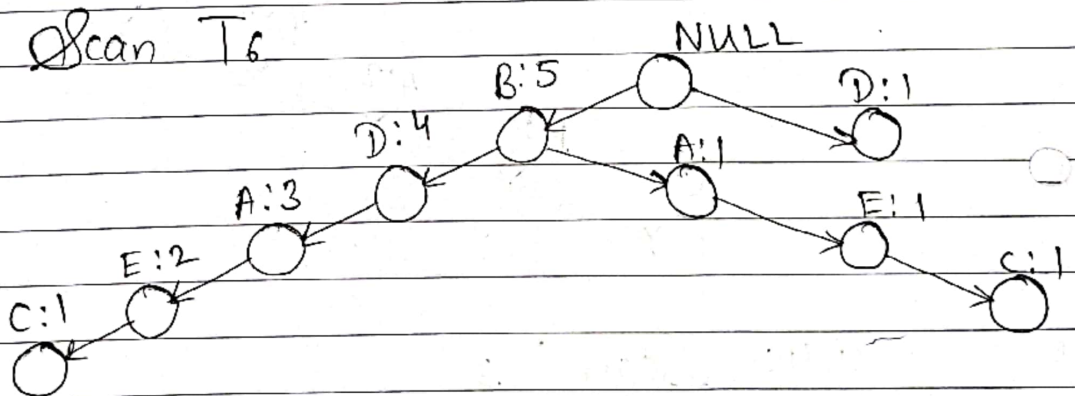
4.5 :- Scan T4



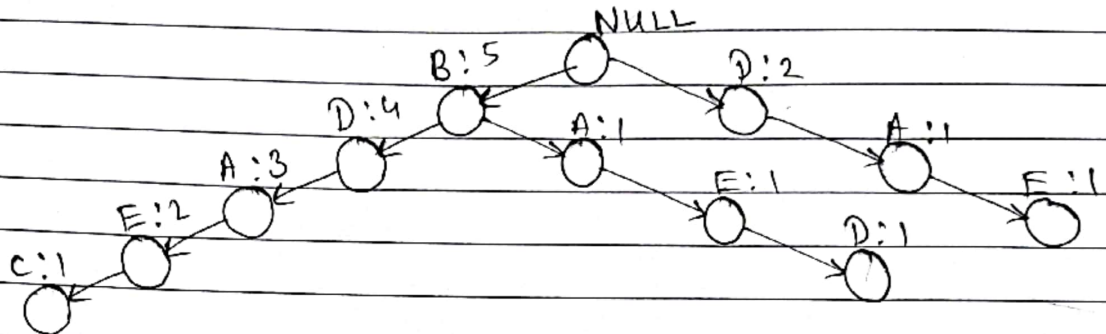
4.6 :- Scan T5



4.7 :- Scan T6



4.7:- Scan T₇



4.8 :- Scan T₈

