CS320 Programming Languages
Exercise #1

1 Primitives

1. Write the function `volumeOfCuboid`, which consumes three non-negative integer numbers `a`, `b`, and `c` denoting lengths of three sides and produces the volume of the cuboid. (Note: $0 \leq \texttt{a}, \texttt{b}, \texttt{c} \leq 1,000$)

2. Write the function `concat`, which consumes two strings `x` and `y`, and it returns their concatenation. For example, `test(concat("abc", "def"), "abcdef")`

2 Function Values

1. Write the function `addN`, which consumes an integer number `n` and produces a function that adds `n` to a given integer number. For example,

```
val f: Int => Int = addN(5)
test(f(3), 8)
test(f(42), 47)
```

2. Write the function `twice`, which consumes a function `f` whose type is `Int => Int` and returns another function that applies the function `f` twice. For example,

```
val g: Int => Int = twice(addN(3))
test(g(2), 8)
test(g(7), 13)
```

3. Write the function `compose`, which consumes two `Int => Int` functions `f` and `g` and returns their composition `f` $\circ$ `g`. For example,

```
val h: Int => Int = compose(addN(3), addN(4))
test(h(5), 12)
test(h(11), 18)
```

3 Data Structures

3.1 Lists

1. Define the function `double`, which consumes a list `l` of integers and returns another list whose elements are doubles of elements of `l`. For example,

```
val l: List[Int] = List(1, 2, 3)
test(double(l), List(2, 4, 6))
test(double(double(l)), List(4, 8, 12))
```

2. Define the function `sum`, which consumes a list `l` of integers and returns the sum of elements of the list `l`. For example,

```
test(sum(List(1,2,3)), 6)
test(sum(List(4,2,3,7,5)), 21)
```

3.2 Maps

1. Define the function `getKey`, which consumes a map `m` from strings to integers and a string `s`. If there exists a mapping for the string `s` in the map `m`, it returns the corresponding integer number. Otherwise, it throws an error with a message containing the string `s` via the helper function `error`. For example,

```
val m: Map[String, Int] = Map("Ryu" -> 42, "PL" -> 37)
test(getKey(m, "Ryu"), 42)
test(getKey(m, "PL"), 37)
testExc(getKey(m, "CS320"), "CS320")
```

3.3 User-defined Structures

We provide the `Tree` type to represent binary trees. It is either `Branch` for a non-leaf node, or a `Leaf` for a leaf node. A `Branch` consists of three members; `left` and `right` denote the left and right sub-trees, and `value` denotes its value. A `Leaf` has unique member `value` to represent its value. (Note: DO NOT re-define `Tree` in `package.scala` because it is already defined in `Exercise01.scala`)

```
trait Tree
case class Branch(left: Tree, value: Int, right: Tree) extends Tree
case class Leaf(value: Int) extends Tree
```

1. Define the function `countLeaves`, which consumes a tree `t` and returns the number of its leaf nodes. For example,

```
val tree: Tree = Branch(Leaf(1), 2, Branch(Leaf(3), 4, Leaf(5)))
test(countLeaves(tree), 3)
```

2. Define the function `flatten`, which consumes a tree `t` and returns a list containing the values of nodes inside the tree `t` with in-order tree traversals.

```
val tree: Tree = Branch(Leaf(1), 2, Branch(Leaf(3), 4, Leaf(5)))
test(flatten(tree), List(1, 2, 3, 4, 5))
```