

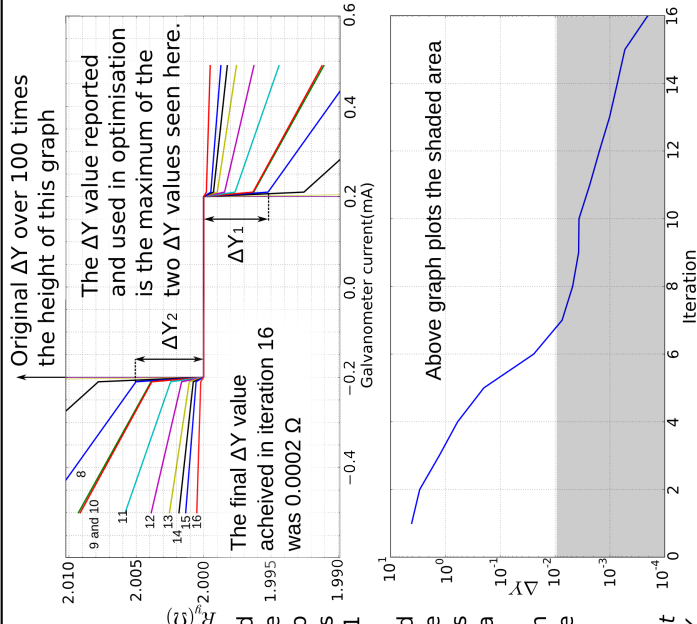
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.Circuit Diagram

The circuit diagram shows a Wheatstone bridge with four resistors: R_A , R_B , R_C , and R_D . A galvanometer (G) is connected between the two central nodes. The bridge is connected to a voltage source V_F . The input voltages are labeled V_x and V_y , and the output voltages are labeled V_z .

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3. Results

ΔV : Optimisation 1	Power: Optimisation 2	Final Chosen Components	Component Tolerances (%)	Component Power rating (mW)	Max. (6 σ) Dissipated power (mW)	Yield (σ)
$V_E=33.810\text{ V}$	$V_E=1.500\text{ V}$	$V_E=1.500\text{ V}$	N/A(-20)			
$R_A=1.0000\text{ }\Omega$	$R_A=1.0006\text{ }\Omega$	$R_A=3.00\text{ }\Omega$	± 1	00	N/A	
$R_B=1.3413\text{ }\Omega$	$R_B=3.6994\text{ }\Omega$	$R_B=12.70\text{ }\Omega$	± 1	00	115	
$R_C=1.2310\text{ }\Omega$	$R_C=7.2199\text{ }\Omega$	$R_C=40.20+36.0=76.2\text{ }\Omega$	± 1	00	19.2	6.53
$R_D=1.8356\text{ }\Omega$	$R_D=3.9033\text{ }\Omega$	$R_D=12.00\text{ }\Omega$	± 1	00	3.1	
$R_F=1.0002\text{ }\Omega$	$R_F=1.0001\text{ }\Omega$	$R_F=1.00\text{ }\Omega$	± 1	00	12.4	

To obtain the greatest accuracy possible the first set of iterations were simply optimising ΔY without considering any other design objectives. These are illustrated in section 2. The high voltage and low resistance made it an

A common battery voltage of 1.5 V was chosen as a reasonable V_E . The power dissipated in each resistor was constrained below 0.1W in subsequent iterations.

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graph TD
    1[1. Control factor ranges] --> 2[2. Test specifications]
    2 --> 3[3. Perform experiment]
    3 --> 4[4. Check model fit]
    4 --> 5[5. Optimise variables]
    5 --> 6[6. Confirmation run]
    4 --> 3
    4 --> Note[As an arbitrary number of experiments could be run a cubic model was built using a full factorial experiment to increase accuracy.  
Five control factors were varied between four different settings, producing 1025 runs. This could be simulated in under a second, but would be impractical.]
  
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A final experiment is always required to validate the optimised design.

Fit of the model can be estimated by the reported R^2 (fit of the model to data) value. This can be improved by applying a y-transform, variance weights or bisquare weights.

$$R^2 = \frac{SS_{reg}}{SS_{obs}}$$

It was necessary to calculate R_C for each circuit to ensure it would balance at 2Ω . This was achieved in the Python code using the following equations, by asserting R_v at 2Ω .

$$R_C = \frac{R_B \times R_D}{R_y} \quad R_C = \frac{R_B \times R_D}{2}$$

Using the `distrib` command in `RS/1` it is possible to estimate the effect of resistor tolerances on the model. However, in order to optimise the yield of the circuit easily a Monte Carlo simulator was written in Python. Ideally, this would be run on the model because it involves many experiments.

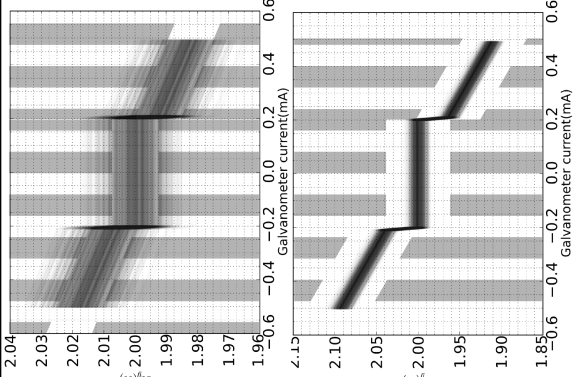


Figure 3: Illustration of the results of Monte Carlo on two optimised designs.

The final circuit is guaranteed to be able to detect a 2Ω resistor to within $70\text{m}\Omega$, while consuming 167mW when balanced and for a resistor cost of £0.047.