

§ Normalization: Normalization is a process to eliminate redundancy, as redundancy is the root cause of a number of problems.

Problems brought about by redundancy:

- Insertion anomalies
- Deletion anomalies
- Update anomalies

Eg: Student

Student ID	Name	Age	PrgID	PrgName	PrgChair
101	A	20	III	CSC	XY2
102	B	18	III	CSC	XY2
301	L	21	IIIA	CSE	XY2

These anomalies are brought by storing program info in one student table.

↳ This can be resolved if we adopt the ER idea.

Student

Student ID	Name	Age	PrgID	PrgID	PrgName	PrgCh
101	A	20	III	III	CSC	XY2
102	B	18	III	IIIA	CSE	XY2
301	L	21	IIIA			

This logical break down is brought about by Normalization
 1NF → 2NF → 3NF → BCNF {using Functional Dep's}

8 Functional Dependencies (FD):

(this is a tool/technique)

Consider the relation $R(x, \beta)$ and the functional dependency $\boxed{fd: x \rightarrow \beta}$

R	x	β
	a	1
	b	1
	c	3
	d	4

determinant \rightarrow $fd: x \rightarrow \beta$ \leftarrow dependent
 \nwarrow search function

i.e., $\rightarrow \approx$ search function; what does this mean?
 consider a function $f(x) = y$ and we make observations on 'y' by changing the values of 'x'.

$\begin{matrix} x & y \\ \downarrow & \downarrow \\ f(1) = a \\ f(2) = b \\ f(1) = c \end{matrix} \left. \vphantom{\begin{matrix} x & y \\ \downarrow & \downarrow \\ f(1) = a \\ f(2) = b \\ f(1) = c \end{matrix}} \right\} \begin{array}{l} \text{do you think the function} \\ \text{is correct?} \end{array}$

the answer is "no". { this is because when $x=1$, we observe different values of y }

So, bringing this idea back to a search function/fd; a fd is a function that enables you to find the value of β given x ; and this is possible only when the values of x preserves a logical ordering in a relation.

so if we go back to relation R; the following edits are made.

R	α	β
$t_1 \rightarrow$	a	1
$t_2 \rightarrow$	a	1
	c	3
	d	4

$$\alpha \subseteq R, \beta \subseteq R$$

if $\alpha \rightarrow \beta$ "holds true" then
 $t_1[\alpha] = t_2[\alpha]$ implies
 $t_1[\beta] = t_2[\beta]$.

Types of FD's:

- trivial: $AB \rightarrow A$ i.e. here $\beta \subseteq \alpha$
- non-trivial: $AB \rightarrow CBA$ i.e. here $\beta \not\subseteq \alpha / \alpha \subseteq \beta$
- completely non-trivial: $AB \rightarrow DE$ i.e. $\alpha \cap \beta = \phi$

Example:

R	A	B	C	D	E
	a	2	3	4	5
	2	a	3	4	5
	a	2	3	6	5
	a	2	3	6	6

a) $A \rightarrow BC$

b) $DE \rightarrow C$

c) $C \rightarrow DE$

d) $BC \rightarrow A$

Given R, determine if a, b, c, & d are valid functional dependencies.

{ HINT: look for a given value of α , do you get the same value of β . }

Important Examples:

R_2	A	B	C	D	E
a	2	3	4	5	
b	a	3	4	5	
c	2	3	6	5	
d	2	3	6	6	

Set 1:

- a) $A \rightarrow BCD$
 b) $A \rightarrow DE$
 c) $A \rightarrow E$

Set 2:

- a) $AB \rightarrow C$
 b) $ED \rightarrow C$
 c) $EA \rightarrow C$

Observation: SET 1: all values of A are unique. \therefore all the fd's are valid; i.e. all values of the "x" (determinant) are unique

SET 2: all fd's are valid if the values of "B" (dependants) are identical.

R_3	X	Y	Z
	1	4	2
	1	5	3
	1	6	3
	3	2	2

R_4	A	B	C
	1	2	4
	3	5	4
	3	7	2
	1	4	2

- a) $XY \rightarrow Z$ & $Z \rightarrow Y$
 b) $YZ \rightarrow X$ & $Y \rightarrow Z$
 c) $YZ \rightarrow X$ & $X \rightarrow Z$
 d) $XZ \rightarrow Y$ & $Y \rightarrow Z$

- a) $A \rightarrow B$ & $BC \rightarrow A$
 b) $C \rightarrow B$ & $CA \rightarrow B$
 c) $B \rightarrow C$ & $AB \rightarrow C$
 d) $A \rightarrow C$ & $BC \rightarrow A$

Hidden Functional Dependencies:

Library Database:

- BOOK (ACC-NO, YR-PUB, TITLE)
- USER (CARD-NO, B-NAME, B-ADDR)
- SUPPLIER (S-NAME, S-ADDR)
- BORROW (ACC-NO, CARD-NO, DOI)
- SUPPLY (ACC-NO, S-NAME, PRICE, DOS)

fd:

- $S\text{-NAME}, DOS \rightarrow PRICE$ (supply table)
- $CARD\text{-NO} \rightarrow DOI$ (borrow table/schema)
- $ACC\text{-NO} \rightarrow YR\text{-PUB}$
- $ACC\text{-NO}, TITLE \rightarrow YR\text{-PUB}$
- $ACC\text{-NO} \rightarrow YR\text{-PUB}, TITLE$

} (Book schema)
too many can we reduce

step 1: look for redundancies in $K \& B$

- $ACC\text{-NO}, \text{TITLE} \rightarrow YR\text{-PUB}$
- $ACC\text{-NO} \rightarrow YR\text{-PUB}$
- $ACC\text{-NO} \rightarrow YR\text{-PUB}, \text{TITLE}$ — redundant (not required)

step 2: weed out hidden fd's.

- $ACC\text{-NO} \rightarrow S\text{-NAME}$ (supply)
- $ACC\text{-NO} \rightarrow S\text{-ADDR}$ — redundant
- $S\text{-NAME} \rightarrow S\text{-ADDR}$ (supplier)

(there is a hidden dependancy)

i.e. $ACC\text{-NO} \rightarrow S\text{-ADDR}$ can be inferred using

$ACC\text{-NO} \rightarrow S\text{-NAME}$

$S\text{-NAME} \rightarrow S\text{-ADDR}$