

*Michael Grossberg*

---

# Intro to Data Science CS59969

Recommender Systems

---

---

# Many Applications

---



---

# Further Resource

---

Survey on recommender systems by Michael D. Ekstrand et al.



- <http://files.grouplens.org/papers/FnT%20CF%20Recsys%20Survey.pdf>

Good slides from Stanford lecture by Lester Mackey


























- [http://web.stanford.edu/~lmackey/papers/cf\\_slides-pml09.pdf](http://web.stanford.edu/~lmackey/papers/cf_slides-pml09.pdf)



# Recommender Data

		Items				
						
Users						Ratings
						Missing Data
						
						
						


























# Problem

- Fill in missing data
- Make recommendations: You might like this movie











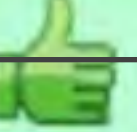
















# Global Fill in Missing Data

				
				
 ave				
				ave
		ave		ave
				

Average cols

# Global Fill in Missing Data


























				
				
 ave				
				ave
		ave		ave
				

Average rows



# Global Fill in Missing Data

Combine: ave rating + user bias + item bias?

				
				
	Comb			
				Comb
		Comb		Comb
				

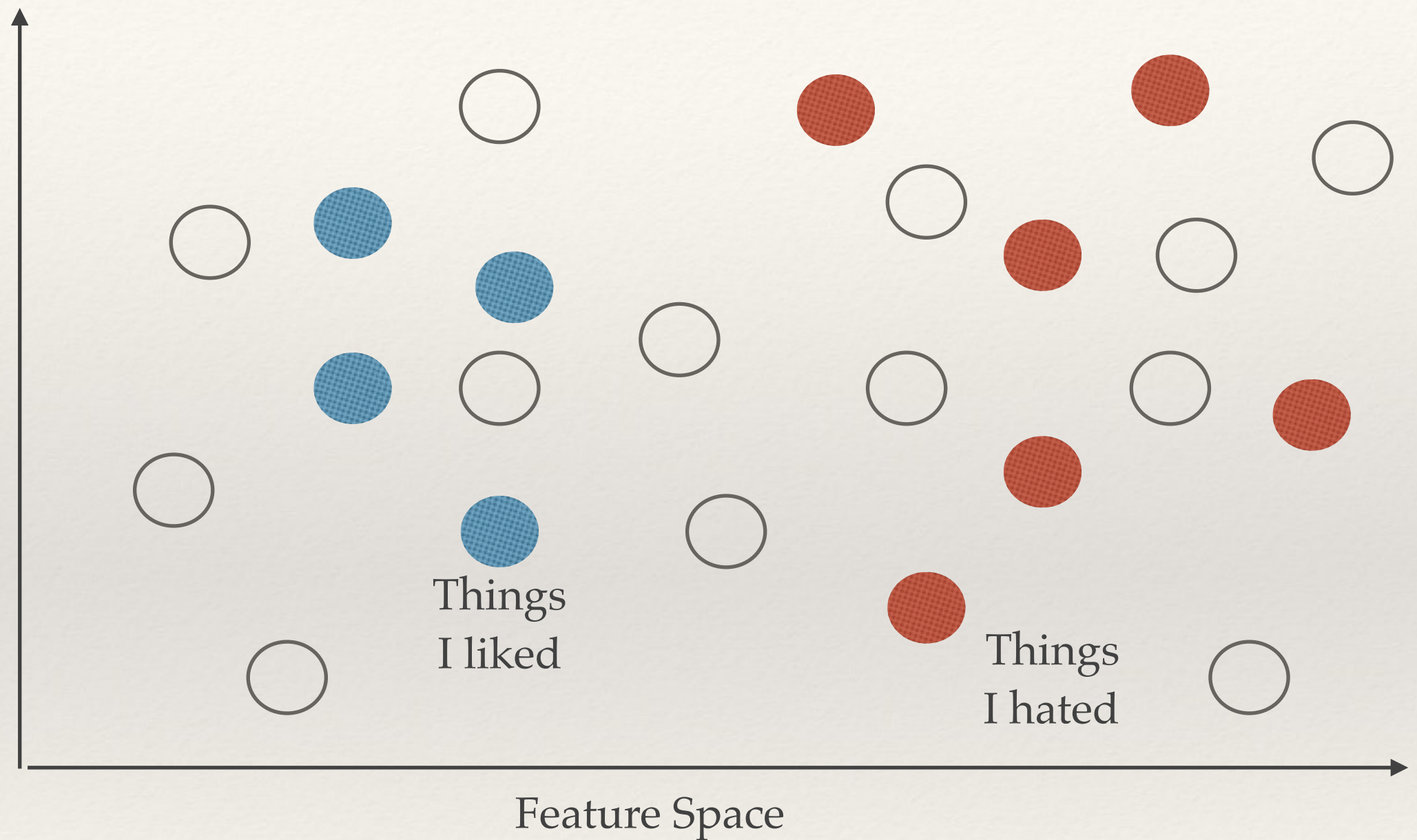
Not very personalized



---

# Approach 1: Content Based Filtering

---



Classic Classification Problem

---

## Approach: 2

# Collaborative Filtering

---



These users like these toys



These users like these toys



Which kind of user are you?



# Differences

## Content Based Recommendation



Likes

Recommends

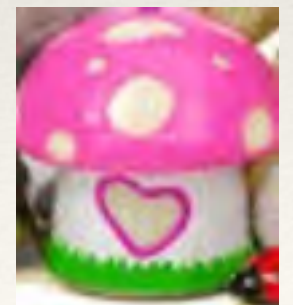
## Collaborative Recommendation



Likes

Similar  
Users

Similar  
preferences



Some advantages

Content-Based: Start from single item


















Collaborative: Discover New Things

Recommends




























# User (row) Based Collaborative Filtering





# Approach: Regression



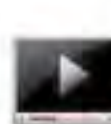






















## Pros:

- Reduces recommendations to a well-studied problem
- Many good prediction algorithms available

## •Cons:

- Have to handle tons of missing data
- Training M predictors is expensive

# KNN

Find neighbor users -> predict user's item rating (average)

Find neighbor items -> predict user's item rating (average)



---

# Similarity Score Option: Pearson

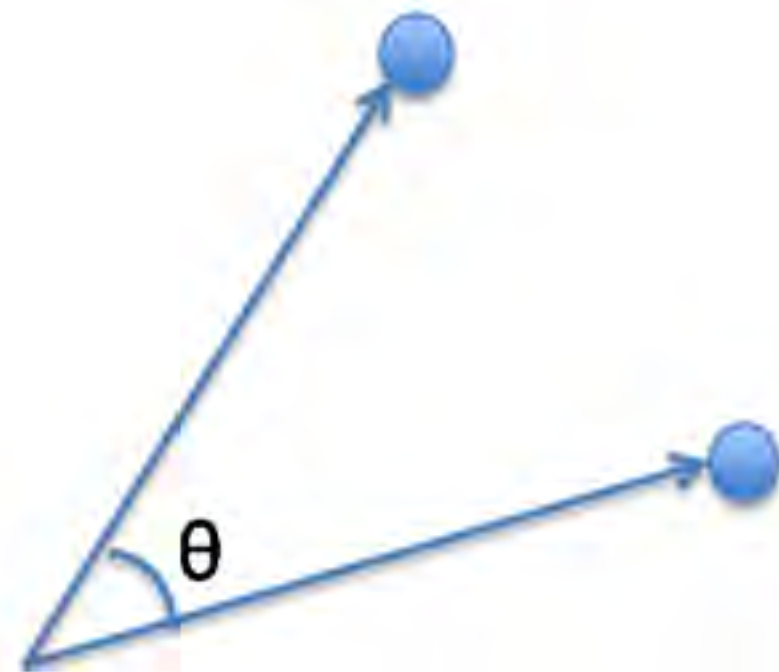
---

$$s(u, v) = \frac{\sum_{i \in I_u \cap I_v} (r_{u,i} - \bar{r}_u)(r_{v,i} - \bar{r}_v)}{\sqrt{\sum_{i \in I_u \cap I_v} (r_{u,i} - \bar{r}_u)^2} \sqrt{\sum_{i \in I_u \cap I_v} (r_{v,i} - \bar{r}_v)^2}}$$

# Similarity Score Option: Cosine

missing values 0

$$\cos(\theta) = \frac{A \cdot B}{\|A\| \|B\|}$$





---

# Netflix Prize

---



---

# SVD Idea

---

- SimonFunk did this publicly on his blog with the title “Try this at home”
- <http://sifter.org/~simon/journal/20061027.2.html>



# SDV

The diagram illustrates the matrix factorization equation  $A = U \Sigma T^T$  for the SDV model. The matrix  $A$  is represented by a large rectangle with dimensions  $|U|$  (height) and  $|I|$  (width). The matrix  $U$  is a tall, narrow rectangle. The matrix  $\Sigma$  is a small square with dimension  $k$  indicated above it. The matrix  $T^T$  is a wide, short rectangle. The equation is shown as  $A = U \Sigma T^T$ .

$$\begin{matrix} |I| \\ \boxed{A} \\ |U| \end{matrix} = \boxed{U} \begin{matrix} k \\ \boxed{\Sigma} \end{matrix} \boxed{T^T}$$

---

# SVD Method

---

Leskovec, Rajaraman, Ullman

- <https://www.youtube.com/watch?v=YKmkAoIUxkU>



# SVD approach

- $A = U \Sigma V^T$  - example: Users to Movies

Matrix

	Alien	Serenity	Casablanca	Amelie
1	1	1	0	0
3	3	3	0	0
4	4	4	0	0
5	5	5	0	0
0	2	0	4	4
0	0	0	5	5
0	1	0	2	2

U

$\Sigma$

$V^T$

n

m

nce

# SVD approach

## ■ $A = U \Sigma V^T$ - example: Users to Movies

$$\begin{array}{c} \text{Matrix} \\ \text{Alien} \\ \text{Serenity} \\ \text{Casablanca} \\ \text{Amelie} \end{array} \begin{bmatrix} 1 & 1 & 1 & 0 & 0 \\ 3 & 3 & 3 & 0 & 0 \\ 4 & 4 & 4 & 0 & 0 \\ 5 & 5 & 5 & 0 & 0 \\ 0 & 2 & 0 & 4 & 4 \\ 0 & 0 & 0 & 5 & 5 \\ 0 & 1 & 0 & 2 & 2 \end{bmatrix} = \begin{array}{c} \text{U: Users x Topics} \\ \begin{bmatrix} 0.13 & 0.02 & -0.01 \\ 0.41 & 0.07 & -0.03 \\ 0.55 & 0.09 & -0.04 \\ 0.68 & 0.11 & -0.05 \\ 0.15 & -0.59 & 0.65 \\ 0.07 & -0.73 & -0.67 \\ 0.07 & -0.29 & 0.32 \end{bmatrix} \end{array} \times \begin{array}{c} \text{\Sigma: Topics x Topics} \\ \begin{bmatrix} 12.4 & 0 & 0 \\ 0 & 9.5 & 0 \\ 0 & 0 & 1.3 \end{bmatrix} \end{array} \times \begin{array}{c} \text{V}^T: \text{Topics x Movies} \\ \begin{bmatrix} 0.56 & 0.59 & 0.56 & 0.09 & 0.09 \\ 0.12 & -0.02 & 0.12 & -0.69 & -0.69 \\ 0.40 & -0.80 & 0.40 & 0.09 & 0.09 \end{bmatrix} \end{array}$$



---

# SVD advantages

---

- Not only good for estimating missing data
- We might actually care about the topics more