## Homework 3

## Portfolio optimization

## Due 4 Nov 2019

- 1. Write a program to read stock data of 5 companies in US market.
- 2. Perform portfolio optimization (finding weights) based on the following objective function.
- Return objective:

minimize 
$$\sigma_P^2(w_1, w_2, ..., w_n)$$
  
Subject to  $E[R_P] = m$ 

$$\sum_{i=1}^{N} w_i = 1$$

- Risk constraint:

$$\begin{aligned} & \underset{w_1, w_2, \dots, w_n}{\text{maximize}} E[R_P(w_1, w_2, \dots, w_n)] \\ & \text{Subject to} \\ & \sigma_P^2(w_1, w_2, \dots, w_n) = v^2 \end{aligned}$$

$$\sum_{i=1}^{N} w_i = 1$$

- Mean-variance optimization:

$$\begin{aligned} & \underset{w_1, w_2, \dots, w_n}{\text{maximize}} & E \left[ R_P \left( w_1, w_2, \dots, w_n \right) \right] - \frac{\lambda}{2} \sigma_P^2 \left( w_1, w_2, \dots, w_n \right) \\ & \sum_{i=1}^N w_i = 1 \end{aligned}$$

- Note that there are different kinds of Python libraries for solving optimization. You should use a library that can solve quadratic problems based on a numerical method directly.
- In the mean-variance optimization problem, use  $\lambda = 0.5, 1.2, 2.3$
- 3. Plot efficient frontier of each case. Analyze and describe the results.